Problem 1 (20 points) A Fibonacci word is defined through a concatenation of strings:

$$f_{1} = 1$$

$$f_{2} = 0$$

$$f_{3} = f_{2}f_{1} = 01$$

$$f_{4} = f_{3}f_{2} = 010$$

$$f_{5} = f_{4}f_{3} = 01001$$

$$\vdots$$

$$f_{n} = f_{n-1}f_{n-2}$$

(see also https://en.wikipedia.org/wiki/Fibonacci_word_fractal).

A Fibonacci fractal is defined on the plane by the following algorithm ($|f_n|$ is the number of digits in f_n)

```
Input: n
Compute: nth Fibonacci word for each digit at position k=1,2,\ldots |f_n| draw a segment forward if digit is 0 if k is even then turn left by 90^o else turn right by 90^o
```

You need to implement this algorithm in the following function, which must produce an image corresponding to the nth Fibonacci word.

```
int fib(int n, int x, int y, int step, RGB bc, RGB fc, int w, int h,
   RGB* image)
/*Input
  n >= 3
  x,y starting position
  step>=2 how many pixels to move when drawing a segment forward
  bc background color
  fc foreground, drawing color
  w width of image in pixels
  h height of image in pixels
  The input x,y must be in [0,w-1] and [0,h-1], respectively.
   image is a pointer to a w*h array of RGB values
 Returns
   O if this function fails, e.g. if a step results in coordinates
       outside the image window or if unable to allocate memory.
  >0 the number of steps the algorithm takes, which is also the
     length of the nth Fibonacci word.
```

From the initial position, draw the first segment vertically up.

The RGB data type is defined in bmp.h. Do not change this file.

```
#ifndef BMP_H_
#define BMP_H_
typedef struct {
    /* red, green, and blue values */
    unsigned char r, g, b;
} RGB;
void saveBMP(char* file, int width, int height, RGB* image);
#endif
```

The function saveBPM stores an image in a bmp file (see e.g. https://en.wikipedia.org/wiki/BMP_file_format). This function is provided as file bmp.c.

You can use the provided main program, main_fib.c.

Store your implementation in a file with name fib.c. Create a makefile similar to this one

so when make fib; make runall is typed, the four bmp files will be created. You may want to convert them to jpg format. On mills, you can do this by

```
convert fib7.bmp fig7.jpg
```

(convert is from ImageMagic, https://www.imagemagick.org).

Submit

- Avenue: fib.c and your makefile. Do not submit image files.
- Hardcopy: fib.c, makefile, and your images printed

Correct images receive:

n	points
7	3
9	4
25	6
26	7

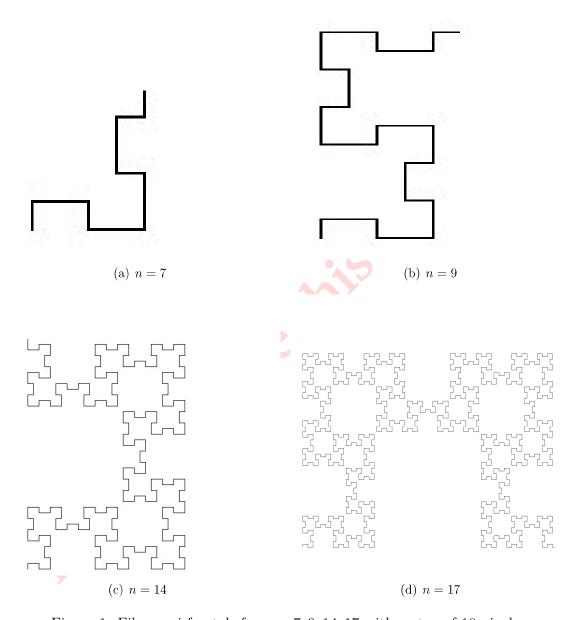


Figure 1: Fibonacci fractals for n=7,9,14,17 with a step of 10 pixels

If we execute make fib and then make runall and nothing is produced, this problem receives 0 marks.

In Figure 1 you can see some of my output. Note your drawing may not start exactly as mine, but you should get the overall plots.

Problem 2 (5 points) Profile the execution of

./fib 30 10 10 5 29000 12000 fib30.bmp

If you cannot reach n = 30, profile with the largest n for which your program works.

Submit a hard copy of your profiling data. Which line(s) of your fib function take most of the time? Explain why.

We will discuss in class and tutorials how to obtain profiling data. You can also read e.g. https://www.thegeekstuff.com/2012/08/gprof-tutorial/ and the more detailed https://ftp.gnu.org/old-gnu/Manuals/gprof-2.9.1/html_chapter/gprof_2.html.

Bonus (3 points) If you can produce an image with n = 34 and step = 2. Submit a hardcopy of it and also the values of x, y, step, w, h you have used.

For fun Optimize your implementation for speed as much as you can.

Compile on mills with an optimization option -02 and then execute on mills

./fib 30 10 10 5 29000 12000 fib30.bmp

Record the steps per second output of the main program at

https://docs.google.com/spreadsheets/d/1GOr-NMUkISSUZOYLBuqOxAhub9P7JgOLWwhJ19MDHJI/edit#gid=0.

I have entered the number from my unoptimized version.

Problem 3 (10 points) In image filtering, an image is convoluted with an $n \times n$ kernel. You can read about convolution of images at https://en.wikipedia.org/wiki/Kernel_(image_processing)#Origin. Also, image convolutions are a basic building block in convolutional neural networks.

The Portable Pixmap Format (PPM) uses ASCII encoding of pixels for image files; for details, see https://en.wikipedia.org/wiki/Netpbm_format#PPM_example.

You can generate a PPM file from a JPG file using

convert -compress none file.jpg file.ppm

On Linux, you can use gimp to view a PPM file. On Mac OS X, simply use open.

Implement a program, name it filter, such that when executed as

./filter input.ppm kernel output.ppm

it reads a PPM image stored in file input.ppm, reads a kernel stored in file kernel, applies the kernel on the image, and writes the resulting image into file output.ppm.

The format of kernel is

n

scale

n rows of n numbers each

For example the 3×3 mean filter

$$\frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

is specified in a text file as

3

9

1 1 1

1 1 1

1 1 1

You can use zero padding. That is, when part of the filter is outside the image, the values that are outside are convoluted with zeros.

For reading and writing PPM files, you can find source code on the Internet. Submit

- Avenue: your source code and a makefile. When make is typed, the executable filter must be created.
- Hardcopy: your source code.

Problem 4 (10 points) You are given the CSV file cities.csv. Write a C program that reads this file and outputs a CSV file with name sorted.csv with columns

city population country

where the rows are sorted in decreasing order by population. For example, the first three rows are

Tokyo,22006299,Japan Mumbai,15834918,India Mexico City,14919501,Mexico

For this problem, you must use the qsort function from the standard C library to sort. See man qsort.

Store your implementation in a file with name cities.c. Submit it to avenue and also a hardcopy of it.