# C1M2\_Assignment

August 31, 2021

# 1 Evaluation of Diagnostic Models

Welcome to the second assignment of course 1. In this assignment, we will be working with the results of the X-ray classification model we developed in the previous assignment. In order to make the data processing a bit more manageable, we will be working with a subset of our training, and validation datasets. We will also use our manually labeled test dataset of 420 X-rays.

As a reminder, our dataset contains X-rays from 14 different conditions diagnosable from an X-ray. We'll evaluate our performance on each of these classes using the classification metrics we learned in lecture.

#### 1.1 Outline

Click on these links to jump to a particular section of this assignment! - Section ?? - Section

By the end of this assignment you will learn about:

- 1. Accuracy
- 2. Prevalence
- 3. Specificity & Sensitivity
- 4. PPV and NPV
- 5. ROC curve and AUCROC (c-statistic)
- 6. Confidence Intervals

### ## 1. Packages

In this assignment, we'll make use of the following packages: - numpy is a popular library for scientific computing - matplotlib is a plotting library compatible with numpy - pandas is what we'll use to manipulate our data - sklearn will be used to measure the performance of our model Run the next cell to import all the necessary packages as well as custom util functions.

```
In [1]: import numpy as np
        import matplotlib.pyplot as plt
        import pandas as pd
        import util
```

#### ## 2. Overview

We'll go through our evaluation metrics in the following order.

#### Metrics

- TP, TN, FP, FN
- Accuracy
- Prevalence
- Sensitivity and Specificity
- PPV and NPV
- AUC
- Confidence Intervals

Let's take a quick peek at our dataset. The data is stored in two CSV files called train\_preds.csv and valid\_preds.csv. We have precomputed the model outputs for our test cases. We'll work with these predictions and the true class labels throughout the assignment.

```
In [3]: train_results = pd.read_csv("train_preds.csv")
        valid_results = pd.read_csv("valid_preds.csv")
        # the labels in our dataset
        class_labels = ['Cardiomegaly',
         'Emphysema',
         'Effusion',
         'Hernia',
         'Infiltration',
         'Mass',
         'Nodule',
         'Atelectasis',
         'Pneumothorax',
         'Pleural_Thickening',
         'Pneumonia',
         'Fibrosis',
         'Edema',
         'Consolidation']
        # the labels for prediction values in our dataset
        pred_labels = [l + "_pred" for l in class_labels]
        pred_labels
Out[3]: ['Cardiomegaly_pred',
         'Emphysema_pred',
         'Effusion_pred',
         'Hernia_pred',
         'Infiltration_pred',
         'Mass_pred',
         'Nodule_pred',
         'Atelectasis pred',
         'Pneumothorax_pred',
         'Pleural Thickening pred',
         'Pneumonia_pred',
```

```
'Fibrosis_pred',
```

Extract the labels (y) and the predictions (pred).

In [4]: y = valid\_results[class\_labels].values
 pred = valid\_results[pred\_labels].values

Run the next cell to view them side by side.

In [5]: # let's take a peek at our dataset
 valid\_results[np.concatenate([class\_labels, pred\_labels])].head()

	٧u	ria_rebarebe	np.concatenat	, , ,	[CIGDD_I	aberb,	prcu_	14501	-01/1	·IIcaa()		
Out[5]:		Cardiomegal	y Emphysema	E	ffusion	Hernia	a Inf	iltra	tion	Mass	Nodul	e \
	0		0 0		0	(	0		0	0		0
	1		0 0		0	(	0		1	0		1
	2		0 0		0	(	0		0	0		0
	3		0 0		0	(	0		0	0		0
	4		0 0		0	(	0		0	0		0
		Atelectasis	Pneumothora	ıx	Pleural	_Thick	ening		Inf	iltrati	on_pre	d \
	0	0		0			0			0	.25602	0
	1	0		0			0			0	.38219	9
	2	0		0			0				.42772	
	3	0		0			0			0	.15859	6
	4	0		0			0	• • •		0	.53676	2
		Mass_pred	Nodule_pred	At	electasi	s_pred	Pneu	motho	rax_p	ored \		
	0	0.266928	0.312440		0.	460342			0.079	9453		
	1	0.176825	0.465807		0.	489424			0.084	4595		
	2	0.115513	0.249030		0.	035105			0.238	3761		
	3	0.259460	0.334870		0.	266489			0.073	3371		
	4	0.198797	0.273110		0.	186771			0.242	2122		
		Pleural_Thi	ckening_pred	P	neumonia	_pred	Fibro	sis_p	red	Edema_	pred	\
	0		0.271495		0.2	76861		0.398	3799	0.01	5867	
	1		0.377318		0.3	63582		0.638	3024	0.02	5948	
	2		0.167095		0.1	66389		0.262	2463	0.00	7758	
	3		0.229834		0.1	91281		0.344	1348	0.00	8559	
	4		0.309786		0.4	11771		0.244	1666	0.12	6930	
		Consolidati	on pred									

### Consolidation\_pred

0	0.156320
1	0.144419
2	0.125790
3	0.119153
4	0.342409

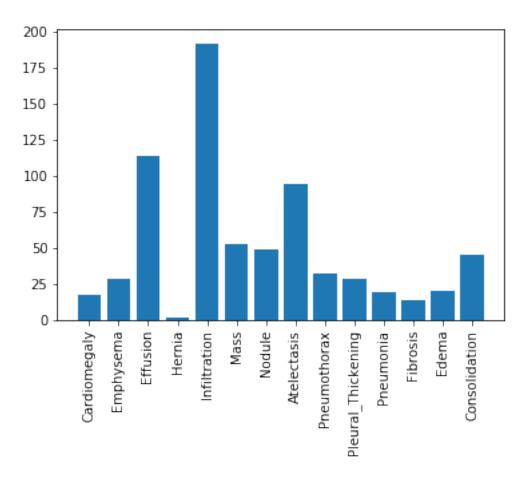
[5 rows x 28 columns]

<sup>&#</sup>x27;Edema\_pred',

<sup>&#</sup>x27;Consolidation\_pred']

To further understand our dataset details, here's a histogram of the number of samples for each label in the validation dataset:

In [6]: plt.xticks(rotation=90)
 plt.bar(x = class\_labels, height= y.sum(axis=0));



It seem like our dataset has an imbalanced population of samples. Specifically, our dataset has a small number of patients diagnosed with a Hernia.

## 3 Metrics

### 3.1 True Positives, False Positives, True Negatives, and False Negatives

The most basic statistics to compute from the model predictions are the true positives, true negatives, false positives, and false negatives.

As the name suggests - true positive (TP): The model classifies the example as positive, and the actual label also positive. - false positive (FP): The model classifies the example as positive, **but** the actual label is negative. - true negative (TN): The model classifies the example as negative, and the actual label is also negative. - false negative (FN): The model classifies the example as negative, **but** the label is actually positive.

We will count the number of TP, FP, TN and FN in the given data. All of our metrics can be built off of these four statistics.

Recall that the model outputs real numbers between 0 and 1. \* To compute binary class predictions, we need to convert these to either 0 or 1. \* We'll do this using a threshold value th. \* Any model outputs above th are set to 1, and below th are set to 0.

All of our metrics (except for AUC at the end) will depend on the choice of this threshold. Fill in the functions to compute the TP, FP, TN, and FN for a given threshold below. The first one has been done for you.

```
In [7]: # UNQ_C1 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
        def true_positives(y, pred, th=0.5):
            Count true positives.
            Args:
                y (np.array): ground truth, size (n_examples)
                pred (np.array): model output, size (n_examples)
                th (float): cutoff value for positive prediction from model
            Returns:
                TP (int): true positives
            11 11 11
            TP = 0
            # get thresholded predictions
            thresholded_preds = pred >= th
            # compute TP
            TP = np.sum((y == 1) & (thresholded_preds == 1))
            return TP
        def true_negatives(y, pred, th=0.5):
            Count true negatives.
            Arqs:
                y (np.array): ground truth, size (n_examples)
                pred (np.array): model output, size (n_examples)
                th (float): cutoff value for positive prediction from model
            Returns:
                TN (int): true negatives
            11 11 11
            TN = 0
            # get thresholded predictions
            thresholded_preds = pred >= th
            ### START CODE HERE (REPLACE INSTANCES OF 'None' with your code) ###
            # compute TN
```

```
TN = np.sum((y == 0) & (thresholded_preds == 0))
    ### END CODE HERE ###
    return TN
def false_positives(y, pred, th=0.5):
    Count false positives.
    Arqs:
        y (np.array): ground truth, size (n_examples)
        pred (np.array): model output, size (n_examples)
        th (float): cutoff value for positive prediction from model
       FP (int): false positives
   FP = 0
    # get thresholded predictions
    thresholded_preds = pred >= th
    ### START CODE HERE (REPLACE INSTANCES OF 'None' with your code) ###
    # compute FP
   FP = np.sum((y == 0) & (thresholded_preds == 1))
    ### END CODE HERE ###
    return FP
def false_negatives(y, pred, th=0.5):
    11 11 11
    Count false positives.
    Args:
        y (np.array): ground truth, size (n_examples)
        pred (np.array): model output, size (n_examples)
        th (float): cutoff value for positive prediction from model
    Returns:
        FN (int): false negatives
    11 11 11
   FN = 0
    # get thresholded predictions
    thresholded_preds = pred >= th
    ### START CODE HERE (REPLACE INSTANCES OF 'None' with your code) ###
```

```
# compute FN
           FN = np.sum((y == 1) & (thresholded_preds == 0))
            ### END CODE HERE ###
            return FN
In [8]: # Note: we must explicity import 'display' in order for the autograder to compile the
        # Even though we could use this function without importing it, keep this import in ord
        from IPython.display import display
        # Test
        df = pd.DataFrame({'y_test': [1,1,0,0,0,0,0,0,0,1,1,1,1,1],
                           'preds_test': [0.8,0.7,0.4,0.3,0.2,0.5,0.6,0.7,0.8,0.1,0.2,0.3,0.4,
                           'category': ['TP','TP','TN','TN','FP','FP','FP','FP','FN','FN'
                          })
        display(df)
        #y_test = np.array([1, 0, 0, 1, 1])
        y_test = df['y_test']
        #preds_test = np.array([0.8, 0.8, 0.4, 0.6, 0.3])
       preds_test = df['preds_test']
        threshold = 0.5
        print(f"threshold: {threshold}\n")
       print(f"""Our functions calculated:
       TP: {true_positives(y_test, preds_test, threshold)}
       TN: {true_negatives(y_test, preds_test, threshold)}
        FP: {false_positives(y_test, preds_test, threshold)}
        FN: {false_negatives(y_test, preds_test, threshold)}
        """)
       print("Expected results")
       print(f"There are {sum(df['category'] == 'TP')} TP")
        print(f"There are {sum(df['category'] == 'TN')} TN")
       print(f"There are {sum(df['category'] == 'FP')} FP")
       print(f"There are {sum(df['category'] == 'FN')} FN")
   y_test preds_test category
0
                   0.8
                             TP
         1
         1
                   0.7
                             TP
1
2
         0
                   0.4
                             TN
3
                   0.3
         0
                             TN
4
         0
                   0.2
                             TN
5
         0
                   0.5
                             FP
                   0.6
                             FP
```

7	0	0.7	FP
8	0	0.8	FP
9	1	0.1	FN
10	1	0.2	FN
11	1	0.3	FN
12	1	0.4	FN
13	1	0.0	FN

### threshold: 0.5

Our functions calculated:

TP: 2 TN: 3 FP: 4 FN: 5

Expected results

There are 2 TP

There are 3  ${\tt TN}$ 

There are 4 FP

There are 5 FN

Run the next cell to see a summary of evaluative metrics for the model predictions for each class.

In [9]: util.get\_performance\_metrics(y, pred, class\_labels)

Out[9]:		TP	TN	FP	FN	Accuracy	Prevalence	Sensitivity	\		
	Cardiomegaly	16	814	169	1	Not Defined	Not Defined	Not Defined			
	Emphysema	20	869	103	8	Not Defined	Not Defined	Not Defined			
	Effusion	99	690	196	15	Not Defined	Not Defined	Not Defined			
	Hernia	1	743	255	1	Not Defined	Not Defined	Not Defined			
	Infiltration	114	543	265	78	Not Defined	Not Defined	Not Defined			
	Mass	40	789	158	13	Not Defined	Not Defined	Not Defined			
	Nodule	28	731	220	21	Not Defined	Not Defined	Not Defined			
	Atelectasis	64	657	249	30	Not Defined	Not Defined	Not Defined			
	Pneumothorax	24	785	183	8	Not Defined	Not Defined	Not Defined			
	Pleural_Thickening	24	713	259	4	Not Defined	Not Defined	Not Defined			
	Pneumonia	14	661	320	5	Not Defined	Not Defined	Not Defined			
	Fibrosis	10	725	261	4	Not Defined	Not Defined	Not Defined			
	Edema	15	767	213	5	Not Defined	Not Defined	Not Defined			
	Consolidation	36	658	297	9	Not Defined	Not Defined	Not Defined			
		Specificity				PPV	NPV	AUC \			
	Cardiomegaly Not Defined Not Defined Not Defined										

Emphysema	Not Defined	Not Defined	Not Defined	Not Defined
Effusion	Not Defined	Not Defined	Not Defined	Not Defined
Hernia	Not Defined	Not Defined	Not Defined	Not Defined
Infiltration	Not Defined	Not Defined	Not Defined	Not Defined
Mass	Not Defined	Not Defined	Not Defined	Not Defined
Nodule	Not Defined	Not Defined	Not Defined	Not Defined
Atelectasis	Not Defined	Not Defined	Not Defined	Not Defined
Pneumothorax	Not Defined	Not Defined	Not Defined	Not Defined
Pleural_Thickening	Not Defined	Not Defined	Not Defined	Not Defined
Pneumonia	Not Defined	Not Defined	Not Defined	Not Defined
Fibrosis	Not Defined	Not Defined	Not Defined	Not Defined
Edema	Not Defined	Not Defined	Not Defined	Not Defined
Consolidation	Not Defined	Not Defined	Not Defined	Not Defined

#### F1 Threshold

Cardiomegaly	Not	Defined	0.5
Emphysema	Not	Defined	0.5
Effusion	Not	Defined	0.5
Hernia	Not	Defined	0.5
Infiltration	Not	Defined	0.5
Mass	Not	Defined	0.5
Nodule	Not	Defined	0.5
Atelectasis	Not	Defined	0.5
Pneumothorax	Not	Defined	0.5
Pleural_Thickening	Not	Defined	0.5
Pneumonia	Not	Defined	0.5
Fibrosis	Not	Defined	0.5
Edema	Not	Defined	0.5
Consolidation	Not	Defined	0.5

Right now it only has TP, TN, FP, FN. Throughout this assignment we'll fill in all the other metrics to learn more about our model performance.

### ### 3.2 Accuracy

Let's use a threshold of .5 for the probability cutoff for our predictions for all classes and calculate our model's accuracy as we would normally do in a machine learning problem.

```
\textit{accuracy} = \frac{\text{true positives} + \text{true negatives}}{\text{true positives} + \text{true negatives} + \text{false positives} + \text{false negatives}}
```

Use this formula to compute accuracy below:

Hints

Remember to set the value for the threshold when calling the functions.

```
Arqs:
                 y (np.array): ground truth, size (n_examples)
                 pred (np.array): model output, size (n_examples)
                 th (float): cutoff value for positive prediction from model
             Returns:
                 accuracy (float): accuracy of predictions at threshold
             accuracy = 0.0
             ### START CODE HERE (REPLACE INSTANCES OF 'None' with your code) ###
             # get TP, FP, TN, FN using our previously defined functions
             TP = true_positives(y, pred, th)
             FP = false_positives(y, pred, th)
             TN = true_negatives(y, pred, th)
             FN = false_negatives(y, pred, th)
             # Compute accuracy using TP, FP, TN, FN
             accuracy = (TP + TN) / (TP + TN + FP + FN)
             ### END CODE HERE ###
             return accuracy
In [11]: # Test
        print("Test case:")
         y_test = np.array([1, 0, 0, 1, 1])
         print('test labels: {y_test}')
         preds_test = np.array([0.8, 0.8, 0.4, 0.6, 0.3])
         print(f'test predictions: {preds_test}')
         threshold = 0.5
         print(f"threshold: {threshold}")
         print(f"computed accuracy: {get_accuracy(y_test, preds_test, threshold)}")
Test case:
test labels: {y_test}
test predictions: [0.8 0.8 0.4 0.6 0.3]
threshold: 0.5
computed accuracy: 0.6
Expected output:
test labels: {y_test}
test predictions: [0.8 0.8 0.4 0.6 0.3]
```

### threshold: 0.5

computed accuracy: 0.6

Run the next cell to see the accuracy of the model output for each class, as well as the number of true positives, true negatives, false positives, and false negatives.

In [12]: util.get\_performance\_metrics(y, pred, class\_labels, acc=get\_accuracy)

				_			_	_	
Out[12]:		TP	TN	FP	FN	Accuracy	y Prevalenc	e Sensitivity	\
	Cardiomegaly	16	814	169	1	0.83	Not Define	d Not Defined	
	Emphysema	20	869	103	8	0.889	Not Define	d Not Defined	
	Effusion	99	690	196	15	0.789	Not Define	d Not Defined	
	Hernia	1	743	255	1	0.744	Not Define	d Not Defined	
	Infiltration	114	543	265	78	0.657	Not Define	d Not Defined	
	Mass	40	789	158	13	0.829	Not Define	d Not Defined	
	Nodule	28	731	220	21	0.759	Not Define	d Not Defined	
	Atelectasis	64	657	249	30	0.721	Not Define	d Not Defined	
	Pneumothorax	24	785	183	8	0.809	Not Define	d Not Defined	
	Pleural_Thickening	24	713	259	4	0.737	Not Define	d Not Defined	
	Pneumonia	14	661	320	5	0.675	Not Define	d Not Defined	
	Fibrosis	10	725	261	4	0.735	Not Define	d Not Defined	
	Edema	15	767	213	5	0.782	Not Define	d Not Defined	
	Consolidation	36	658	297	9	0.694	Not Define	d Not Defined	
		Spec	cifici	ty		PPV	NPV	AUC \	\
	Cardiomegaly	Not	Defin	ed 1	Not :	Defined	Not Defined	Not Defined	
	Emphysema	Not	Defin	ed 1	Not :	Defined	Not Defined	Not Defined	
	Effusion	Not	Defin	ed 1	Not :	Defined	Not Defined	Not Defined	
	Hernia	Not	Defin	ed 1	Not :	Defined	Not Defined	Not Defined	
	Infiltration	Not	Defin	ed 1	Not :	Defined	Not Defined	Not Defined	
	Mass	Not	Defin	ed 1	Not :	Defined	Not Defined	Not Defined	
	Nodule	Not	Defin	ed 1	Not :	Defined	Not Defined	Not Defined	
	Atelectasis	Not	Defin	ed 1	Not :	Defined	Not Defined	Not Defined	
	Pneumothorax	Not	Defin	ed 1	Not :	Defined	Not Defined	Not Defined	
	Pleural_Thickening	Not	Defin	ed 1	Not :	Defined	Not Defined	Not Defined	
	Pneumonia	Not	Defin	ed 1	Not :	Defined	Not Defined	Not Defined	
	Fibrosis	Not	Defin	ed 1	Not :	Defined	Not Defined	Not Defined	
	Edema	Not	Defin	ed 1	Not :	Defined	Not Defined	Not Defined	
	Consolidation	Not	Defin	ed 1	Not :	Defined	Not Defined	Not Defined	
				F1 T	hres	hold			
	Cardiomegaly	Not	Defin	ed		0.5			
	Emphysema	Not	Defin	ed		0.5			
	Effusion	Not	Defin	ed		0.5			
	Hernia	Not	Defin	ed		0.5			
	Infiltration	Not	Defin	ed		0.5			

Mass	Not	Defined	0.5
Nodule	Not	Defined	0.5
Atelectasis	Not	Defined	0.5
Pneumothorax	Not	Defined	0.5
Pleural_Thickening	Not	Defined	0.5
Pneumonia	Not	Defined	0.5
Fibrosis	Not	Defined	0.5
Edema	Not	Defined	0.5
Consolidation	Not	Defined	0.5

If we were to judge our model's performance based on the accuracy metric, we would say that our model is not very accurate for detecting the Infiltration cases (accuracy of 0.657) but pretty accurate for detecting Emphysema (accuracy of 0.889).

### But is that really the case?...

Let's imagine a model that simply predicts that any patient does **Not** have Emphysema, regardless of patient's measurements. Let's calculate the accuracy for such a model.

```
In [13]: get_accuracy(valid_results["Emphysema"].values, np.zeros(len(valid_results)))
Out[13]: 0.972
```

As you can see above, such a model would be 97% accurate! Even better than our deep learning based model.

But is this really a good model? Wouldn't this model be wrong 100% of the time if the patient actually had this condition?

In the following sections, we will address this concern with more advanced model measures - sensitivity and specificity - that evaluate how well the model predicts positives for patients with the condition and negatives for cases that actually do not have the condition.

### 3.3 Prevalence Another important concept is **prevalence**. \* In a medical context, prevalence is the proportion of people in the population who have the disease (or condition, etc). \* In machine learning terms, this is the proportion of positive examples. The expression for prevalence is:

$$prevalence = \frac{1}{N} \sum_{i} y_i$$

where  $y_i = 1$  when the example is 'positive' (has the disease).

Let's measure prevalence for each disease:

Hints

You can use np.mean to calculate the formula.

Actually, the automatic grader is expecting numpy.mean, so please use it instead of using an equally valid but different way of calculating the prevalence. =)

```
Returns:
                 prevalence (float): prevalence of positive cases
            prevalence = 0.0
             ### START CODE HERE (REPLACE INSTANCES OF 'None' with your code) ###
            prevalence = (1/y.shape[0]) * np.sum(y)
             ### END CODE HERE ###
            return prevalence
In [15]: # Test
        print("Test case:\n")
        y_{test} = np.array([1, 0, 0, 1, 1, 0, 0, 0, 0, 1])
        print(f'test labels: {y_test}')
        print(f"computed prevalence: {get_prevalence(y_test)}")
Test case:
test labels: [1 0 0 1 1 0 0 0 0 1]
computed prevalence: 0.4
In [16]: util.get_performance_metrics(y, pred, class_labels, acc=get_accuracy, prevalence=get_
Out[16]:
                             TP
                                  TN
                                       FP FN Accuracy Prevalence Sensitivity \
                                                  0.83
                                                            0.017 Not Defined
        Cardiomegaly
                             16 814
                                      169
                                            1
        Emphysema
                             20
                                 869
                                      103
                                            8
                                                 0.889
                                                            0.028 Not Defined
        Effusion
                             99
                                 690
                                      196 15
                                                 0.789
                                                            0.114 Not Defined
        Hernia
                              1
                                 743
                                      255
                                                 0.744
                                                            0.002 Not Defined
                                            1
         Infiltration
                                                            0.192 Not Defined
                             114 543
                                      265
                                          78
                                                 0.657
        Mass
                             40
                                 789
                                      158
                                           13
                                                 0.829
                                                            0.053 Not Defined
        Nodule
                             28
                                 731
                                      220
                                           21
                                                 0.759
                                                            0.049 Not Defined
         Atelectasis
                                 657
                                      249
                                                            0.094 Not Defined
                             64
                                           30
                                                 0.721
        Pneumothorax
                             24 785
                                      183
                                            8
                                                 0.809
                                                            0.032 Not Defined
        Pleural_Thickening
                             24
                                713
                                      259
                                            4
                                                 0.737
                                                            0.028 Not Defined
                                      320
        Pneumonia
                             14 661
                                            5
                                                 0.675
                                                            0.019 Not Defined
        Fibrosis
                                 725
                                            4
                                                 0.735
                                                            0.014 Not Defined
                             10
                                      261
        Edema
                             15
                                 767
                                      213
                                            5
                                                 0.782
                                                             0.02 Not Defined
                                 658
                                                            0.045 Not Defined
         Consolidation
                             36
                                      297
                                            9
                                                 0.694
                                                                           AUC \
                            Specificity
                                                 PPV
                                                              NPV
                            Not Defined Not Defined Not Defined
        Cardiomegaly
```

Emphysema	Not	Defined	Not	Defined	Not	Defined	Not	Defined
Effusion	Not	Defined	Not	Defined	Not	Defined	Not	Defined
Hernia	Not	Defined	Not	Defined	Not	Defined	Not	Defined
Infiltration	Not	Defined	Not	Defined	Not	Defined	Not	Defined
Mass	Not	Defined	Not	Defined	Not	Defined	Not	Defined
Nodule	Not	Defined	Not	Defined	Not	Defined	Not	Defined
Atelectasis	Not	Defined	Not	Defined	Not	Defined	Not	Defined
Pneumothorax	Not	Defined	Not	Defined	Not	Defined	Not	Defined
Pleural_Thickening	Not	Defined	Not	Defined	Not	Defined	Not	Defined
Pneumonia	Not	Defined	Not	Defined	Not	Defined	Not	Defined
Fibrosis	Not	Defined	Not	Defined	Not	Defined	Not	Defined
Edema	Not	Defined	Not	Defined	Not	Defined	Not	Defined
Consolidation	Not	Defined	Not	Defined	Not	Defined	Not	Defined

#### F1 Threshold

Cardiomegaly	Not	Defined	0.5
Emphysema	Not	Defined	0.5
Effusion	Not	Defined	0.5
Hernia	Not	Defined	0.5
Infiltration	Not	Defined	0.5
Mass	Not	Defined	0.5
Nodule	Not	Defined	0.5
Atelectasis	Not	Defined	0.5
Pneumothorax	Not	Defined	0.5
Pleural_Thickening	Not	Defined	0.5
Pneumonia	Not	Defined	0.5
Fibrosis	Not	Defined	0.5
Edema	Not	Defined	0.5
Consolidation	Not	Defined	0.5

Hernia has a prevalence 0.002, which is the rarest among the studied conditions in our dataset. ### 3.4 Sensitivity and Specificity

Sensitivity and specificity are two of the most prominent numbers that are used to measure diagnostics tests. - Sensitivity is the probability that our test outputs positive given that the case is actually positive. - Specificity is the probability that the test outputs negative given that the case is actually negative.

We can phrase this easily in terms of true positives, true negatives, false positives, and false negatives:

$$sensitivity = \frac{\text{true positives}}{\text{true positives} + \text{false negatives}}$$
$$specificity = \frac{\text{true negatives}}{\text{true negatives} + \text{false positives}}$$

Let's calculate sensitivity and specificity for our model:

```
n n n
    Compute sensitivity of predictions at threshold.
    Args:
        y (np.array): ground truth, size (n_examples)
        pred (np.array): model output, size (n_examples)
        th (float): cutoff value for positive prediction from model
    Returns:
        sensitivity (float): probability that our test outputs positive given that th
    sensitivity = 0.0
    ### START CODE HERE (REPLACE INSTANCES OF 'None' with your code) ###
    # get TP and FN using our previously defined functions
    TP = true_positives(y, pred, th)
    FN = false_negatives(y, pred, th)
    # use TP and FN to compute sensitivity
    sensitivity = TP / (TP + FN)
    ### END CODE HERE ###
    return sensitivity
def get_specificity(y, pred, th=0.5):
    Compute specificity of predictions at threshold.
    Args:
        y (np.array): ground truth, size (n_examples)
        pred (np.array): model output, size (n_examples)
        th (float): cutoff value for positive prediction from model
    Returns:
        specificity (float): probability that the test outputs negative given that th
    specificity = 0.0
    ### START CODE HERE (REPLACE INSTANCES OF 'None' with your code) ###
    # get TN and FP using our previously defined functions
    TN = true_negatives(y, pred, th)
    FP = false_positives(y, pred, th)
    # use TN and FP to compute specificity
    specificity = TN / (TN + FP)
    ### END CODE HERE ###
```

```
return specificity
In [18]: # Test
         print("Test case")
         y_test = np.array([1, 0, 0, 1, 1])
         print(f'test labels: {y_test}\n')
         preds_test = np.array([0.8, 0.8, 0.4, 0.6, 0.3])
         print(f'test predictions: {preds_test}\n')
         threshold = 0.5
         print(f"threshold: {threshold}\n")
         print(f"computed sensitivity: {get_sensitivity(y_test, preds_test, threshold):.2f}")
         print(f"computed specificity: {get_specificity(y_test, preds_test, threshold):.2f}")
Test case
test labels: [1 0 0 1 1]
test predictions: [0.8 0.8 0.4 0.6 0.3]
threshold: 0.5
computed sensitivity: 0.67
computed specificity: 0.50
Expected output:
Test case
test labels: [1 0 0 1 1]
test predictions: [0.8 0.8 0.4 0.6 0.3]
threshold: 0.5
computed sensitivity: 0.67
computed specificity: 0.50
In [19]: util.get_performance_metrics(y, pred, class_labels, acc=get_accuracy, prevalence=get_j
                                 sens=get_sensitivity, spec=get_specificity)
Out[19]:
                              TP
                                            FN Accuracy Prevalence Sensitivity \
                                   TN
         Cardiomegaly
                              16 814
                                       169
                                             1
                                                   0.83
                                                              0.017
                                                                          0.941
         Emphysema
                              20 869
                                       103
                                             8
                                                  0.889
                                                              0.028
                                                                          0.714
         Effusion
                              99 690
                                       196 15
                                                  0.789
                                                              0.114
                                                                          0.868
```

Hernia	1	743	255	1	0.7	744	0.002	0.5	
Infiltration	114	543	265	78	0.6	357	0.192	0.594	
Mass	40	789	158	13	0.8	329	0.053	0.755	
Nodule	28	731	220	21	0.7	759	0.049	0.571	
Atelectasis	64	657	249	30	0.7	721	0.094	0.681	
Pneumothorax	24	785	183	8	0.8	309	0.032	0.75	
Pleural_Thickening	24	713	259	4	0.7	737	0.028	0.857	
Pneumonia	14	661	320	5	0.6	375	0.019	0.737	
Fibrosis	10	725	261	4	0.7	735	0.014	0.714	
Edema	15	767	213	5	0.7	782	0.02	0.75	
Consolidation	36	658	297	9	0.6	394	0.045	0.8	
	Speci	ficit	У		PPV		NPV	AUC	١
Cardiomegaly		0.82	8 No	ot. De	fined	Not.	Defined	Not Defined	
Emphysema		0.89			fined		Defined	Not Defined	
Effusion		0.77			fined		Defined	Not Defined	
Hernia		0.74			fined		Defined	Not Defined	
Infiltration		0.67			fined		Defined	Not Defined	
Mass		0.83			fined		Defined	Not Defined	
Nodule		0.76			fined		Defined	Not Defined	
Atelectasis		0.72			fined		Defined	Not Defined	
Pneumothorax		0.81			fined		Defined	Not Defined	
Pleural_Thickening		0.73			fined		Defined	Not Defined	
Pneumonia		0.67			fined	Not	Defined	Not Defined	
Fibrosis		0.73		ot De	fined	Not	Defined	Not Defined	
Edema		0.78			fined		Defined	Not Defined	
Consolidation		0.68			fined		Defined	Not Defined	
			F1 Th	nresh	old				
Q1:	M - +	D - 4			٥. ٦				
Cardiomegaly		Defin			0.5				
Emphysema		Defin			0.5				
Effusion Hernia		Defin			0.5 0.5				
Infiltration		Defin Defin							
		Defin			0.5				
Mass					0.5				
Nodule Atelectasis		Defin Defin			0.5 0.5				
Pneumothorax		Defin			0.5				
Pleural_Thickening					0.5				
Pneumonia		Defin			0.5				
Fibrosis		Defin			0.5 0.5				
Edema		Defin			0.5				
Consolidation		Defin			0.5				
COMPOTINGLION	MOL	DELTI	.eu		0.0				

Note that specificity and sensitivity do not depend on the prevalence of the positive class in the dataset. \* This is because the statistics are only computed within people of the same class \* Sensi-

tivity only considers output on people in the positive class \* Similarly, specificity only considers output on people in the negative class.

### 3.5 PPV and NPV

Diagnostically, however, sensitivity and specificity are not helpful. Sensitivity, for example, tells us the probability our test outputs positive given that the person already has the condition. Here, we are conditioning on the thing we would like to find out (whether the patient has the condition)!

What would be more helpful is the probability that the person has the disease given that our test outputs positive. That brings us to positive predictive value (PPV) and negative predictive value (NPV).

- Positive predictive value (PPV) is the probability that subjects with a positive screening test truly have the disease.
- Negative predictive value (NPV) is the probability that subjects with a negative screening test truly don't have the disease.

Again, we can formulate these in terms of true positives, true negatives, false positives, and false negatives:

$$PPV = \frac{\text{true positives}}{\text{true positives} + \text{false positives}}$$
 
$$NPV = \frac{\text{true negatives}}{\text{true negatives} + \text{false negatives}}$$

Let's calculate PPV & NPV for our model:

```
In [20]: # UNQ_C5 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
         def get_ppv(y, pred, th=0.5):
             11 11 11
             Compute PPV of predictions at threshold.
             Args:
                 y (np.array): ground truth, size (n_examples)
                 pred (np.array): model output, size (n_examples)
                 th (float): cutoff value for positive prediction from model
             Returns:
                 PPV (float): positive predictive value of predictions at threshold
             PPV = 0.0
             ### START CODE HERE (REPLACE INSTANCES OF 'None' with your code) ###
             # get TP and FP using our previously defined functions
             TP = true_positives(y, pred, th)
             FP = false_positives(y, pred, th)
             # use TP and FP to compute PPV
             PPV = TP / (TP + FP)
```

```
### END CODE HERE ###
             return PPV
         def get_npv(y, pred, th=0.5):
             Compute NPV of predictions at threshold.
             Args:
                 y (np.array): ground truth, size (n_examples)
                 pred (np.array): model output, size (n_examples)
                 th (float): cutoff value for positive prediction from model
             Returns:
                 NPV (float): negative predictive value of predictions at threshold
             NPV = 0.0
             ### START CODE HERE (REPLACE INSTANCES OF 'None' with your code) ###
             # get TN and FN using our previously defined functions
             TN = true_negatives(y, pred, th)
             FN = false_negatives(y, pred, th)
             \# use TN and FN to compute NPV
             NPV = TN / (TN + FN)
             ### END CODE HERE ###
             return NPV
In [21]: # Test
        print("Test case:\n")
         y_test = np.array([1, 0, 0, 1, 1])
         print(f'test labels: {y_test}')
         preds_test = np.array([0.8, 0.8, 0.4, 0.6, 0.3])
         print(f'test predictions: {preds_test}\n')
         threshold = 0.5
         print(f"threshold: {threshold}\n")
         print(f"computed ppv: {get_ppv(y_test, preds_test, threshold):.2f}")
         print(f"computed npv: {get npv(y test, preds test, threshold):.2f}")
Test case:
test labels: [1 0 0 1 1]
```

test predictions: [0.8 0.8 0.4 0.6 0.3]

threshold: 0.5

computed ppv: 0.67 computed npv: 0.50

### **Expected output:**

Test case:

test labels: [1 0 0 1 1]

test predictions: [0.8 0.8 0.4 0.6 0.3]

threshold: 0.5

computed ppv: 0.67 computed npv: 0.50

In [22]: util.get\_performance\_metrics(y, pred, class\_labels, acc=get\_accuracy, prevalence=get\_sensitivity, spec=get\_specificity, ppv=get\_ppv, npv=get\_sensitivity

Out[22]:		TP	TN	FP	FN	Accuracy	Prevalence	Sensitivity	\
	Cardiomegaly	16	814	169	1	0.83	0.017	0.941	
	Emphysema	20	869	103	8	0.889	0.028	0.714	
	Effusion	99	690	196	15	0.789	0.114	0.868	
	Hernia	1	743	255	1	0.744	0.002	0.5	
	Infiltration	114	543	265	78	0.657	0.192	0.594	
	Mass	40	789	158	13	0.829	0.053	0.755	
	Nodule	28	731	220	21	0.759	0.049	0.571	
	Atelectasis	64	657	249	30	0.721	0.094	0.681	
	Pneumothorax	24	785	183	8	0.809	0.032	0.75	
	Pleural_Thickening	24	713	259	4	0.737	0.028	0.857	
	Pneumonia	14	661	320	5	0.675	0.019	0.737	
	Fibrosis	10	725	261	4	0.735	0.014	0.714	
	Edema	15	767	213	5	0.782	0.02	0.75	
	Consolidation	36	658	297	9	0.694	0.045	0.8	
		Speci	cificity		PPV	NPV	AUC	F1	\
	Cardiomegaly		0.82	8 0.	086	0.999	Not Defined	Not Defined	
	Emphysema		0.89	4 0.	163	0.991	Not Defined	Not Defined	
	Effusion		0.77	9 0.	336	0.979	Not Defined	Not Defined	
	Hernia		0.74	4 0.	004	0.999	Not Defined	Not Defined	
	Infiltration		0.67	2 0.	301	0.874	Not Defined	Not Defined	
	Mass		0.83	3 0.	202	0.984	Not Defined	Not Defined	

Nodule	0.769	0.113	0.972	Not Defined	Not Defined
Atelectasis	0.725	0.204	0.956	Not Defined	Not Defined
Pneumothorax	0.811	0.116	0.99	Not Defined	Not Defined
Pleural_Thickening	0.734	0.085	0.994	Not Defined	Not Defined
Pneumonia	0.674	0.042	0.992	Not Defined	Not Defined
Fibrosis	0.735	0.037	0.995	Not Defined	Not Defined
Edema	0.783	0.066	0.994	Not Defined	Not Defined
Consolidation	0.689	0.108	0.987	Not Defined	Not Defined

### Threshold

Cardiomegaly	0.5
Emphysema	0.5
Effusion	0.5
Hernia	0.5
Infiltration	0.5
Mass	0.5
Nodule	0.5
Atelectasis	0.5
Pneumothorax	0.5
Pleural_Thickening	0.5
Pneumonia	0.5
Fibrosis	0.5
Edema	0.5
Consolidation	0.5

Notice that despite having very high sensitivity and accuracy, the PPV of the predictions could still be very low.

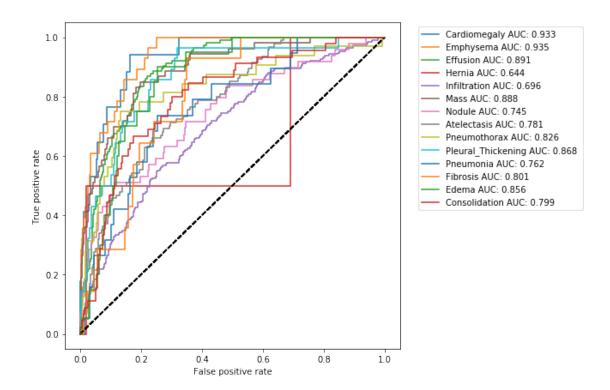
This is the case with Edema, for example. \* The sensitivity for Edema is 0.75. \* However, given that the model predicted positive, the probability that a person has Edema (its PPV) is only 0.066! ### 3.6 ROC Curve

So far we have been operating under the assumption that our model's prediction of 0.5 and above should be treated as positive and otherwise it should be treated as negative. This however was a rather arbitrary choice. One way to see this, is to look at a very informative visualization called the receiver operating characteristic (ROC) curve.

The ROC curve is created by plotting the true positive rate (TPR) against the false positive rate (FPR) at various threshold settings. The ideal point is at the top left, with a true positive rate of 1 and a false positive rate of 0. The various points on the curve are generated by gradually changing the threshold.

Let's look at this curve for our model:

```
In [23]: util.get_curve(y, pred, class_labels)
```



The area under the ROC curve is also called AUCROC or C-statistic and is a measure of goodness of fit. In medical literature this number also gives the probability that a randomly selected patient who experienced a condition had a higher risk score than a patient who had not experienced the event. This summarizes the model output across all thresholds, and provides a good sense of the discriminative power of a given model.

Let's use the sklearn metric function of roc\_auc\_score to add this score to our metrics table.

Out[24]:		TP	TN	FP	FN	Accuracy	Prevalence	Sensitivity	\
	Cardiomegaly	16	814	169	1	0.83	0.017	0.941	
	Emphysema	20	869	103	8	0.889	0.028	0.714	
	Effusion	99	690	196	15	0.789	0.114	0.868	
	Hernia	1	743	255	1	0.744	0.002	0.5	
	Infiltration	114	543	265	78	0.657	0.192	0.594	
	Mass	40	789	158	13	0.829	0.053	0.755	
	Nodule	28	731	220	21	0.759	0.049	0.571	
	Atelectasis	64	657	249	30	0.721	0.094	0.681	
	Pneumothorax	24	785	183	8	0.809	0.032	0.75	
	Pleural_Thickening	24	713	259	4	0.737	0.028	0.857	
	Pneumonia	14	661	320	5	0.675	0.019	0.737	
	Fibrosis	10	725	261	4	0.735	0.014	0.714	

Edema	15	767	213	5	0.78	32	0.02	2	0.75
Consolidation	36	658	297	9	0.69	94	0.04	5	0.8
	Speci	ficit	У	PPV	NPV	AUC		F1	Threshold
Cardiomegaly		0.82	8 0	.086	0.999	0.933	Not	Defined	0.5
Emphysema		0.89	4 0	.163	0.991	0.935	Not	Defined	0.5
Effusion		0.77	9 0	.336	0.979	0.891	Not	Defined	0.5
Hernia		0.74	4 0	.004	0.999	0.644	Not	Defined	0.5
Infiltration		0.67	2 0	.301	0.874	0.696	Not	Defined	0.5
Mass		0.83	3 0	.202	0.984	0.888	Not	Defined	0.5
Nodule		0.76	9 0	.113	0.972	0.745	Not	Defined	0.5
Atelectasis		0.72	5 0	.204	0.956	0.781	Not	Defined	0.5
Pneumothorax		0.81	1 0	.116	0.99	0.826	Not	Defined	0.5
Pleural_Thickening		0.73	4 0	.085	0.994	0.868	Not	Defined	0.5
Pneumonia		0.67	4 0	.042	0.992	0.762	Not	Defined	0.5
Fibrosis		0.73	5 0	.037	0.995	0.801	Not	Defined	0.5
Edema		0.78	3 0	.066	0.994	0.856	Not	Defined	0.5
Consolidation		0.68	9 0	.108	0.987	0.799	Not	Defined	0.5

#### ## 4. Confidence Intervals

Of course our dataset is only a sample of the real world, and our calculated values for all above metrics is an estimate of the real world values. It would be good to quantify this uncertainty due to the sampling of our dataset. We'll do this through the use of confidence intervals. A 95% confidence interval for an estimate  $\hat{s}$  of a parameter s is an interval I=(a,b) such that 95% of the time when the experiment is run, the true value s is contained in s. More concretely, if we were to run the experiment many times, then the fraction of those experiments for which s contains the true parameter would tend towards 95%.

While some estimates come with methods for computing the confidence interval analytically, more complicated statistics, such as the AUC for example, are difficult. For these we can use a method called the *bootstrap*. The bootstrap estimates the uncertainty by resampling the dataset with replacement. For each resampling i, we will get a new estimate,  $\hat{s}_i$ . We can then estimate the distribution of  $\hat{s}$  by using the distribution of  $\hat{s}_i$  for our bootstrap samples.

In the code below, we create bootstrap samples and compute sample AUCs from those samples. Note that we use stratified random sampling (sampling from the positive and negative classes separately) to make sure that members of each class are represented.

```
In [25]: def bootstrap_auc(y, pred, classes, bootstraps = 100, fold_size = 1000):
    statistics = np.zeros((len(classes), bootstraps))

for c in range(len(classes)):
    df = pd.DataFrame(columns=['y', 'pred'])
    df.loc[:, 'y'] = y[:, c]
    df.loc[:, 'pred'] = pred[:, c]
    # get positive examples for stratified sampling
    df_pos = df[df.y == 1]
    df_neg = df[df.y == 0]
    prevalence = len(df_pos) / len(df)
```

```
for i in range(bootstraps):
    # stratified sampling of positive and negative examples
    pos_sample = df_pos.sample(n = int(fold_size * prevalence), replace=True)
    neg_sample = df_neg.sample(n = int(fold_size * (1-prevalence)), replace=True)
    y_sample = np.concatenate([pos_sample.y.values, neg_sample.y.values])
    pred_sample = np.concatenate([pos_sample.pred.values, neg_sample.pred.values)
    score = roc_auc_score(y_sample, pred_sample)
    statistics[c][i] = score
    return statistics

statistics = bootstrap_auc(y, pred, class_labels)
```

Now we can compute confidence intervals from the sample statistics that we computed.

In [26]: util.print\_confidence\_intervals(class\_labels, statistics)

Out[26]:		${\tt Mean \ AUC}$	(CI 5%-95%)
	Cardiomegaly	0.93	(0.90-0.96)
	Emphysema	0.93	(0.91-0.96)
	Effusion	0.89	(0.87 - 0.91)
	Hernia	0.64	(0.30-0.98)
	Infiltration	0.70	(0.67 - 0.73)
	Mass	0.89	(0.86-0.92)
	Nodule	0.75	(0.69-0.81)
	Atelectasis	0.78	(0.75-0.83)
	Pneumothorax	0.83	(0.76-0.89)
	Pleural_Thickening	0.87	(0.80-0.92)
	Pneumonia	0.76	(0.68-0.85)
	Fibrosis	0.80	(0.72 - 0.86)
	Edema	0.86	(0.81-0.89)
	Consolidation	0.80	(0.74-0.85)

As you can see, our confidence intervals are much wider for some classes than for others. Hernia, for example, has an interval around (0.30 - 0.98), indicating that we can't be certain it is better than chance (at 0.5).

### ## 5. Precision-Recall Curve

Precision-Recall is a useful measure of success of prediction when the classes are very imbalanced

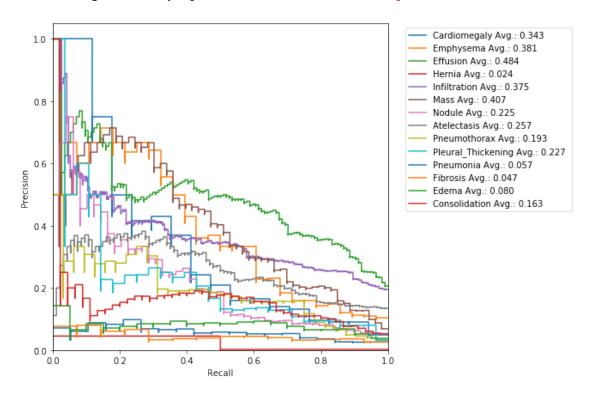
In information retrieval - Precision is a measure of result relevancy and that is equivalent to our previously defined PPV. - Recall is a measure of how many truly relevant results are returned and that is equivalent to our previously defined sensitivity measure.

The precision-recall curve (PRC) shows the trade-off between precision and recall for different thresholds. A high area under the curve represents both high recall and high precision, where high precision relates to a low false positive rate, and high recall relates to a low false negative rate.

High scores for both show that the classifier is returning accurate results (high precision), as well as returning a majority of all positive results (high recall).

Run the following cell to generate a PRC:

In [27]: util.get\_curve(y, pred, class\_labels, curve='prc')



### ## 6. F1 Score

F1 score is the harmonic mean of the precision and recall, where an F1 score reaches its best value at 1 (perfect precision and recall) and worst at 0.

Again, we can simply use sklearn's utility metric function of f1\_score to add this measure to our performance table.

Out[28]:		TP	TN	FP	FN	Accuracy	Prevalence	Sensitivity	\
	Cardiomegaly	16	814	169	1	0.83	0.017	0.941	
	Emphysema	20	869	103	8	0.889	0.028	0.714	
	Effusion	99	690	196	15	0.789	0.114	0.868	
	Hernia	1	743	255	1	0.744	0.002	0.5	
	Infiltration	114	543	265	78	0.657	0.192	0.594	
	Mass	40	789	158	13	0.829	0.053	0.755	
	Nodule	28	731	220	21	0.759	0.049	0.571	
	Atelectasis	64	657	249	30	0.721	0.094	0.681	
	Pneumothorax	24	785	183	8	0.809	0.032	0.75	
	Pleural_Thickening	24	713	259	4	0.737	0.028	0.857	
	Pneumonia	14	661	320	5	0.675	0.019	0.737	

Fibrosis	10	725	261	4	0.73	5	0.014	0.714
Edema	15	767	213	5	0.78	2	0.02	0.75
Consolidation	36	658	297	9	0.69	4	0.045	0.8
	Speci	ficit	У	PPV	NPV	AUC	F1	Threshold
Cardiamagaly		0.828	> ^	.086	0.999	0.933	0.158	0.5
Cardiomegaly								
Emphysema		0.894		. 163	0.991	0.935	0.265	0.5
Effusion		0.779	9 0	. 336	0.979	0.891	0.484	0.5
Hernia		0.74	4 0	.004	0.999	0.644	0.008	0.5
Infiltration		0.672	2 0	.301	0.874	0.696	0.399	0.5
Mass		0.83	3 0	.202	0.984	0.888	0.319	0.5
Nodule		0.769	9 0	.113	0.972	0.745	0.189	0.5
Atelectasis		0.72	5 0	.204	0.956	0.781	0.314	0.5
Pneumothorax		0.81	1 0	.116	0.99	0.826	0.201	0.5
Pleural_Thickening		0.73	4 0	.085	0.994	0.868	0.154	0.5
Pneumonia		0.674	4 0	.042	0.992	0.762	0.079	0.5
Fibrosis		0.73	5 0	.037	0.995	0.801	0.07	0.5
Edema		0.783	3 0	.066	0.994	0.856	0.121	0.5
Consolidation		0.689	9 0	.108	0.987	0.799	0.19	0.5

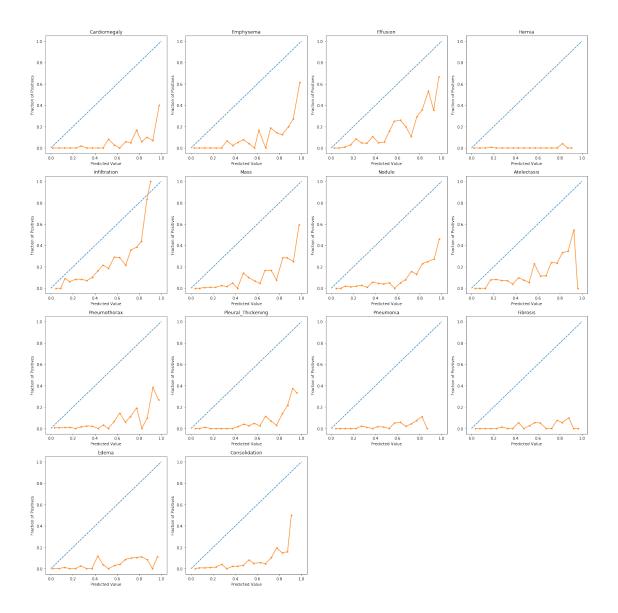
#### ## 7. Calibration

When performing classification we often want not only to predict the class label, but also obtain a probability of each label. This probability would ideally give us some kind of confidence on the prediction. In order to observe how our model's generated probabilities are aligned with the real probabilities, we can plot what's called a *calibration curve*.

In order to generate a calibration plot, we first bucketize our predictions to a fixed number of separate bins (e.g. 5) between 0 and 1. We then calculate a point for each bin: the x-value for each point is the mean for the probability that our model has assigned to these points and the y-value for each point fraction of true positives in that bin. We then plot these points in a linear plot. A well-calibrated model has a calibration curve that almost aligns with the y=x line.

The sklearn library has a utility calibration\_curve for generating a calibration plot. Let's use it and take a look at our model's calibration:

In [30]: plot\_calibration\_curve(y, pred)



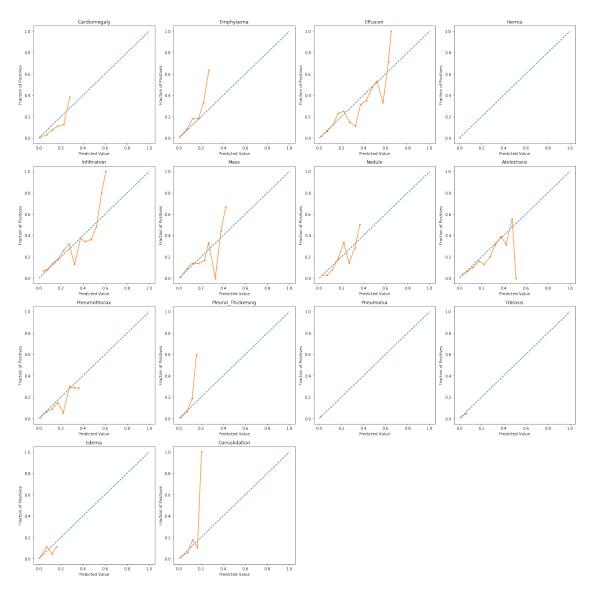
As the above plots show, for most predictions our model's calibration plot does not resemble a well calibrated plot. How can we fix that?...

Thankfully, there is a very useful method called Platt scaling which works by fitting a logistic regression model to our model's scores. To build this model, we will be using the training portion of our dataset to generate the linear model and then will use the model to calibrate the predictions for our test portion.

```
In [31]: from sklearn.linear_model import LogisticRegression as LR
    y_train = train_results[class_labels].values
    pred_train = train_results[pred_labels].values
    pred_calibrated = np.zeros_like(pred)
    for i in range(len(class_labels)):
```

```
lr = LR(solver='liblinear', max_iter=10000)
lr.fit(pred_train[:, i].reshape(-1, 1), y_train[:, i])
pred_calibrated[:, i] = lr.predict_proba(pred[:, i].reshape(-1, 1))[:,1]
```

In [32]: plot\_calibration\_curve(y[:,], pred\_calibrated)



## 2 That's it!

Congratulations! That was a lot of metrics to get familiarized with. We hope that you feel a lot more confident in your understanding of medical diagnostic evaluation and test your models correctly in your future work:)