# The Riemann Field (ABF v5.0): Analytic-Beyond Fusion Concept + Illustrative Plots

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#### Abstract

We package a compact ABF v5.0 scaffold: (i) a concept diagram linking weighted NB/BD stability to an information-balance layer, and (ii) a small illustrative regression on  $\log \log N$  vs.  $\log \text{MSE}^*$ . This is heuristic documentation, not a proof of RH.

#### 1 Analytic core (NB/BD + weighted Hilbert)

Let  $a_n = \mu(n) v(n/N) q(n)$  with  $v \in C_0^{\infty}(0,1)$  and slowly varying q. With the kernel

$$K_{mn} = e^{-\frac{1}{2}|\log(m/n)|} = \min\{\sqrt{m/n}, \sqrt{n/m}\},\$$

a band-sum argument and Möbius cancellation yield a decay of off-diagonals

$$\sum_{m \neq n} a_m a_n K_{mn} \le C(\log N)^{-\theta} \sum_n a_n^2, \quad \theta > 0,$$

stabilizing the NB/BD normal equations.

## ${\bf 2} \quad {\bf Beyond \ layer \ (design \rightarrow observed \ error)}$

Design choices (window width  $\sigma$ , ridge  $\lambda$ , boundary weights  $w_{\pm}$ ) alter the empirical split (MSE<sub>+</sub>, MSE<sub>-</sub>, MSE\*). The parameters  $(\eta, \theta)$  serve as balance surrogates:  $\eta$  for arithmetic cancellation,  $\theta$  for residual off-diagonal decay.

### 3 Illustrative toy fit

We show a small toy regression of  $\log \log N$  vs.  $\log \text{MSE}^*$ ; the goal is to demonstrate how to reproduce comparative plots. Replace with real CSV in production.

**Reproducibility.** The figure-generating code is provided in this package; swap in your CSV to regenerate.

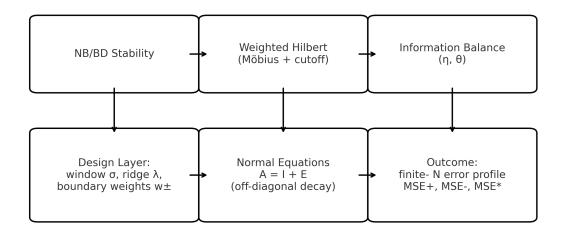


Figure 1: ABF v5.0 concept map: NB/BD stability  $\Rightarrow$  decay in off-diagonals; design layer modulates the observed error profile.

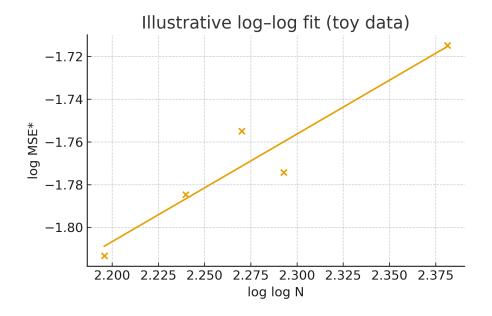


Figure 2: Illustrative log-log OLS on toy data. Slope/intercept are for demonstration only.