

A Deep Neural Network for Unsupervised Anomaly Detection and Diagnosis in Multivariate Time Series Data

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Introduction

- Anomaly detection and diagnosis in multivariate time series
 - Identifying abnormal status in certain time steps and pinpointing the root causes

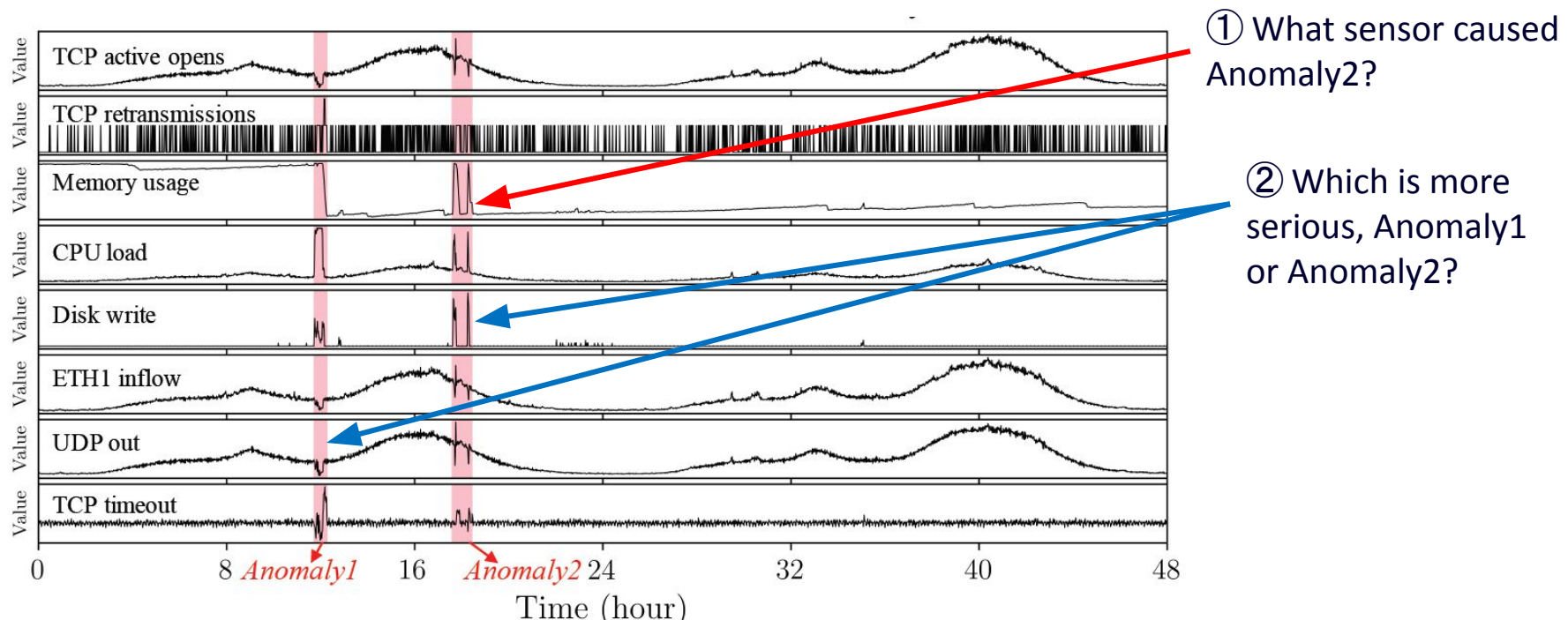


Fig. 8-dimensional multivariate time series in 2-day from the server machine dataset

- If we can know about the root causes and the severity of anomalies, it is easy to know what to repair first

Related Work with Issue

1. Distance/clustering methods
 - Grouping a set of data which are similar each other
 - e.g. k-Nearest Neighbor (kNN) [1]
 2. Classification methods
 - Learning decision function and classifying data as similar or dissimilar
 - e.g. One-Class SVM (OC-SVM) [2]
 3. Density estimation methods
 - Modeling data density for outlier detection
 - e.g. Deep Autoencoding Gaussian Mixture Model (DAGMM) [3]
 4. Prediction methods
 - Modeling the temporal dependency of data and predicts the value
 - e.g. Autoregressive Moving Average (ARMA) [4]
- ①, ②, ③ → Cannot capture temporal dependencies across different time steps
 - ④ → Sensitive to noise

Motivations

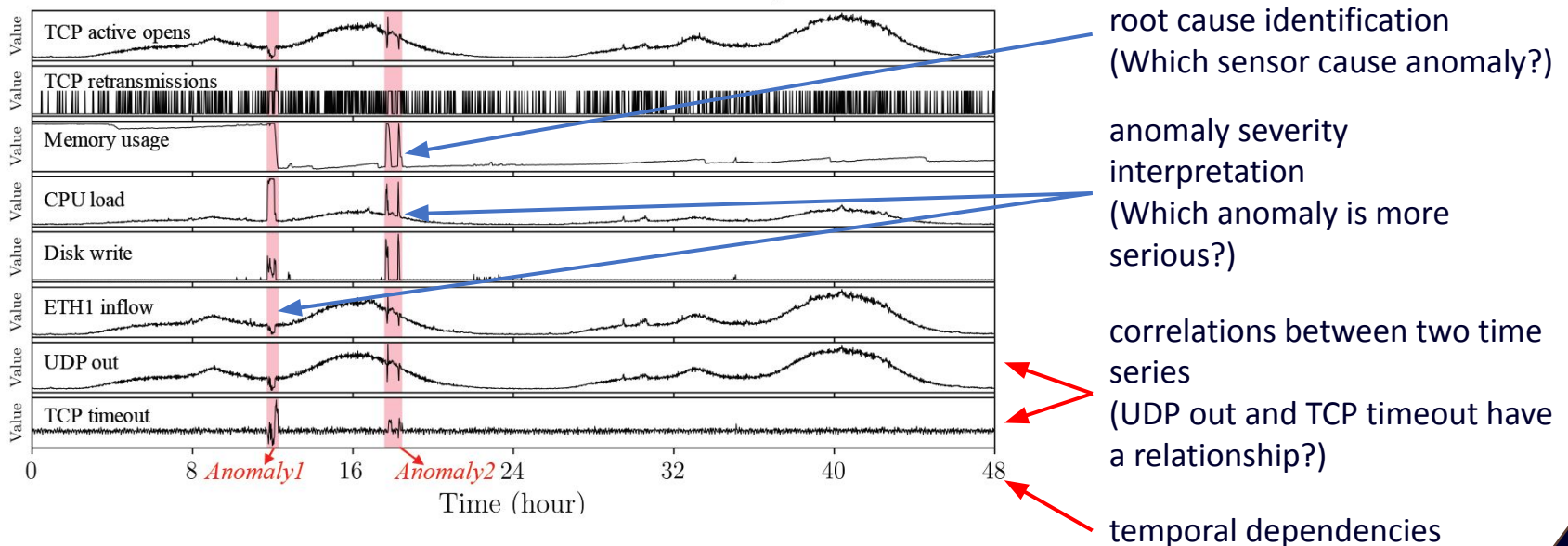
- Main challenges in two aspects

1. **Anomaly Detection**

- Detect anomalies in certain time steps
- Consider temporal dependencies and correlations between two time series

2. **Anomaly Diagnosis**

- Identify the root causes of anomalies
- Provide the anomaly severity interpretation



Proposed method: MSCRED

- Overview

- Characterizing status with signature matrices
 - ✓ Construct signature matrices, considering the correlation between two time series
- Convolutional encoder
 - ✓ Encode the spatial patterns of signature matrices
- Attention based ConvLSTM
 - ✓ Capture the spatial patterns of signature matrices with temporal information
- Convolutional decoder
 - ✓ Reconstruct the signature matrices with the outputs of attention based ConvLSTM

Proposed method: MSCRED

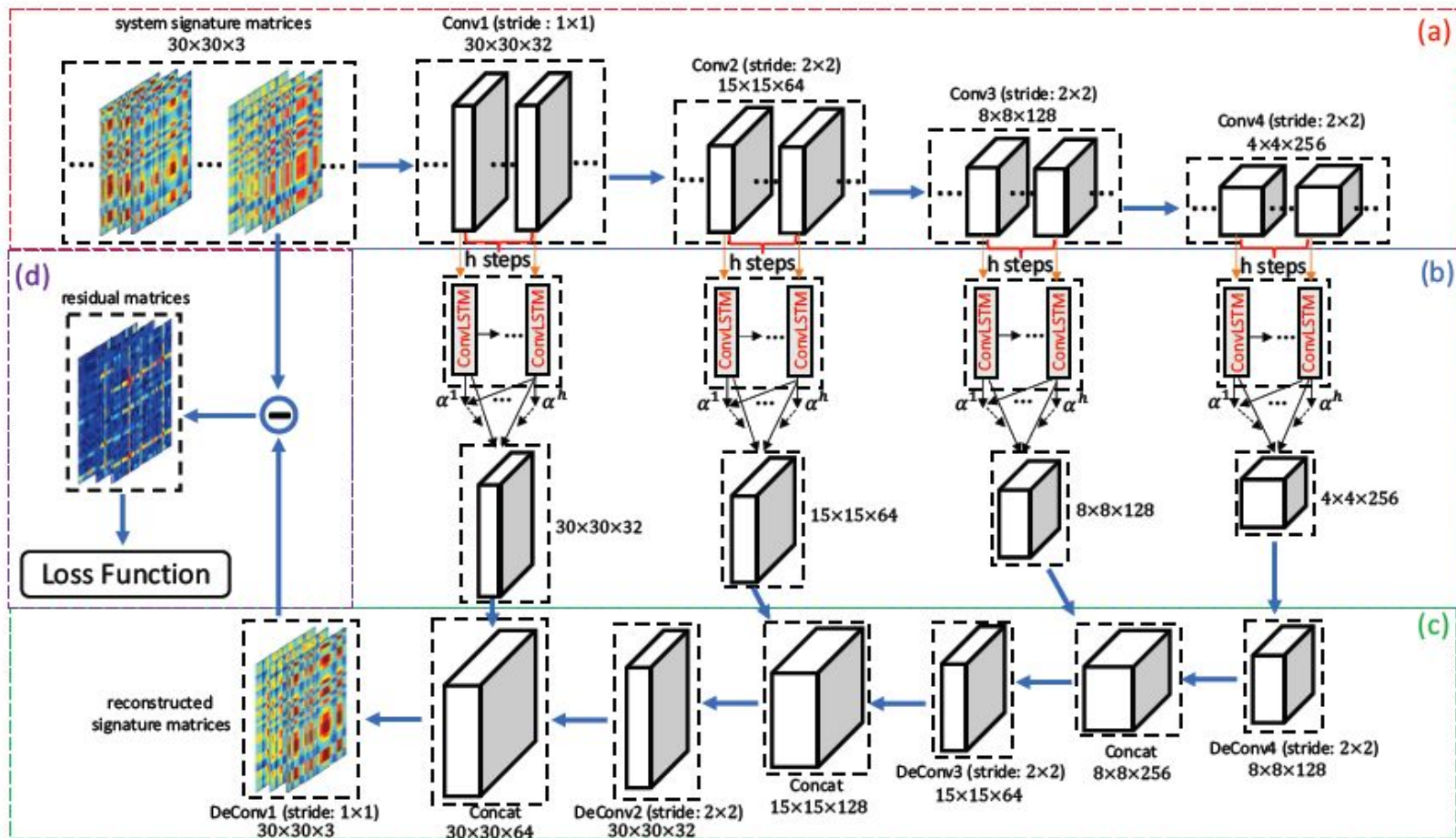


Figure 1.

- (a) Characterizing Status with Signature Matrices & Convolutional Encoder
- (b) Attention based ConvLSTM
- (c) Convolutional Decoder
- (d) Loss function

Proposed method: MSCRED

- Characterizing status with s signature matrices M^t (Figure 1.(a))
 - Construct signature matrices, considering the correlation between two time series


- $\Upsilon^\omega = (X_1^\omega, \dots, X_n^\omega) \in \mathbb{R}^{n \times \omega}$: n time series with length ω
- $X_i^\omega = (x_i^{t-\omega}, x_i^{t-\omega-1}, \dots, x_i^t)$: i -th time series from $t - \omega$ to t
- ω : window size
- M^t : $n \times n$ signature matrix
- $m_{ij}^t \in M^t$: an element of the signature matrix

$$\checkmark \quad m_{ij}^t = \frac{\sum_{\delta=0}^{\omega} x_i^{t-\delta} x_j^{t-\delta}}{K}$$

$$\checkmark \quad K = \omega$$

- Example

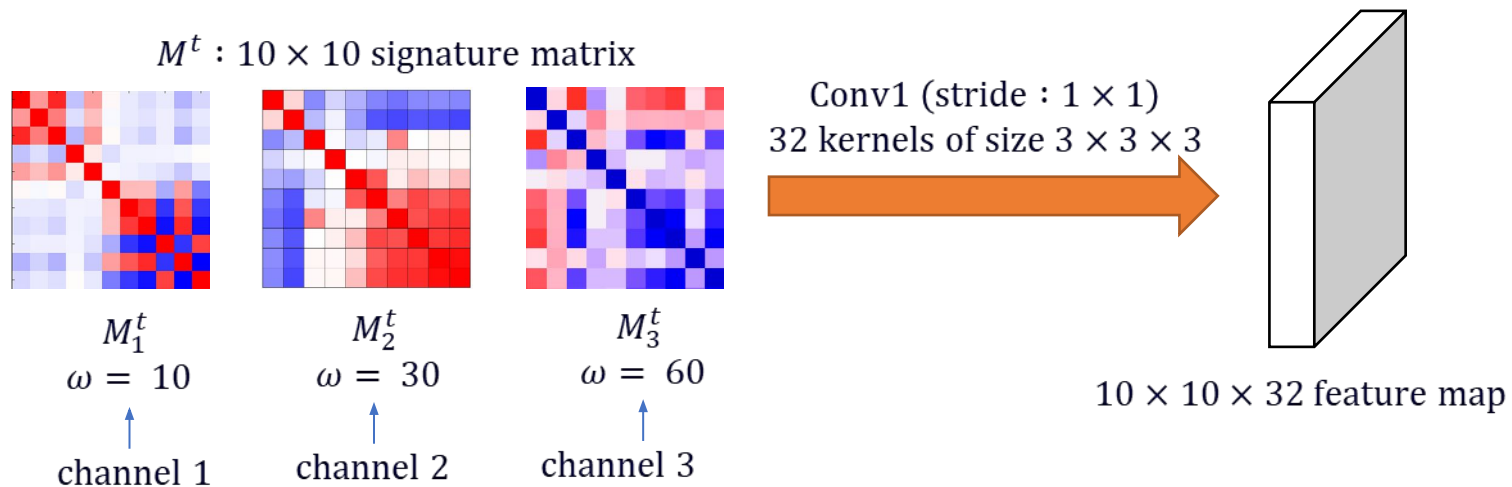
- $\Upsilon^2 = (X_1^2, X_2^2)$ ($\omega = 2, n = 2$) : 2 time series with length 2
- X_1 : temperature, X_2 : atmospheric pressure
- $X_1^2 = (15^\circ\text{C}, 14^\circ\text{C})$
- $X_2^2 = (3 \text{ atm}, 2 \text{ atm})$

	X_1	X_2	$\frac{15 * 3 + 14 * 2}{2}$
X_1	210.5	36.5	
X_2	36.5	6.5	

M^t

Proposed method: MSCRED

- Convolutional Encoder (Figure 1.(a))
 - Encode the spatial patterns of system signature matrices
 - $\chi^{t,l} \in \mathbb{R}^{n_l \times n_l \times d_l}$: a feature map in the l -th layer
 - d_l : the number of kernels (filters)
 - ✓ $\chi^{t,l} = f(W^l * \chi^{t,l-1} + b^l)$
 - ✓ $*$: the convolutional operation
 - ✓ $f(\cdot)$: the activation function
 - ✓ $W^l \in \mathbb{R}^{k_l \times k_l \times d_{l-1} \times d_l}$: d_l convolutional kernels of size $k_l \times k_l \times d_{l-1}$
 - ✓ $b^l \in \mathbb{R}^{d_l}$: bias
- Example



Proposed method: MSCRED

■ Attention based ConvLSTM (Figure 1.(b))

① Train model to capture the spatial patterns of signature matrices with temporal information

- $H^{t,l} = \text{ConvLSTM}(\chi^{t,l}, H^{t-1,l})$

- ✓ $H^{t,l} \in \mathbb{R}^{n_l \times n_l \times d_l}$: the hidden state of l - th layer at time t

② To select the steps that are relevant to current step, adopt a temporal attention mechanism

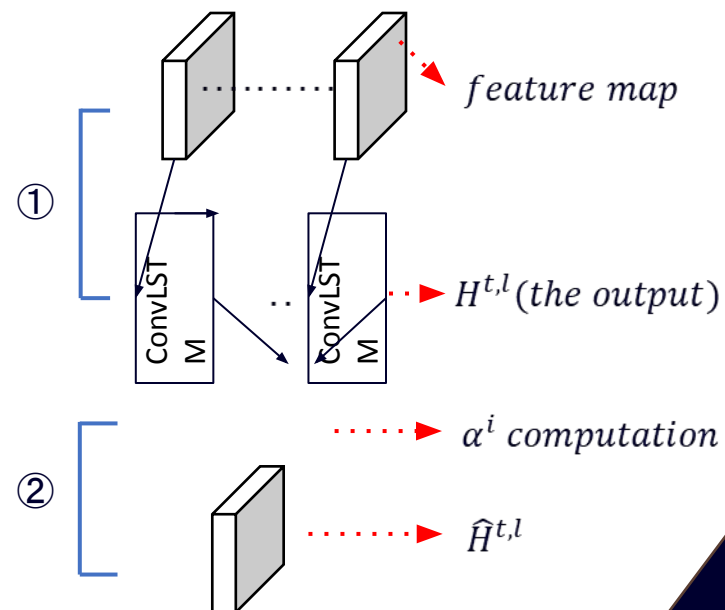
- $\hat{H}^{t,l} = \sum_{i \in (t-h, t)} \alpha^i H^{i,l}$

- ✓ $\hat{H}^{t,l}$: the refined output of feature maps

- ✓ α^i : the importance weights

- $$\alpha^i = \frac{\exp\left\{\frac{\text{Vec}(H^{t,l})^T \text{Vec}(H^{i,l})}{x}\right\}}{\sum_{i \in (t-h, t)} \exp\left\{\frac{\text{Vec}(H^{t,l})^T \text{Vec}(H^{i,l})}{x}\right\}}$$

- ✓ $x (= 0.5)$: rescale factor



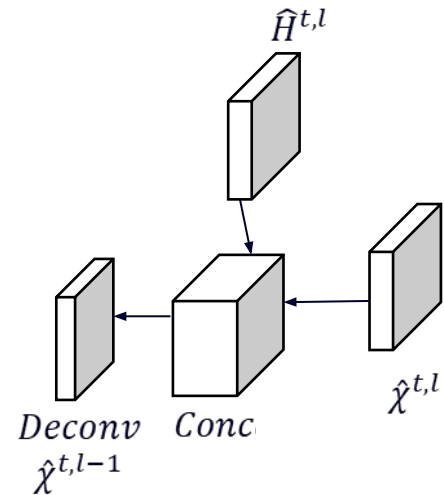
Proposed method: MSCRED

Convolutional Decoder (Figure 1.(c))

- With trained model, reconstruct the signature matrices

$$\hat{\chi}^{t,l-1} = \begin{cases} f(\hat{W}^{t,l} \circledast \hat{H}^{t,l} + \hat{b}^{t,l}) & l = 4 \\ f(\hat{W}^{t,l} \circledast [\hat{H}^{t,l} \oplus \hat{\chi}^{t,l}] + \hat{b}^{t,l}) & l = 3, 2, 1 \end{cases}$$

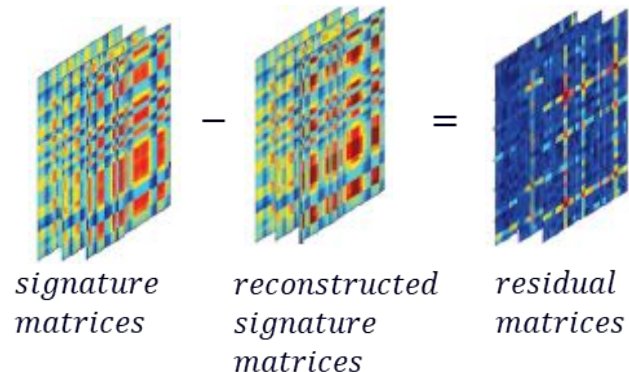
- ✓ $\hat{\chi}^{t,l-1}$: the output feature map
- ✓ \circledast : the deconvolution operation
- ✓ \oplus : the concatenation operation
- ✓ $f(\cdot)$: the activation function
- ✓ \hat{W}^l : the kernel of l - th deconvolutional layer
- ✓ \hat{b}^l : bias of l - th deconvolutional layer



- $\hat{\chi}^{t,l-1}$ is concatenated with the output of previous ConvLSTM layer, making the decoder process stacked

Loss function (Figure 1.(d))

$$\mathcal{L}_{MSCRED} = \sum_t \sum_{c=1}^s \|\chi_{:, :, c}^{t,0} - \hat{\chi}_{:, :, c}^{t,0}\|_F^2$$



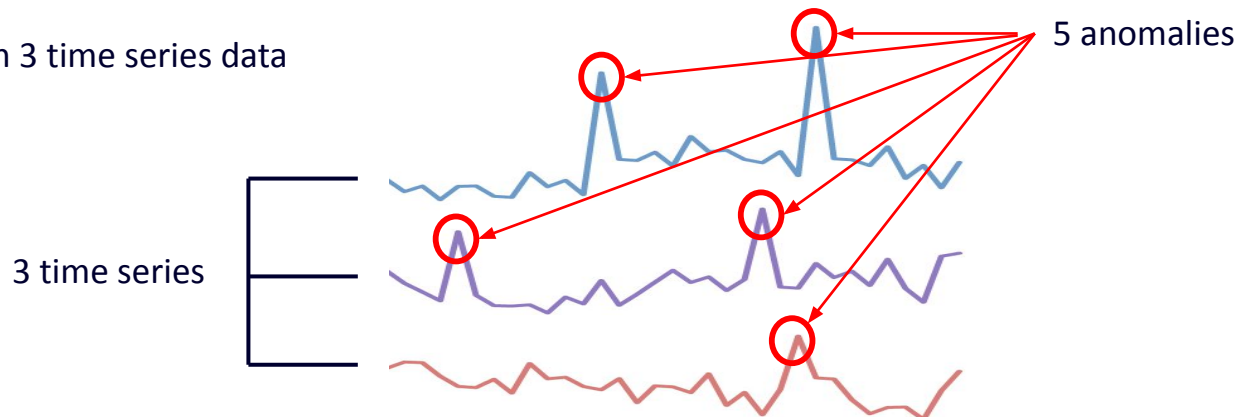
Experiments

- Dataset
 - Synthetic data
 - Generate time series data, using the following formula
 - $$S(t) = \begin{cases} \sin[(t - t_0)/w] + \lambda \cdot \epsilon, & s_{rand} = 0 \\ \cos[(t - t_0)/w] + \lambda \cdot \epsilon, & s_{rand} = 1 \end{cases}$$
 - ✓ $t_0 \in [50, 100]$: time delay
 - ✓ $w \in [40, 50]$: frequency
 - ✓ $\epsilon \sim N(0,1)$: random gaussian noise
 - ✓ $\lambda = 0.3$: scale factor
 - Power plant data
 - Collected on a real power plant
 - 1 anomaly + injected 4 additional anomalies

Experiments

Statistics	Synthetic	Power Plant
# time series	30	36
# points	20,000	23,040
# anomalies	5	5
# root cause	3	3
Train period	0 ~ 8000	0 ~ 10,080
Valid period	8001 ~ 10,000	10,081 ~ 18,720
Test period	10,001 ~ 20,000	18,721 ~ 23,040

5 anomalies in 3 time series data



Experiments

- Compare MSCRED with 8 baseline methods
 - Classification model
 - ✓ One-Class SVM model (OC-SVM)
 - Density estimation model
 - ✓ Deep Autoencoding Gaussian Mixture model (DAGMM)
 - ✓ The anomaly score : the energy score (Zong et al. 2018)
 - Prediction model
 - ✓ History Average (HA)
 - ✓ Auto Regression Moving Average (ARMA)
 - ✓ LSTM encoder-decoder (LSTM-ED)
 - ✓ The anomaly score : the average prediction error over all time series
 - MSCRED variants
 - ✓ $CNN_{ConvLSTM}^{ED(4)}$: MSCRED with attention module + first three ConvLSTM layers been removed
 - ✓ $CNN_{ConvLSTM}^{ED(3,4)}$: MSCRED with attention module + first two ConvLSTM layers been removed
 - ✓ $CNN_{ConvLSTM}^{ED}$: MSCRED with attention module been removed

Experiments

- The anomaly score
 - the residual matrix : $\chi - \hat{\chi}$
 - x : an element in the residual signature matrix of test data
 - If $x > \text{threshold } \tau$, $x \rightarrow \text{anomaly}$
 - threshold $\tau = \beta \cdot \max\{s(t)_{\text{valid}}\}$
 - ✓ $s(t)_{\text{valid}}$: the anomaly scores over the validation period
 - ✓ $\beta \in [1,2]$: set to maximize the F1 score over the validation period
- Use 3 metrics
 - Precision, recall and F1 score
 - Recall and precision scores over the test period are computed based on the threshold
- Experiments on both datasets are repeated 5 times and the average results are reported for comparison

Experiments

Table 1 : Anomaly detection results on two datasets

Method	Synthetic Data			Power Plant Data		
	Pre	Rec	F ₁	Pre	Rec	F ₁
OC-SVM	0.14	0.44	0.22	0.11	0.28	0.16
DAGMM	0.33	0.20	0.25	0.26	0.20	0.23
HA	0.71	0.52	0.60	0.48	0.52	0.50
ARMA	0.91	0.52	0.66	0.58	0.60	0.59
LSTM-ED	<u>1.00</u>	<u>0.56</u>	<u>0.72</u>	<u>0.75</u>	<u>0.68</u>	<u>0.71</u>
CNN ^{ED(4)} _{ConvLSTM}	0.37	0.24	0.29	0.67	0.56	0.61
CNN ^{ED(3,4)} _{ConvLSTM}	0.63	0.56	0.59	0.80	0.72	0.76
CNN ^{ED} _{ConvLSTM}	0.80	0.76	0.78	0.85	0.72	0.78
MSCRED	1.00	0.80	0.89	0.85	0.80	0.82
Gain (%)	–	30.0	23.8	13.3	19.4	15.5

The best
Baseline
method

The best
score

The improvement (%) of
MSCRED over the best
baseline method

Observation

- Performance Evaluation

1. **Anomaly detection**

- ✓ (RQ1) Whether MSCRED can outperform baseline methods for anomaly detection in multivariate time series?
- ✓ (RQ2) How does each component of MSCRED affect its performance?

2. **Anomaly diagnosis**

- ✓ (RQ3) Whether MSCRED can perform root cause identification and (RQ4) anomaly severity (duration) interpretation effectively?

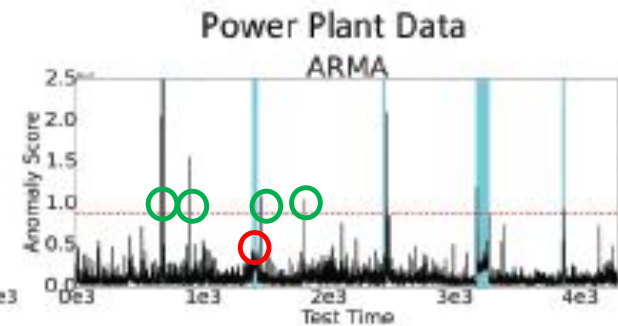
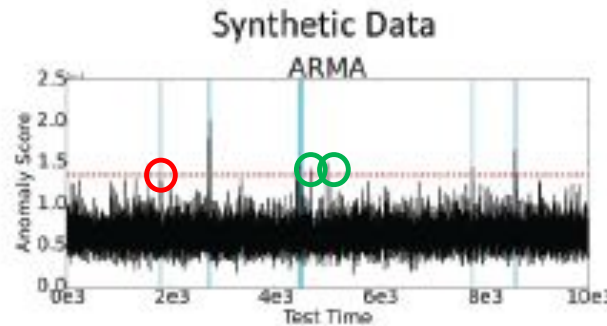
3. **Robustness to noise**

- ✓ (RQ5) Compared with baseline methods, whether MSCRED is more robust to input noise?

Observation

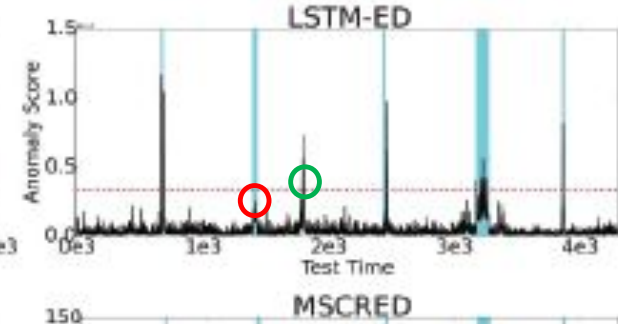
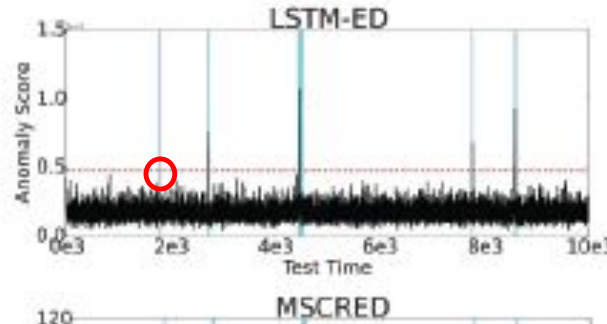
- False positive
- False negative

The second best baseline method



threshold τ

The best baseline method



MSCRED

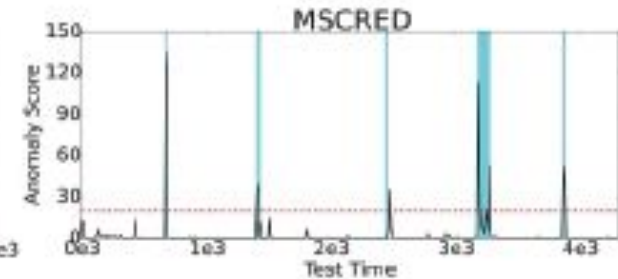
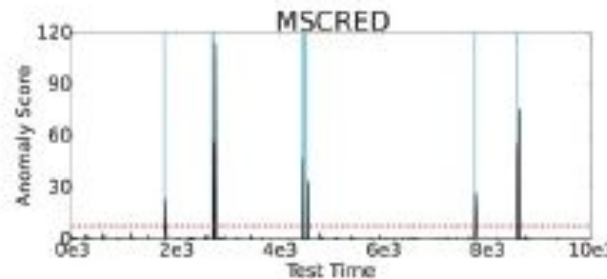


Figure 2 : Case study of anomaly detection. The shaded regions represent anomaly periods. The red dash line is the cutting threshold of anomaly

Observation

- (RQ1) comparison with baseline
 - In Table 1 (p.16)
 - ✓ MSCRED performs best on all settings
 - ✓ The improvements over the best baseline : 13.3% ~ 30.0%
 - In Figure 2 (p.18)
 - ARMA & LSTM-ED
 - ✓ The anomaly score is not stable
 - ✓ Many false positives and false negatives
 - MSCRED
 - ✓ The anomaly score is stable
 - ✓ Detect all anomalies without any false positive and false negative

Observation

- (RQ2) comparison with model variants
 - In Table 1 (p.16), by increasing the number of ConvLSTM layers,
 - $CNN_{ConvLSTM}^{ED(3,4)}$ outperforms $CNN_{ConvLSTM}^{ED(4)}$
 - $CNN_{ConvLSTM}^{ED}$ outperforms $CNN_{ConvLSTM}^{ED(3,4)}$
 - The effectiveness of ConvLSTM layers & stacked decoding process for model refinement
 - $CNN_{ConvLSTM}^{ED}$ is worse than MSCRED
 - The effectiveness of attention based ConvLSTM

Observation

- (RQ3) Root cause identification result
 - Rank all time series by their anomaly scores
 - Then, identify the top-k series as the root causes
 - MSCRED outperforms LSTM-ED by a margin of 25.9% and 32.4% in the synthetic and power plant data

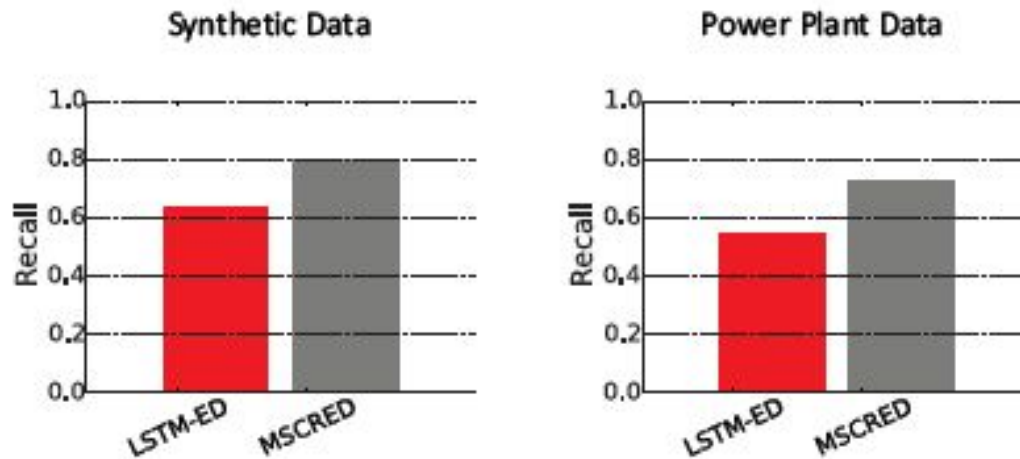
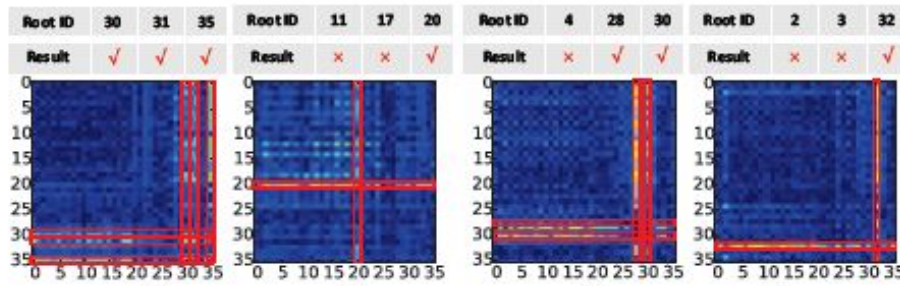


Figure 3 : Performance of root cause identification

Observation

- (RQ4) Anomaly severity (duration) interpretation
 - Compute anomaly scores based on the residual signature matrices of three channels
 - ✓ $\omega = 10$ (channel 1) – MSCRED(S)
 - ✓ $\omega = 30$ (channel 2) – MSCRED(M)
 - ✓ $\omega = 60$ (channel 3) – MSCRED(L)
 - Evaluate their performances on three types of anomalies
 - ✓ The duration of 10 = short anomaly
 - ✓ The duration of 30 = medium anomaly
 - ✓ The duration of 60 = long anomaly



Root cause identification

Long anomaly

Short anomaly

medium
anomaly

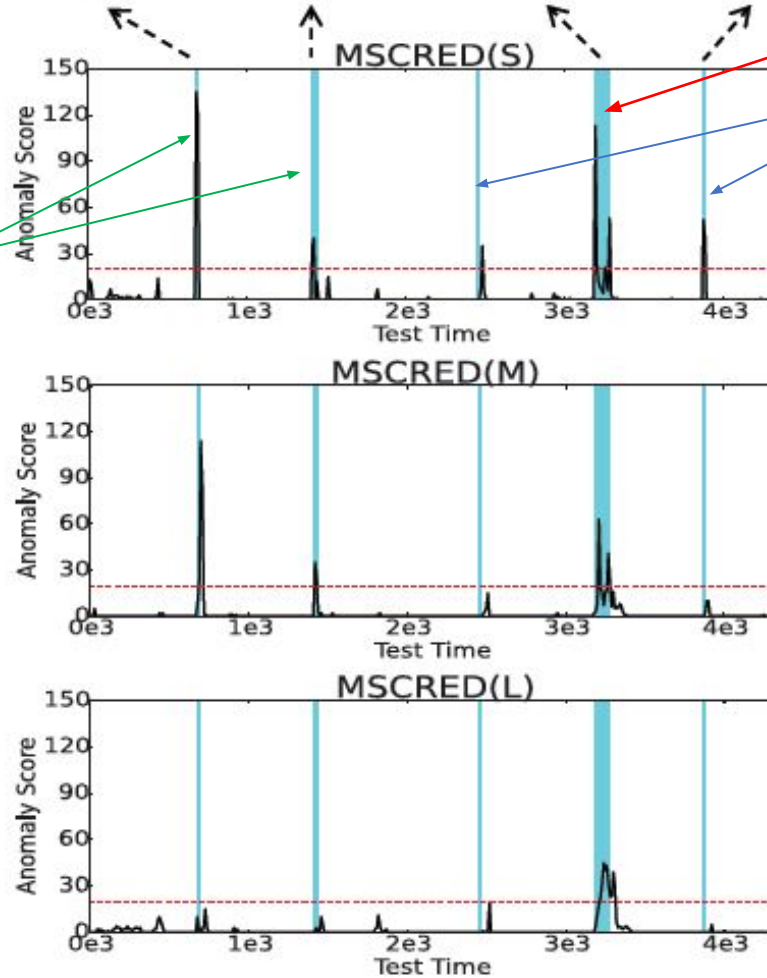


Figure 4 : Case study of anomaly diagnosis

Observation

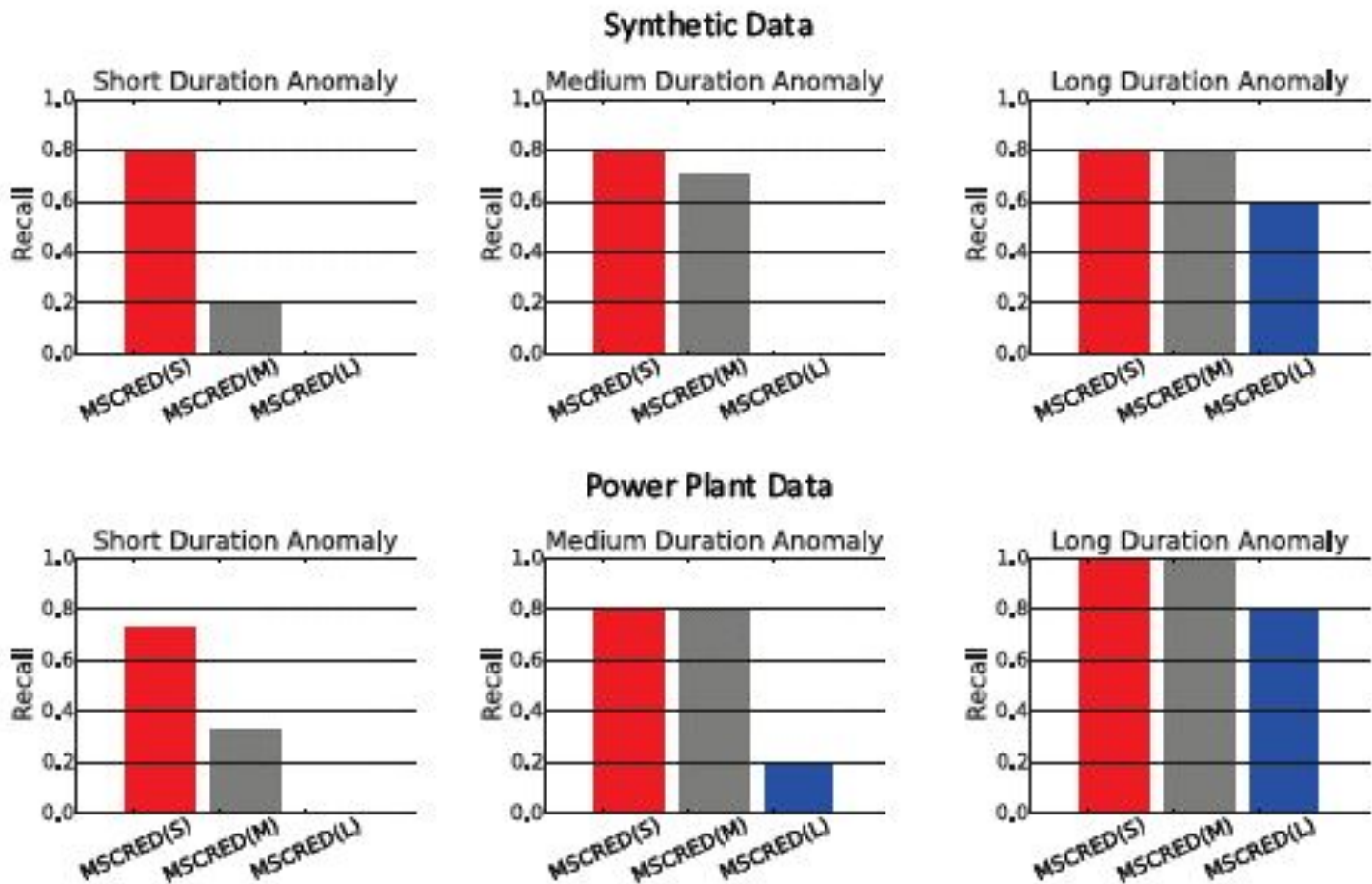
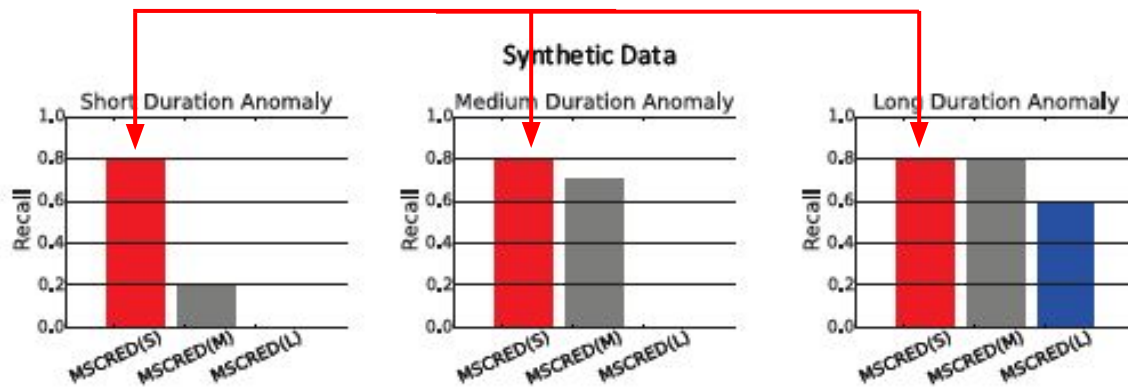


Figure 5 : Performance of 3 channels of MSCRED over different types of anomalies

Observation

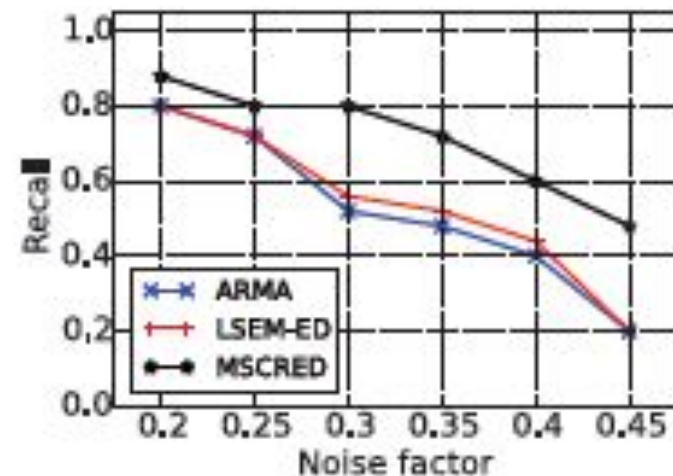
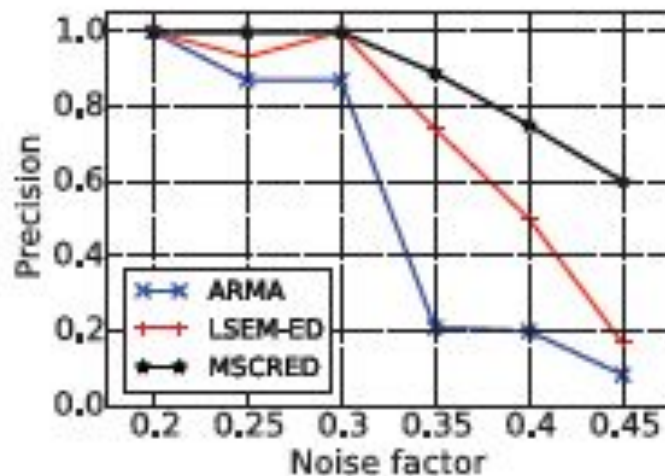
- (RQ4) Anomaly severity (duration) interpretation
 - MSCRED(S)
 - Detect all types of anomalies



- MSCRED(M)
 - Detect both medium and long duration anomalies
- MSCRED(L)
 - Detect the long duration anomaly
- For anomaly severity interpretation, we consider the three anomaly scores
 - eg) if the anomaly is detected in three channels, the anomaly is likely to be long duration

Observation

- (RQ5) Robustness to Noise
 - MSCRED consistently outperforms ARMA and LSTM-ED



The scale of noise varies from 0.2 to 0.45

Figure 6 : Impact of data noise on anomaly detection

Conclusion

- This paper proposed MSCRED for **anomaly detection and diagnosis in multivariate time series**
- MSCRED not only detects anomalies in certain time steps, but also identifies the root causes of anomalies and provides the interpretations of anomaly severity
- MSCRED employs multi-scale signature matrices and a deep encoder-decoder framework to reconstruct the signature matrices
- MSCRED is able to model both inter-sensor correlations and temporal dependencies in multivariate time series
- However, MSCRED cannot **model correlations between 3 or more elements** since the signature matrices calculate the correlation values between 2 elements
- It needs further study to solve this issue

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Thank you