Contribution Title

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Abstract. Despite the remarkable success of deep reinforcement learning (deep RL) across various domains, its deployment in real-world remains limited due to safety concerns. To address this challenge, constrained reinforcement learning (constrained RL) has been proposed to learn safe policies while maintaining performance. However, since constrained RL enforces constraints in the form of cumulative costs, it cannot guarantee state-wise safety. In this paper, we extend the Lagrangian based approach, a representative method in constrained RL, by introducing state-dependent Lagrange multipliers so that the policy is trained to account for state-wise safety.

1 INTRODUCTION

Reinforcement learning (RL) learns policy that maximize rewards through trial and error. This way of learning the desired behaviors may seem simple and straightforward, but it is highly effective. Over the past few years, RL has demonstrated impressive achievements in diverse applications ... [7] [3] [5]. Nevertheless, deploying RL in physical real-world environments remains a major challenge. To deploy RL-trained agents in real-world environments, two requirements must be satisfied: First, the ability to successfully accomplish the given tasks, and second, the safety and reliability of the learned agent. In standard RL, such requirements are learned exclusively from reward signals, thereby necessitating careful reward engineering. However, even with carefully designed rewards and successful training in simulation, the learned policy may fail when tasks change or when transferring to real-world environments, due to issues such as reward hacking or lack of generalization [2]. To address these issues, constrained reinforcement learning (constrained RL) has recently been widely studied.

Constrained RL is a method that learns policy maximizing rewards while satisfying constraints, thus enabling agents to behave safely while successfully performing tasks. A common formulation of constrained RL specifies constraints at the trajectory level [4]. As a result, since the constraints are specified over entire trajectory, violations occurring at individual timesteps cannot be directly constrained/restricted. For example, even if a constraint is defined to limit the number of lane departures during the entire trip of an autonomous vehicle, a single deviation from the lane that results in a collision with another vehicle can lead to a catastrophic failure. This illustrates that trajectory-level constraints

regulate only the outcome of a task but are limited in controlling the risky process itself. Therefore, in this paper, we propose an approach that considers state-wise constraints. Specifically, we extend the Lagrangian-based approach, a representative method in constrained RL, by introducing state-wise Lagrange multipliers so that the policy is encouraged to take safe actions at every timestep.

2 Related Work

3 Methodology

3.1 Preliminaries

Constrained Markov Decision Processes In RL, problems are typically formulated as Markov decision process (MDP) [8], in contrast, constrained RL employs a constrained Markov decision process (CMDP) [1]. A CMDP extends an MDP by introducing a set of cost functions $C_1, \ldots, C_m$, which are separate from the reward function, together with corresponding thresholds $d_1, \ldots, d_m$. Formally, a CMDP is defined as a tuple $\langle S, A, P, R, C, d, \gamma \rangle$, where S and A denotes the state and action spaces, P is the transition probability, R is the reward function, C is the set of cost functions, and d denotes the corresponding cost thresholds, γ is the discount factor. In a CMDP, the set of feasible policies Π_C is defined as:

$$\Pi_C = \{\pi \in \Pi : \forall i, J_{C_i}(\pi) \leq d_i\}, \tag{1}$$

where $J_{C_i} = \mathbb{E}_{\tau\sim\pi}[\sum_{t=0}^{\infty} \gamma^t C(s_t, a_t)]$ is a cost-based constraint function, commonly defined in the same way as the expected return. Specifically, the expected return is defined as $J_R = \mathbb{E}_{\tau\sim\pi}[\sum_{t=0}^{\infty} \gamma^t R(s_t, a_t)]$, and d_i is a threshold chosen as a human-specified hyperparameter. Here, $\tau = (s_0, a_0, s_1, a_1, \ldots)$ denotes a trajectory generated by following policy π. In standard RL, the objective is to sove an optimization problem that maximizes the expected return $\pi^* = \arg\max J_R(\pi)$. Whereas constrained RL solves the following constrained optimization problem:

$$\pi^* = \arg\max_{\pi} J_R(\pi) \text{ s. t. } J_C(\pi) \leq d. \tag{2}$$

State-wise Constrained Markov Decision Process The CMDP framework can be extended to incorporate various types of cost-based constraints. One such extension is the state-wise constrained Markov decision process (SCMDP) [9], which introduces state-wise constraints to ensure that the expected cost at each state does not exceed a specified threshold. In a SCMDP, the set of feasible policies Π_{SC} is defined as:

$$\begin{aligned} \Pi_{SC} = \{\pi \in \Pi : \forall (s_t, a_t, s_{t+1}) \sim \tau, \\ \forall i, C_i(s_t, a_t, s_{t+1}) \leq d_i\} \end{aligned} \tag{3}$$

where $C_i(s_t, a_t, s_{t+1})$ is the cost incurred at state s_t after taking action a_t and transitioning to state s_{t+1}, and d_i is the corresponding threshold. Similar to

CMDPs, the optimization problem in SCMDPs can be formulated as

$$\pi^* = \arg\max_{\pi} J_R(\pi) \text{ s.t. } J_{SC}(\pi) \leq d, \tag{4}$$

where $J_{SC}(\pi)$ denotes the state-wise constraints.

Lagrangian Relaxation for Constrained Policy Optimization A common approach to solve constrained optimization problems is to use Lagrangian relaxation. In this approach, the constrained optimization problem (2) is reformulated as an unconstrained optimization problem by introducing Lagrange multiplier $\lambda \geq 0$ that penalizes constraint violations. The resulting Lagrangian can be written as:

$$L(\theta, \lambda) = J_R(\pi_\theta) - \lambda(J_C(\pi_\theta) - d), \tag{5}$$

where θ denotes the parameter of the policy π_θ. The objective is then to find a saddle point (θ^*, λ^*) that satisfies:

$$L(\theta^*, \lambda) \geq L(\theta^*, \lambda^*) \geq L(\theta, \lambda^*). \tag{6}$$

Since finding a global saddle point is often computationally intractable, in practice one aims to find a locally optimal solution using iterative updates of the policy parameters and the Lagrange multiplier. A common approach is to apply gradient-based updates of the form

$$\theta_{n+1} = \theta_n + \eta_\theta \nabla_\theta \Big(J_R(\pi_\theta) - \lambda_n J_C(\pi_\theta) \Big), \tag{7}$$

$$\lambda_{n+1} = \Big[\lambda_n + \eta_\lambda \big(J_C(\pi_\theta) - d \big) \Big]_+, \tag{8}$$

where $\eta_\theta, \eta_\lambda > 0$ are step sizes, and $[\cdot]_+$ denotes the projection onto the nonnegative orthant to ensure $\lambda \geq 0$.

3.2 Proposed Method

In this paper, we propose a method to extend constrained reinforcement learning algorithm to state-wise constrained reinforcement learning by estimating state-wise Lagrange multipliers. We build our method on Proximal Policy Optimization (PPO) [6], a widely used policy gradient algorithm, due to its simplicity and effectiveness.

4 Experiments

5 CONCLUSIONS

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Disclosure of Interests. It is now necessary to declare any competing interests or to specifically state that the authors have no competing interests. Please place the statement with a bold run-in heading in small font size beneath the (optional) acknowledgments[1], for example: The authors have no competing interests to declare that are relevant to the content of this article. Or: Author A has received research grants from Company W. Author B has received a speaker honorarium from Company X and owns stock in Company Y. Author C is a member of committee Z.

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