

Midterm

Prescriptive Analytics

2024

Instruction

Grading

This midterm is optional. Please put the following letter in the top right corner of your answer sheet:

- N: the grade of the midterm will not be considered
- Y: the grade of the midterm will be considered and will substitute the attendance grade

Answers

There is one and only one correct answer.

- Each correct answer is worth 1pt.
- Each incorrect answer is worth -0.5 pts.
- Each blank answer is worth 0 pts.

Question 1:

The plot below represents a sensitivity analysis of a dependent variable **Net Profit** versus two independent variables **Proportion of Supers(%)** and **Demand**.

The sensitivity of the **Net Profit** to **Proportion of Supers(%)** is...

- (a) Higher when the **Demand** is higher
- (b) Lower when the **Demand** is around 150000 than when **Demand** is around 250000
- (c) Equal to the sensitivity to **Demand**
- (d) Higher when the **Demand** is around 150000 than when the **Demand** is around 50000

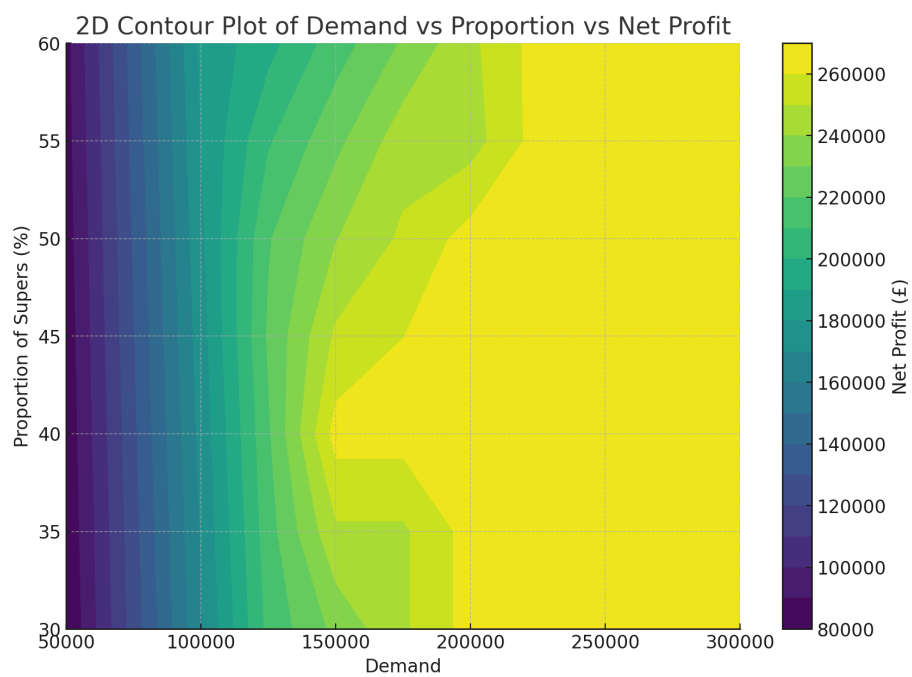


Figure 1: Question 1

Question 2

The plot below shows the cumulative distribution function of the output variable of the profit of the Wellyntoy company.

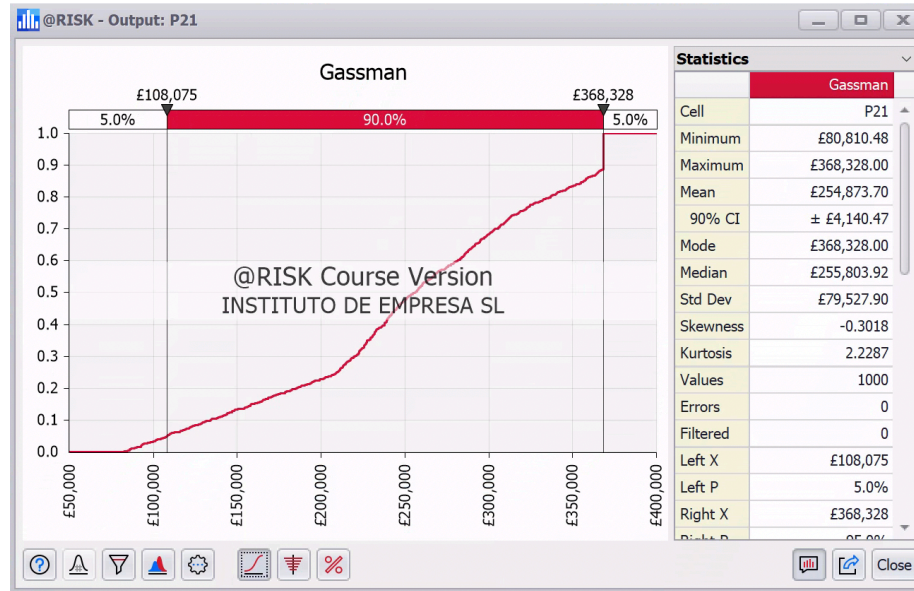


Figure 2: Question 2

Choose the correct statement:

- (a) There is a 90% probability that the profit is £328,328
- (b) There is a 5% probability that the profit is between 0 and £108,075
- (c) There is a 5% probability that the profit is below 0.9 (approx.)
- (d) There is a 30% probability that the profit is £225,000 (approx.)

Question 3

Choose the correct statement:

- (a) There is a 90% probability that the profit is £357,328
- (b) There is a 5% probability that the profit is £54,465
- (c) There is a 90% probability that the profit is between £54,465 and £357,328
- (d) There is a 5% probability that the profit is £50,000 (approx.)

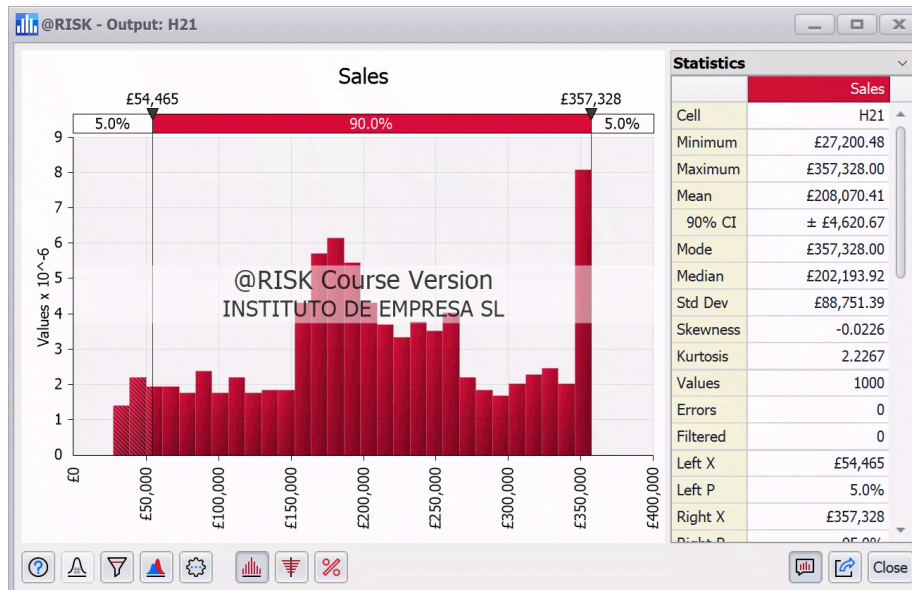


Figure 3: Question 3

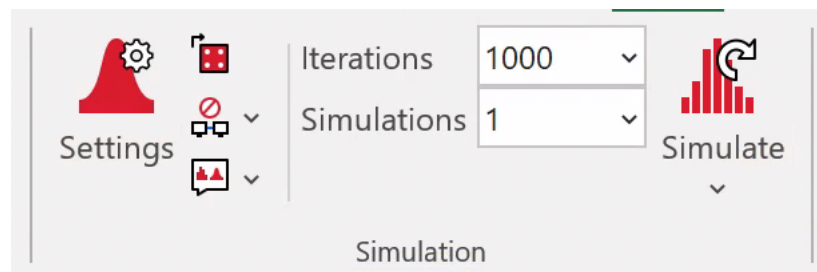


Figure 4: Question 4

Question 4

What does this represent?:

- (a) 1,000 Monte Carlo simulations
- (b) A Monte Carlo simulation with 1,000 draws from each input random variable
- (c) 1,000 iterations of a linear programming
- (d) A Monte Carlo simulation with 1,000 iterations, each with 1,000 random variables

Question 5

The screenshot shows the 'OpenSolver - Model' dialog box. At the top, there's a section 'What is AutoModel?' with an 'AutoModel' button. Below it, the 'Objective Cell' is '\$D\$21', and the 'maximise' radio button is selected. The 'Variable Cells' are '\$B\$3:\$C\$3'. In the 'Constraints' section, a single constraint is listed: '\$B\$5:\$C\$5 <= \$B\$7:\$C\$7'. To the right of the constraints list are input fields for the constraint formula and a dropdown for the comparison operator, with 'Add constraint' and 'Cancel' buttons below. Further down, there are checkboxes for 'Make unconstrained variable cells non-' and 'Show named ranges in constraint list', both of which are checked. At the bottom, the 'Solver Engine' is set to 'CBC', and there are buttons for 'Show model after saving', 'Clear Model', 'Options...', 'Save Model', and 'Cancel'.

Figure 5: Question 5

Which one is correct?

- (a) The model has several decision variables
- (b) The model has a single constraint
- (c) The model tries to maximize the error between cell D21 and the target value
- (d) The model is not using Simplex as Solver

Question 6

Which one is false?

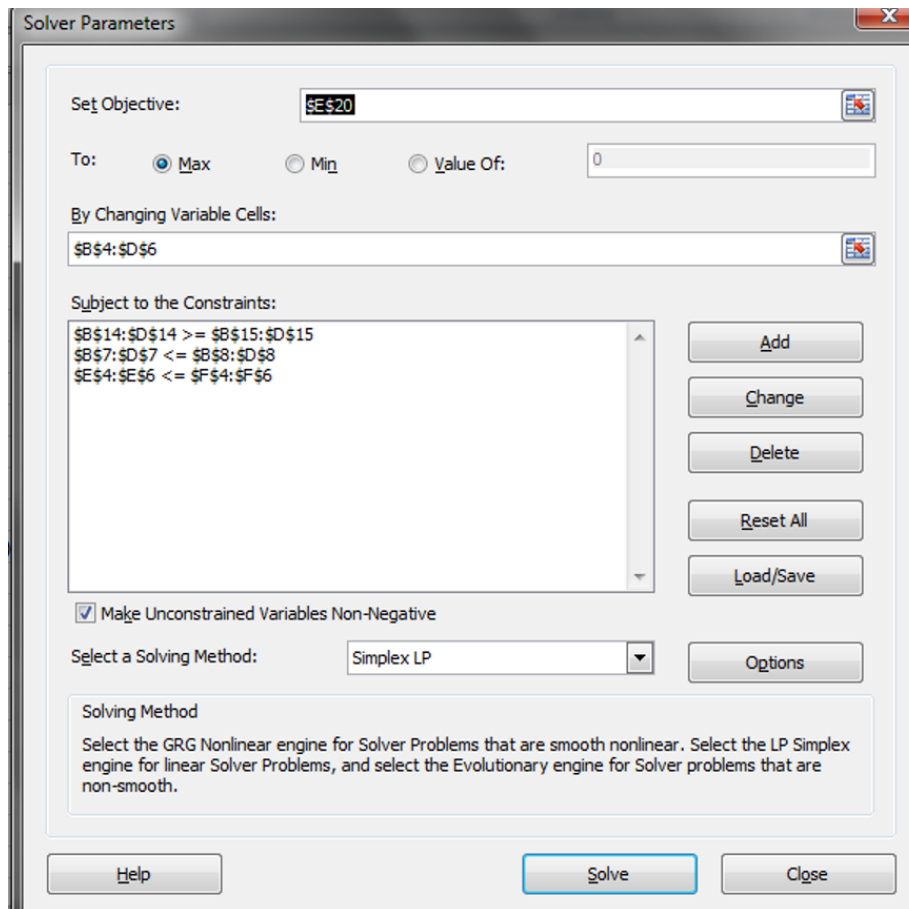


Figure 6: Question 6

- (a) The model has several sets of constraints
- (b) The models assumes that this is a linear programming problem
- (c) The model has several objective functions
- (d) The model takes six decision variables

Question 7

RED BRAND CANNERS					
MIX DECISION	Whole	Juice	Paste	Total Required	Available
Grade A	239	125	0	364	364
Grade B	80	375	1,000	1,455	≤ 1,455
Total Production	318	500	1,000		1,818
Demand	≤ 600	500	1,000		
QUALITY	Whole	Juice	Paste	Quality	
Grade A	2,148	1,125	0	9	
Grade B	398	1,875	5,000	5	
Total Quality	2,545	3,000	5,000		
Required Total Quality	≥ 2,545	3,000	5,000		
Average Quality	8.0	6.0	5.0		
Required Average Quality	8.0	6.0	5.0		
PROFIT	Whole	Juice	Paste	Total Contribution	Profit
Contribution Margin	\$247	\$198	\$222	\$399,591	max \$72,318

Figure 7: Question 7 and 8

Which one is correct?

- (a) The multiple-cell boxes highlight the decision variables
- (b) The single-cell box highlights the decision variables
- (c) The pink shades highlight the constraints
- (d) The horizontal boxes highlight a constraint

Question 8

Which one is correct?

- (a) The demand of juice seems to be not binding
- (b) The demand of whole tomatoes seems to be not binding
- (c) The available A tomatoes seems to be not binding
- (d) The quality of whole tomatoes seems to be not binding

Question 9

Choose the correct one (don't worry about the units or the conversion to 1,000s):

- (a) Increasing the production of grade A tomatoes would bring a benefit of 600

OpenSolver Sensitivity Report - CBC
Worksheet: [RBC Lecture.xlsx] Model Sensitivity
Report Created: 23/9/24 22:35:41

Decision Variables						
Cells	Name	Final Value	Reduced Costs	Objective Value	Allowable Increase	Allowable Decrease
B4	Grade A Whole	525	0	247	462.6666669	65.3333334
C4	Grade A Juice	75	0	198	65.33333342	462.6666669
D4	Grade A Paste	0	-98	222	98	1E+100
B5	Grade B Whole	175	0	247	1388.0000001	65.33333342
C5	Grade B Juice	225	0	198	43.1111112	154.2222223
D5	Grade B Paste	2000	0	222	1E+100	48.5000001

Constraints						
Cells	Name	Final Value	Shadow Price	RHS Value	Allowable Increase	Allowable Decrease
B12>=B13	Total Quality Whole	0	-24.5	0	466.6666667	600
C12>=C13	Total Quality Juice	0	-24.5	0	1400	200
D12>=D13	Total Quality Paste	0	0	0	0	1E+100
B6<=B7	Total Production Whole	700	0	14400	1E+100	13700
C6<=C7	Total Production Juice	300	0	1000	1E+100	700
D6<=D7	Total Production Paste	2000	48.5	2000	200	466.6666667
E4<=F4	Grade A Total Required	600	271.5	600	600	466.6666667
E5<=F5	Grade B Total Required	2400	173.5	2400	466.6666667	200

Figure 8: Question 9

- (b) Increasing the production of grade B tomatoes would bring a benefit of 2,400
- (c) Increasing the production of grade A tomatoes would bring a benefit of 271.5 for at least 600 additional tomatoes
- (d) Increasing the production of grade B tomatoes would bring a benefit of 173.5 for at least 200 additional tomatoes

Question 10

Which one is false?

- (a) the b coefficients are the decision variables
- (b) Z is the objective function
- (c) the a coefficients are part of the definition of the constraints
- (d) the b coefficients are the shadow prices

Maximize:

$$Z = C_1X_1 + C_2X_2 + \cdots + C_nX_n$$

Subject to:

$$a_{11}X_1 + a_{12}X_2 + \cdots + a_{1n}X_n = b_1$$

$$a_{21}X_1 + a_{22}X_2 + \cdots + a_{2n}X_n = b_2$$

$$\vdots$$

$$a_{m1}X_1 + a_{m2}X_2 + \cdots + a_{mn}X_n = b_m$$

With:

$$X_1, X_2, \dots, X_n \geq 0$$

$$b_1, b_2, \dots, b_m \geq 0$$

Figure 9: Question 10