

Assignment Two

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Question One

Derivation

You will find the derivation tree below for the modified Missionaries and Cannibals problem, with four members of each party. A small problem arises since the boat's capacity is $n - 1$, where n is the members of one party, and both partys have n members.

Assume the same starting conditions, where c is the number of cannibals and m is the number of missionaries on the target side of the river. All cannibals and missionaries are on the starting side of the river, thus $c = 0$ and $m = 0$.

$$\begin{aligned}
 S(c, m) &\rightarrow^1 A(1, 1) \\
 &\rightarrow^2 p(1, 1) A(3, 0) \\
 &\rightarrow^2 p(1, 1) p(3, 0) A(2, 2) \\
 &\rightarrow^2 p(1, 1) p(3, 0) p(2, 2) A(1, 3) \\
 &\rightarrow^2 p(1, 1) p(3, 0) p(2, 2) p(1, 3) A(2, 3) \\
 &\rightarrow^2 p(1, 1) p(3, 0) p(2, 2) p(1, 3) p(2, 3) A(3, 3) \\
 &\rightarrow^2 p(1, 1) p(3, 0) p(2, 2) p(1, 3) p(2, 3) p(3, 3) A(3, 4) \\
 &\rightarrow^2 p(1, 1) p(3, 0) p(2, 2) p(1, 3) p(2, 3) p(3, 3) p(3, 4) A(4, 4) \\
 &\rightarrow^3 p(1, 1) p(3, 0) p(2, 2) p(1, 3) p(2, 3) p(3, 3) p(3, 4) p(4, 4)
 \end{aligned} \tag{1}$$

Grammar

Below is the general controlled grammar for the Missionaries and Cannibals problem. Most of the changes occur in the functions and predicates.

Let c be the number of cannibals and m be the number of missionaries on the target side of the river, and n be the number of members in each party. If we assume the capacity of the boat is also n , then much of the problem stays the same.

L	Q	Kernel	F _T	F _F
1	Q ₁	$S(c, m) \rightarrow A(c + 1, m + 1)$	$\{2\}$	\emptyset
2	Q ₂	$A(c, m) \rightarrow p(c, m) A(f_1(c, m), f_2(m))$	$\{2\}$	$\{3\}$
3	Q ₃	$A(c, m) \rightarrow p(c, m)$	\emptyset	\emptyset

- Predicates

- $Q_1 = \text{true}$
- $Q_2(c, m) = \text{true}$ if $(c > 0 \wedge c < n) \vee (m > 0 \wedge m < n)$
- $Q_3(c, m) = \text{false}$ if $(c = n \wedge m = n) \vee ((c > m) \vee (3 - c) > (3 - m))$

- Functions

- The functions stay the same as well, only replacing n where there are $/3/s$.

Question Two

Grammar

Below is a derivation for the Tower of Hanoi with four pivots and n disks.

L	Q	Kernel	F_T	F_F
1	Q_1	$S(n,x,y,z) \rightarrow A(n,x,y,z)$	$\{2\}$	\emptyset
2	Q_2	$A(n,x,y,z) \rightarrow A(f_1(n),x,f_2(x,y,z),z), \setminus (n,x,y,z)A(f_1(n),f_2(x,y,z),y,z)$	$\{2\}$	$\{3\}$
3	Q_3	$A(n,x,y,z) \rightarrow p(n,x,y,z)$		

Derivation