

yang_seonhyeHW9

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```
library(data.table)
hybrid_reg <- fread("http://users.stat.ufl.edu/~winner/data/hybrid_reg.csv")
hybrid <- data.table("hotel_energy.csv", header = TRUE)
```

Question 1

```
attach(hybrid_reg, warn.conflicts = F)
model <- lm(msrp~mpgmpge+accelrate)
model1 = confint(model,level=.95)
model1
```

```
##              2.5 %      97.5 %
## (Intercept) -26628.4764 2008.72023
## mpgmpge      -277.3895   14.43946
## accelrate    3828.8331 5651.44832
```

```
summary(model)
```

```
##
## Call:
## lm(formula = msrp ~ mpgmpge + accelrate)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -38435   -8709   -2836    7755   51093
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -12309.88    7246.60  -1.699   0.0914 .
## mpgmpge      -131.48     73.85   -1.780   0.0770 .
## accelrate    4740.14     461.21  10.278  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 15330 on 150 degrees of freedom
## Multiple R-squared:  0.4945, Adjusted R-squared:  0.4878
## F-statistic: 73.37 on 2 and 150 DF, p-value: < 2.2e-16
```

We are 95% confident that $\beta_{mpgmpge}$ falls between -277.38 and 14.43946. Additionally, We are 95% confident that $\beta_{accelrate}$ falls between -3828.8331 and 5651.44832. This means that 95% of all cars are affected in relation to MPGe and Acceleration by this range of values

-12309.88 + 4740.14*4500 ## Question 2

```
attach(hybrid_reg, warn.conflicts = F)
xstar=data.frame(mpgmpge = 40, accelrate = 10)
predict(model,xstar,interval = "confidence",level = .99)
```

```
##          fit          lwr          upr
## 1 29832.53 25890.53 33774.53

x1star=data.frame(1, mpgmpge = 40, accelrate = 10)
predict(model,x1star,interval = "prediction",level=.99)
```

```
##          fit          lwr          upr
## 1 29832.53 -10360.25 70025.3
```

Looking at the first interval, we can see that the lower and upper bounds are 25890.53 and 33774.53 respectively, meaning that for a car with 40 MPGe and an acceleration of 10, the price falls within that range. Looking at our predicted ranges, we can see that the lower bounds are -10360.25 and 70025.3, indicating that our predictor fits well for creating a range of prices based on these values.

Question 3

```
modelcoef<-coef(summary(model))
modelcoef

##              Estimate Std. Error   t value    Pr(>|t|)
## (Intercept) -12309.878  7246.6014 -1.698711 9.144694e-02
## mpgmpge      -131.475    73.8469 -1.780373 7.703926e-02
## accelrate    4740.141   461.2101 10.277616 4.336620e-19

tval1<-(modelcoef[3, 1]-4500)/modelcoef[3, 2];tval1

## [1] 0.5206753

dffit2<-model$df.residual;dffit2

## [1] 150

pval=pt(tval1,dffit2,lower=F)
pval

## [1] 0.3016804
```

We obtain a p value of 0.3016, which is greater than 0.05, so we cannot reject the null hypothesis and must accept our hypothesis to be significant

Question 4

```
model3=lm(msrp~1, data = hybrid_reg, offset=-120*mpgmpge+4500*accelrate)
anova(model3,model)

## Analysis of Variance Table
##
## Model 1: msrp ~ 1
## Model 2: msrp ~ mpgmpge + accelrate
##   Res.Df        RSS Df Sum of Sq      F Pr(>F)
## 1     152 3.5357e+10
## 2     150 3.5257e+10  2 100566428 0.2139 0.8076
```

Looking at the ANOVA results, we can see that there is a computed P value of 0.2139, which is greater than 0.05. This result implies that we cannot reject the null hypothesis of $H_1:H_0$ is false.

Question 5

We can start with $\text{var}(y_* - \hat{y}_*)$:

$$\begin{aligned} & \text{var}(y_*) - \text{var}(\hat{y}_*) \\ & \text{var}(\mathbf{X}_*^T \beta + \epsilon_*) - \text{var}(\hat{y}_*) \end{aligned}$$

We know that $\text{var}(\mathbf{X}_*^T \beta + \epsilon_*) = \sigma^2$, so:

$$\begin{aligned} & \sigma^2 - \text{var}(\hat{y}_*) \\ & \sigma^2 - (\mathbf{X}_*^T)^2 \text{var}(\hat{\beta}) \\ & \sigma^2 - (\mathbf{X}_*^T)^2 (\sigma^2 (\mathbf{X}^T \mathbf{X})^{-1}) \end{aligned}$$

Rearranging this, we get:

$$\sigma^2 - (\mathbf{X}_*^T) (\sigma^2 (\mathbf{X}^T \mathbf{X})^{-1}) (\mathbf{X}_*)$$

Factoring:

$$\sigma^2 (1 + \mathbf{X}_*^T (\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}_*)$$

Which is equivalent to the solution we were looking for.