## Math Homework Week #4, Continuous Optimization

OSM Lab, Eun-Seok Lee

1. (6.1) 
$$\min - e^{-w^T x}$$
 
$$s.t - w^T x + w^T A w - w^T A y \le -a$$
 
$$y^T w - w^T x = b$$

2. 
$$(6.5)$$
  
 $min - (0.07m + 0.05k)$   
 $s.t \ 4m + 3k \le 240,000$   
 $2m + k \le 6,000$ 

3. (6.6)  

$$f_1(x,y) = 6xy + 4y^2 + y = 0$$

$$f_2(x,y) = 3x^2 + 8xy + x = 0$$

$$Hessian = \begin{bmatrix} 6y & 6x + 8y + 1 \\ 6x + 8y + 1 & 8x \end{bmatrix}$$

i) (0,0) – saddle point because Hessian is indefinite.

ii) (0, -1/4) – saddle point because Hessian is indefinite.

iii) (-1/3, 0) – saddle point because Hessian is indefinite.

iv) (-1/9, -1/12) – local maximum because Hessian is negative definite.

4. (6.11)
$$x_1 = x_0 - \frac{f'(x_0)}{f''(x_0)}$$

$$f'(x) = 0$$

$$x = -\frac{b}{2a} \text{ is an unique maxizer.}$$

$$f''(x) = 2a > 0 \text{ so, this is maximizer.}$$

Now, 
$$x_1 = x_0 - (2ax_0 + b)\frac{1}{2a} = -\frac{b}{2a}$$
  
So, for any  $x_0$ ,  $x_1$  is an unique maxizer.

## References