

# Flow Around an Inclined NACA 0012 Airfoil

## Introduction

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This example simulates the flow around an inclined NACA 0012 airfoil using the SST turbulence model and compares the results with the experimental lift data of Ladson ([Ref. 1](#)) and pressure data of Gregory and O'Reilly ([Ref. 2](#)). The SST model combines the near-wall capabilities of the  $k-\omega$  model with the superior free-stream behavior of the  $k-\varepsilon$  model to enable accurate simulations of a wide variety of internal and external flow problems. See the theory for the SST turbulence model in the *CFD Module User's Guide* for further information.

## Model Definition

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Consider the flow relative to a reference frame fixed on a NACA 0012 airfoil with chord-length  $c = 1.8$  m. The temperature of the ambient air is 20 °C and the relative free-stream velocity is  $U_\infty = 50$  m/s resulting in a Mach number of 0.15. The Reynolds number based on the chord length is roughly  $6 \cdot 10^6$ , so you can assume that the boundary layers are turbulent over practically the entire airfoil. The airfoil is inclined at an angle  $\alpha$  to the oncoming stream,

$$(u_\infty, v_\infty) = U_\infty (\cos \alpha, \sin \alpha)$$

To obtain a sharp trailing edge, the airfoil is slightly altered from its original shape ([Ref. 3](#)),

$$y = \pm c \cdot 0.594689181 \cdot \left( 0.298222773 \cdot \sqrt{\frac{x}{c}} - 0.127125232 \cdot \frac{x}{c} - 0.357907906 \cdot \left(\frac{x}{c}\right)^2 + 0.291984971 \cdot \left(\frac{x}{c}\right)^3 - 0.105174696 \cdot \left(\frac{x}{c}\right)^4 \right)$$

The upstream, top, and bottom edges of the computational domain are located 100 chord-lengths away from the trailing edge of the airfoil and the downstream edge is located 200 chord-lengths away. This is to minimize the effect of the applied boundary conditions.

Figure 1 shows the flow domain and the applied far-field boundary conditions,

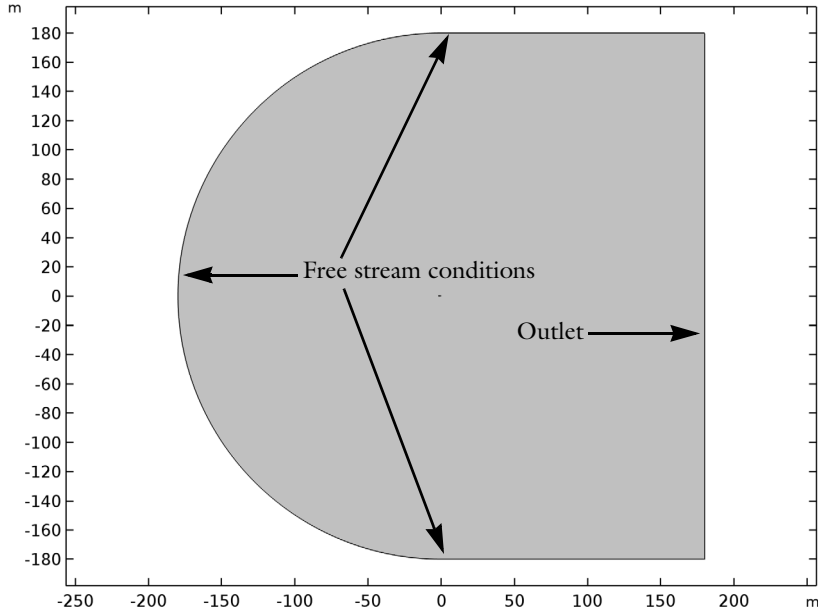


Figure 1: Flow domain and far-field boundary conditions.

Ref. 4 provides far-field values for the turbulence variables,

$$\omega_{\infty} = (1 \rightarrow 10) \frac{U_{\infty}}{L}, \quad \frac{\nu_{T\infty}}{\nu_{\infty}} = 10^{-(2 \rightarrow 5)}$$

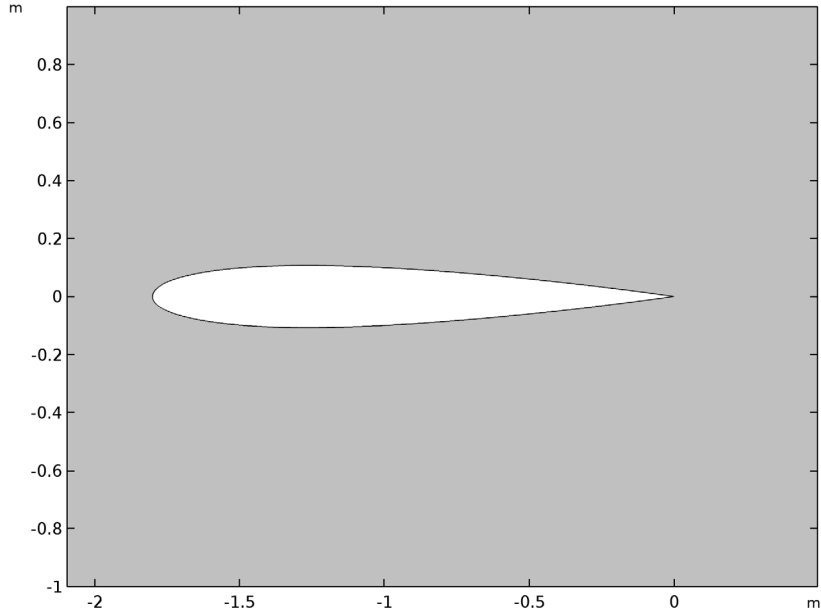
where the free-stream value of the turbulence kinetic energy is given by

$$k_{\infty} = \nu_{T\infty} \omega_{\infty}$$

and  $L$  is the appropriate length of the computational domain. The current model applies the upper limit of the provided free-stream turbulence values,

$$\omega_{\infty} = 10 \frac{U_{\infty}}{L}, \quad k_{\infty} = 0.1 \frac{\nu_{\infty} U_{\infty}}{L}$$

Figure 2 shows a close-up of the airfoil section. A no-slip condition is applied on the surface of the airfoil.



*Figure 2: Close-up of the airfoil section.*

The computations employ a structured mesh with a high size ratio between the outermost and wall-adjacent elements.

#### POTENTIAL FLOW SOLUTION

The simplest option when setting the initial velocity field is to use a constant velocity, which does not satisfy the wall boundary conditions. A more accurate and robust initial guess can be obtained solving the potential flow equation.

Assuming irrotational, inviscid flow, the velocity potential  $\phi$  is defined as

$$\mathbf{u} = -\nabla\phi$$

The velocity potential  $\phi$  must satisfy the continuity equation for incompressible flow,  $\nabla \cdot \mathbf{u} = 0$ . The continuity equation can be expressed as a Laplace equation

$$\nabla \cdot (-\nabla\phi) = 0$$

which is the potential flow equation.

Once the velocity potential  $\phi$  is computed, the pressure can be approximated using Bernoulli's equation for steady flows:

$$p = -\frac{\rho}{2}|\nabla\phi|^2$$

## Results and Discussion

The study performs a Parametric Sweep with the angle of attack  $\alpha$  taking the values,

$$\alpha = 0^\circ, 2^\circ, 4^\circ, 6^\circ, 8^\circ, 10^\circ, 12^\circ, 14^\circ$$

Figure 3 shows the velocity magnitude and the streamlines for the steady flow around the NACA 0012 profile at  $\alpha = 14^\circ$ .

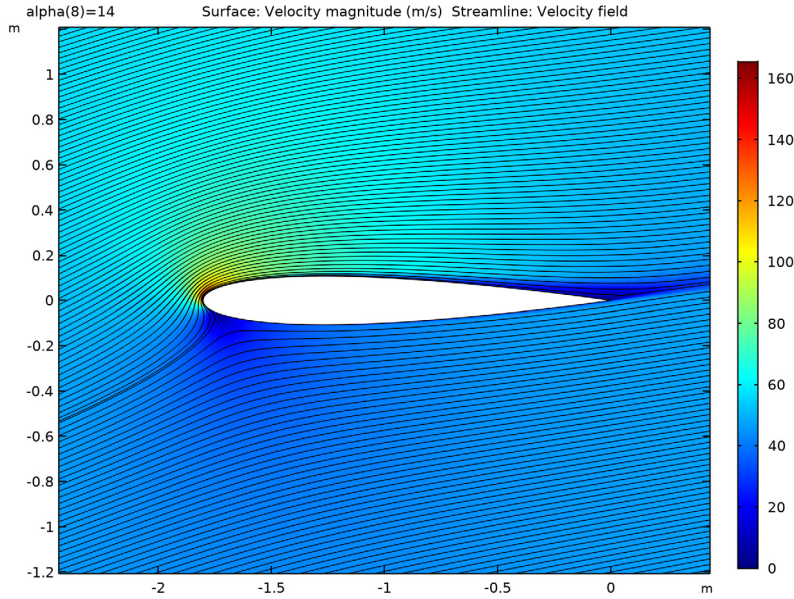


Figure 3: Velocity magnitude and streamlines for the flow around a NACA 0012 airfoil.

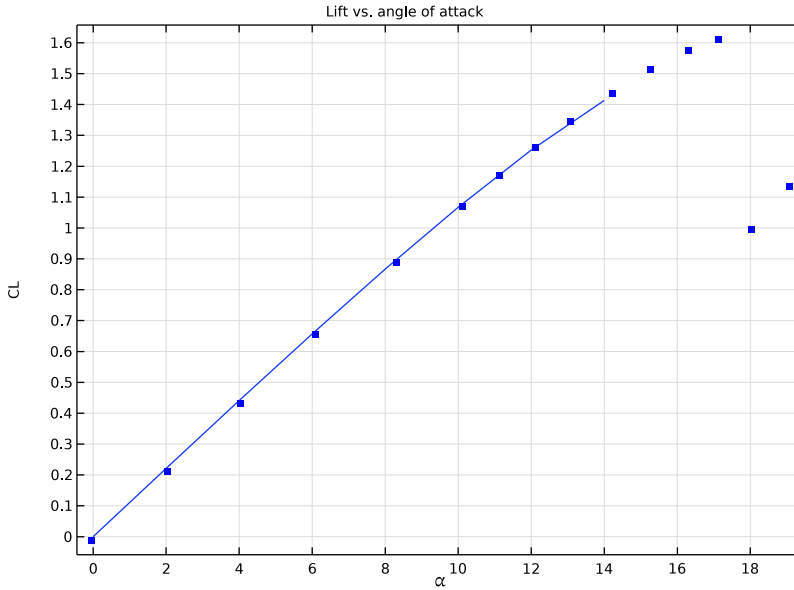
A small separation bubble appears at the trailing edge for higher values of  $\alpha$  and the flow is unlikely to remain steady and two-dimensional hereon. Ref. 1 provides experimental data for the lift coefficient versus the angle of attack,

$$C_L(\alpha) = \oint_c (c_p(s)/c)(n_y(s)\cos(\alpha) - n_x(s)\sin(\alpha)) ds$$

where the pressure coefficient is defined as,

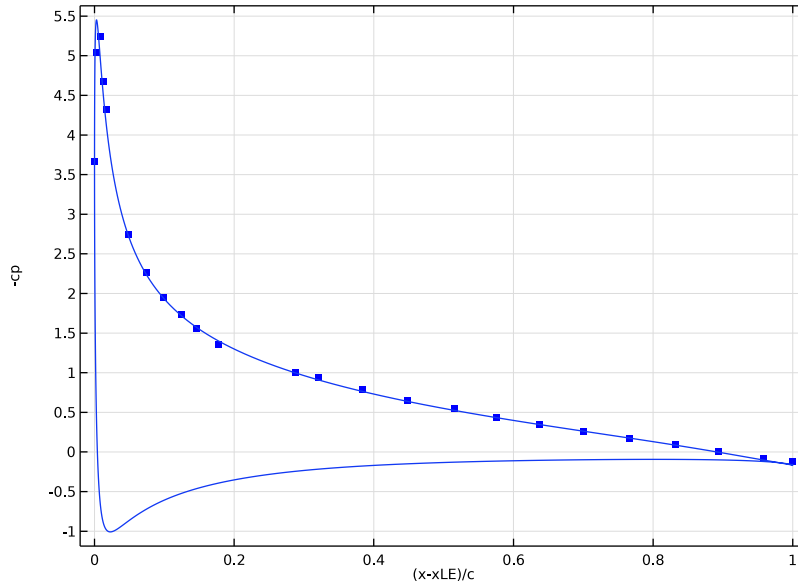
$$c_p(s) = \frac{p(s) - p_\infty}{\frac{1}{2}\rho_\infty U_\infty^2}$$

and  $c$  is the chord length. Note that the normal is directed outward from the flow domain (into the airfoil). [Figure 4](#) shows computational and experimental results for the lift coefficient versus angle of attack.



*Figure 4: Computational (solid) and experimental (dots) results for the lift coefficient vs. angle of attack.*

No discernible discrepancy between the computational and experimental results occurs within the range of  $\alpha$  values used in the computations. The experimental results continue through the parameter regime where the airfoil stalls. [Figure 5](#) shows a comparison between the computed pressure coefficient at  $\alpha = 10^\circ$  and the experimental results in [Ref. 2](#).



*Figure 5: Computational (solid) and experimental (dots) results for the pressure coefficient along the airfoil.*

Experimental data is only available on the low-pressure side of the airfoil. The agreement between the computational and experimental results is very good.

### *Notes About the COMSOL Implementation*

The model uses the SST turbulence model together with a Parametric Sweep for the angle of attack to compute the different flows on a mapped mesh.

The initial values for the velocity components are obtained by solving a potential flow equation, which is set up using a PDE interface.

### *References*

1. C.L. Ladson, "Effects of Independent Variation of Mach and Reynolds Numbers on the Low-Speed Aerodynamic Characteristics of the NACA 0012 Airfoil Section," *NASA TM 4074*, 1988.

2. N. Gregory and C. L. O'Reilly, "Low-Speed Aerodynamic Characteristics of NACA 0012 Aerofoil Section, including the Effects of Upper-Surface Roughness Simulating Hoar Frost," *A.R.C., R. & M.* no. 3726, 1970.
3. NASA Langley Research Centre, Turbulence Modeling Resource, "2D NACA 0012 Airfoil Validation Case," [http://turbmodels.larc.nasa.gov/naca0012\\_val.html](http://turbmodels.larc.nasa.gov/naca0012_val.html)
4. F.R. Menter, "Two-Equation Eddy-Viscosity Models for Engineering Applications," *AIAA Journal*, vol. 32, no. 8, pp. 1598–1605, 1994.

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**Application Library path:** CFD\_Module/Verification\_Examples/  
naca0012\_airfoil

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### *Modeling Instructions*

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From the **File** menu, choose **New**.

#### **NEW**

In the **New** window, click **Model Wizard**.

#### **MODEL WIZARD**

- 1 In the **Model Wizard** window, click **2D**.
- 2 In the **Select Physics** tree, select **Mathematics>Classical PDEs>Laplace Equation (lpeq)**.
- 3 Click **Add**.
- 4 Click **Study**.
- 5 In the **Select Study** tree, select **General Studies>Stationary**.
- 6 Click **Done**.

#### **LAPLACE EQUATION (LPEQ)**

- 1 In the **Model Builder** window, under **Component 1 (comp1)** click **Laplace Equation (lpeq)**.
- 2 In the **Settings** window for **Laplace Equation**, click to expand the **Dependent Variables** section.
- 3 In the **Dependent variable** text field, type  $\phi$ .

#### **ADD PHYSICS**

- 1 In the **Home** toolbar, click **Add Physics** to open the **Add Physics** window.



- 2 Go to the **Add Physics** window.
- 3 In the tree, select **Fluid Flow>Single-Phase Flow>Turbulent Flow>Turbulent Flow, SST (spf)**.
- 4 Click **Add to Component 1** in the window toolbar.
- 5 In the **Model Builder** window, click **Component 1 (comp1)**.
- 6 In the **Home** toolbar, click **Add Physics** to close the **Add Physics** window.

## GLOBAL DEFINITIONS

### *Parameters 1*

- 1 In the **Settings** window for **Parameters**, locate the **Parameters** section.
- 2 In the table, enter the following settings:

Name	Expression	Value	Description
U_inf	50[m*s <sup>-1</sup> ]	50 m/s	Free-stream velocity
rho_inf	1.2043[kg*m <sup>-3</sup> ]	1.2043 kg/m <sup>3</sup>	Free-stream density
mu_inf	1.81397e-5[kg*m <sup>-1</sup> *s <sup>-1</sup> ]	1.814E-5 kg/(m*s)	Free-stream dynamic viscosity
L	180[m]	180 m	Domain reference length
c	1.8[m]	1.8 m	Chord length
k_inf	0.1*mu_inf*U_inf/(rho_inf*L)	4.184E-7 m <sup>2</sup> /s <sup>2</sup>	Free-stream turbulent kinetic energy
om_inf	10*U_inf/L	2.7778 1/s	Free-stream specific dissipation rate
alpha	0	0	Angle of attack

## GEOMETRY 1

### *Circle 1 (c1)*

- 1 In the **Geometry** toolbar, click **Circle**.
- 2 In the **Settings** window for **Circle**, locate the **Size and Shape** section.
- 3 In the **Radius** text field, type L.
- 4 In the **Sector angle** text field, type 90.
- 5 Locate the **Rotation Angle** section. In the **Rotation** text field, type 90.

### *Parametric Curve 1 (pc1)*

- 1 In the **Geometry** toolbar, click **More Primitives** and choose **Parametric Curve**.
- 2 In the **Settings** window for **Parametric Curve**, locate the **Expressions** section.

- 3 In the **x** text field, type  $c*s$ .
- 4 In the **y** text field, type  $c*0.594689181*(0.298222773*\sqrt{s})-0.127125232*s-0.357907906*s^2+0.291984971*s^3-0.105174696*s^4$ .
- 5 Locate the **Position** section. In the **x** text field, type  $-c$ .

#### *Union I (unil)*

- 1 In the **Geometry** toolbar, click **Booleans and Partitions** and choose **Union**.
- 2 Click in the **Graphics** window and then press Ctrl+A to select both objects.

#### *Delete Entities I (dell)*

- 1 In the **Model Builder** window, right-click **Geometry I** and choose **Delete Entities**.
- 2 In the **Settings** window for **Delete Entities**, locate the **Entities or Objects to Delete** section.
- 3 From the **Geometric entity level** list, choose **Domain**.
- 4 On the object **unil**, select Domain 2 only.
- 5 Click **Build All Objects**.
- 6 Click **Build Selected**.

#### *Rectangle I (rl)*

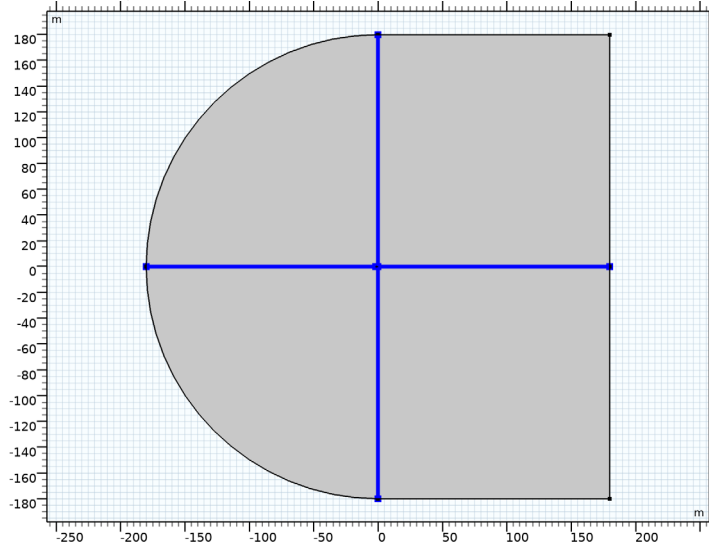
- 1 In the **Geometry** toolbar, click **Rectangle**.
- 2 In the **Settings** window for **Rectangle**, locate the **Size and Shape** section.
- 3 In the **Width** text field, type L.
- 4 In the **Height** text field, type L.
- 5 Click **Build Selected**.
- 6 Click the **Zoom Extents** button in the **Graphics** toolbar.

#### *Mirror I (mirI)*

- 1 In the **Geometry** toolbar, click **Transforms** and choose **Mirror**.
- 2 In the **Settings** window for **Mirror**, locate the **Input** section.
- 3 Select the **Keep input objects** check box.
- 4 Click in the **Graphics** window and then press Ctrl+A to select both objects.
- 5 Locate the **Normal Vector to Line of Reflection** section. In the **x** text field, type 0.
- 6 In the **y** text field, type 1.
- 7 Click **Build Selected**.
- 8 Click the **Zoom Extents** button in the **Graphics** toolbar.

### Mesh Control Edges 1 (mce1)

- 1 In the **Geometry** toolbar, click **Virtual Operations** and choose **Mesh Control Edges**.
- 2 On the object **fin**, select Boundaries 1, 2, 4, and 5 only.



- 3 In the **Geometry** toolbar, click **Build All**.

### ADD MATERIAL

- 1 In the **Home** toolbar, click **Add Material** to open the **Add Material** window.
- 2 Go to the **Add Material** window.
- 3 In the tree, select **Liquids and Gases>Gases>Air**.
- 4 Click **Add to Component** in the window toolbar.
- 5 In the **Home** toolbar, click **Add Material** to close the **Add Material** window.

### LAPLACE EQUATION (LPEQ)

- 1 In the **Model Builder** window, under **Component 1 (comp1)** click **Laplace Equation (lpeq)**.
- 2 In the **Settings** window for **Laplace Equation**, locate the **Units** section.
- 3 Click **Define Dependent Variable Unit**.
- 4 In the **Dependent variable quantity** table, enter the following settings:

Dependent variable quantity	Unit
Custom unit	$\text{m}^2/\text{s}$

- 5 Click **Define Source Term Unit**.
- 6 In the **Source term quantity** table, enter the following settings:

Source term quantity	Unit
Custom unit	s <sup>-1</sup>

#### *Dirichlet Boundary Condition I*

- 1 In the **Physics** toolbar, click **Boundaries** and choose **Dirichlet Boundary Condition**.
- 2 In the **Settings** window for **Dirichlet Boundary Condition**, locate the **Boundary Selection** section.
- 3 Click **Paste Selection**.
- 4 In the **Paste Selection** dialog box, type 2 in the **Selection** text field.
- 5 Click **OK**.

#### *Flux/Source I*

- 1 In the **Physics** toolbar, click **Boundaries** and choose **Flux/Source**.
- 2 In the **Settings** window for **Flux/Source**, locate the **Boundary Selection** section.
- 3 Click **Paste Selection**.
- 4 In the **Paste Selection** dialog box, type 1 in the **Selection** text field.
- 5 Click **OK**.
- 6 In the **Settings** window for **Flux/Source**, locate the **Boundary Flux/Source** section.
- 7 In the *g* text field, type  $-n_x \cdot U_{\text{inf}}$ .

### **TURBULENT FLOW, SST (SPF)**

Since the density variation is not small, the flow cannot be regarded as incompressible. Therefore set the flow to be compressible.

- 1 In the **Model Builder** window, expand the **Component 1 (comp1)>Turbulent Flow, SST (spf)** node, then click **Turbulent Flow, SST (spf)**.
- 2 In the **Settings** window for **Turbulent Flow, SST**, locate the **Physical Model** section.
- 3 From the **Compressibility** list, choose **Compressible flow (Ma<0.3)**.
- 4 Locate the **Turbulence** section. From the **Wall treatment** list, choose **Low Re**.

#### *Fluid Properties I*

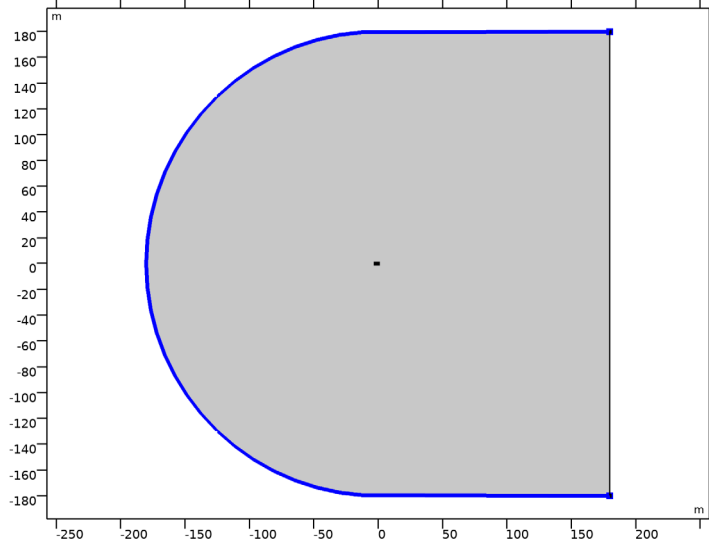
- 1 In the **Model Builder** window, under **Component 1 (comp1)>Turbulent Flow, SST (spf)** click **Fluid Properties I**.
- 2 In the **Settings** window for **Fluid Properties**, locate the **Distance Equation** section.

- 3 From the  $l_{\text{ref}}$  list, choose **Manual**.
- 4 In the text field, type 0.2.

#### *Inlet I*

- 1 In the **Physics** toolbar, click **Boundaries** and choose **Inlet**.
- 2 Select Boundary 1 only.

It might be easier to select the correct boundary by using the **Selection List** window. To open this window, in the **Home** toolbar click **Windows** and choose **Selection List**. (If you are running the cross-platform desktop, you find **Windows** in the main menu.)



- 3 In the **Settings** window for **Inlet**, locate the **Turbulence Conditions** section.
- 4 Click the **Specify turbulence variables** button.
- 5 In the  $k_0$  text field, type  $k_{\text{inf}}$ .
- 6 In the  $\omega_0$  text field, type  $\omega_{\text{inf}}$ .
- 7 Locate the **Velocity** section. Click the **Velocity field** button.
- 8 Specify the  $\mathbf{u}_0$  vector as

$U_{\text{inf}} \cos(\alpha \pi / 180)$	x
$U_{\text{inf}} \sin(\alpha \pi / 180)$	y

#### *Initial Values I*

- 1 In the **Model Builder** window, click **Initial Values I**.

- 2 In the **Settings** window for **Initial Values**, locate the **Initial Values** section.
- 3 Specify the **u** vector as

-phix	x
-phiy	y

- 4 In the  $p$  text field, type  $-spf.rho/2*(phix^2+phiy^2)$ .
- 5 In the  $k$  text field, type  $k_{inf}$ .
- 6 In the  $\omega$  text field, type  $\omega_{inf}$ .

#### *Open Boundary 1*

- 1 In the **Physics** toolbar, click **Boundaries** and choose **Open Boundary**.
- 2 Select Boundary 2 only.
- 3 In the **Settings** window for **Open Boundary**, locate the **Turbulence Conditions** section.
- 4 Click the **Specify turbulence variables** button.
- 5 In the  $k_0$  text field, type  $k_{inf}$ .
- 6 In the  $\omega_0$  text field, type  $\omega_{inf}$ .

### **MESH 1**

#### *Mapped 1*

- 1 In the **Model Builder** window, under **Component 1 (comp1)** right-click **Mesh 1** and choose **Mapped**.
- 2 In the **Settings** window for **Mapped**, locate the **Domain Selection** section.
- 3 From the **Geometric entity level** list, choose **Domain**.
- 4 Select Domain 3 only.
- 5 Click to expand the **Control Entities** section. Clear the **Smooth across removed control entities** check box.

#### *Distribution 1*

- 1 Right-click **Mapped 1** and choose **Distribution**.
- 2 Select Boundary 11 only.
- 3 In the **Settings** window for **Distribution**, locate the **Distribution** section.
- 4 From the **Distribution type** list, choose **Predefined**.
- 5 In the **Number of elements** text field, type 100.
- 6 In the **Element ratio** text field, type 15000000.

7 From the **Growth formula** list, choose **Geometric sequence**.

8 Select the **Reverse direction** check box.

#### *Distribution 2*

1 In the **Model Builder** window, right-click **Mapped 1** and choose **Distribution**.

2 Select Boundary 7 only.

3 In the **Settings** window for **Distribution**, locate the **Distribution** section.

4 From the **Distribution type** list, choose **Predefined**.

5 In the **Number of elements** text field, type 25.

6 In the **Element ratio** text field, type 25.

7 From the **Growth formula** list, choose **Geometric sequence**.

#### *Distribution 3*

1 Right-click **Mapped 1** and choose **Distribution**.

2 Select Boundary 12 only.

3 In the **Settings** window for **Distribution**, locate the **Distribution** section.

4 From the **Distribution type** list, choose **Predefined**.

5 In the **Number of elements** text field, type 25.

6 In the **Element ratio** text field, type 480000.

7 From the **Growth formula** list, choose **Geometric sequence**.

8 Select the **Reverse direction** check box.

#### *Distribution 4*

1 Right-click **Mapped 1** and choose **Distribution**.

2 Select Boundary 2 only.

3 In the **Settings** window for **Distribution**, locate the **Distribution** section.

4 In the **Number of elements** text field, type 100.

#### *Mapped 2*

1 In the **Model Builder** window, right-click **Mesh 1** and choose **Mapped**.

2 In the **Settings** window for **Mapped**, locate the **Domain Selection** section.

3 From the **Geometric entity level** list, choose **Domain**.

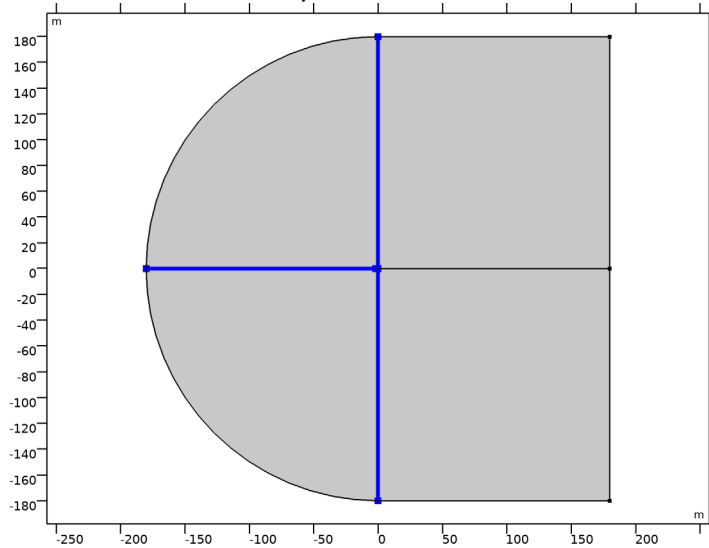
4 Select Domains 1 and 4 only.

5 Locate the **Control Entities** section. Clear the **Smooth across removed control entities** check box.

### *Distribution 1*

1 Right-click **Mapped 2** and choose **Distribution**.

2 Select Boundaries 9–11 only.



3 In the **Settings** window for **Distribution**, locate the **Distribution** section.

4 From the **Distribution type** list, choose **Predefined**.

5 In the **Number of elements** text field, type 100.

6 In the **Element ratio** text field, type 15000000.

7 From the **Growth formula** list, choose **Geometric sequence**.

### *Distribution 2*

1 In the **Model Builder** window, right-click **Mapped 2** and choose **Distribution**.

2 Select Boundaries 3 and 4 only.

3 In the **Settings** window for **Distribution**, locate the **Distribution** section.

4 From the **Distribution type** list, choose **Predefined**.

5 In the **Number of elements** text field, type 256.

6 In the **Element ratio** text field, type 256.

7 From the **Growth formula** list, choose **Geometric sequence**.

8 Select the **Symmetric distribution** check box.

### *Mapped 3*

1 In the **Model Builder** window, right-click **Mesh 1** and choose **Mapped**.



- 2 In the **Settings** window for **Mapped**, locate the **Domain Selection** section.
- 3 From the **Geometric entity level** list, choose **Domain**.
- 4 Select Domain 2 only.
- 5 Locate the **Control Entities** section. Clear the **Smooth across removed control entities** check box.

#### *Distribution 1*

- 1 Right-click **Mapped 3** and choose **Distribution**.
- 2 Select Boundary 10 only.
- 3 In the **Settings** window for **Distribution**, locate the **Distribution** section.
- 4 From the **Distribution type** list, choose **Predefined**.
- 5 In the **Number of elements** text field, type 100.
- 6 In the **Element ratio** text field, type 15000000.
- 7 From the **Growth formula** list, choose **Geometric sequence**.

#### *Distribution 2*

- 1 In the **Model Builder** window, right-click **Mapped 3** and choose **Distribution**.
- 2 Select Boundary 1 only.
- 3 In the **Settings** window for **Distribution**, locate the **Distribution** section.
- 4 From the **Distribution type** list, choose **Predefined**.
- 5 In the **Number of elements** text field, type 25.
- 6 In the **Element ratio** text field, type 25.
- 7 From the **Growth formula** list, choose **Geometric sequence**.
- 8 Select the **Reverse direction** check box.

#### *Distribution 3*

- 1 Right-click **Mapped 3** and choose **Distribution**.
- 2 Select Boundary 8 only.
- 3 In the **Settings** window for **Distribution**, locate the **Distribution** section.
- 4 In the **Number of elements** text field, type 100.
- 5 In the **Model Builder** window, click **Mesh 1**.
- 6 Click **Build All**.

#### **STUDY 1**

In the **Model Builder** window, expand the **Study 1** node.

### *Step 1: Stationary*

- 1 In the **Model Builder** window, expand the **Study 1** node, then click **Step 1: Stationary**.
- 2 In the **Settings** window for **Stationary**, locate the **Physics and Variables Selection** section.
- 3 In the table, clear the **Solve for** check box for the **Turbulent Flow, SST** interface.
- 4 In the **Home** toolbar, click **Compute**.

### **COMPONENT 1 (COMP1)**

In the **Model Builder** window, expand the **Component 1 (comp1)** node.

### **DEFINITIONS**

#### *View 1*

In the **Model Builder** window, expand the **Component 1 (comp1)>Definitions** node.

#### *Axis*

- 1 In the **Model Builder** window, expand the **View 1** node, then click **Axis**.
- 2 In the **Settings** window for **Axis**, locate the **Axis** section.
- 3 In the **x minimum** text field, type -2.5.
- 4 In the **x maximum** text field, type 0.5.
- 5 In the **y minimum** text field, type -1.1.
- 6 In the **y maximum** text field, type 1.1.
- 7 Click **Update**.

### **DEFINITIONS**

#### *View 1*

- 1 In the **Model Builder** window, expand the **Results** node, then click **Component 1 (comp1)>Definitions>View 1**.
- 2 In the **Settings** window for **View**, locate the **View** section.
- 3 Select the **Lock axis** check box.

### **RESULTS**

#### *2D Plot Group 1*

- 1 In the **Model Builder** window, under **Results** click **2D Plot Group 1**.
- 2 In the **Settings** window for **2D Plot Group**, locate the **Plot Settings** section.
- 3 From the **View** list, choose **View 1**.

- 4 Right-click **Results>2D Plot Group 1** and choose **Rename**.
- 5 In the **Rename 2D Plot Group** dialog box, type **Potential Flow** in the **New label** text field.
- 6 Click **OK**.

#### *Surface 1*

- 1 In the **Model Builder** window, expand the **Results>Potential Flow** node, then click **Surface 1**.
- 2 In the **Settings** window for **Surface**, locate the **Expression** section.
- 3 In the **Expression** text field, type  $\sqrt{\phi_{ix}^2 + \phi_{iy}^2}$ .

#### *Streamline 1*

- 1 In the **Model Builder** window, right-click **Potential Flow** and choose **Streamline**.
- 2 In the **Settings** window for **Streamline**, locate the **Expression** section.
- 3 In the **x component** text field, type  $-\phi_{ix}$ .
- 4 In the **y component** text field, type  $-\phi_{iy}$ .
- 5 Locate the **Streamline Positioning** section. From the **Positioning** list, choose **Starting-point controlled**.
- 6 From the **Entry method** list, choose **Coordinates**.
- 7 In the **x** text field, type 0.
- 8 In the **y** text field, type  $\text{range}(-2, 0.025, 2)$ .

#### *Potential Flow*

- 1 In the **Model Builder** window, click **Potential Flow**.
- 2 In the **Settings** window for **2D Plot Group**, click to expand the **Title** section.
- 3 From the **Title type** list, choose **Manual**.
- 4 In the **Title** text area, type **Velocity magnitude and streamlines for potential-flow solution**.
- 5 In the **Potential Flow** toolbar, click **Plot**.

### **ADD STUDY**

- 1 In the **Home** toolbar, click **Add Study** to open the **Add Study** window.
- 2 Go to the **Add Study** window.
- 3 Find the **Studies** subsection. In the **Select Study** tree, select **Preset Studies for Selected Physics Interfaces>Turbulent Flow, SST>Stationary with Initialization**.

- 4 Click **Add Study** in the window toolbar.
- 5 In the **Home** toolbar, click **Add Study** to close the **Add Study** window.

## STUDY 2

### *Step 1: Wall Distance Initialization*

- 1 In the **Settings** window for **Wall Distance Initialization**, locate the **Physics and Variables Selection** section.
- 2 In the table, clear the **Solve for** check box for the **Laplace Equation** interface.
- 3 Click to expand the **Values of Dependent Variables** section. Find the **Initial values of variables solved for** subsection. From the **Settings** list, choose **User controlled**.
- 4 Find the **Values of variables not solved for** subsection. From the **Settings** list, choose **User controlled**.
- 5 From the **Study** list, choose **Study 1, Stationary**.

### *Step 2: Stationary*

- 1 In the **Model Builder** window, click **Step 2: Stationary**.
- 2 In the **Settings** window for **Stationary**, locate the **Physics and Variables Selection** section.
- 3 In the table, clear the **Solve for** check box for the **Laplace Equation** interface.
- 4 Click to expand the **Values of Dependent Variables** section. Find the **Initial values of variables solved for** subsection. From the **Settings** list, choose **User controlled**.
- 5 From the **Study** list, choose **Study 1, Stationary**.
- 6 Click to expand the **Study Extensions** section. Select the **Auxiliary sweep** check box.
- 7 Click **Add**.
- 8 In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
alpha (Angle of attack)	0, 2, 4, 6, 8, 10, 12, 14	

- 9 In the **Home** toolbar, click **Compute**.

## RESULTS

### *Line Integration 1*

- 1 In the **Results** toolbar, click **More Derived Values** and choose **Integration>Line Integration**.

- 2 Select Boundaries 3 and 4 only.
- 3 In the **Settings** window for **Line Integration**, locate the **Expressions** section.
- 4 In the table, enter the following settings:

Expression	Unit	Description
$p/(1/2 \cdot \rho_{\infty} U_{\infty}^2) / c \cdot (\text{spf.nymesh} \cdot \cos(\alpha \cdot \pi / 180) - \text{spf.nxmesh} \cdot \sin(\alpha \cdot \pi / 180))$	1	

- 5 Locate the **Data** section. From the **Dataset** list, choose **Study 2/Solution 2 (sol2)**.
- 6 Click **Evaluate**.

**TABLE**

- 1 Go to the **Table** window.
- 2 Click **Table Graph** in the window toolbar.

**RESULTS**

*Table 2*

- 1 In the **Results** toolbar, click **Table**.
- 2 In the **Settings** window for **Table**, locate the **Data** section.
- 3 Click **Import**.
- 4 Browse to the model's Application Libraries folder and double-click the file naca0012\_airfoil\_Ladson\_CL.dat.

*Table Graph 2*

- 1 In the **Model Builder** window, right-click **ID Plot Group 5** and choose **Table Graph**.
- 2 In the **Settings** window for **Table Graph**, locate the **Data** section.
- 3 From the **Table** list, choose **Table 2**.
- 4 Locate the **Coloring and Style** section. Find the **Line style** subsection. From the **Line** list, choose **None**.
- 5 From the **Color** list, choose **Blue**.
- 6 Find the **Line markers** subsection. From the **Marker** list, choose **Point**.
- 7 From the **Positioning** list, choose **In data points**.

*ID Plot Group 5*

- 1 In the **Model Builder** window, click **ID Plot Group 5**.
- 2 In the **Settings** window for **ID Plot Group**, click to expand the **Title** section.

- 3 From the **Title type** list, choose **Manual**.
- 4 In the **Title** text area, type Lift vs. angle of attack.
- 5 Locate the **Plot Settings** section. Select the **x-axis label** check box.
- 6 In the associated text field, type  $\alpha$ .
- 7 Select the **y-axis label** check box.
- 8 In the associated text field, type CL.
- 9 In the **ID Plot Group 5** toolbar, click **Plot**.

#### *Table 3*

- 1 In the **Results** toolbar, click **Table**.
- 2 In the **Settings** window for **Table**, locate the **Data** section.
- 3 Click **Import**.
- 4 Browse to the model's Application Libraries folder and double-click the file naca0012\_airfoil\_Gregory\_OReilly\_Cp.dat.

#### **TABLE**

- 1 Go to the **Table** window.
- 2 Click **Table Graph** in the window toolbar.

#### **RESULTS**

##### *Table Graph 1*

- 1 In the **Model Builder** window, under **Results>ID Plot Group 6** click **Table Graph 1**.
- 2 In the **Settings** window for **Table Graph**, locate the **Coloring and Style** section.
- 3 Find the **Line style** subsection. From the **Line** list, choose **None**.
- 4 From the **Color** list, choose **Blue**.
- 5 Find the **Line markers** subsection. From the **Marker** list, choose **Point**.
- 6 From the **Positioning** list, choose **In data points**.

##### *Line Graph 1*

- 1 In the **Model Builder** window, right-click **ID Plot Group 6** and choose **Line Graph**.
- 2 In the **Settings** window for **Line Graph**, locate the **Data** section.
- 3 From the **Dataset** list, choose **Study 2/Solution 2 (sol2)**.
- 4 From the **Parameter selection (alpha)** list, choose **From list**.
- 5 In the **Parameter values (alpha)** list, select **10**.

- 6 Locate the **Selection** section. Click **Paste Selection**.
- 7 In the **Paste Selection** dialog box, type 3 4 in the **Selection** text field.
- 8 Click **OK**.
- 9 In the **Settings** window for **Line Graph**, locate the **y-Axis Data** section.
- 10 In the **Expression** text field, type  $-p / (1/2 * \rho_{inf} * U_{inf}^2)$ .
- 11 Locate the **x-Axis Data** section. From the **Parameter** list, choose **Expression**.
- 12 In the **Expression** text field, type  $(x+c) / c$ .
- 13 In the **ID Plot Group 6** toolbar, click **Plot**.

#### *ID Plot Group 6*

- 1 In the **Model Builder** window, click **ID Plot Group 6**.
- 2 In the **Settings** window for **ID Plot Group**, locate the **Title** section.
- 3 From the **Title type** list, choose **None**.
- 4 Locate the **Plot Settings** section. Select the **x-axis label** check box.
- 5 In the associated text field, type  $(x-xLE) / c$ .
- 6 Select the **y-axis label** check box.
- 7 In the associated text field, type  $-cp$ .
- 8 In the **ID Plot Group 6** toolbar, click **Plot**.

#### *Velocity (spf)*

- 1 In the **Model Builder** window, click **Velocity (spf)**.
- 2 In the **Settings** window for **2D Plot Group**, locate the **Plot Settings** section.
- 3 From the **View** list, choose **View I**.

#### *Streamline I*

- 1 In the **Model Builder** window, expand the **Velocity (spf)** node.
- 2 Right-click **Velocity (spf)** and choose **Streamline**.
- 3 In the **Settings** window for **Streamline**, locate the **Expression** section.
- 4 In the **x component** text field, type  $u$ .
- 5 In the **y component** text field, type  $v$ .
- 6 Locate the **Streamline Positioning** section. From the **Positioning** list, choose **Starting-point controlled**.
- 7 From the **Entry method** list, choose **Coordinates**.
- 8 In the **x** text field, type 0.

- 9** In the **y** text field, type `range (-2,0.025,2)`.
- 10** In the **Velocity (spf)** toolbar, click **Plot**.