Package 'boss'

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Description An implementation of best orthogonalized subset selection (BOSS) and forward stepwise selection (fs), together with feasible selection rules to choose the best candidate subset.
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boss	Best orthogonalized subset selection (BOSS).

Description

- Compute the solution path of BOSS and forward stepwise selection (FS).
- Compute various information criteria based on a heuristic degrees of freedom that can serve as the selection rule to choose the optimal subset given by BOSS. Only work when n>p.

Usage

```
boss(x, y, intercept = FALSE, fs.only = FALSE, hdf.ic.boss = TRUE,
    ...)
```

Arguments

X	A matrix of predictors, with $nrow(x) = length(y) = n$ observations and $ncol(x) = p$ predictors. Intercept shall not be included.
У	A vector of response variable, with length(y)=n.
intercept	Whether to include an intercept term.
fs.only	Whether to ignore BOSS and perform FS only.
hdf.ic.boss	Whether to calculate the heuristic degrees of freedom (hdf) and information criteria (IC) for BOSS. IC includes AIC, BIC, AICc, BICc, GCV, Cp. Note that if the option fs.only=TRUE or n<=p, hdf.ic.boss=FALSE no matter what.
	Extra parameters to allow flexibility. Currently none argument allows or requires, just for the convinience of call from other parent functions like cv.boss.

Details

This function computes the full solution path given by FS and (or) BOSS on a given dataset (x,y) with n observations and p predictors. Meanwhile, in the case where n>p, it calculates the heuristic degrees of freedom for BOSS, and various information criteria, which can further be used to select the optimal candidate along the path. Please refer to the example section below for implementation details and Tian et al. (2018) for methodology details.

Value

- beta_fs: A matrix of regression coefficients for each step performed by FS, from a null model until stop, with nrow=p and ncol=min(n,p)+1, where min(n,p) is the maximum number of steps performed.
- beta_boss: A matrix of regression coefficients for each step performed by BOSS, with nrow=p and ncol=min(n,p)+1. Note that unlike beta_fs and due to the nature of BOSS, the number of non-zero components in columns of beta_boss may not be unique, i.e. there maybe multiple columns corresponding to the same size of subset. beta_boss=NULL if the option fs.only=TRUE.
- steps_fs: A vector of numbers representing which predictor joins at each step, with length(steps_fs)=min(n,p).
- hdf_boss: A vector of heuristic degrees of freedom (hdf) for BOSS, with length(hdf_boss)=p+1. Note that hdf_boss=NULL if n<=p or hdf.ic.boss=FALSE.

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• IC_boss: A list of information criteria (IC) for BOSS, where each element in the list is a vector representing values of a given IC for each candidate subset of BOSS (or each column in beta_boss). The output IC includes AIC, BIC, AICc, BICc, GCV and Mallows' Cp. Note that each IC is calculated by plugging in hdf_boss.

Author(s)

Sen Tian

References

Tian, Hurvich and Simonoff (2018), On the use of information criterion in least squares based subset selection problems. (Link to be added)

Examples

```
# Generate a trivial dataset, X has mean 0 and norm 1, y has mean 0
n = 20
p = 5
x = matrix(rnorm(n*p), nrow=n, ncol=p)
x = scale(x, center = colMeans(x))
x = scale(x, scale = sqrt(colSums(x^2)))
beta = c(1, 1, 0, 0, 0)
y = x%*%beta + scale(rnorm(20, sd=0.01), center = TRUE, scale = FALSE)
# run the model
boss_result = boss(x, y)
# select the best candidate along the path based on IC
beta_boss_aicc = boss_result$beta_boss[, which.min(boss_result$IC_boss$aicc), drop=FALSE]
# Same purpose, use the S3 function
beta_boss_aicc = coef(boss_result)$boss
# fitted values for the first observation
mu_boss_aicc = x[1,] %*% beta_boss_aicc
# Same purpose, use the S3 function
mu_boss_aicc = predict(boss_result, newx=x[1,])$boss
# Mallow's Cp
beta_boss_cp = boss_result$beta_boss[, which.min(boss_result$IC_boss$cp), drop=FALSE]
# Same purpose, use the S3 function
beta_boss_cp = coef(boss_result, method.boss='cp')$boss
# fitted values for the first observation
mu_boss_cp = x[1,] %*% beta_boss_cp
# Same purpose, use the S3 function
mu_boss_cp = predict(boss_result, newx=x[1,], method.boss='cp')$boss
```

calc.ic

Calculate information criterion.

Description

Calculate a specified information criterion (IC) for an estimate or a group of estimates. Such IC includes AIC, BIC, AICc, BICc, GCV and Mallows' Cp.

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Usage

```
calc.ic(y_hat, y, method = c("aicc", "bicc", "aic", "bic", "gcv", "cp"),
   df, sigma = NULL)
```

Arguments

y_hat	A vector of fitted values with length(y_hat)=length(y)=n, or a matrix, with nrow(coef)=length(y)=n and ncol(y_hat)=m, containing m different fits.
у	A vector of response variable, with length(y)=n.
method	A specified IC to calculate. Default is AICc ('aicc'). Other choices include AIC ('aic'), BIC ('bic'), BICc ('bicc'), GCV ('gcv') and Mallows' Cp ('cp').
df	A number if y_hat is a vector, or a vector with length(df)=ncol(y_hat)=m if y_hat is a matrix. df represents the degrees of freedom for each fit.
sigma	Standard deviation of the error term. It only needs to be specified if method='cp'.

Details

This function enables the computation of various common IC for model fits, which can further be used to choose the optimal fit. This allows user comparing the effect of different IC. In order to calculate IC, df needs to be specified. To be more specific, here are the formulas used to calculate each IC:

$$AIC = \log(\frac{RSS}{n}) + 2\frac{df}{n}$$

$$BIC = \log(\frac{RSS}{n}) + \log(n)\frac{df}{n}$$

$$AICc = \log(\frac{RSS}{n}) + 2\frac{df+1}{n-df-2}$$

$$BICc = \log(\frac{RSS}{n}) + \log(n)\frac{df+1}{n-df-2}$$

$$GCV = \frac{RSS}{(n-df)^2}$$

$$Mallows'Cp = RSS + 2 \times \sigma^2 \times df$$

Value

The value(s) of the specified IC for each fit.

Author(s)

Sen Tian

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Examples

```
\# Generate a trivial dataset, X has mean 0 and norm 1, y has mean 0
set.seed(11)
n = 20
p = 5
x = matrix(rnorm(n*p), nrow=n, ncol=p)
x = scale(x, center = colMeans(x))
x = scale(x, scale = sqrt(colSums(x^2)))
beta = c(1, 1, 0, 0, 0)
y = x\%*beta + scale(rnorm(20, sd=0.01), center = TRUE, scale = FALSE)
# run the model
boss_result = boss(x, y)
# what are the values of AICc for all candidates of BOSS?
print(boss_result$IC_boss$aicc)
# calculate them manually using the calc.ic function
print(calc.ic(x%*%boss_result$beta_boss, y, df=boss_result$hdf_boss))
# they shall match
```

coef.boss

Select coefficient vector(s) from boss object.

Description

This function returns coefficient vector(s) for given step(s) of FS and BOSS. For BOSS, it can also return the optimal coefficient vector selected by AICc (by default) or other IC.

Usage

```
## S3 method for class 'boss'
coef(object, select.fs = NULL, select.boss = NULL,
 method.boss = c("aicc", "bicc", "aic", "bic", "gcv", "cp"), ...)
```

Arguments

object	The boss object, returned from calling 'boss' function.
select.fs	Given step(s) of FS, corresponding to columns in the coefficient matrix. For example, the first column in beta_fs corresponds to step 1, the second column corresponds to step 2, etc. We enforce the first column, that has all 0 entries, to be step 1, just for convinience of usage.
select.boss	Given columns(s) in beta_boss, similar to select.fs.
method.boss	Which IC is used to select the optimal coefficient vector for BOSS.
	Extra arguments (unused for now)

Details

If select.fs or select.boss is specified, the function returns corresponding column(s) in the coefficient matrix.

If select.fs is unspecified, we return the entire coefficient matrix (beta_fs) for FS, since we currently do not have a hands-on way of calculating IC for FS. But user can use their own rules and specify e.g. select.fs=which.min(rule) in order to pick the optimal coefficient vector.

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If select.boss is unspecified, we will try to return the optimal coefficient vector selected by AICc-hdf (other choice of IC can be specified in method.boss). The only exception is when n>=p, where hdf is not well defined, and we will return the entire coefficient matrix.

Value

- fs: The chosen coefficient vector(s) for FS.
- boss: The chosen coefficient vector(s) for FS.

Examples

```
# See the example in the section of \code{boss}. Or type ?boss in R.
```

coef.cv.boss

Select coefficient vector based on cross validation (CV).

Description

This function returns coefficient vector that minimizes out-of-sample (OOS) cross validation score.

Usage

```
## S3 method for class 'cv.boss'
coef(object, ...)
```

Arguments

object The cv.boss object, returned from calling 'cv.boss' function.

... Extra arguments (unused for now).

Value

- fs: The chosen coefficient vector for FS.
- boss: The chosen coefficient vector for FS.

Examples

```
\# See the example in the section of \code{cv.boss}. Or type ?cv.boss in R.
```

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cv.boss Cross validation for BOSS.	
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Description

Cross validation for BOSS and FS.

Usage

```
cv.boss(x, y, n.folds=10, n.rep=1, ...)
```

Arguments

x	A matrix of predictors, see boss.
У	A vector of response variable, see boss.
n.folds	The number of cross validation folds.
n.rep	The number of replications of cross validation.
•••	Arguments to boss.

Details

This function fits BOSS and FS (boss) on the full dataset, and performs n.folds cross validation. The cross validation process can be repeated n.rep times to evaluate the out-of-sample (OOS) performance for the candidate subsets given by both methods.

Value

- boss: An object boss that fits on the full dataset.
- n.folds: The number of cross validation folds.
- cvm.fs: Mean OOS deviance for each candidate given by FS.
- cvm.boss: Mean OSS deviance for each candidate given by BOSS.
- i.min.fs: The index of minimum cvm.fs.
- i.min.boss: The index of minimum cvm.boss.

Author(s)

Sen Tian

References

Tian, Hurvich and Simonoff (2018), On the use of information criterion in least squares based subset selection problems. (Link to be added)

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Examples

```
\# Generate a trivial dataset, X has mean 0 and norm 1, y has mean 0
set.seed(11)
n = 20
p = 5
x = matrix(rnorm(n*p), nrow=n, ncol=p)
x = scale(x, center = colMeans(x))
x = scale(x, scale = sqrt(colSums(x^2)))
beta = c(1, 1, 0, 0, 0)
y = x\%*\%beta + scale(rnorm(20, sd=0.01), center = TRUE, scale = FALSE)
# perform 10-fold CV without replication
boss_cv_result = cv.boss(x, y, n.folds = 2)
boss_result = boss_cv_result$boss
# select the best candidate based on minimum CV OSS score
beta_boss_cv = boss_result$beta_boss[, boss_cv_result$i.min.boss, drop=FALSE]
# Same purpose, using the S3 function
beta_boss_cv = coef(boss_cv_result)$boss
# fitted values for the first observation
mu_boss_cv = x[1,] %*% beta_boss_cv
# Same purpose, use the S3 function
mu_boss_cv = predict(boss_cv_result, newx=x[1,])$boss
```

predict.boss

Prediction given new data entries.

Description

This function returns the prediction(s) given new observation(s), for FS and BOSS, where the optimal coefficient vector is chosen via certain selection rule.

Usage

```
## S3 method for class 'boss'
predict(object, newx, ...)
```

Arguments

object The boss object, returned from calling 'boss' function.

A new data entry or several entries. It can be a vector, or a matrix with nrow(newx) being the number of new entries and ncol(newx)=p being the number of predictors. The function takes care of the intercept, NO need to add 1 to newx.

Extra arguments to be plugged into coef, such as select.boss, see the description of coef for more details.

Details

The function basically calculates x*coef, where coef is a coefficient vector chosen by a selection rule. See more details about the default and available choices of the selection rule in the description of coef.boss.

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Value

- fs: The prediction(s) for FS.
- boss: The prediction(s) for BOSS.

Examples

#See the example in the section of \code{boss}. Or type ?boss in R.

predict.cv.boss

Prediction given new data entries.

Description

This function returns the prediction(s) given new observation(s), for FS and BOSS, where the optimal coefficient vector is chosen via cross-validation.

Usage

```
## S3 method for class 'cv.boss'
predict(object, newx, ...)
```

Arguments

object The cv.boss object, returned from calling 'cv.boss' function.

newx A new data entry or several entries. It can be a vector, or a matrix with nrow(newx)

being the number of new entries and ncol(newx)=p being the number of predictors. The function takes care of the intercept, NO need to add 1 to newx.

... Extra arguments (unused for now).

Value

- fs: The prediction for FS.
- boss: The prediction for BOSS.

Examples

See the example in the section of $\code{cv.boss}$. Or type ?cv.boss in R.

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