TESSLA—A Temporal Stream-based Specification Language

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1 Introduction

Outline

- 1. purpose, motivation
 - online processing of data
 - monitoring of trace properties, specifically execution traces of programs
 - Functional reactive programming as related concept
- 2. What you describe with a TESSLA specification
 - input, output streams
 - application of functions, composition of function
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- 3. Modelling data in terms of streams
 - timing model ($\mathbb{R}, \mathbb{N}, \mathbb{Q}, \dots$), restrictions to streams with discrete set of time stamps (event streams) or peace-wise constant streams (continuous stream)
 - continuous streams and event streams
- 4. Functions on streams and desired properties (in general)
 - small examples
 - causality, statefulness, time invariance
 - (composition lemmata)
- 5. Tessla syntax
 - base grammar with functions and type annotations
 - syntactical extensions: infix operators, named arguments, the "on"

- 6. Types
 - Generic types
 - Coercion
- 7. Functional semantics of operators, small examples
- 8. Larger example/case study
 - producer/consumer, ring buffer, ...

2 Syntax

This section describes the syntax of TESSLA.

2.1 Basic Syntax

As basic syntactic elements of TESSLA we consider a set of types T, names \mathcal{N} and function symbols \mathcal{F} . Formally, the latter are two families $\mathcal{N} = (N_t)_{t \in T}$ and $\mathcal{F} = (F_{(t_1 \dots t_m)t_{m+1}})_{t_1 \dots t_{m+1} \in T^+}$ of distinct sets of symbols that correspond to a specific type or signature, respectively. We refer to the tuple $\Sigma = (T, \mathcal{N}, \mathcal{F})$ as a signature providing the basic syntactical elements of our specification language.

Built from those we define terms x of type $t \in T$ and sequences of terms seq by the grammar

$$x ::= n \mid f_c \mid f(seq) \mid x : t$$

$$seq ::= x \mid x, seq$$

where $n \in N_t$, $f_c \in F_{()t}$ (i.e., constants) and $f \in F_{(t_1 \dots t_m)t}$.

2.2 Syntactical Extensions

We consider three syntactical extensions to the base syntax presented above. The first is an *on* operator, the second are *infix operators* and the third are *named arguments*.

In the *on* operator only stateless functions are allowed. Therefore, for a set of function symbols $F_{(t_1...t_m)t}$ let $F_{(t_1...t_m)t}^s \subseteq F_{(t_1...t_m)t}$ be the set of function symbols of stateless functions. Hence the *terms* x of a type $t \in T$ including the *on* operator can be defined by the grammar

$$x ::= n \mid f_c \mid f(seq) \mid \text{on } f_s(seq_s) \mid x : t$$

$$seq ::= x \mid x, seq$$

$$y ::= n \mid f_c \mid f_s(seq_s) \mid \text{on } f_s(seq_s) \mid y : t$$

$$seq_s ::= y \mid y, seq_s$$

where $f_s \in F^s_{(t_1 \dots t_m)t}$ and the rest is defined as before.

3 Semantics

In this section, the semantics of TESSLA is defined. All in all, the functions used in TESSLA can be categorized in six different types. Before we start with the semantics of the function we will fix some notation first.

In the following we will use \mathcal{S}, \mathcal{C} and \mathcal{E} for the sets of all streams, continuous streams and event streams, respectively. With $\mathcal{C}[T]$ we refer to the set of continuous streams that only contain elements of the type T (f.e. $\mathcal{C}[\mathbb{B}]$ is the set of continuous boolean streams). We will use \mathbb{D} as the set of all values.

Furthermore we will use the function prev : $\mathcal{C} \times \mathbb{Q} \to \mathcal{C}$ to refer to the value that was on the stream prior to a certain time stamp, which is defined as follows:

$$\operatorname{prev}(c,t) = n \text{ with } \exists t' < t : c(t') = n \land \nexists t' < t'' < t : c(t'') \neq n$$

3.1 Arithmetic Functions

Arithmetic functions take a certain number of value streams of type integer and return a stream that contains either integer or boolean values. The semantics for the arithmetic functions are defined in the following.

The function add : $\mathcal{C}[\mathbb{N}] \times \mathcal{C}[\mathbb{N}] \to \mathcal{C}[\mathbb{N}]$ for adding the values of two integer streams is defined as follows:

$$add(n_1, n_2) = n_3$$
 with $n_3(t) = n_1(t) + n_2(t)$

The function sub : $\mathcal{C}[\mathbb{N}] \times \mathcal{C}[\mathbb{N}] \to \mathcal{C}[\mathbb{N}]$ for subtracting the values of the second integer stream from the value of the first integer stream is defined as follows:

$$sub(n_1, n_2) = n_3$$
 with $n_3(t) = n_1(t) - n_2(t)$

The function mul: $\mathcal{C}[\mathbb{N}] \times \mathcal{C}[\mathbb{N}] \to \mathcal{C}[\mathbb{N}]$ for multiplying the values of two integer streams is defined as follows:

$$\text{mul}(n_1, n_2) = n_3 \text{ with } n_3(t) = n_1(t) \cdot n_2(t)$$

The function geq: $\mathcal{C}[\mathbb{N}] \times \mathcal{C}[\mathbb{N}] \to \mathcal{C}[\mathbb{B}]$ for checking if the values of the first integer stream is at least as big as the value of the second integer stream is defined as follows:

$$geq(n_1, n_2) = b_1$$
 with $b_1(t) = n_1(t) \ge n_2(t)$

The function leq: $\mathcal{C}[\mathbb{N}] \times \mathcal{C}[\mathbb{N}] \to \mathcal{C}[\mathbb{B}]$ for checking if the values of the first integer stream is at least as big as the value of the second integer stream is defined as follows:

$$leq(n_1, n_2) = b_1$$
 with $b_1(t) = n_1(t) \le n_2(t)$

The function equals : $\mathcal{C}[\mathbb{N}] \times \mathcal{C}[\mathbb{N}] \to \mathcal{C}[\mathbb{B}]$ for checking if the values of two integer streams are equal is defined as follows:

equals
$$(n_1, n_2) = b_1$$
 with $b_1(t) = \begin{cases} \text{true} & \text{if } n_1(t) = n_2(t) \\ \text{false} & \text{else} \end{cases}$

The function max : $\mathcal{C}[\mathbb{N}] \times \mathcal{C}[\mathbb{N}] \to \mathcal{C}[\mathbb{N}]$ for getting the maximum of the current values of two integer streams is defined as follows:

$$\max(n_1, n_2) = n_3 \text{ with } n_3(t) = \begin{cases} n_1(t) & \text{if } n_1(t) > n_2(t) \\ n_2(t) & \text{else} \end{cases}$$

The function $\min: \mathcal{C}[\mathbb{N}] \times \mathcal{C}[\mathbb{N}] \to \mathcal{C}[\mathbb{N}]$ for getting the minimum of the current values of two integer streams is defined as follows:

$$\max(n_1, n_2) = n_3 \text{ with } n_3(t) = \begin{cases} n_1(t) & \text{if } n_1(t) < n_2(t) \\ n_2(t) & \text{else} \end{cases}$$

The function not : $\mathcal{C}[\mathbb{B}] \to \mathcal{C}[\mathbb{B}]$ for getting the negation of the value of a boolean stream is defined as follows:

$$not(b_1) = b_2 \text{ with } b_2(t) = \neg b_1(t)$$

The function or : $\mathcal{C}[\mathbb{B}] \times \mathcal{C}[\mathbb{B}] \to \mathcal{C}[\mathbb{B}]$ for combining two boolean streams with an or is defined as follows:

$$or(b_1, b_2) = b_3$$
 with $b_3(t) = b_1(t) \vee b_2(t)$

3.2 Timing Functions

Timing functions take a certain number of continuous streams and return a continuous or event stream. The semantics for the timing functions are defined in the following.

The function delay: $\mathcal{C} \times \mathbb{Q} \to \mathcal{C}$ for delaying the values of the input stream for a certain amount of time is defined as follows:

$$delay(c_1, q) = c_2$$
 with $c_2(t) = c_1(t - q)$

The function getTimestamp : $\mathcal{C} \to \mathbb{Q}$ for replacing the values of the input stream with its timestamps is defined as follows:

getTimestamp
$$(c_1) = c_2$$
 with $c_2(t) = t$

The function in Past : $\mathcal{C} \times \mathbb{D} \times \mathbb{Q} \to \mathcal{C}[\mathbb{B}]$ for checking if a certain value holds in a given time frame in the past is defined as follows:

inPast
$$(c_1, d, q) = b$$
 with $b(t) = \begin{cases} \text{true} & \text{if } \exists t - q \leq t' \leq t : c_1(t') = d \\ \text{false} & \text{else} \end{cases}$

The function synchronize : $\mathcal{C} \times \mathcal{C} \times \mathbb{Q} \to \mathcal{E}$ for checking whether a corresponding event occurs in the second stream for each event in the first stream within a certain time frame is defined as follows:

$$\operatorname{synchronize}(c_1,c_2,q) = e_1 \text{ with } e_1(t) = \begin{cases} \top & \text{if } c_1(t-q) = x_i \land \forall t-q \leq t' \leq t : c_2(t') \neq y_i \\ \bot & \text{else} \end{cases}$$

 x_i bzw. y_i . Is there a better way?

3.3 Aggregations

Aggregation functions take a certain number of continuous streams and return an continuous integer stream. The semantics for the aggregation functions are defined in the following. second input / reset still missing!

The function maximum : $\mathcal{C}[\mathbb{N}] \to \mathcal{C}[\mathbb{N}]$ for computing the maximum of all values that occurred on the stream is defined as follows:

$$\max(n_1) = n_2 \text{ with } \forall t' < t : n_2(t) \ge n_1(t') \land \exists t' < t : n_2(t) = n_1(t')$$

The function minimum : $\mathcal{C}[\mathbb{N}] \to \mathcal{C}[\mathbb{N}]$ for computing the minimum of all values that occurred on the stream is defined as follows:

$$\min(n_1) = n_2 \text{ with } \forall t' < t : n_2(t) \le n_1(t') \land \exists t' < t : n_2(t) = n_1(t')$$

The function sum : $\mathcal{C}[\mathbb{N}] \to \mathcal{C}[\mathbb{N}]$ for computing the sum of all values that occurred on the stream is defined as follows:

$$\operatorname{sum}(n_1) = n_2 \text{ with } ???$$

The function event Count : $\mathcal{S} \to \mathcal{C}[\mathbb{N}]$ for computing the number of Events that occurred on the stream is defined as follows:

eventCount
$$(s_1) = n_1$$
 with ???

3.4 Selectors/Filters/Conditionals/Combinators

The function if Then: $\mathcal{C}[\mathbb{B}] \times \mathcal{C} \to \mathcal{C}$ for returning the value of the second input stream if the value of the first stream is true is defined as follows:

if Then
$$(b_1, c_1) = c_2$$
 with $c_2(t) = \begin{cases} c_1(t) & \text{if } b_1(t) \\ \text{prev}(c_2, t) & \text{else} \end{cases}$

The function if ThenElse : $\mathcal{C}[\mathbb{B}] \times \mathcal{C} \times \mathcal{C} \to \mathcal{C}$ for returning the value of the second input stream if the value of the first stream is true and the value of the third input stream otherwise is defined as follows:

ifThenElse
$$(b_1, c_1, c_2) = c_3$$
 with $c_3(t) = \begin{cases} c_1(t) & \text{if } b_1(t) \\ c_2(t) & \text{else} \end{cases}$

The function merge : $\mathcal{C} \times \mathcal{C} \to \mathcal{C}$ for merging two streams is defined as follows:

$$merge(c_1, c_2) = c_3$$
 with ????

3.5 Monitors

The monitor function can be used to enable the usage of temporal logics within TESSLA. A monitor takes a temporal logic formula and returns an output value that depends on the evaluation status of the given formula at the current point in time. Let TL be a temporal logic, $\varphi \in TL$ a formula of TL and $[\![.,.]\!]_{TL}: TL \times \mathbb{Q} \to \mathcal{C}$ be the function that returns the truth value of φ at a certain point in time. Then the semantics of the function monitor: $TL \to \mathcal{C}$ is given as follows:

monitor(
$$\varphi$$
) = c_1 with $c_1(t) = [\![\varphi, t]\!]_{TL}$

3.6 On