

# Sequential Parameter Optimization

## Using sklearn Surrogates

- This notebook explains how different surrogate models from `scikit-learn` can be used as surrogates in `spotPython` optimization runs.

```
import numpy as np
from math import inf
from spotPython.fun.objectivefunctions import analytical
from spotPython.spot import spot
from scipy.optimize import shgo
from scipy.optimize import direct
from scipy.optimize import differential_evolution
import matplotlib.pyplot as plt
```

### 1 Example: Branin Function with `spotPython`'s Internal Kriging Surrogate

#### The Objective Function Branin

- The `spotPython` package provides several classes of objective functions.
- We will use an analytical objective function, i.e., a function that can be described by a (closed) formula.
- Here we will use the Branin function:

$y = a * (x_2 - b * x_1^2 + c * x_1 - r) ** 2 + s * (1 - t) * \cos(x_1) + s$ ,  
where values of  $a$ ,  $b$ ,  $c$ ,  $r$ ,  $s$  and  $t$  are:  $a = 1$ ,  $b = 5.1 / (4 * \pi^2)$ ,  
 $c = 5 / \pi$ ,  $r = 6$ ,  $s = 10$  and  $t = 1 / (8 * \pi)$ .

- It has three global minima:

$f(x) = 0.397887$  at  $(-\pi, 12.275)$ ,  $(\pi, 2.275)$ , and  $(9.42478, 2.475)$ .

```
from spotPython.fun.objectivefunctions import analytical
lower = np.array([-5,-0])
upper = np.array([10,15])
```

```
fun = analytical().fun_branin
```

## Running the surrogate model based optimizer Spot:

```
spot_2 = spot.Spot(fun=fun,
                   lower = lower,
                   upper = upper,
                   fun_evals = 20,
                   max_time = inf,
                   seed=123,
                   design_control={"init_size": 10})
```

```
spot_2.run()
```

<spotPython.spot.spot.Spot at 0x1055146d0>

## Print the Results

```
spot_2.print_results()
```

min y: 0.3982295132785083

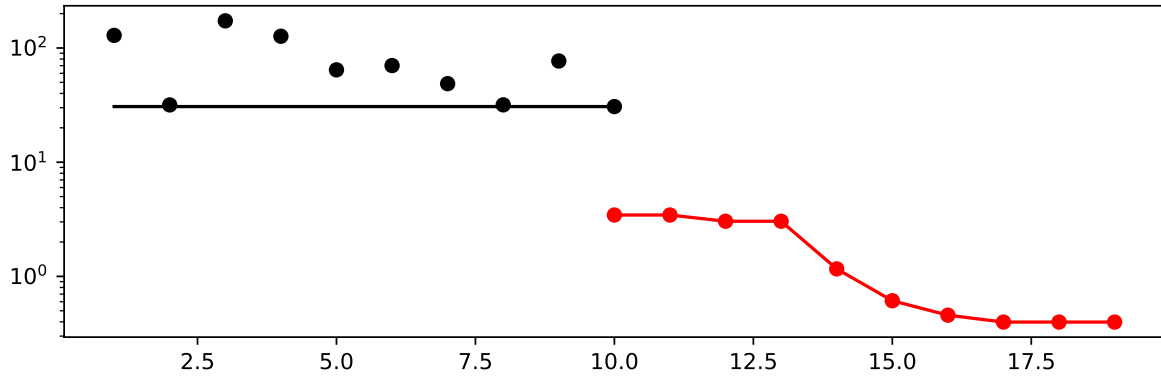
x0: 3.135528626303215

x1: 2.2926027772585886

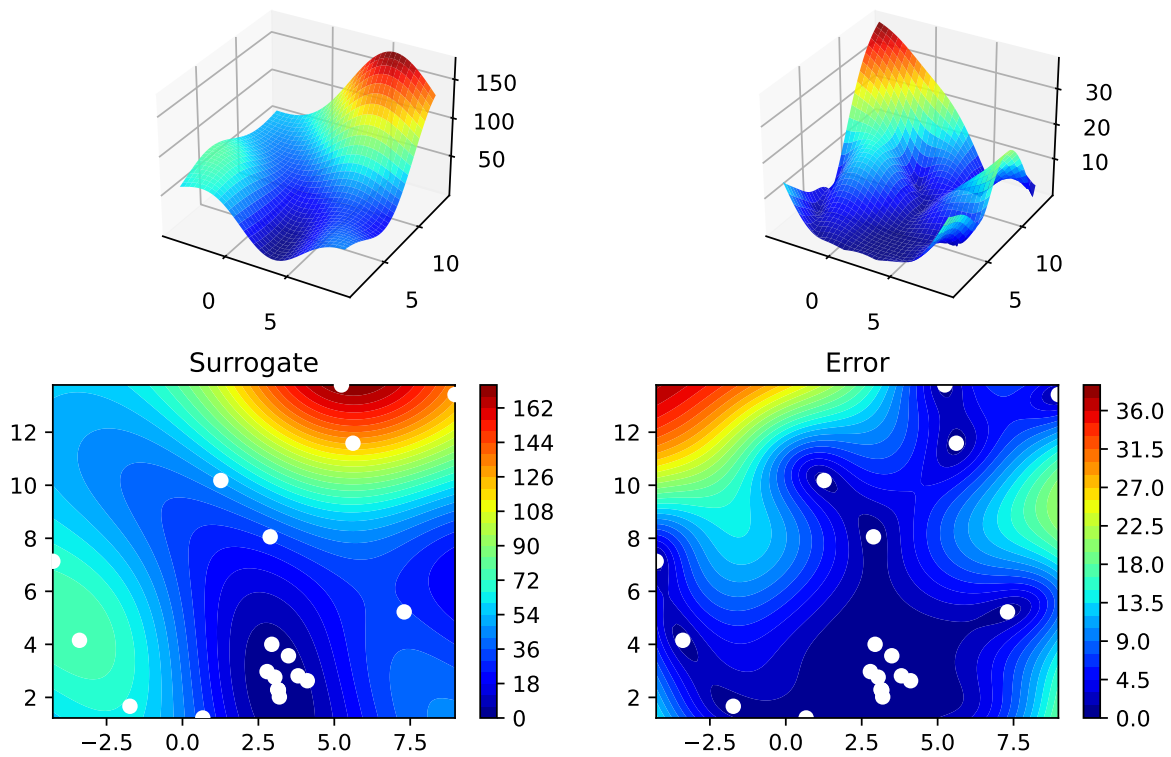
```
[['x0', 3.135528626303215], ['x1', 2.2926027772585886]]
```

## Show the Progress and the Surrogate

```
spot_2.plot_progress(log_y=True)
```



```
spot_2.surrogate.plot()
```



## 2 Example: Using Surrogates From scikit-learn

- Default is the `spotPython` (i.e., the internal) `kriging` surrogate.

- It can be called explicitly and passed to `Spot`.

```
from spotPython.build.kriging import Kriging
S_0 = Kriging(name='kriging', seed=123)
```

- Alternatively, models from `scikit-learn` can be selected, e.g., Gaussian Process, RBFs, Regression Trees, etc.

```
# Needed for the sklearn surrogates:
from sklearn.gaussian_process import GaussianProcessRegressor
from sklearn.gaussian_process.kernels import RBF
from sklearn.tree import DecisionTreeRegressor
from sklearn.ensemble import RandomForestRegressor
from sklearn import linear_model
from sklearn import tree
import pandas as pd
```

- Here are some additional models that might be useful later:

```
S_Tree = DecisionTreeRegressor(random_state=0)
S_LM = linear_model.LinearRegression()
S_Ridge = linear_model.Ridge()
S_RF = RandomForestRegressor(max_depth=2, random_state=0)
```

## GaussianProcessRegressor as a Surrogate

- To use a Gaussian Process model from `sklearn`, that is similar to `spotPython`'s `Kriging`, we can proceed as follows:

```
kernel = 1 * RBF(length_scale=1.0, length_scale_bounds=(1e-2, 1e2))
S_GP = GaussianProcessRegressor(kernel=kernel, n_restarts_optimizer=9)
```

- The `scikit-learn` GP model `S_GP` is selected for `Spot` as follows:

```
surrogate = S_GP
```

- We can check the kind of surrogate model with the command `isinstance`:

```
isinstance(S_GP, GaussianProcessRegressor)
```

True

```
isinstance(S_0, Kriging)
```

True

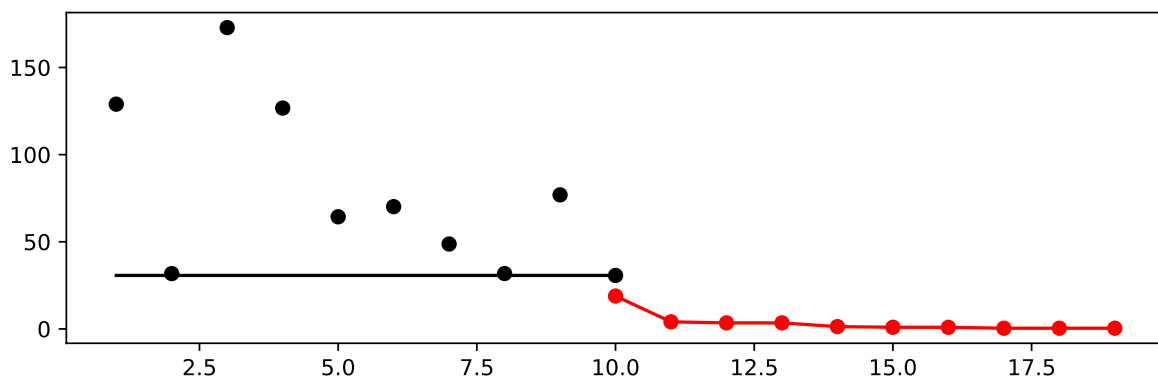
- Similar to the `Spot` run with the internal `Kriging` model, we can call the run with the `scikit-learn` surrogate:

```
fun = analytical(seed=123).fun_branin
spot_2_GP = spot.Spot(fun=fun,
                      lower = lower,
                      upper = upper,
                      fun_evals = 20,
                      seed=123,
                      design_control={"init_size": 10},
                      surrogate = S_GP)

spot_2_GP.run()
```

<spotPython.spot.spot.Spot at 0x15f6d8520>

```
spot_2_GP.plot_progress()
```



```
spot_2_GP.print_results()
```

min y: 0.3981374078297275

x0: 3.1487804058178295

x1: 2.270819139265872

```
[['x0', 3.1487804058178295], ['x1', 2.270819139265872]]
```

### 3 Example: One-dimensional Sphere Function With spotPython's Kriging

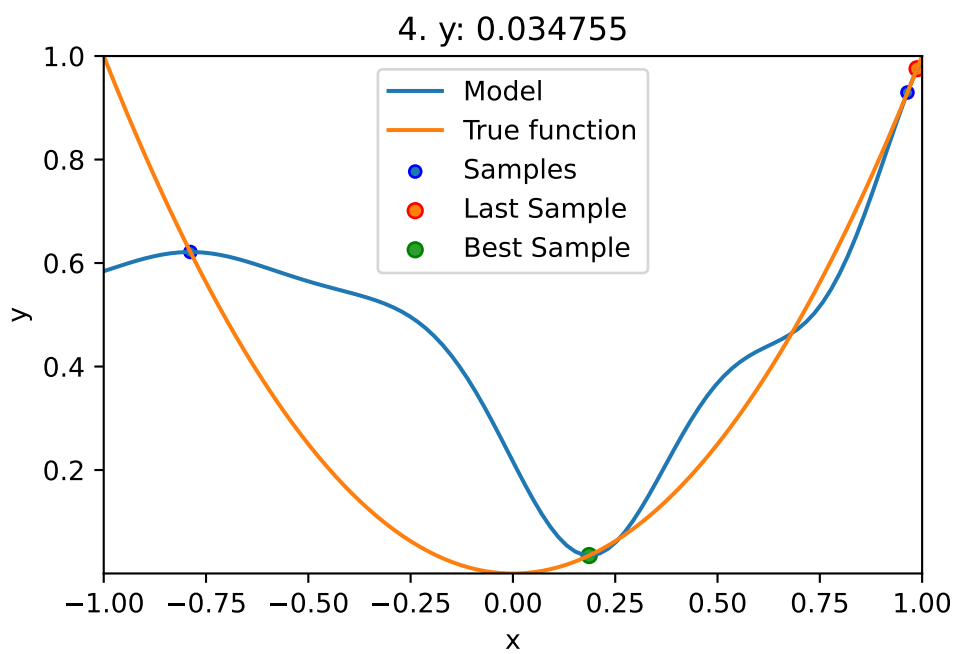
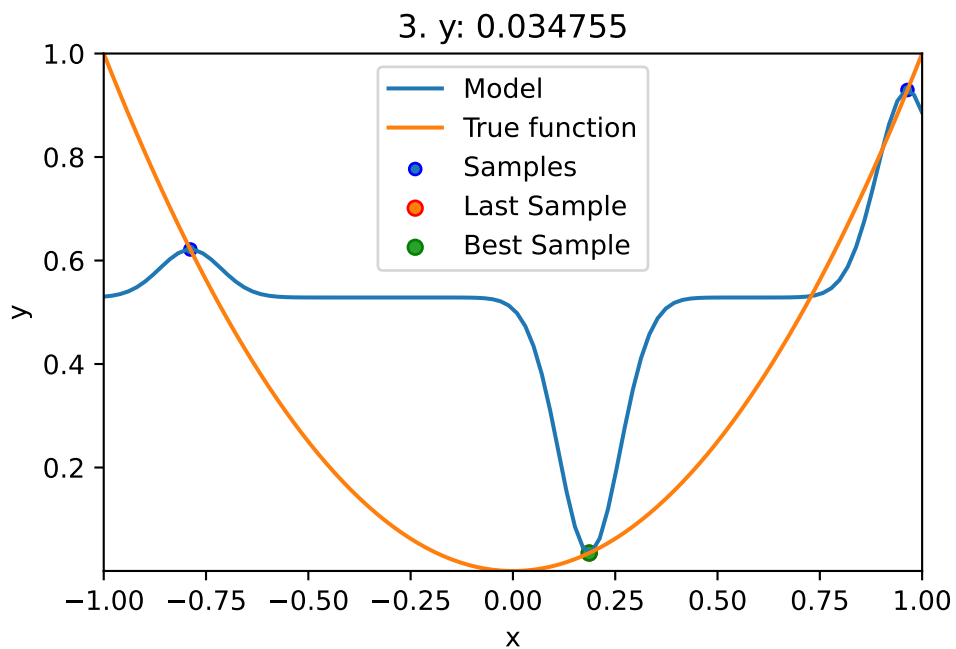
- In this example, we will use an one-dimensional function, which allows us to visualize the optimization process.

– `show_models= True` is added to the argument list.

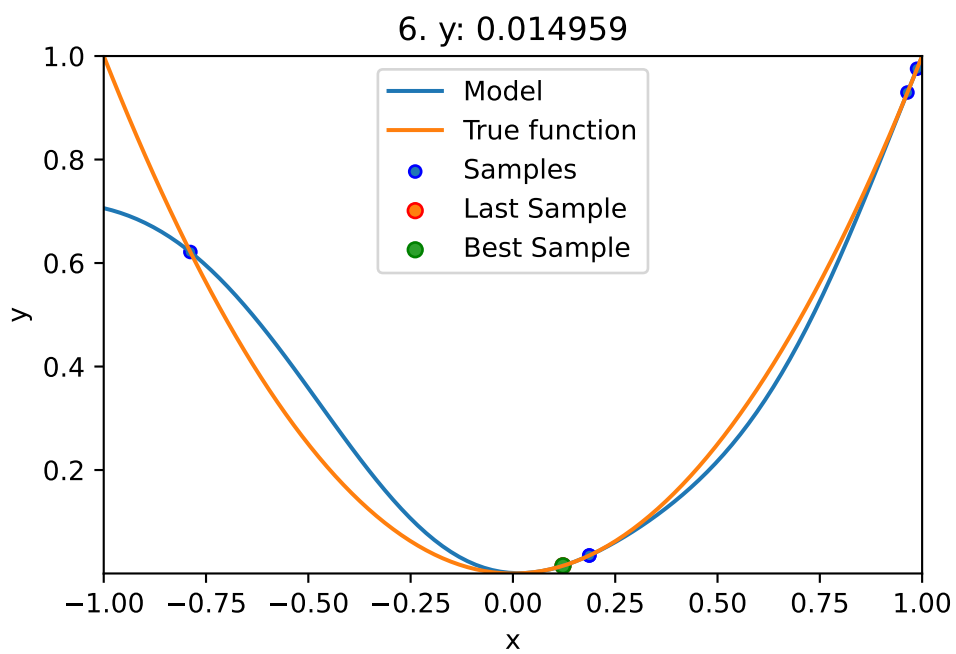
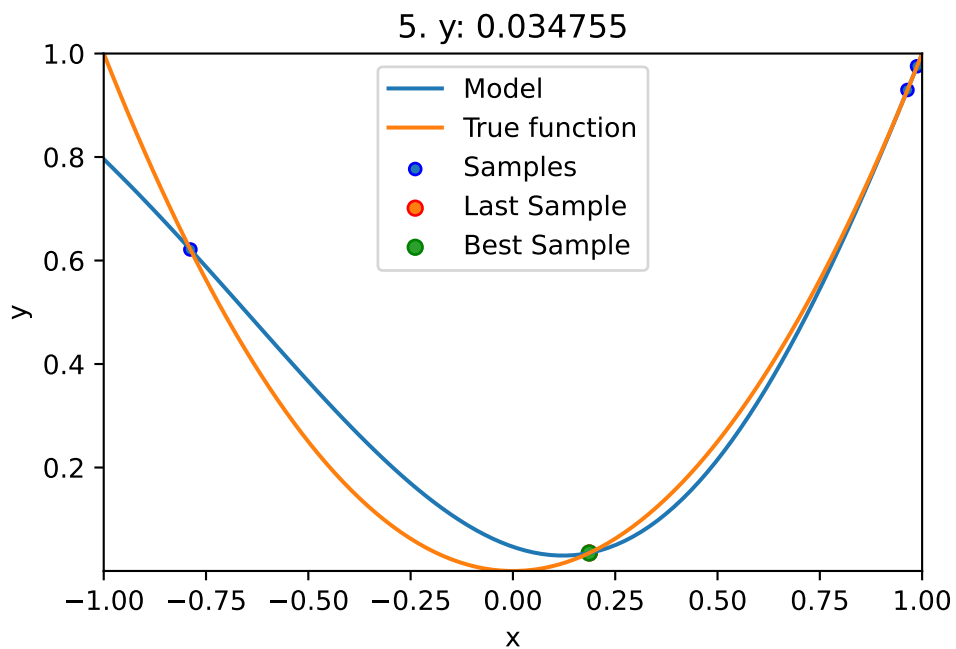
```
from spotPython.fun.objectivefunctions import analytical
lower = np.array([-1])
upper = np.array([1])
fun = analytical(seed=123).fun_sphere
```

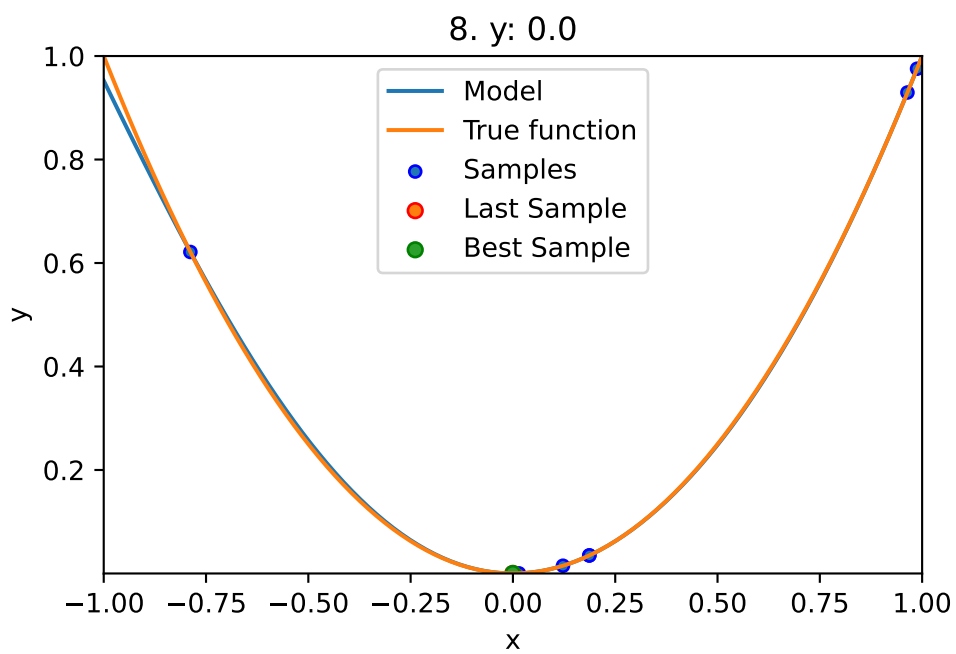
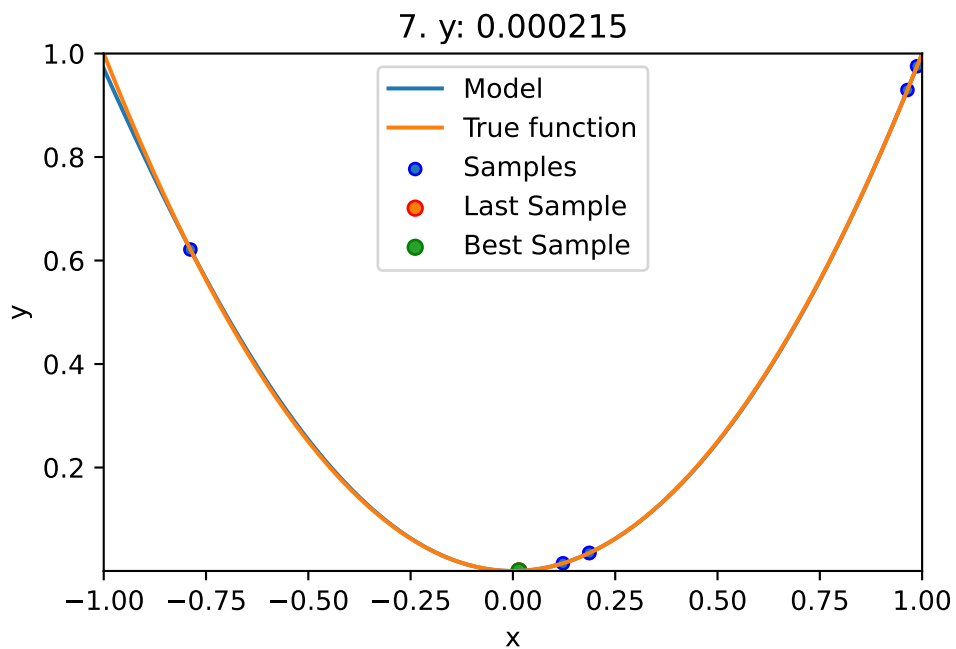
```
spot_1 = spot.Spot(fun=fun,
                   lower = lower,
                   upper = upper,
                   fun_evals = 10,
                   max_time = inf,
                   seed=123,
                   show_models= True,
                   tolerance_x = np.sqrt(np.spacing(1)),
                   design_control={"init_size": 3},)

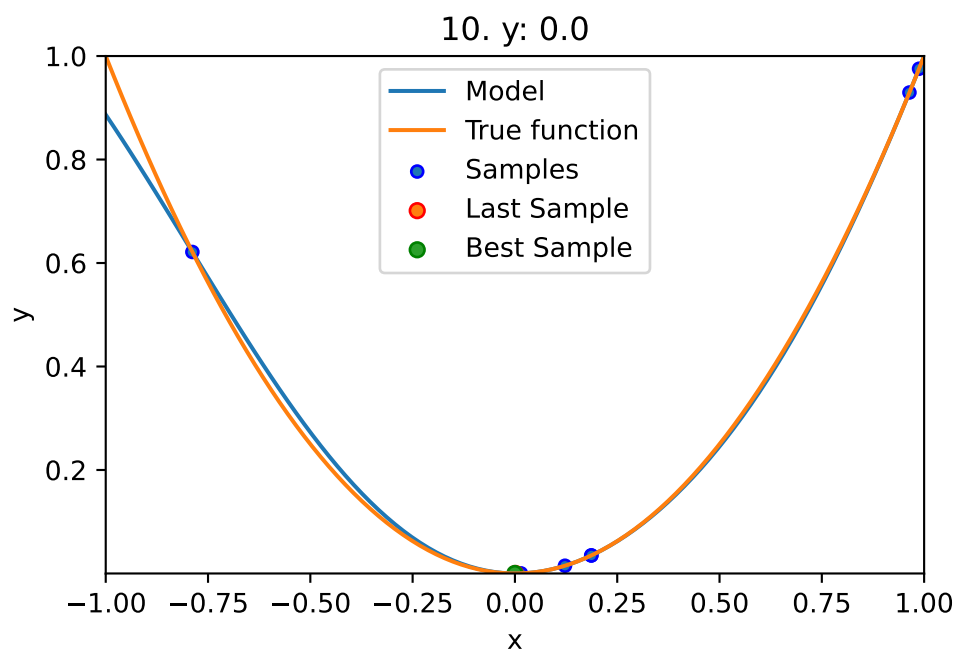
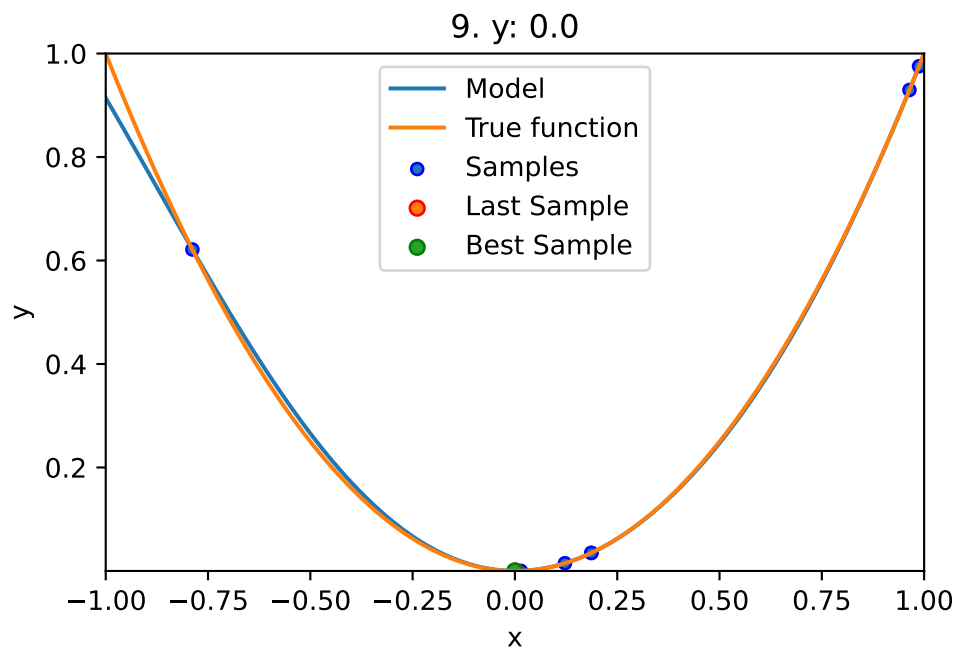
spot_1.run()
```











<spotPython.spot.spot.Spot at 0x16c684820>

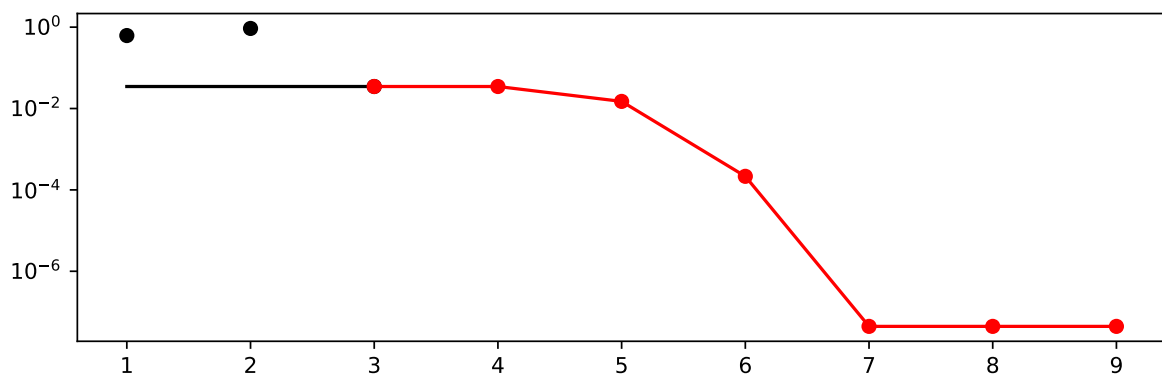
## Results

```
spot_1.print_results()
```

```
min y: 4.41925228274096e-08  
x0: -0.00021022017702259125
```

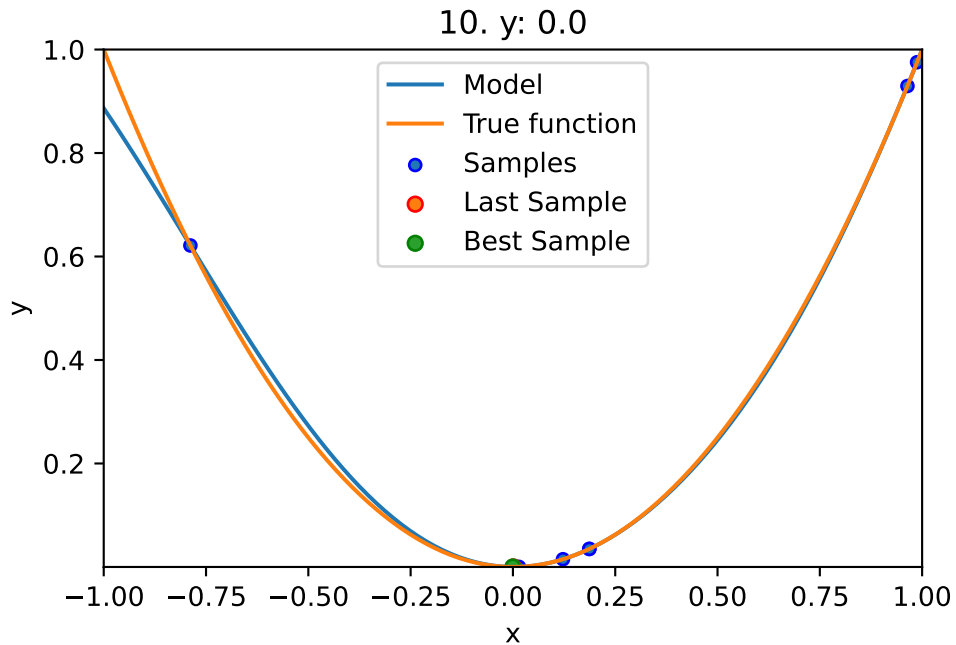
```
[['x0', -0.00021022017702259125]]
```

```
spot_1.plot_progress(log_y=True)
```



- The method `plot_model` plots the final surrogate:

```
spot_1.plot_model()
```

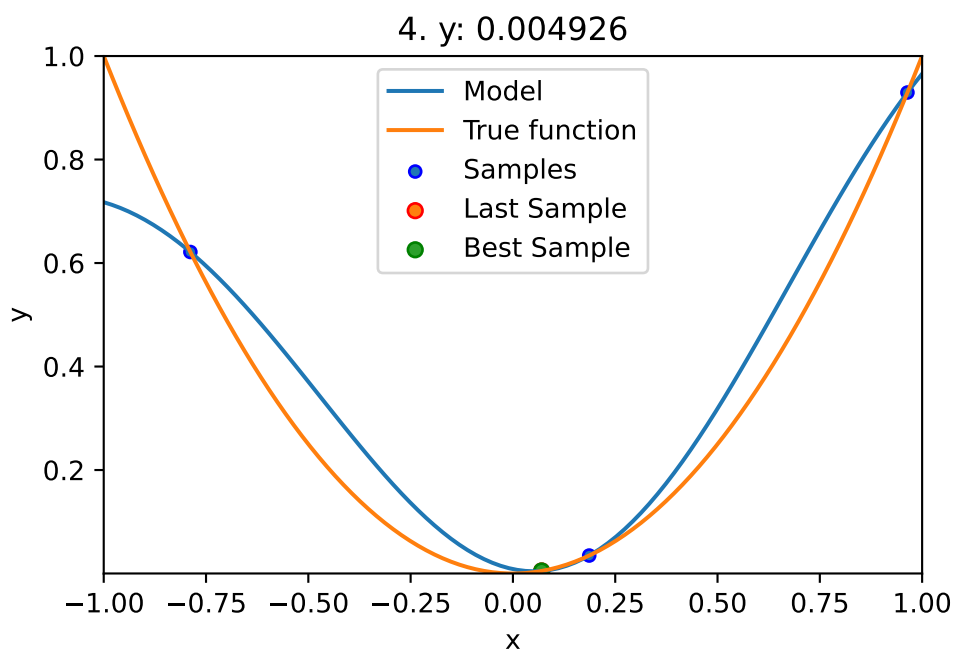
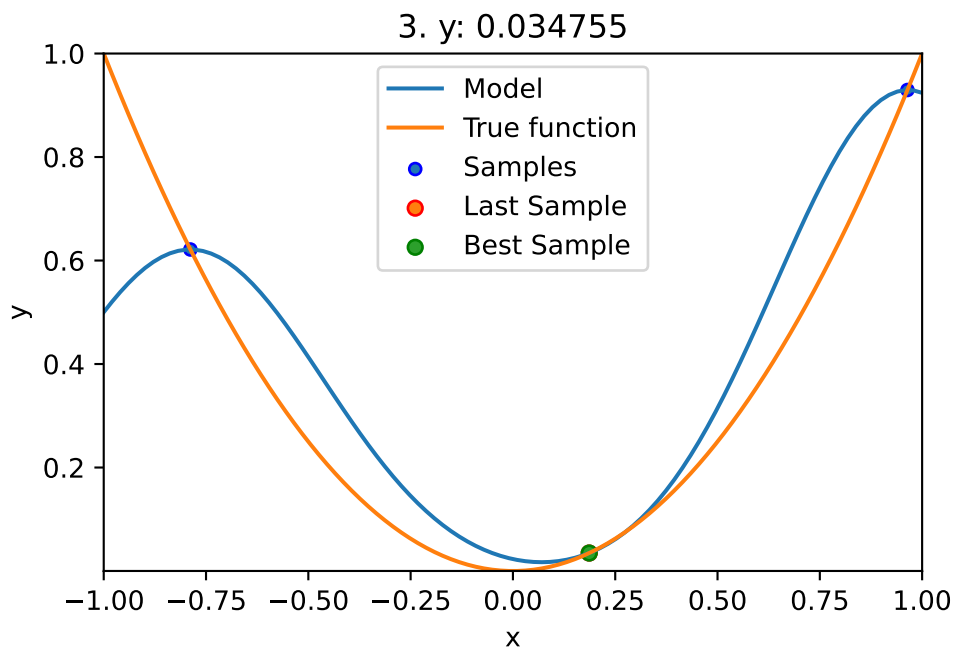


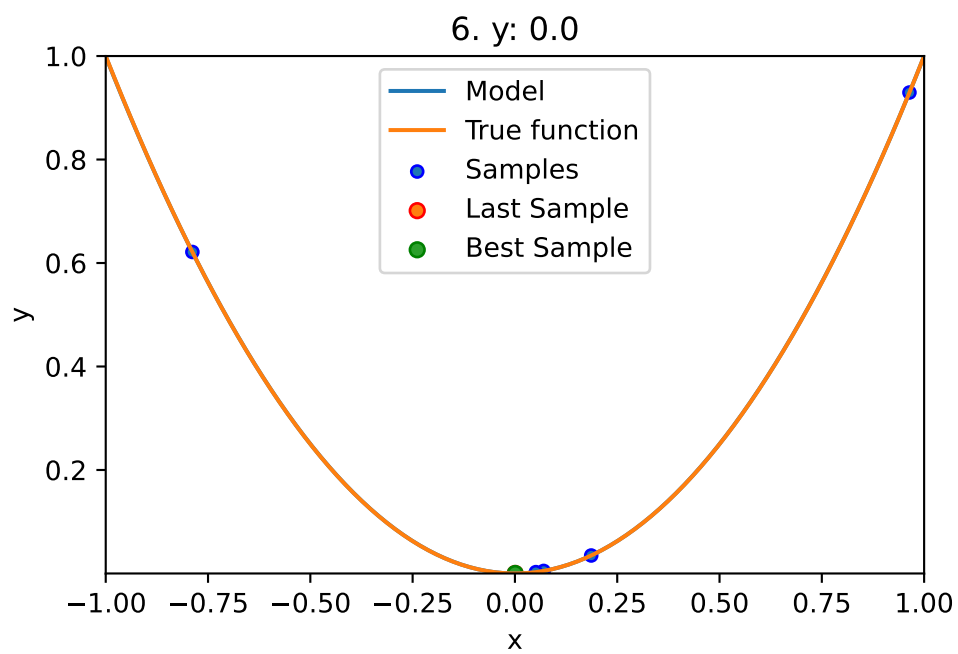
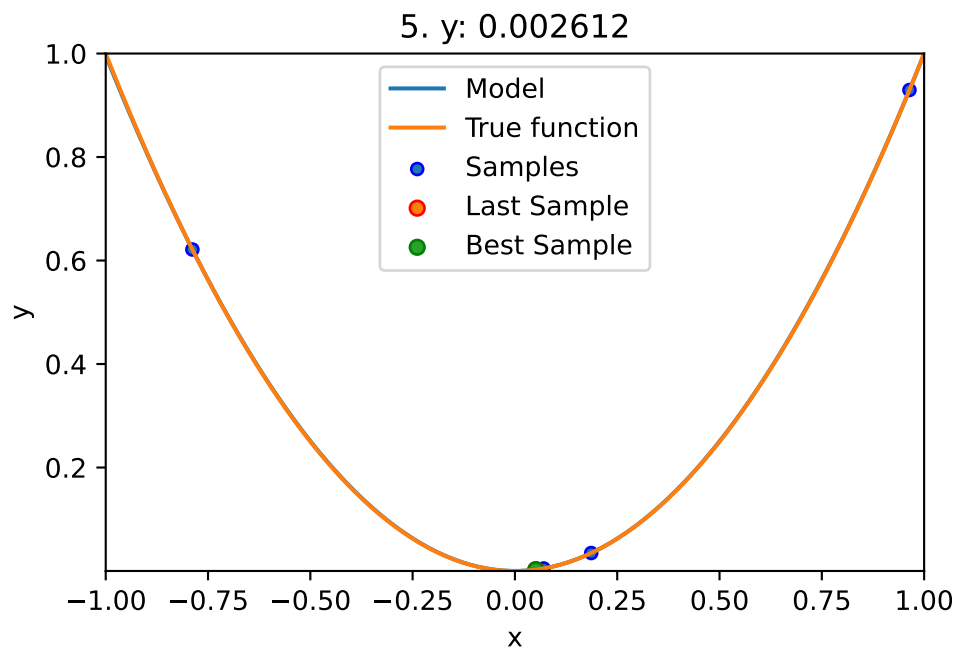
#### 4 Example: Sklearn Model GaussianProcess

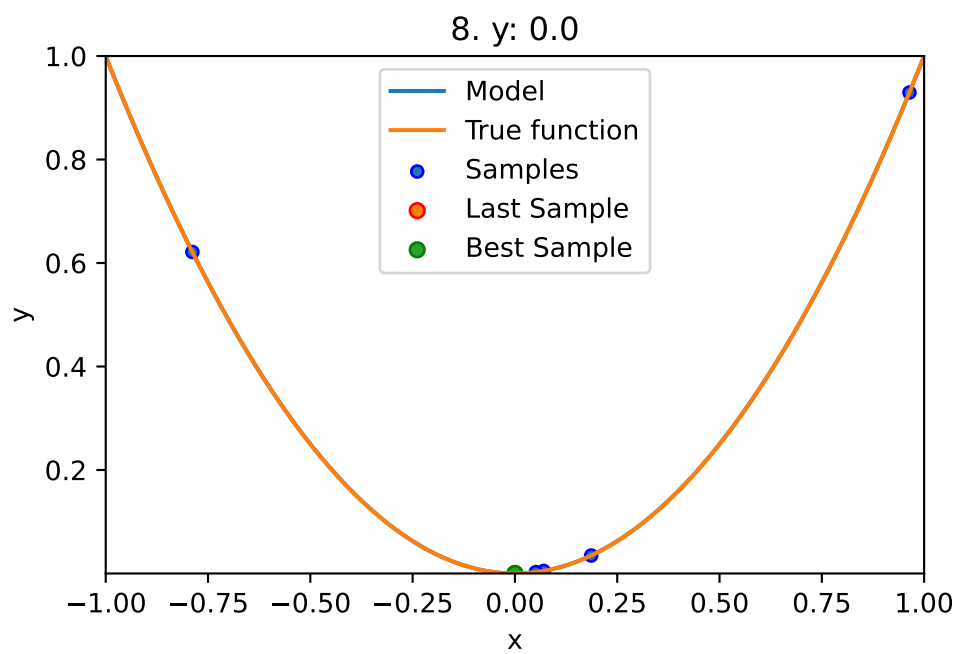
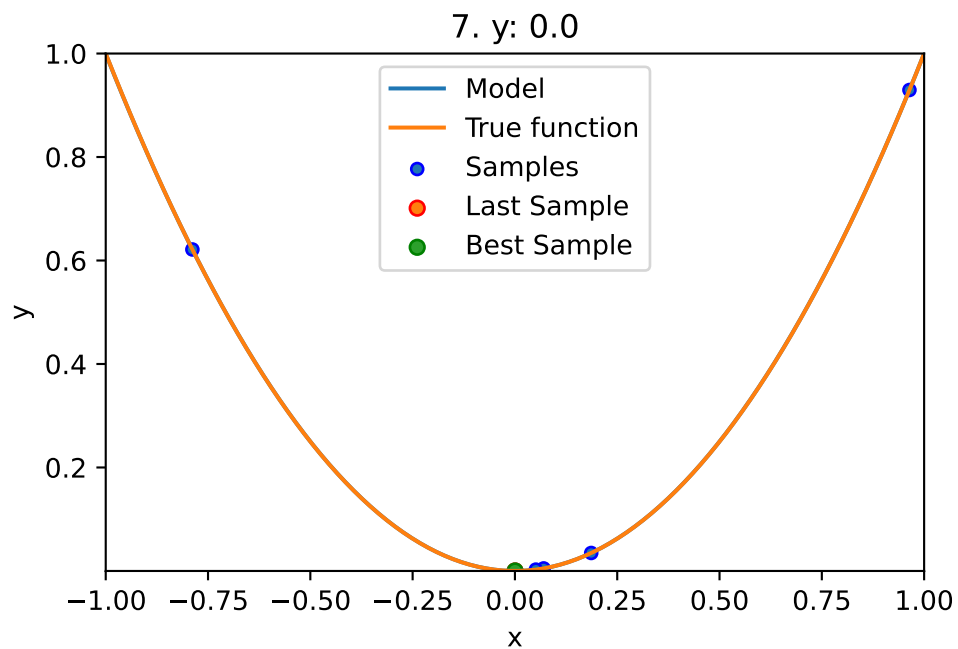
- This example visualizes the search process on the `GaussianProcessRegression` surrogate from `sklearn`.
- Therefore `surrogate = S_GP` is added to the argument list.

```
fun = analytical(seed=123).fun_sphere
spot_1_GP = spot.Spot(fun=fun,
                      lower = lower,
                      upper = upper,
                      fun_evals = 10,
                      max_time = inf,
                      seed=123,
                      show_models= True,
                      design_control={"init_size": 3},
                      surrogate = S_GP)

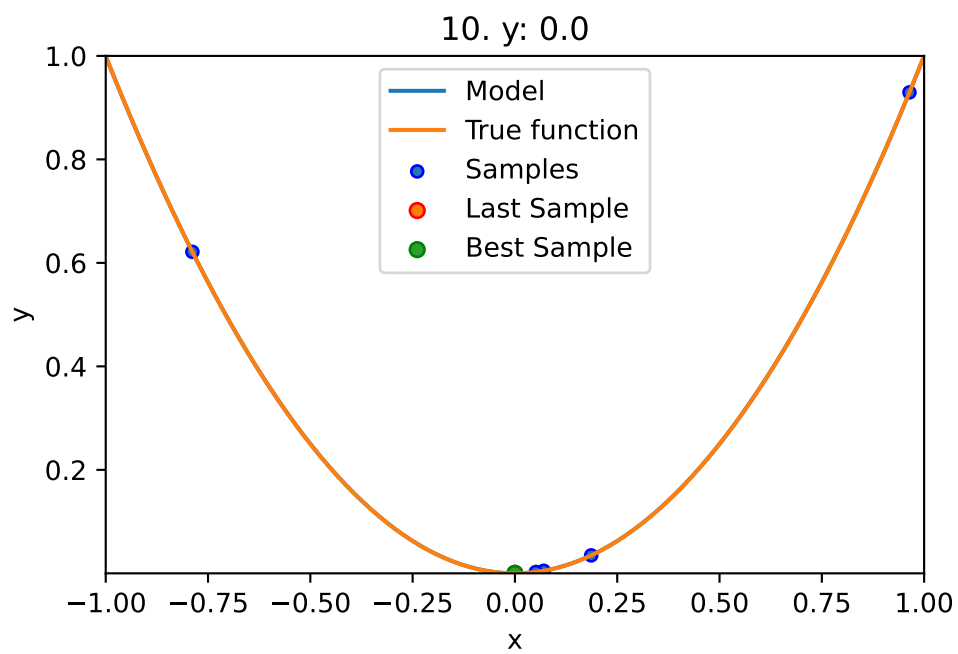
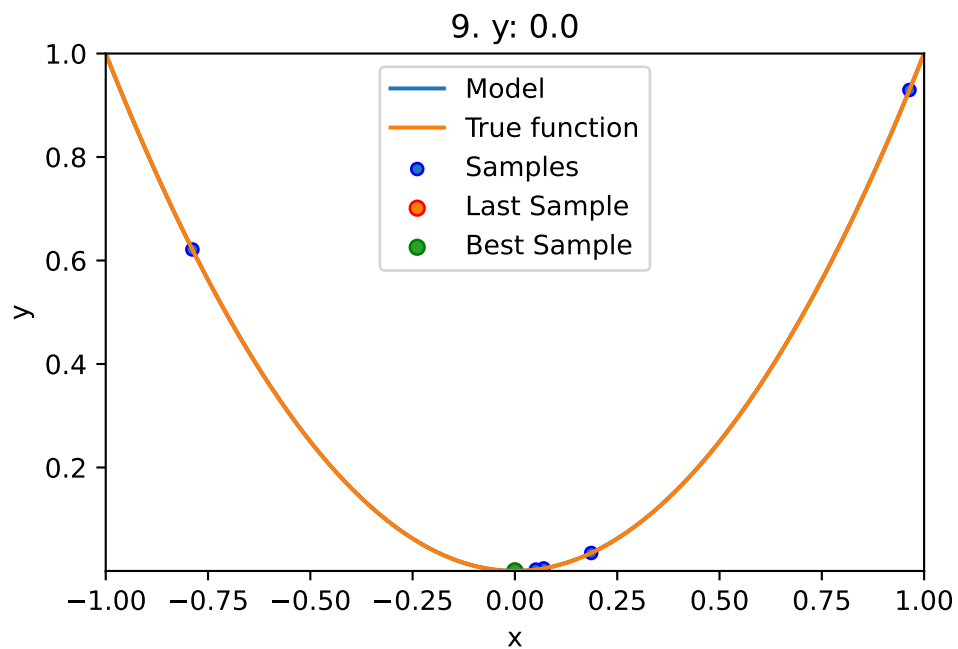
spot_1_GP.run()
```











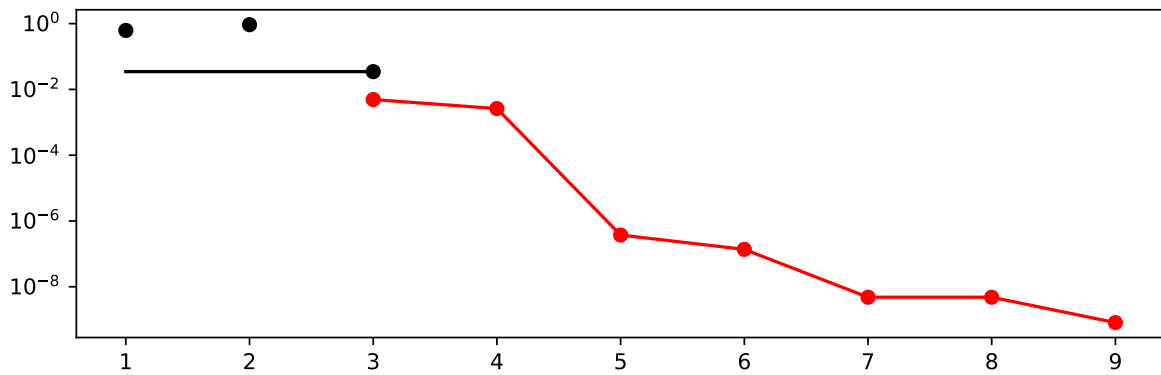
<spotPython.spot.spot.Spot at 0x2973dd660>

```
spot_1_GP.print_results()
```

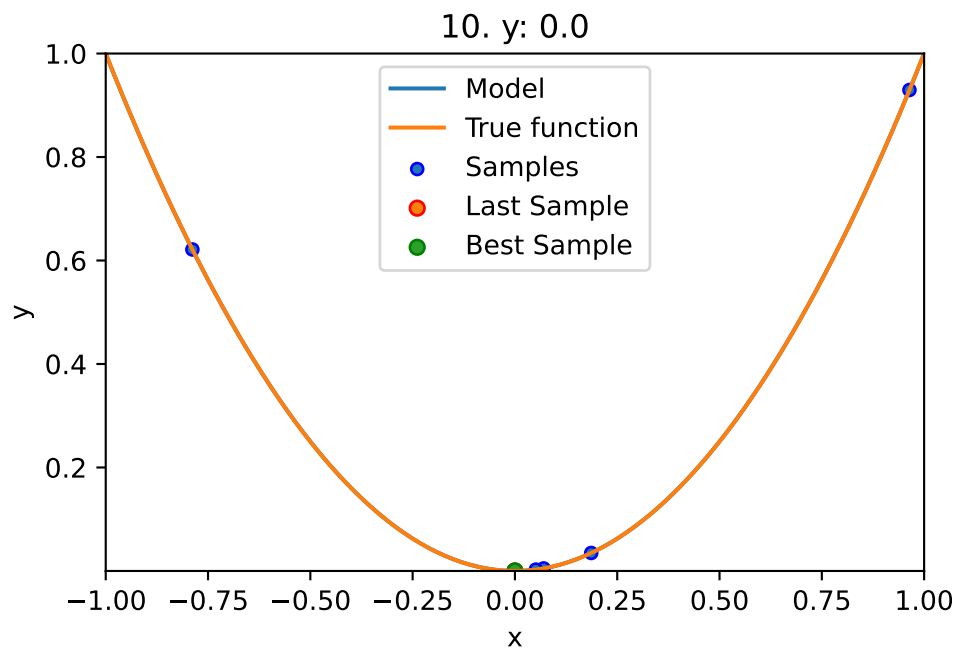
```
min y: 8.124838862354748e-10  
x0: -2.8504102971949052e-05
```

```
[['x0', -2.8504102971949052e-05]]
```

```
spot_1_GP.plot_progress(log_y=True)
```



```
spot_1_GP.plot_model()
```



# Exercises

- Important:
  - Results from these exercises should be added to this document, i.e., you should submit an updated version of this notebook.
  - Please combine your results using this notebook.
  - Only one notebook from each group!
  - Presentation is based on this notebook. No additional slides are required!
  - spotPython version 0.16.11 (or greater) is required (see <http://www.gm.fh-koeln.de/~bartz/site/download/>)

## Exercise 1

- Each team member should choose one of the following surrogates and repeat the experiments from Example 2 and Example 4.
- Please add your name to the section title!

### 1. `DecisionTreeRegressor`

- Describe the surrogate model.
- Use the surrogate as the model for optimization.

### 2. `RandomForestRegressor`

- Describe the surrogate model.
- Use the surrogate as the model for optimization.

### 3. `linear_model.LinearRegression`

- Describe the surrogate model.
- Use the surrogate as the model for optimization.

#### 4. `linear_model.Ridge`

- Describe the surrogate model.
- Use the surrogate as the model for optimization.

### Exercise 2

- (All group members): Compare the performance of the 5 different surrogates on both objective functions:
  - `spotPython`'s internal Kriging
  - `DecisionTreeRegressor`
  - `RandomForestRegressor`
  - `linear_model.LinearRegression`
  - `linear_model.Ridge`

## **Solutions**

### **1. DecisionTreeRegressor**

#### **1.1. Branin**

#### **1.2. Sphere**

### **2. RandomForestRegressor**

#### **2.1 Branin**

#### **2.2 Sphere**

### **3. linear\_model.LinearRegression**

#### **3.1 Branin**

#### **3.2 Sphere**

### **4. linear\_model.Ridge**

#### **4.1 Branin**

#### **4.2 Sphere**