

## QUIZ 1 Applied Calculus

3wightage =12 marks

Q.1: Prove:  $\lim_{n \rightarrow \infty} \left(1 + \frac{2}{n}\right)^n = 1$

Q.2: Find formulas for  $f \circ g$  and  $g \circ f$  if  $f(x) = \sqrt{x-3}$ ,  $g(x) = \frac{x+1}{1-x}$ .

Q.3: For what value of 'k' so that  $f(x)$  is continuous

$$f(x) = \begin{cases} 7x - 2, & x \leq 1 \\ kx^2, & x > 1 \end{cases}$$

Also find differentiability of function.

Q#4. Evaluate:  $\int x e^x dx$

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FAST – National University of Computer & Emerging Sciences

Computer Science Department

*QUIZ*

CALCULUS AND ANALYTICAL GEOMETRY

Time Allowed: 25 min

FALL 2023

Max. Marks: 3marks 15 point

Q#1. Use L' Hospital's rule to find the limits of the following.

[10 Points]

$$(i) \lim_{t \rightarrow 0} \frac{te^{3t} - t}{1 - \cos(2t)} \quad (ii) \lim_{x \rightarrow 0} \left( \frac{1}{x} - \frac{1}{\sin x} \right)$$

Q#2. Find the values of  $a$  and  $b$  that makes  $f(x)$  is continuous everywhere.

$$f(x) = \begin{cases} \frac{x^2 - 4}{x - 2}, & x < 2 \\ ax^2 - bx + 3, & 2 \leq x \leq 3 \\ 2x - a - b, & x \geq 3 \end{cases}$$

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Q#1. Use L' Hospital's rule to find the limits of the following.

[10 Points]

$$(i) \lim_{x \rightarrow \frac{\pi}{4}} (1 - \tan x) \sec 2x, \quad (ii) \lim_{x \rightarrow 0^+} \left( \frac{1}{x} - \frac{1}{\sin x} \right)$$

Q#2. Find values of the constants  $k$  and  $m$ , if possible that will make the function  $f$  continuous everywhere.

[5 Points]

$$f(x) = \begin{cases} x^2 + 5 & x > 2 \\ m(x+1) + k & -1 < x \leq 2 \\ 2x^3 + x + 7 & x \leq -1 \end{cases}$$

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*QUIZ*

CALCULUS AND ANALYTICAL GEOMETRY

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Q#1. Use L'Hospital's rule to find the limits of the following.

|10 Points|

$$(i) \lim_{x \rightarrow \frac{\pi}{4}} (1 - \tan x) \sec 2x, \quad (ii) \lim_{x \rightarrow 0^+} \left( \frac{1}{x} - \frac{1}{\sin x} \right)$$

Q#2. Find the values of  $a$  that makes  $f(x)$  is continuous everywhere.

|5 Points|

$$f(x) = \begin{cases} \frac{\sqrt{x+4} - 2}{x} + 2a & x \neq 0 \\ 3a + 5 - x & , \quad x = 0 \end{cases}$$