Math Homework Week #4, Continuous Optimization

OSM Lab, Eun-Seok Lee

1. (6.1)
$$min - e^{-w^{T}x}$$

$$s.t - w^{T}x \le -w^{T}Aw + w^{T}Ay - a$$

$$y^{T}w = w^{T}x + b$$

2.
$$(6.5)$$

 $min - (0.07m + 0.05k)$
 $s.t \ 4m + 3k = 240,000$
 $2m + k = 6,000$

3. (6.6)

$$f_1(x,y) = 6xy + 4y^2 + y = 0$$

$$f_2(x,y) = 3x^2 + 8xy + x = 0$$

$$Hessian = \begin{bmatrix} 6y & 6x + 8y + 1 \\ 6x + 8y + 1 & 8x \end{bmatrix}$$

- i) (0,0) saddle point because Hessian is indefinite.
- ii) (0, -1/4) saddle point because Hessian is indefinite.
- iii) (-1/3, 0) saddle point because Hessian is indefinite.
- iv) (-1/9, -1/12) local maximum because Hessian is negative definite.

4. (6.11)
$$x_1 = x_0 - \frac{f'(x_0)}{f''(x_0)}$$

$$f'(x) = 0$$

$$x = -\frac{b}{2a} is an unique maxizer.$$

$$f''(x) = 2a > 0 so, this is maximizer.$$

Now,
$$x_1 = x_0 - (2ax_0 + b)\frac{1}{2a} = -\frac{b}{2a}$$

So, for any x_0 , x_1 is an unique maxizer.

References