



# Bölüm 8: Öncelikli Kuyruk

## Veri Yapıları



# Öncelik Kuyruğu (Priority Queue)

- Verilerin öncelik sırasına göre saklandığı bir veri yapısıdır.
- Özellikle öncelikli işlemlerin yönetiminde sıkça kullanılır.
- En yüksek öncelikli öğeyi çıkarmak için sadece  $O(1)$  zaman gerekir.



# Temel Kavramlar

- **Öncelik Kuyruğu:** Verilerin saklandığı yapı.
- **Öncelik:** Her veriye atanan bir öncelik değeri.
- **En Yüksek Öncelik:** Kuyruğun başında bulunan en önemli veri.
- **FIFO İlkesi:** Aynı öncelikteki veriler arasında sıra.



# Kullanım Alanları

- **İşletim Sistemleri:** İşlem sıralaması ve zaman paylaşımında kullanılır.
- **Çizge Algoritmaları:** Dijkstra ve A\* algoritmaları gibi.
- **Acil Durum Yönetimi:** Hasta sıralaması ve olay yönetimi.
- **Veri Sıkıştırma:** Huffman kodlaması.



# Temel İşlemler

- **Ekleme (Insertion):** Veri eklerken önceliğe göre sıralama yapar.
- **Çıkarma (Extraction):** En yüksek öncelikli veriyi çıkarır.
- **Sorgulama (Peek):** En yüksek öncelikli veriyi döndürür.
- **Boş mu Kontrolü (isEmpty):** Kuyruk boş mu dolu mu?



# Dizi Temelli Gerçekleştirim

- Öncelik kuyruğu basit bir şekilde dizi ile temsil edilebilir.
- Dizi öncelik sırasına göre sıralanarak, en yüksek öncelikli veri bulunabilir.
- Yeni öğeler eklemek ve öğeleri çıkarmak için sıralamayı güncellemek zor olabilir.



# Bağlı Liste Temelli Gerçekleştirim

- Öncelik kuyruğu bağlı liste ile temsil edilebilir.
- Veriler önceliklerine göre sıralı bir şekilde bağlı listeye eklenebilir.
- En yüksek öncelikli öğeyi bulmak için bağlı listeyi taramak gerekebilir.



# İkili Heap Gerçekleştirimi

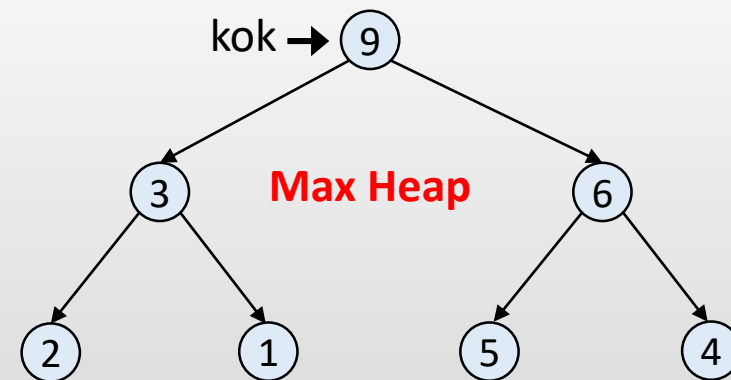
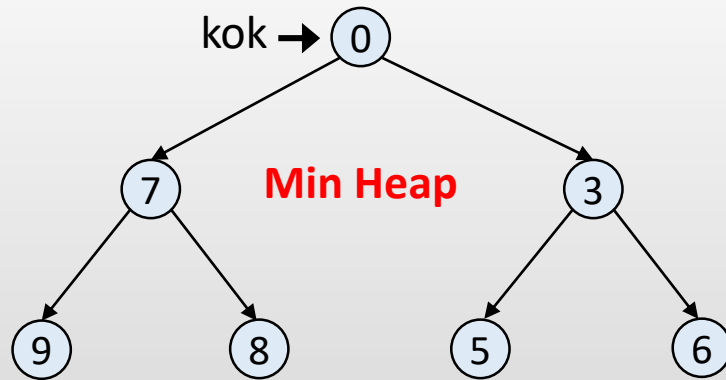
- İkili heap (min-heap veya max-heap) öncelik kuyruğu uygulamaları için en yaygın kullanılan veri yapısıdır.
- En yüksek öncelikli öge kökte bulunur.
- Ekleme ve öge çıkarma işlemleri  $O(\log n)$  zaman karmaşıklığına sahiptir.





# İkili Heap

- İkili Heap, özel bir ikili ağaç yapısıdır.
- Min-Heap ve Max-Heap olmak üzere iki türü vardır.
- **Min-Heap:** En küçük öge kökte, her alt ağaç da bir min-heap'tir.
- **Max-Heap:** En büyük öge kökte, her alt ağaç da bir max-heap'tir.





# Ekleme İşlemi

- Ekleme işlemi, ağacın sonuna yeni bir öge ekler.
- Ekledikten sonra ağacın yapısı bozulmuş olabilir.
- Yapının yeniden dengelemesi için "heapify" adı verilen bir işlem yapılır.



# Çıkarma İşlemi

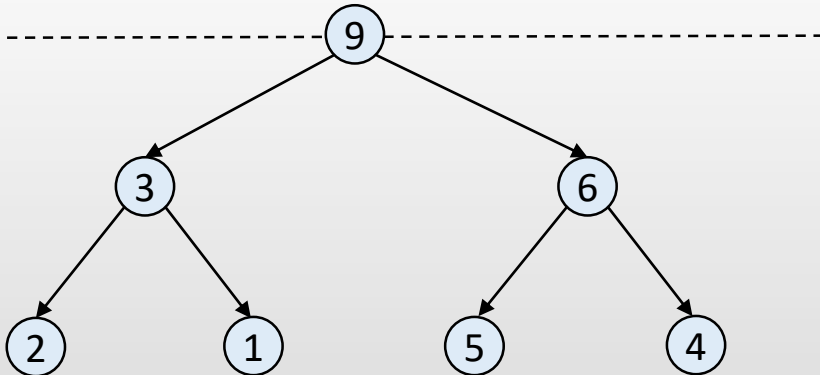
- Çıkarma işlemi, kökteki en küçük (veya en büyük) öğeyi çıkarır.
- Son öğeyi köke taşır ve "heapify" işlemi ile ağacın yapısını yeniden dengeler.
- İkili Heap, bu işlemi hızlı bir şekilde yapar ( $O(\log n)$ ).



# İkili Heap Gösterimi

- İkili heap genellikle dizi veri yapısı ile gerçekleştirilir. İlk elemanı boş bırakılır.
- Tam ikili ağaçtır. Değerler soldan sağa doğru düzey ağaç dolaşımı ile dizi içinde saklanır.

d1



**Max Heap**

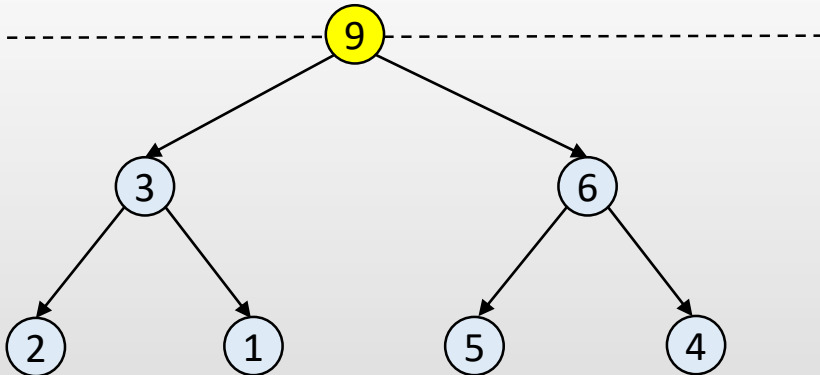




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d1



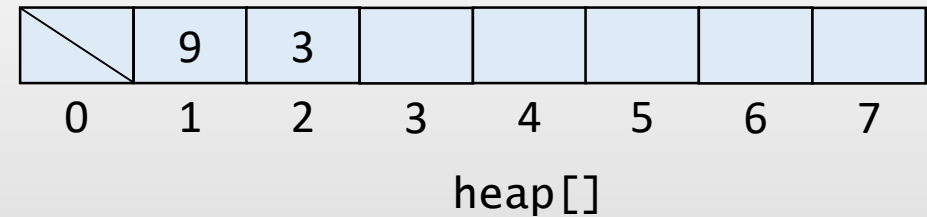
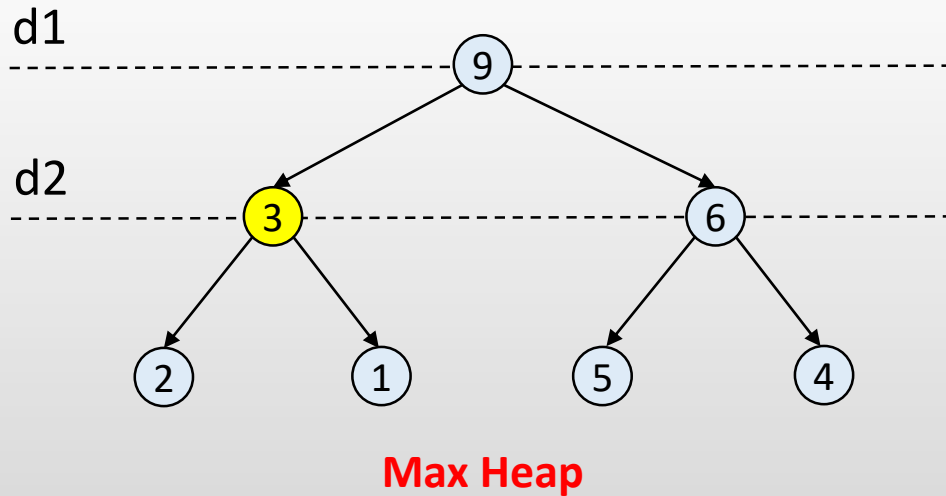
**Max Heap**





# İkili Heap Gösterimi

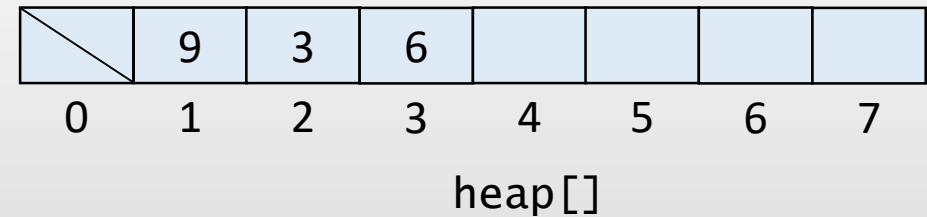
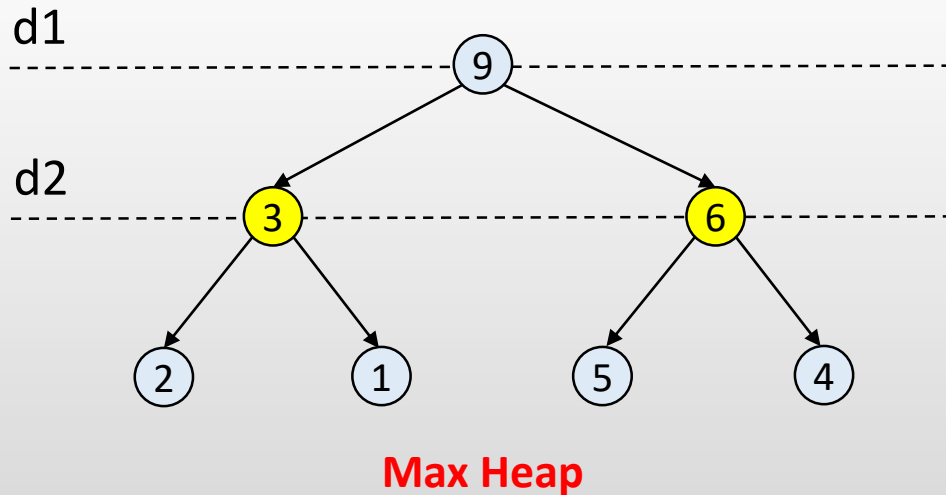
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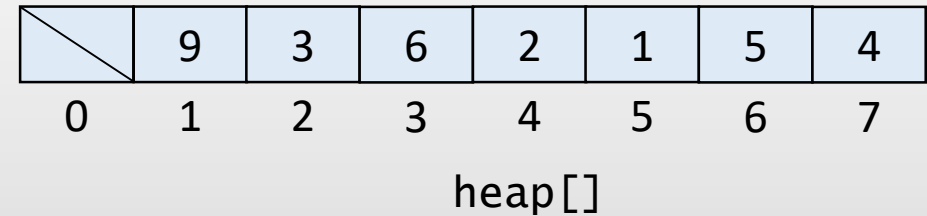
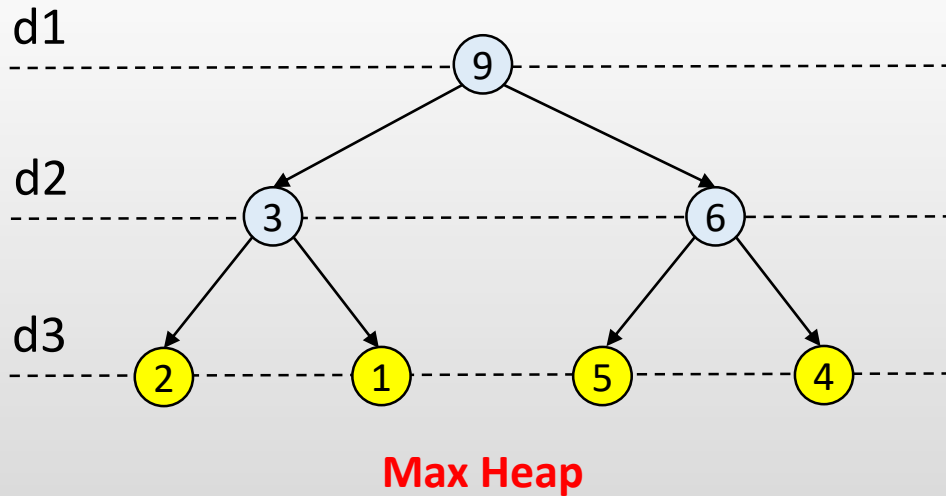
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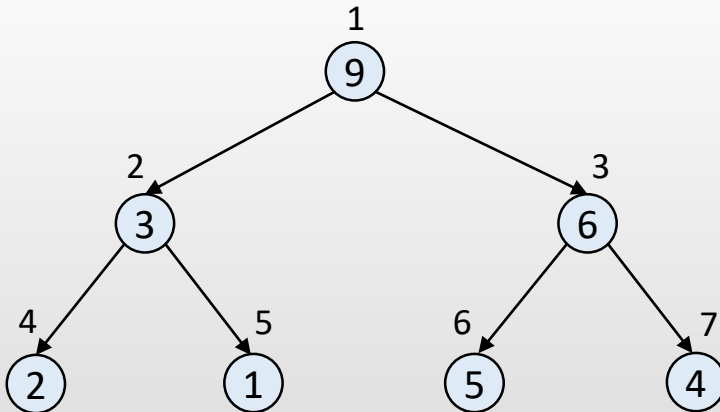




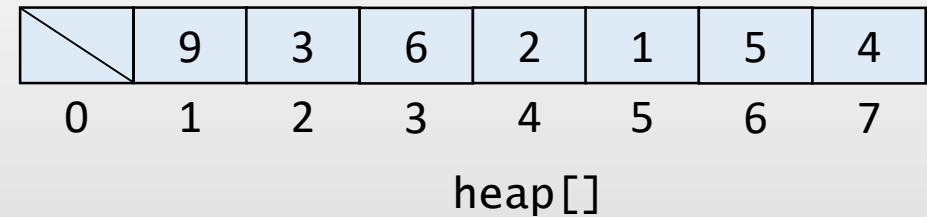


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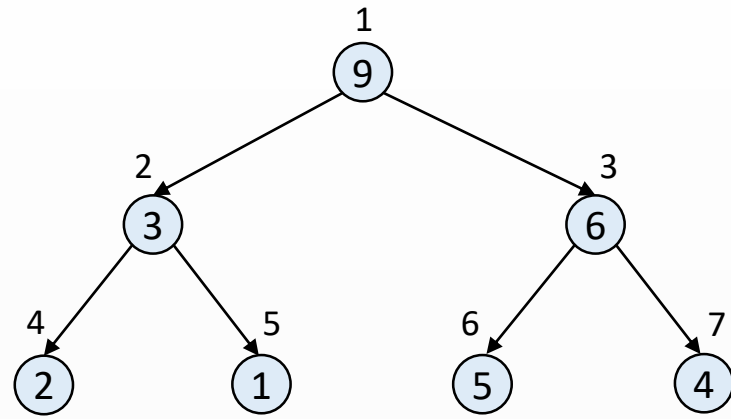


**Max Heap**



# Ebeveyn ve Çocuk Hesaplamaları

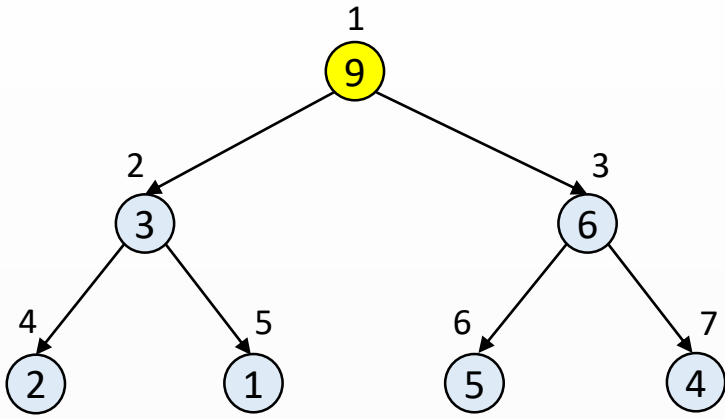




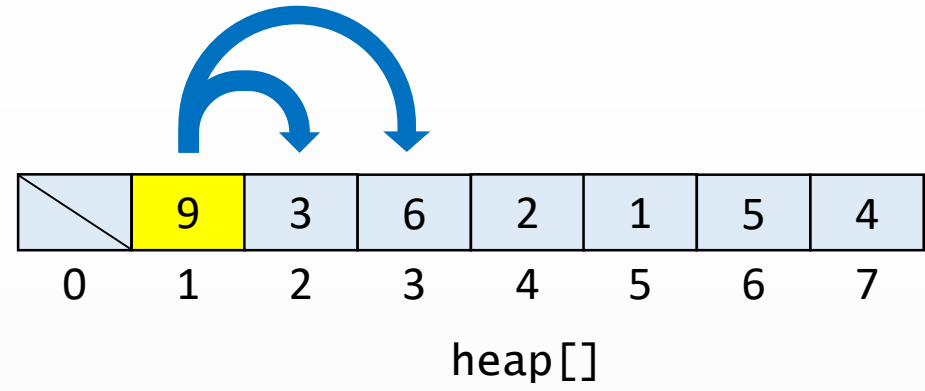
**Max Heap**

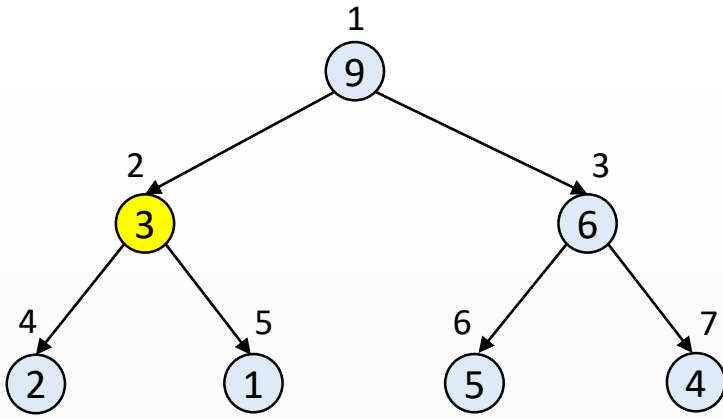
	9	3	6	2	1	5	4
0	1	2	3	4	5	6	7

heap[]

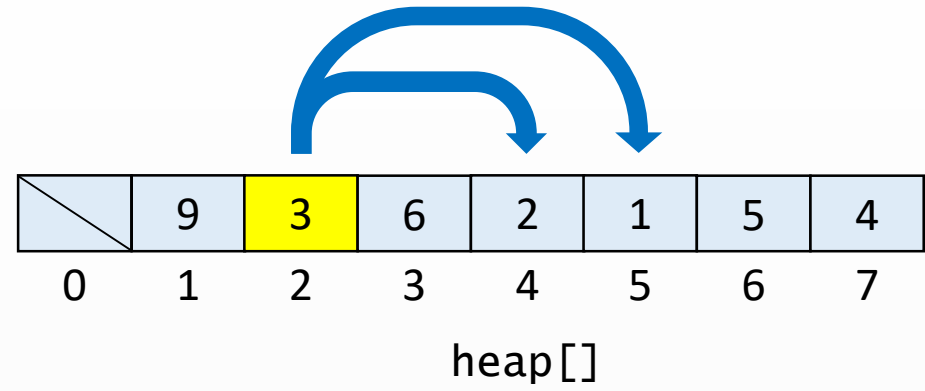


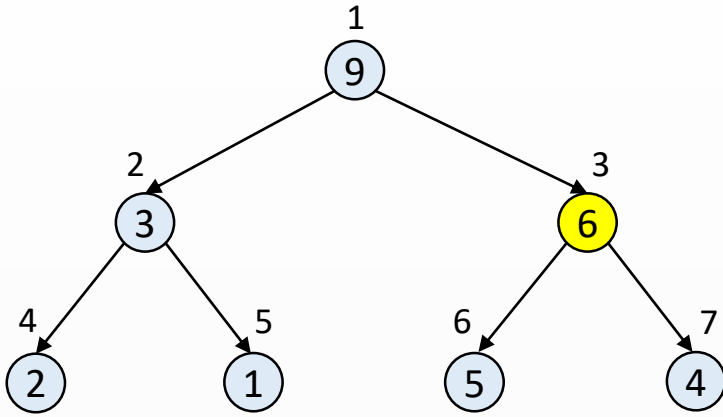
**Max Heap**





**Max Heap**





**Max Heap**

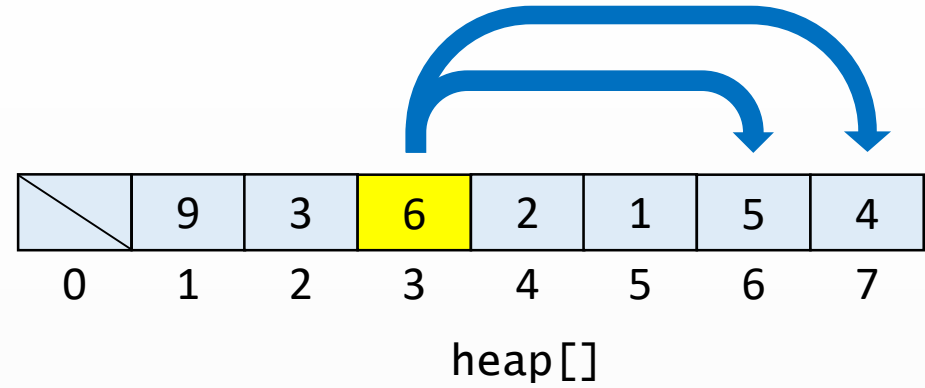
### Çocuklar:

indeks 1  $\rightarrow$  2, 3

indeks 2  $\rightarrow$  4, 5

indeks 3  $\rightarrow$  6, 7

indeks k  $\rightarrow$  2\*k, 2\*k + 1



### Ebeveyn:

indeks 7  $\rightarrow \lfloor 7/2 \rfloor = 3$

indeks 6  $\rightarrow \lfloor 6/2 \rfloor = 3$

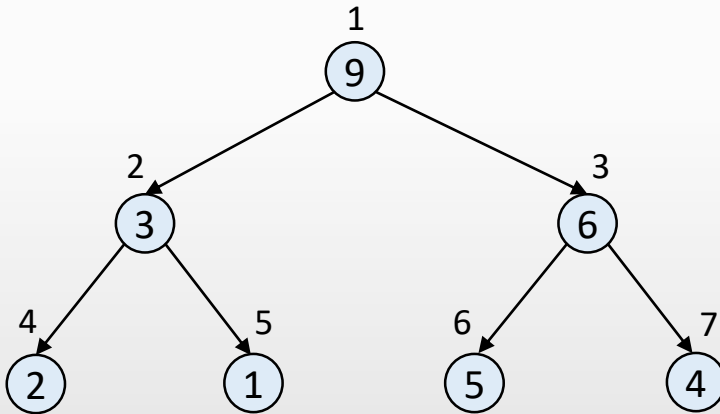
indeks 5  $\rightarrow \lfloor 5/2 \rfloor = 2$

indeks k  $\rightarrow \lfloor k/2 \rfloor$

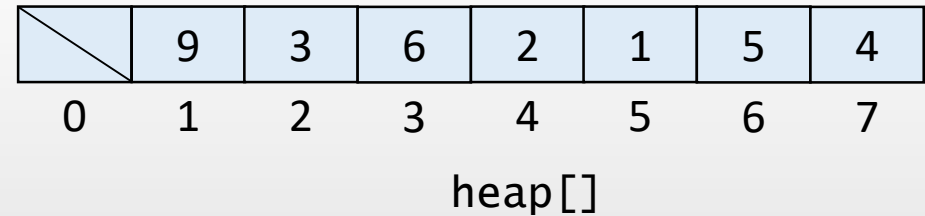


# Max İkili Heap Ağacı

- Her bir düğümün değerinin, çocuklarının değerlerinden büyük olduğu tam ikili ağaçtır.
- En büyük değer köktedir ve kökün indeksi 1'dir.



**Max Heap**

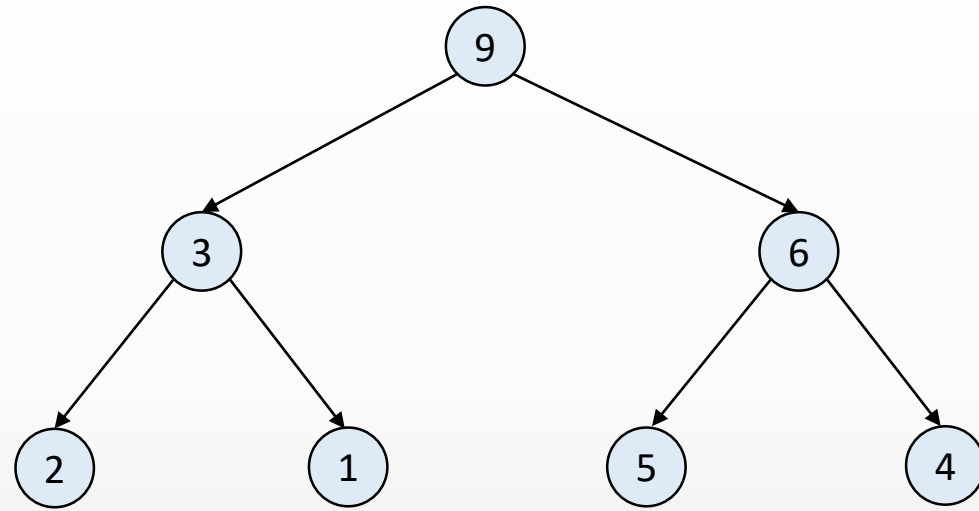




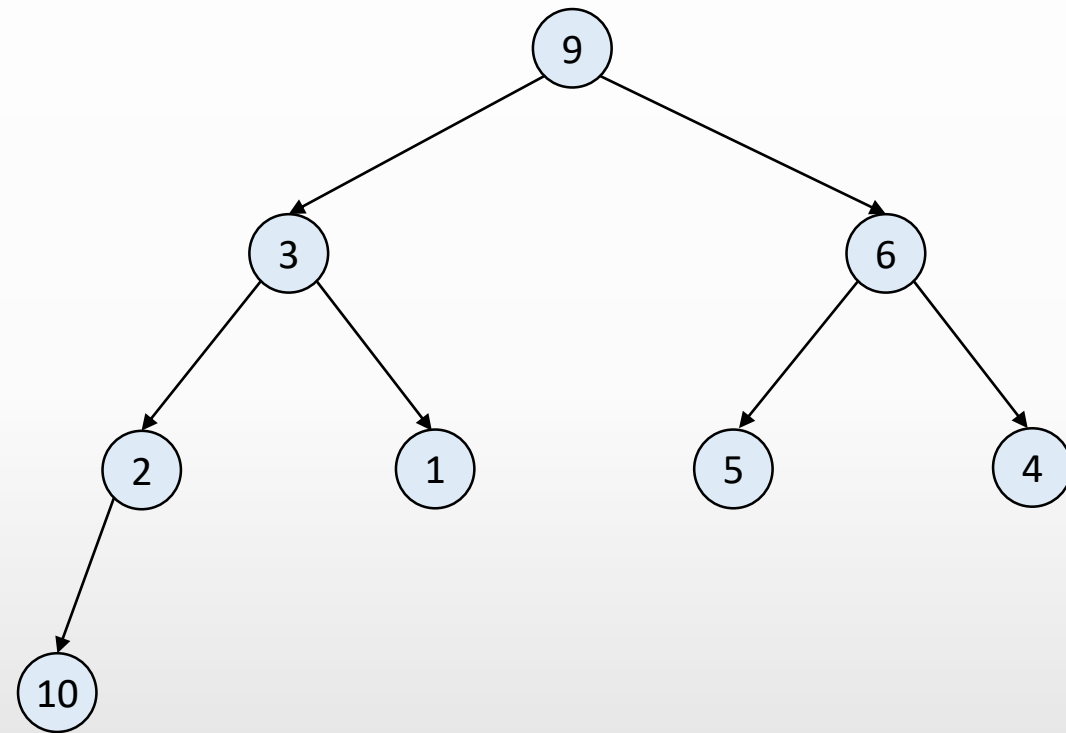
# Aşağıdan Yukarıya Heap Ağacına Dönüştürme

- Max heap ikili ağacının her bir düğümünün değeri, çocuklarının değerlerinden büyük olma özelliğini taşır.
- Ancak heap ağacına bir eleman eklendikten sonra bu özellik bozulabilir.
- Bu nedenle elemanların yerlerini aşağıdan yukarıya değiştirerek yeniden heap ağacına dönüştürme işlemi (yüzdür - swim) gerçekleştirilir (bottom-up heapify).

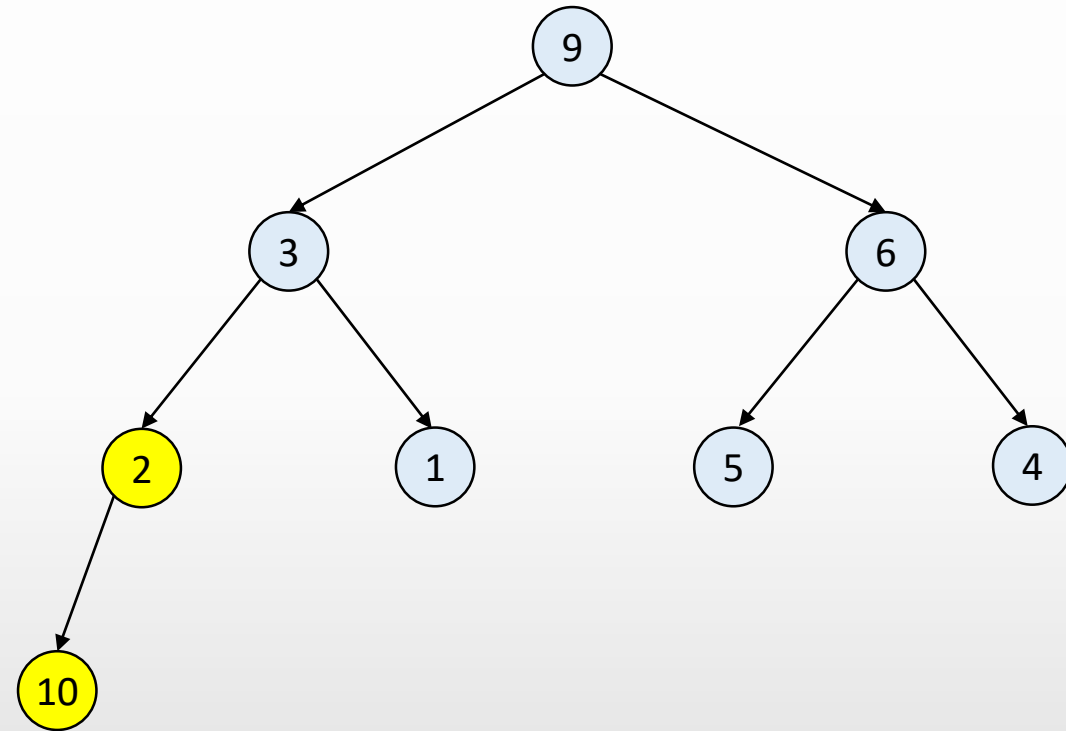




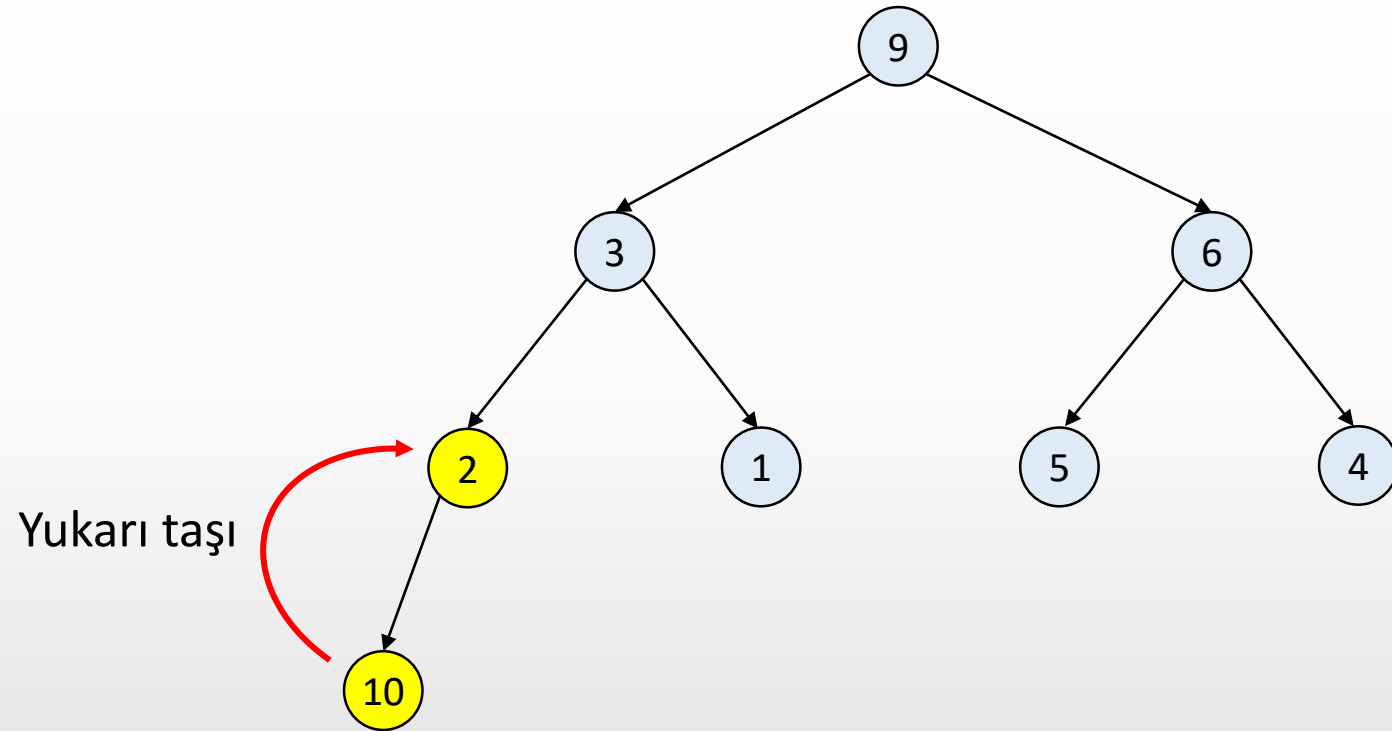
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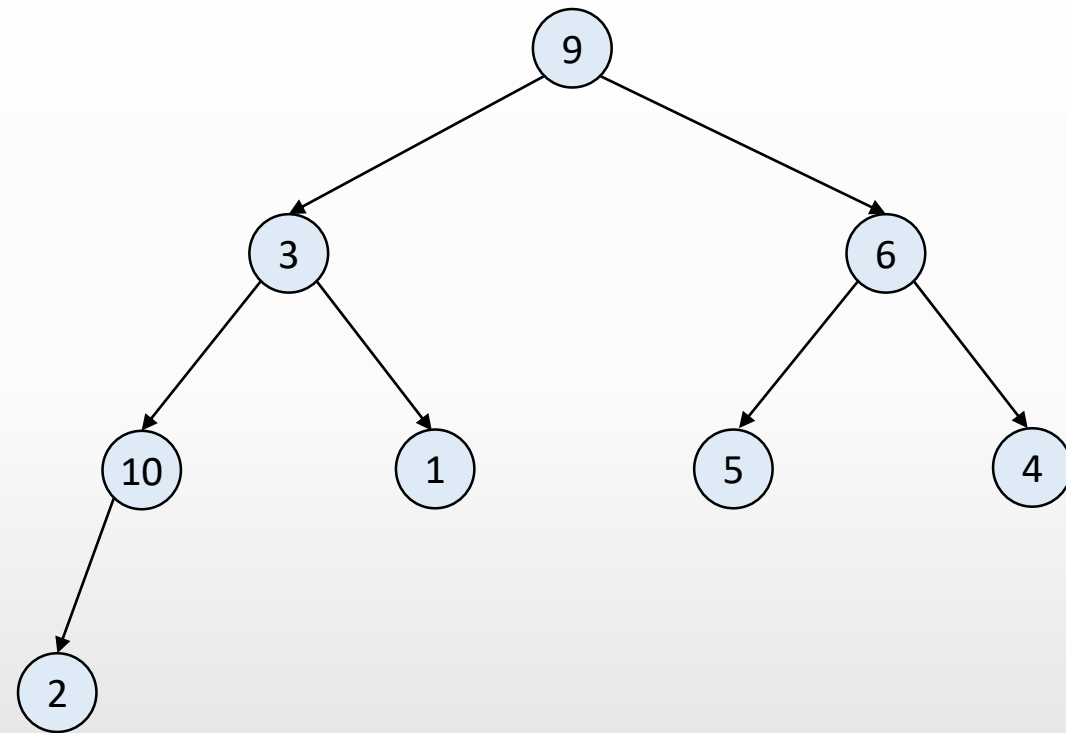
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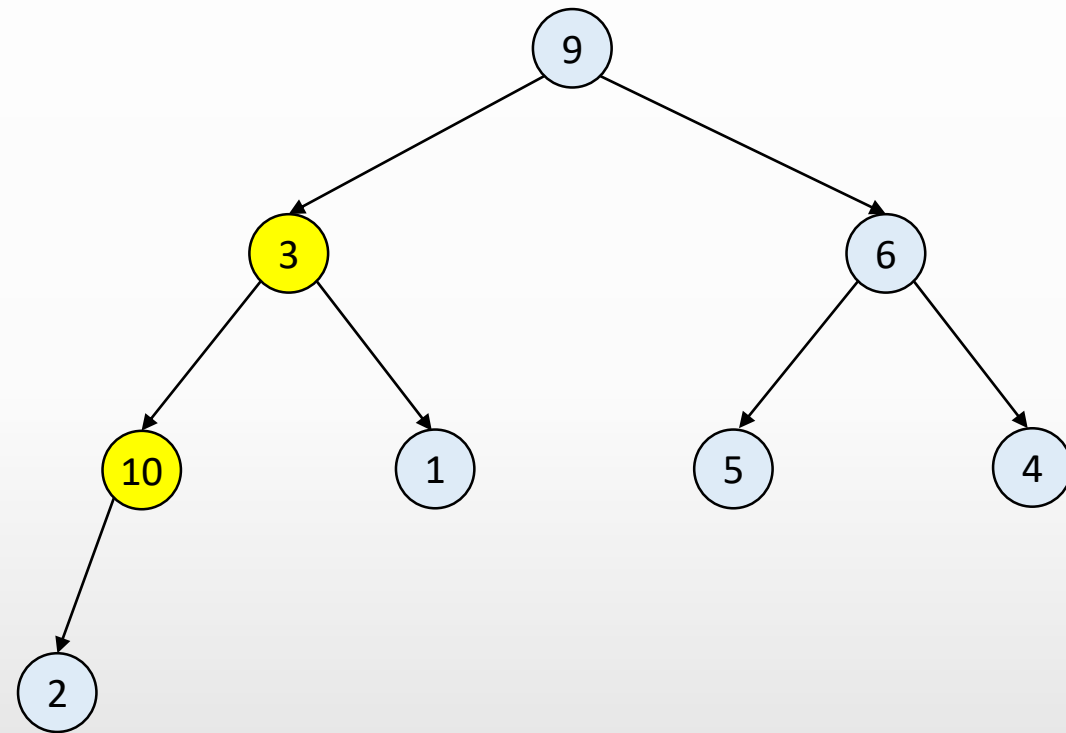
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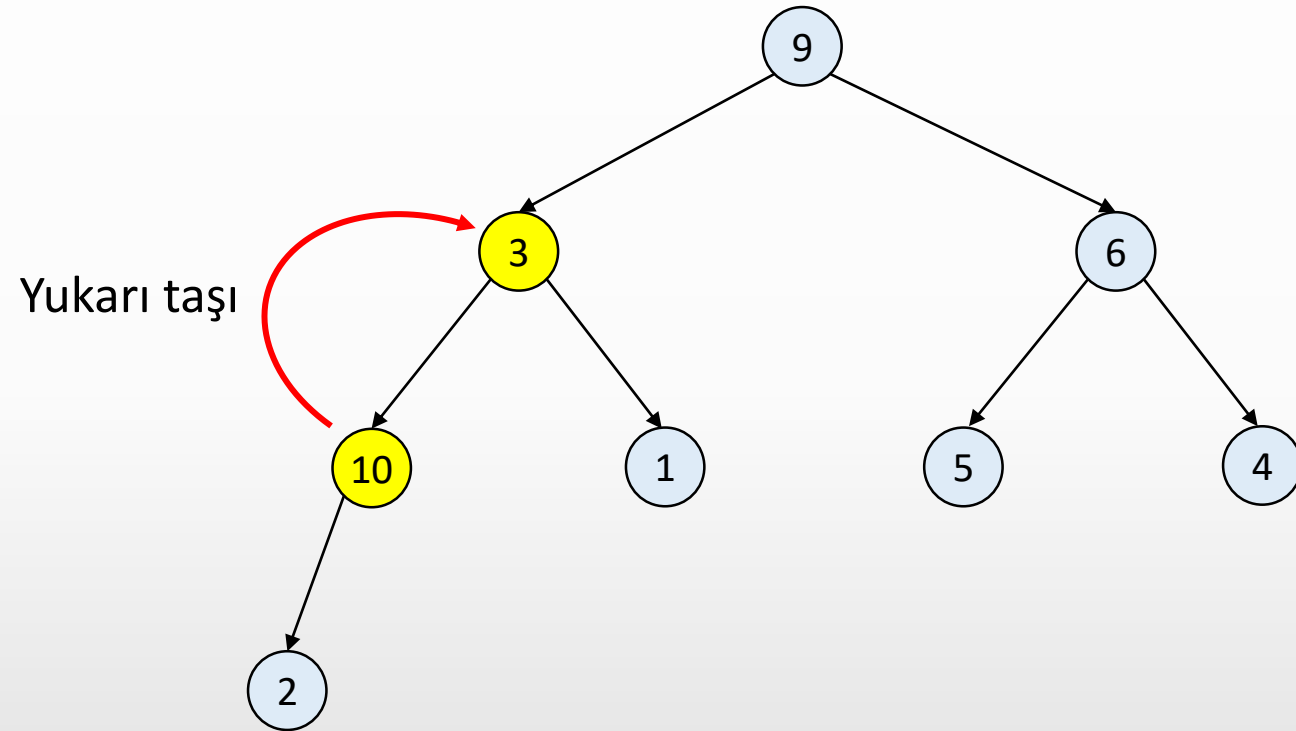
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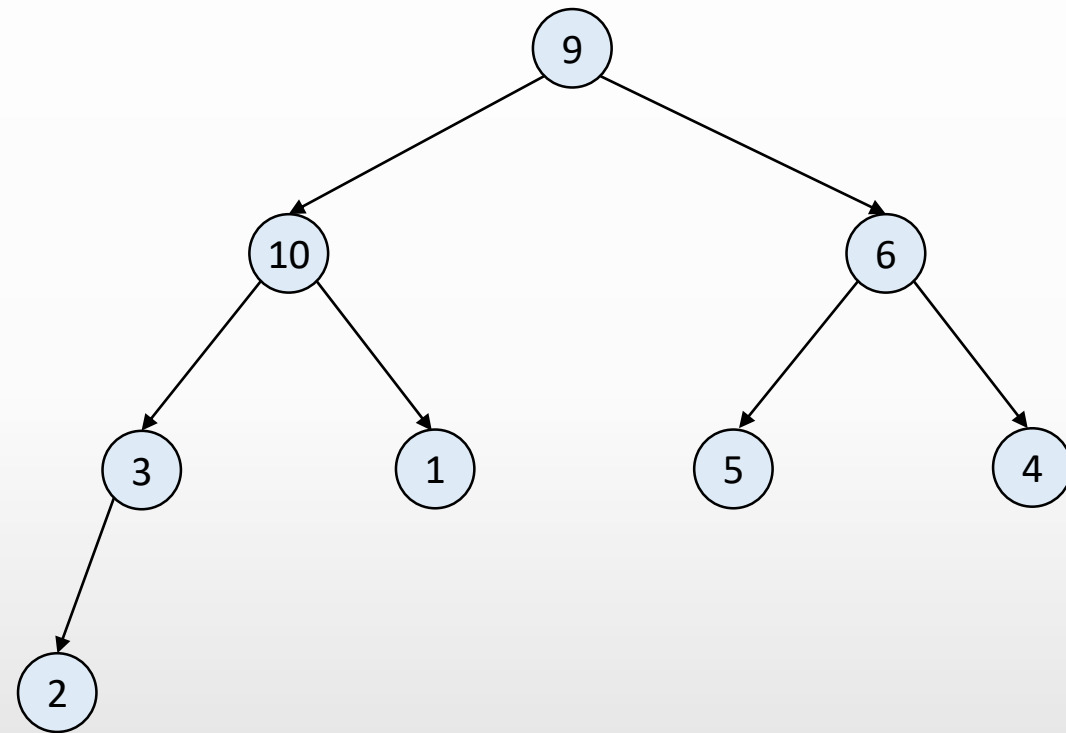
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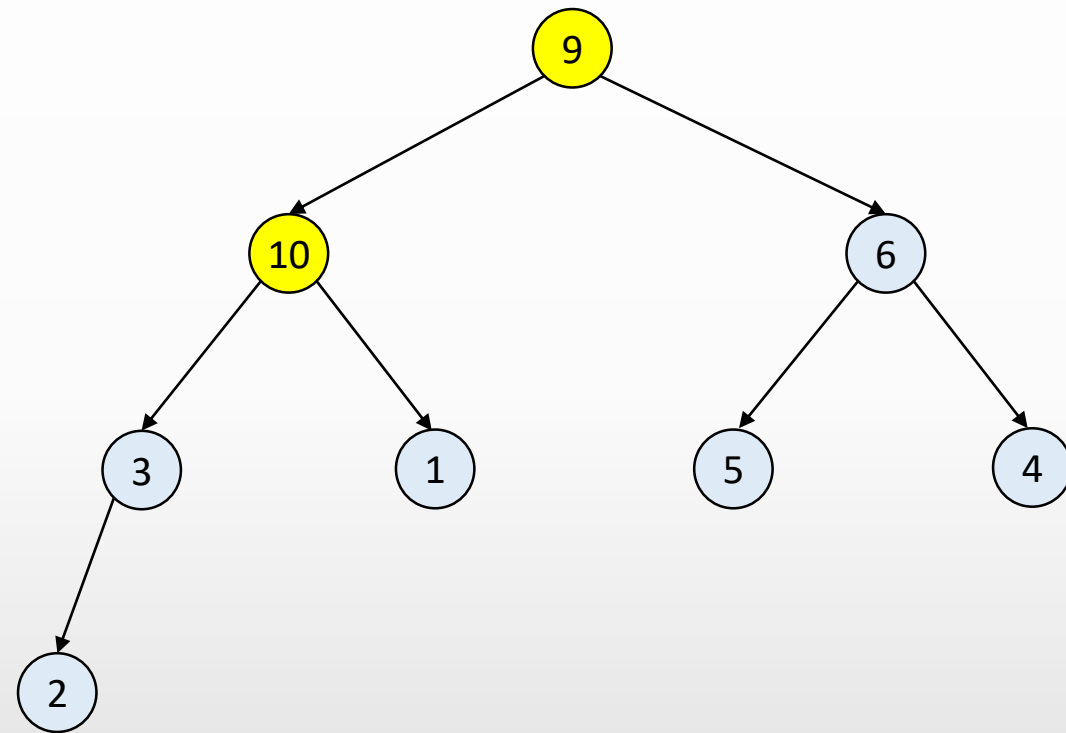


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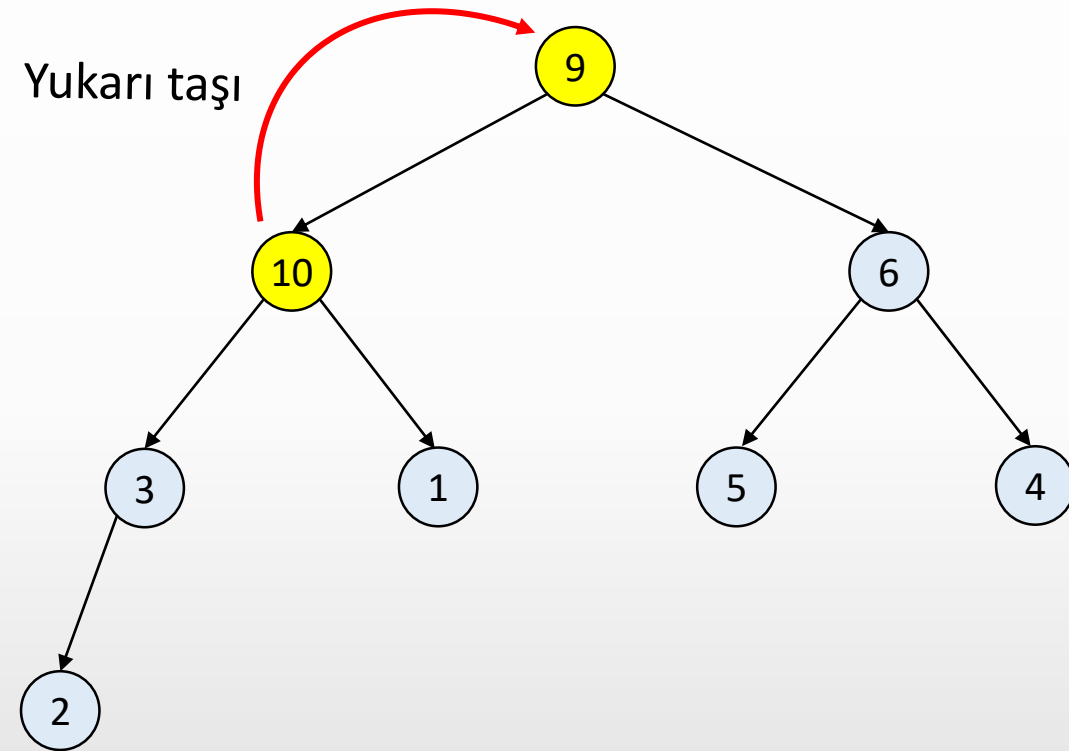


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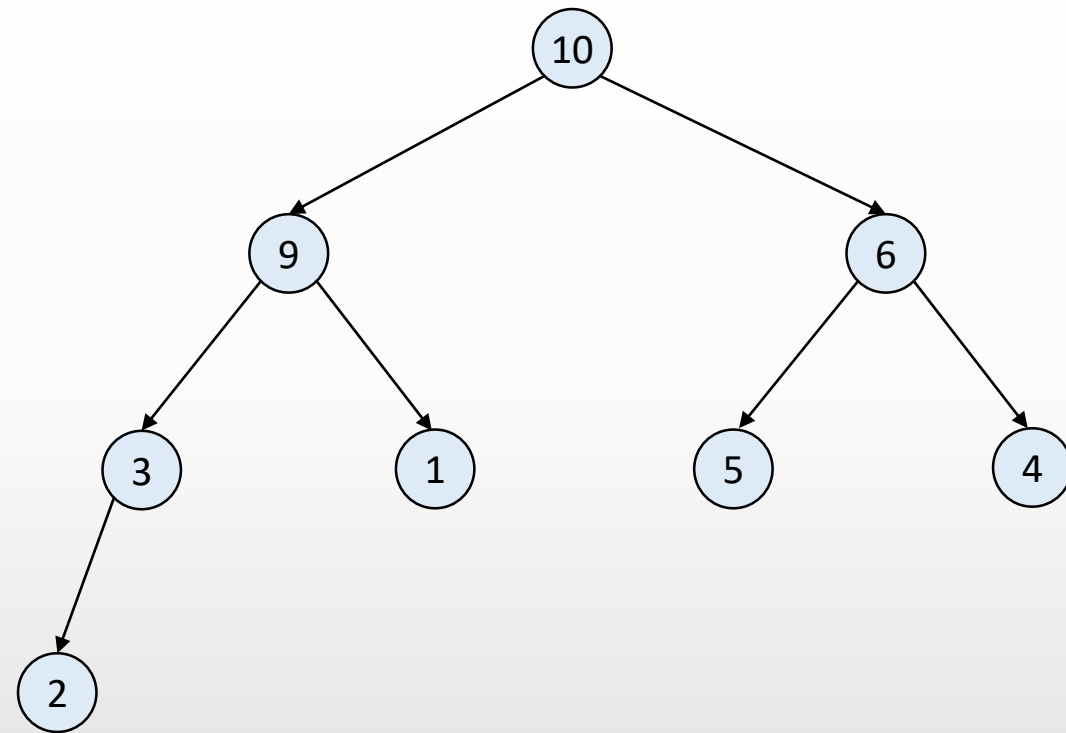


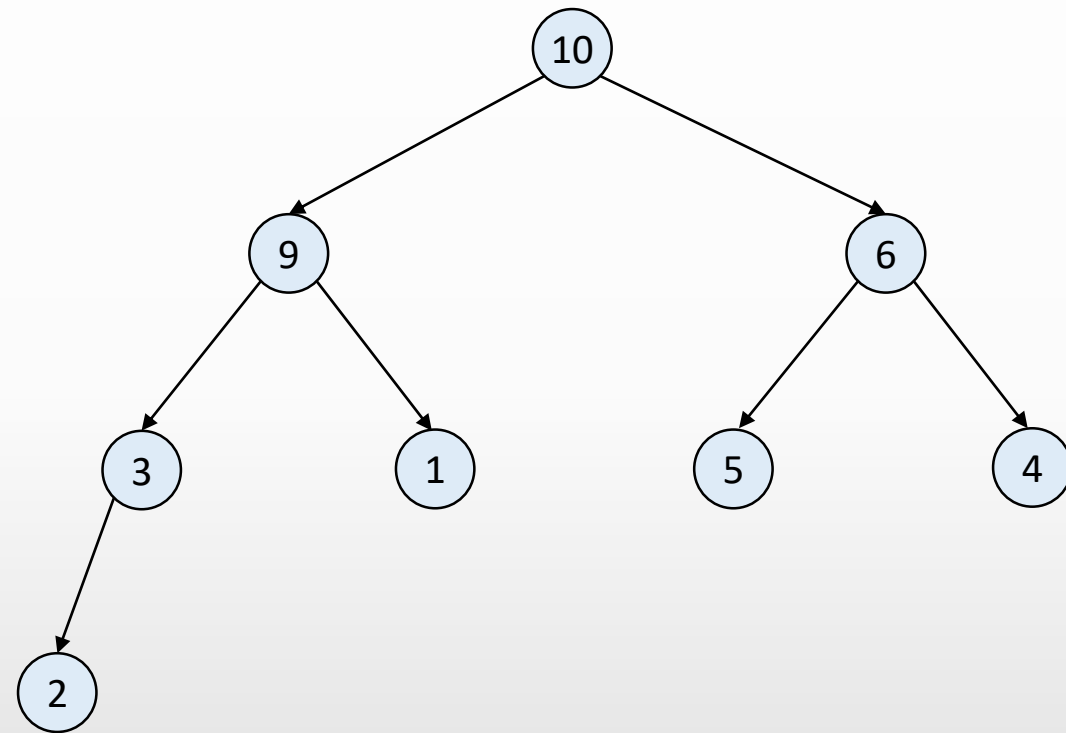


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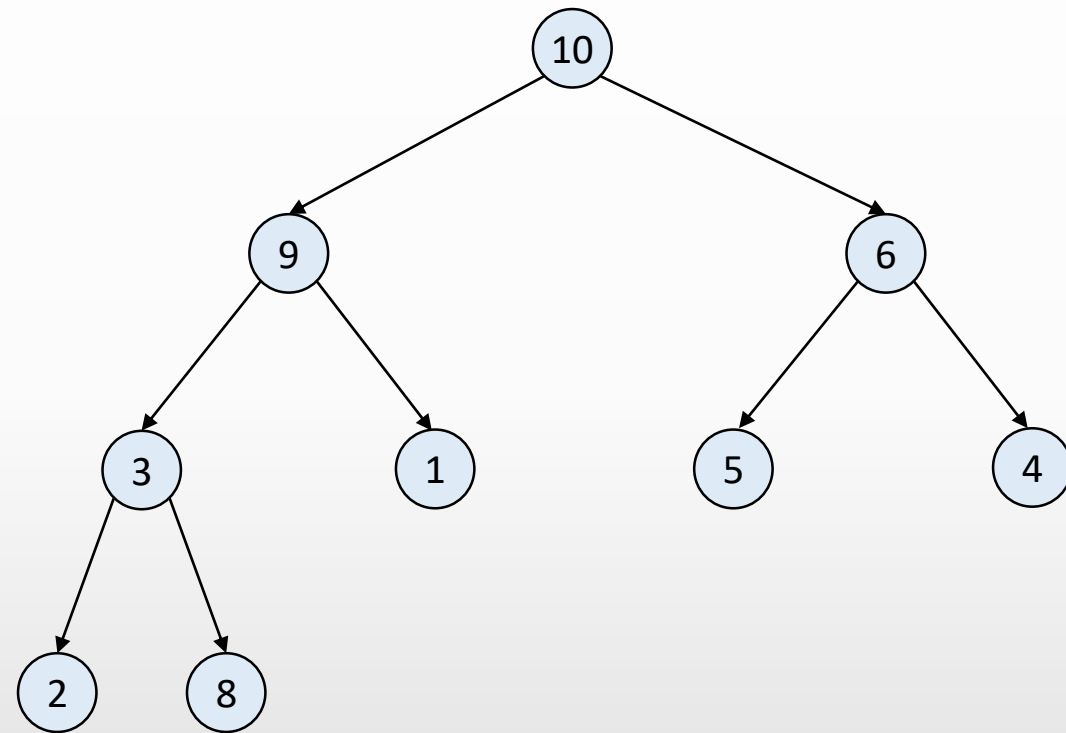


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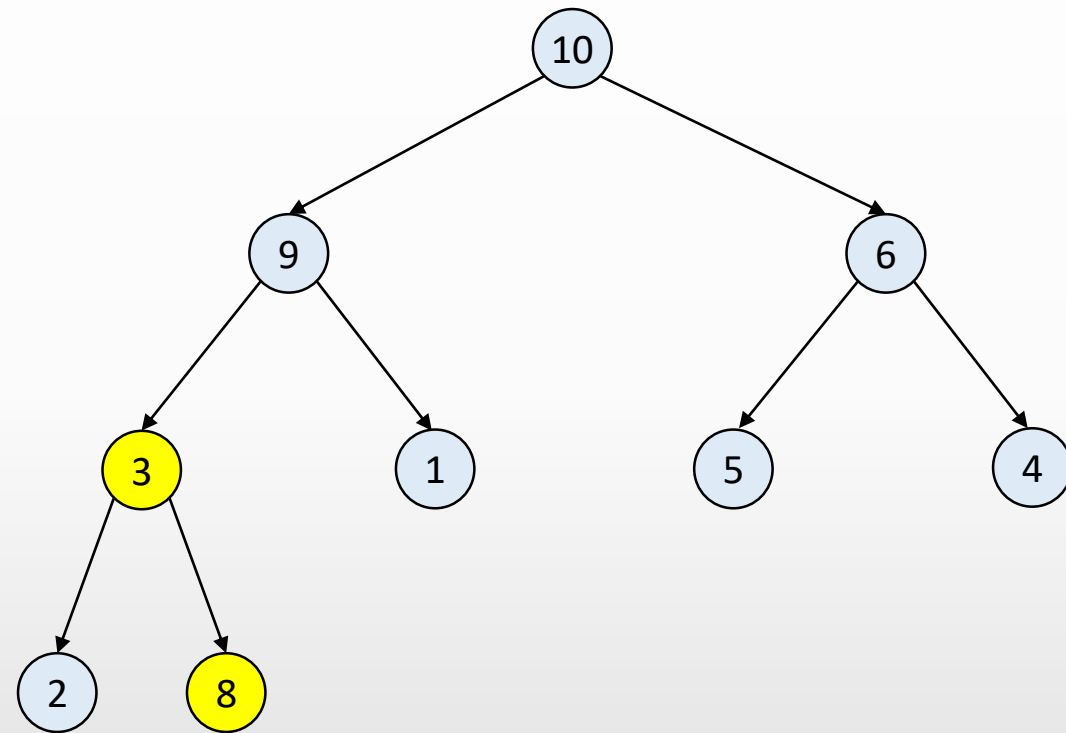




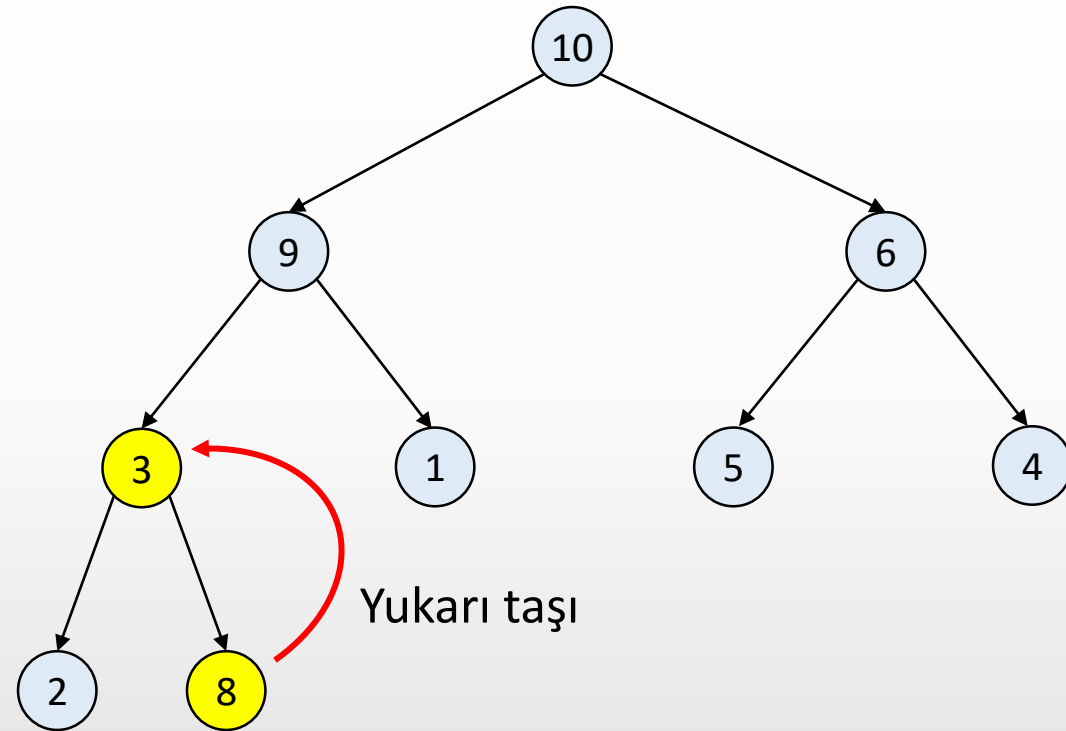
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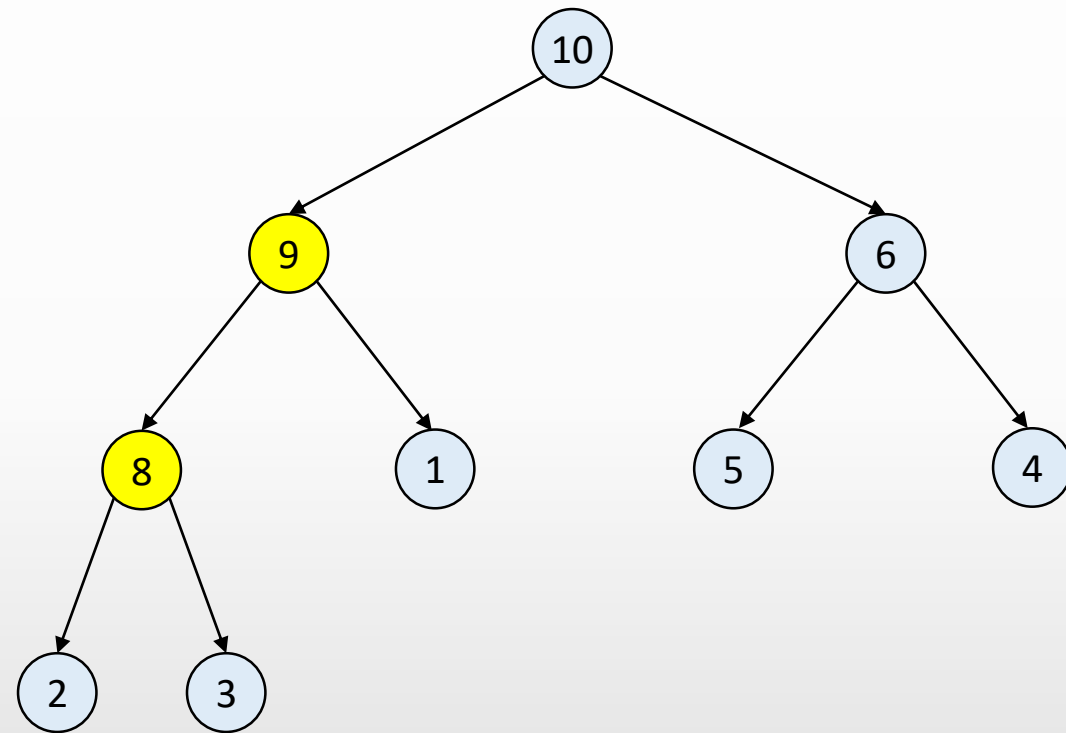
ek1e(8)



ek1e(8)



ekle(8)



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# Aşağıdan Yukarıya Heap Ağacına Dönüştürme



ek1e(4)



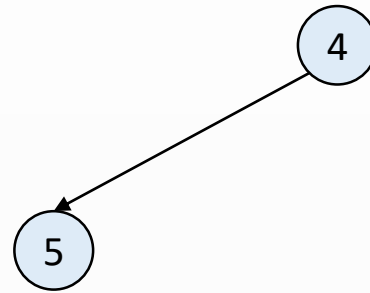
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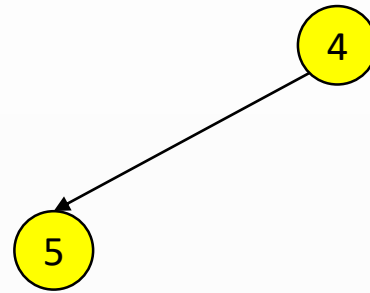


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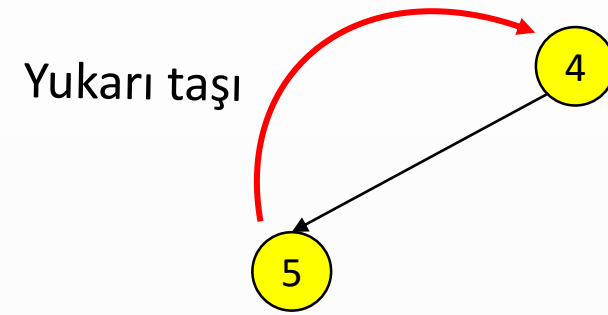
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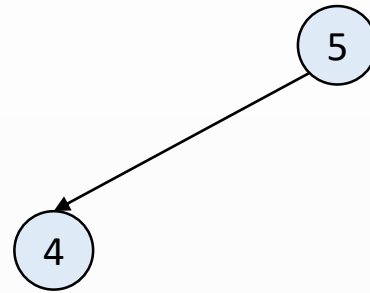
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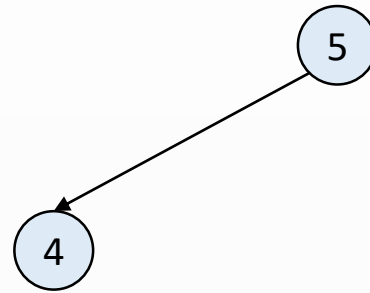


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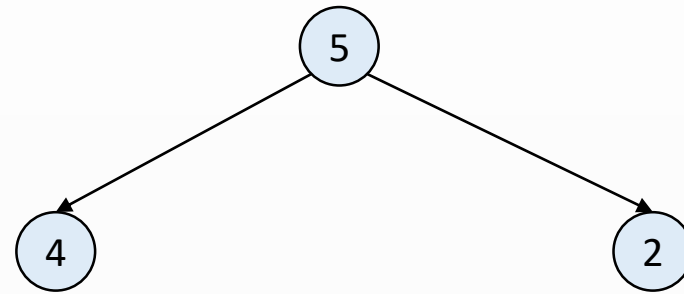


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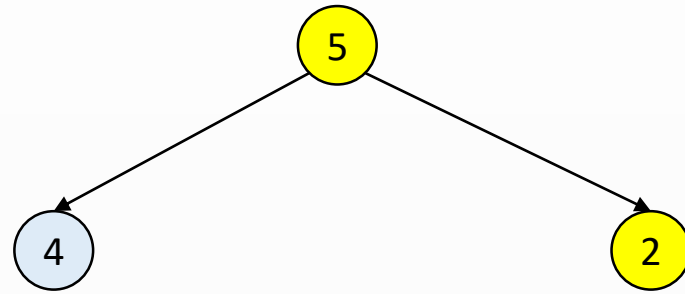




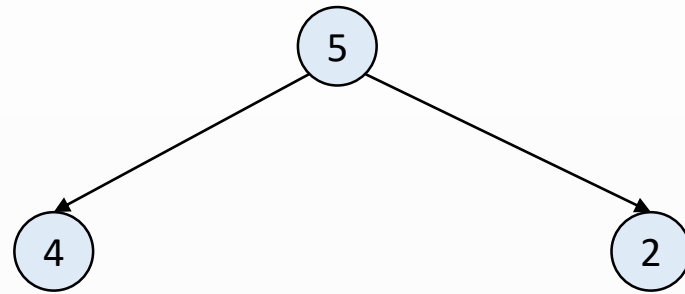
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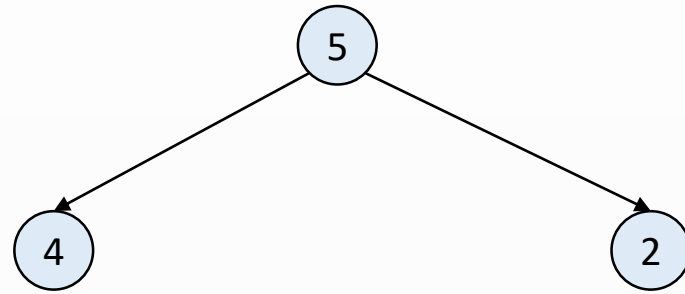
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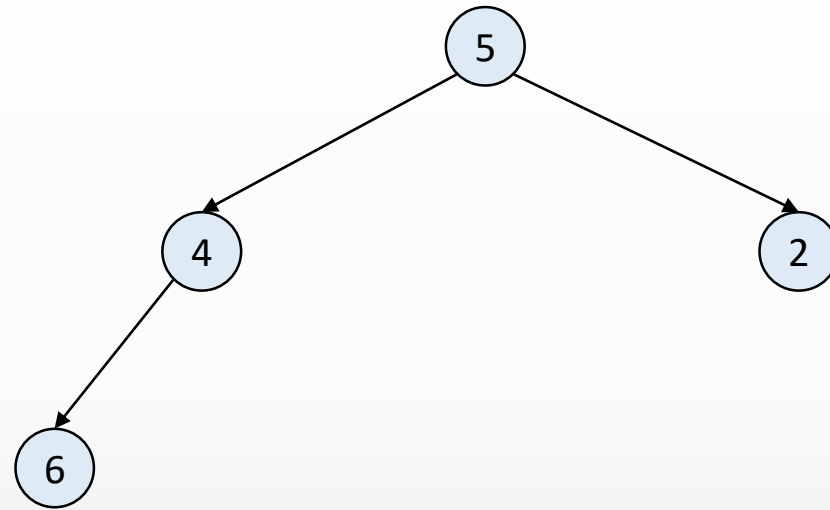
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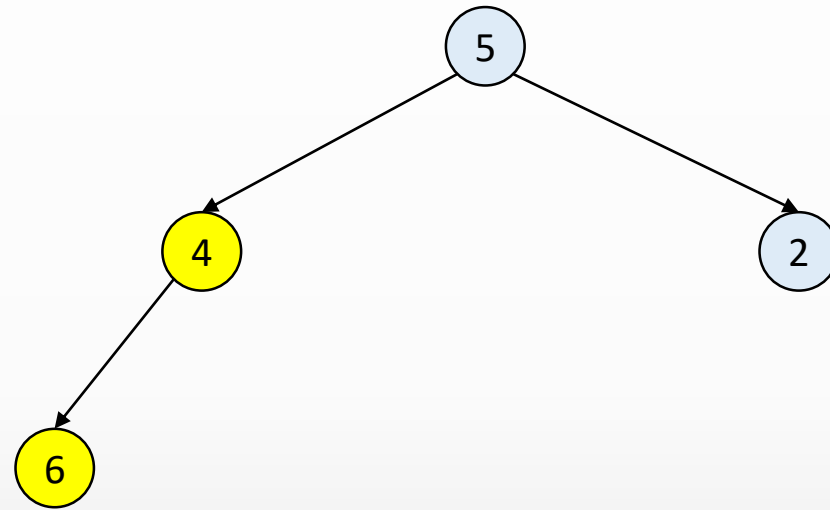
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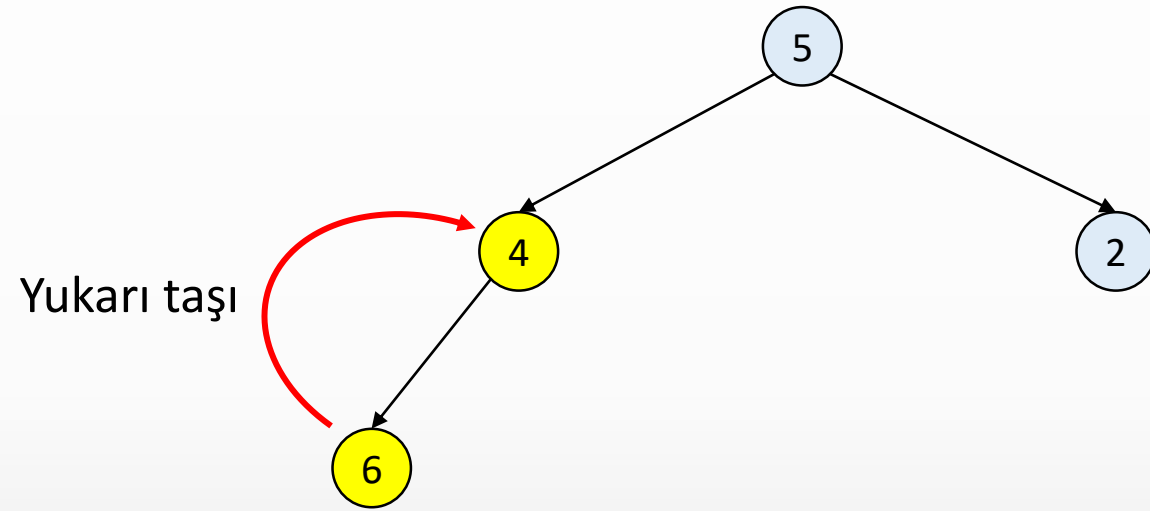
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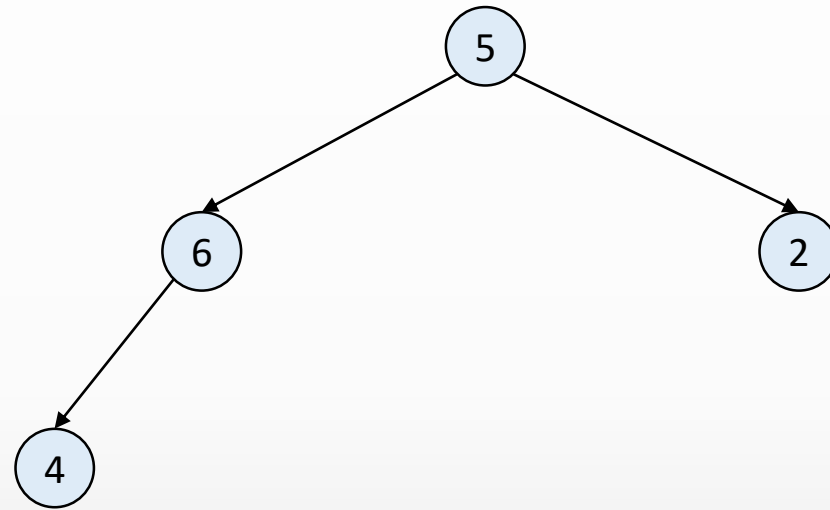


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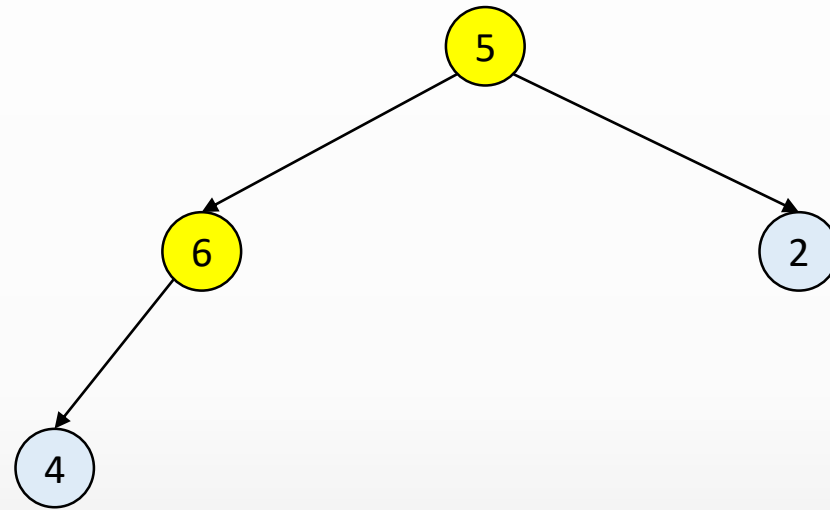


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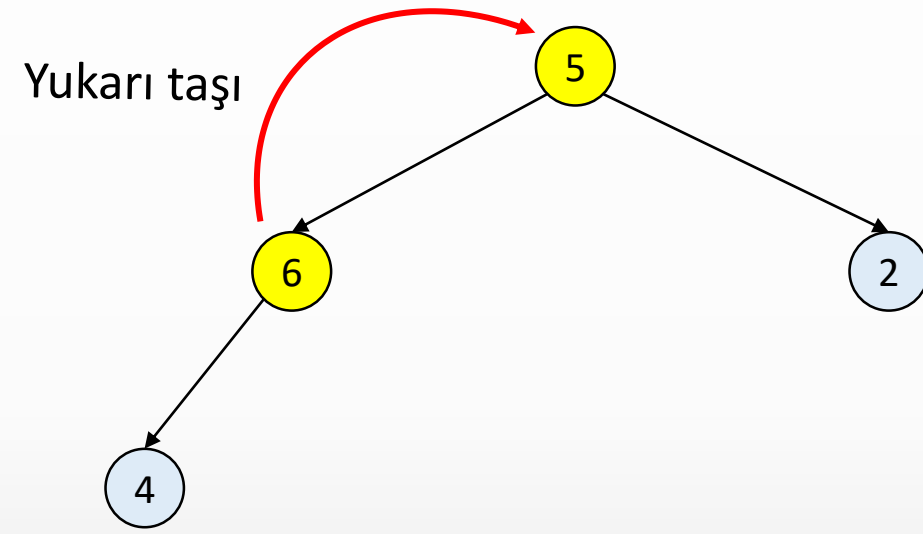




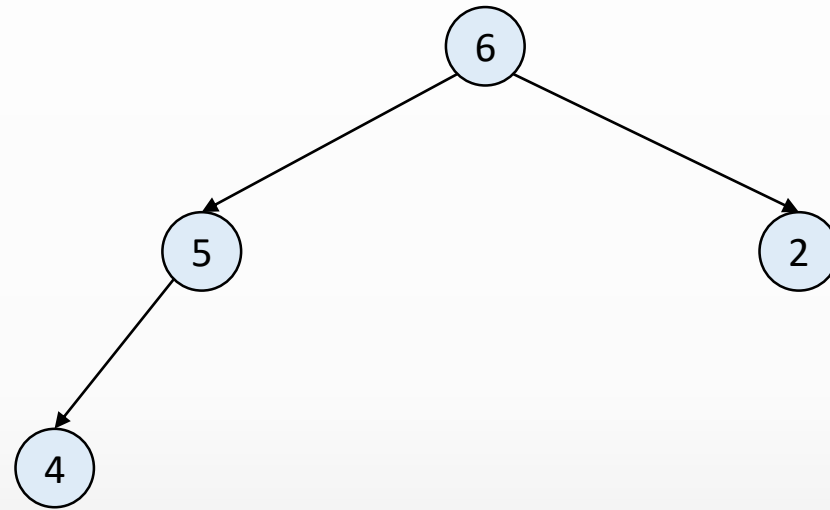
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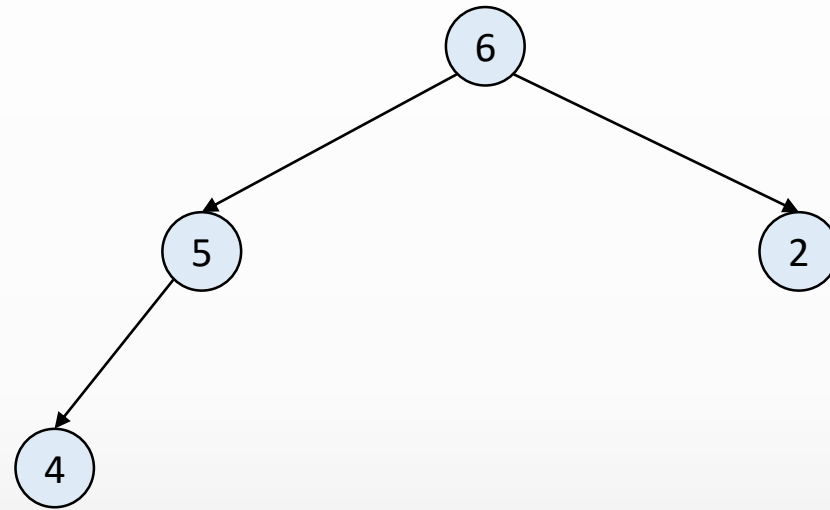
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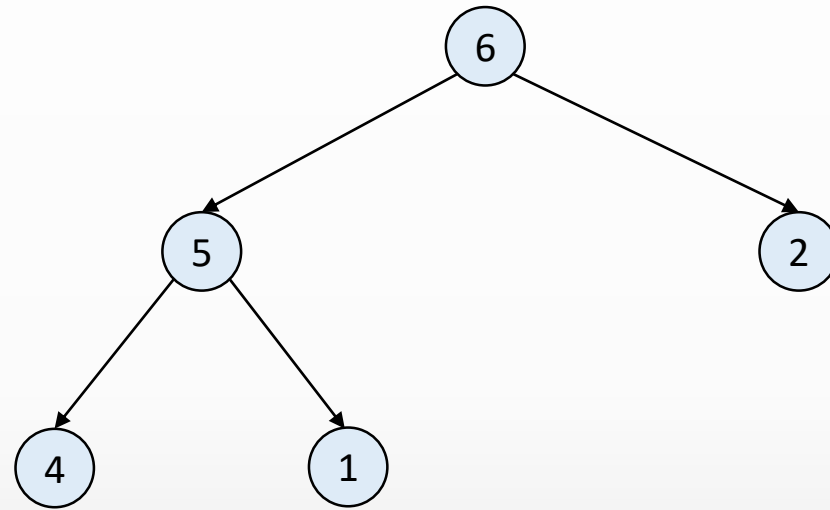
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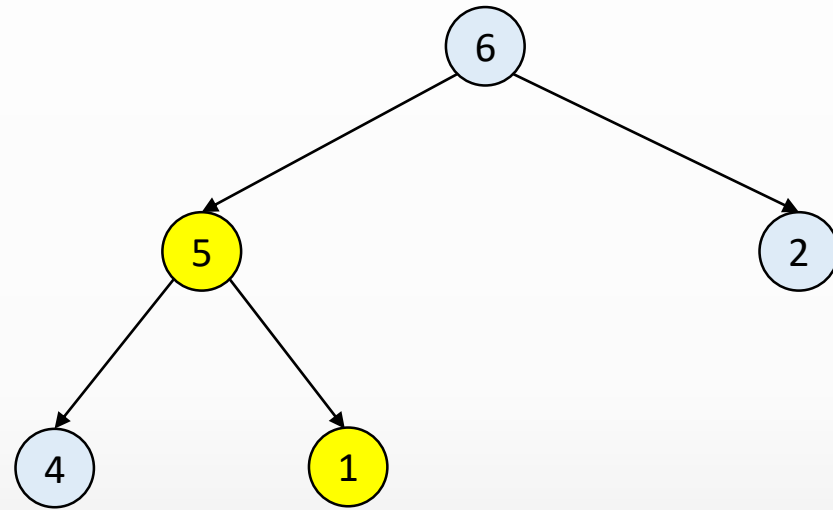
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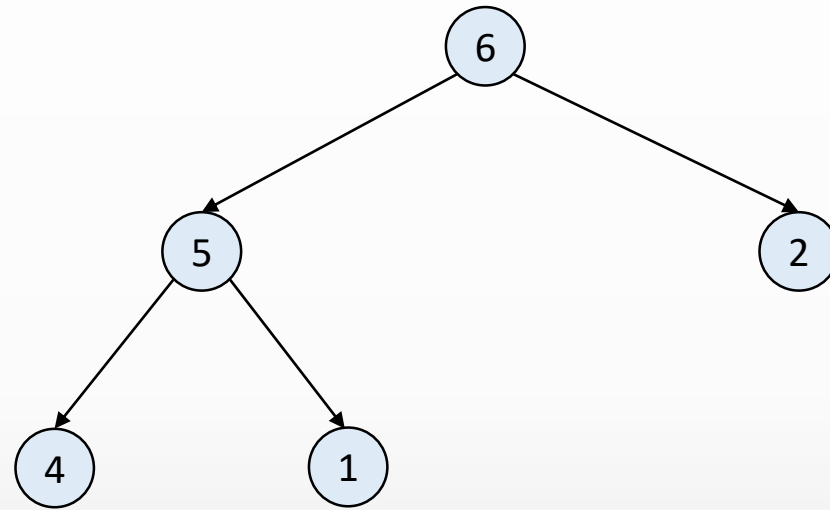
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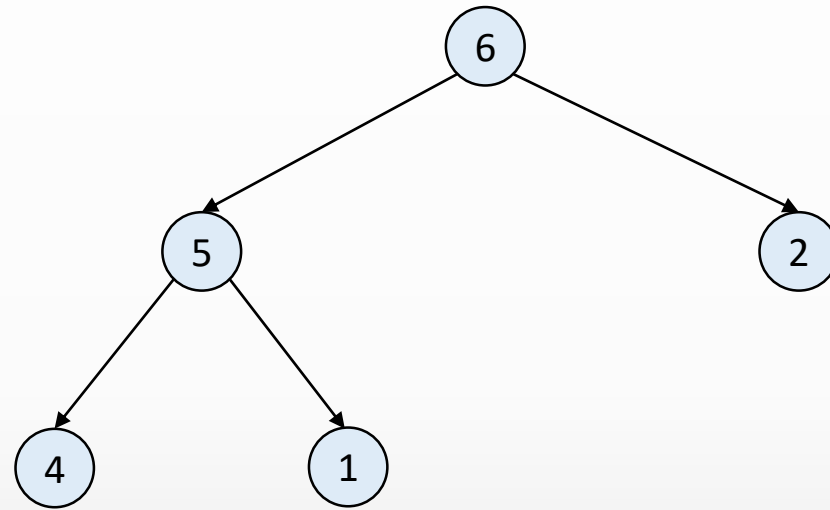


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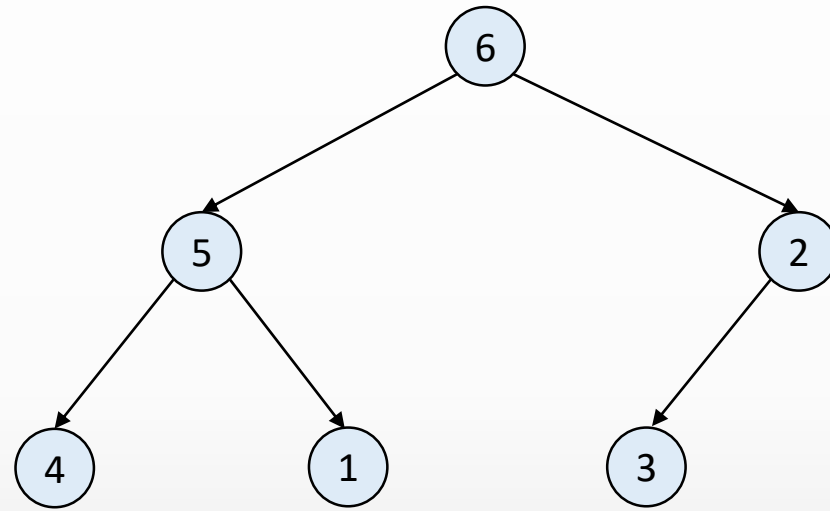


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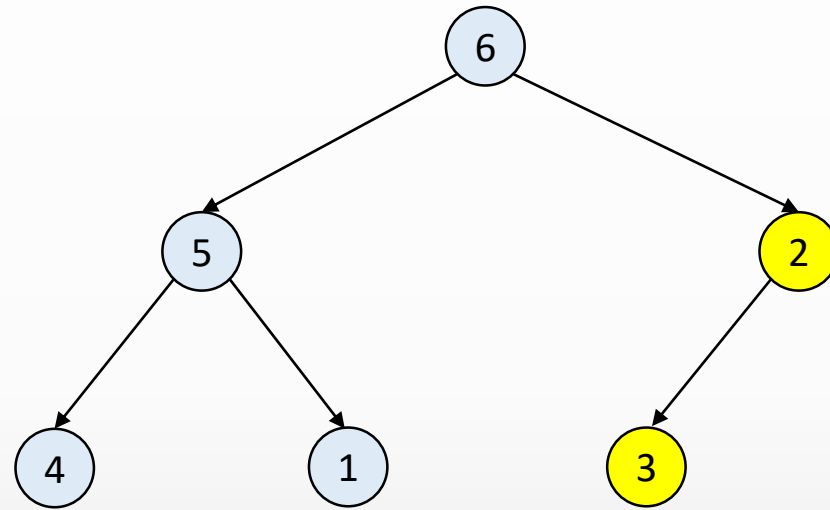




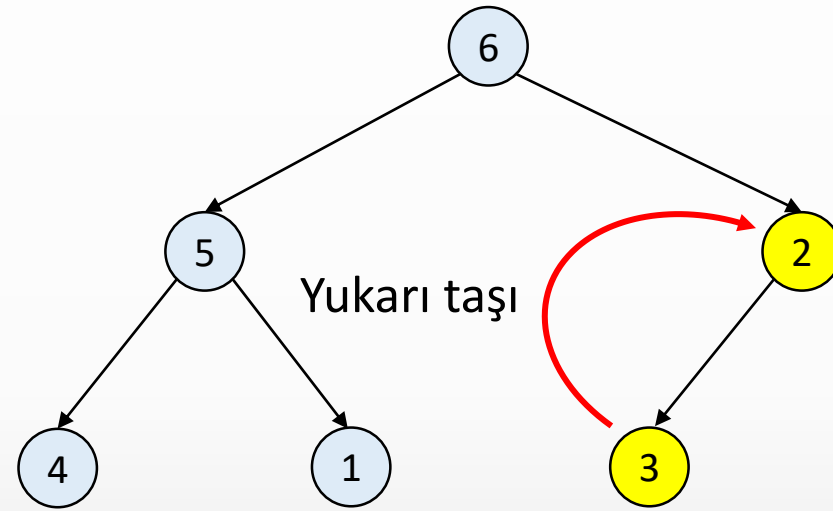
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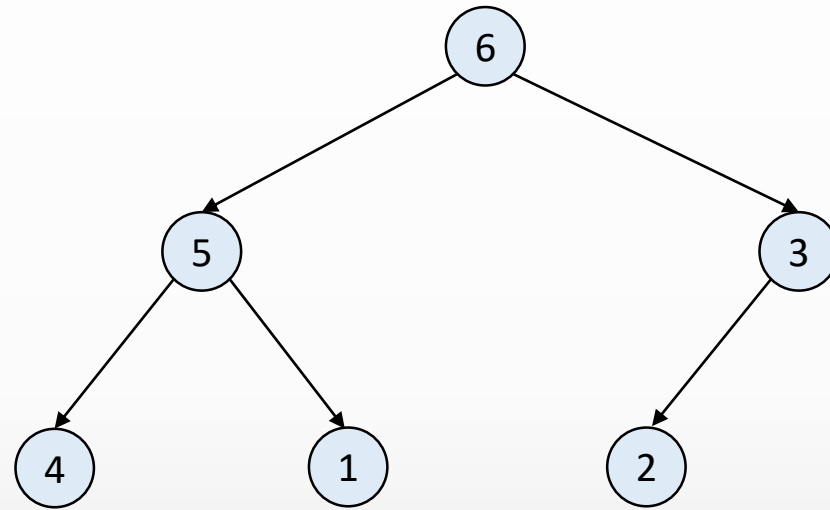
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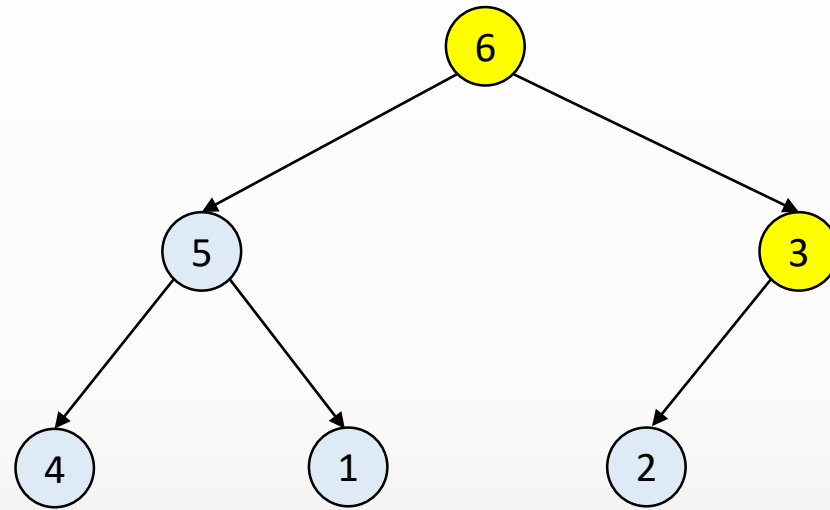
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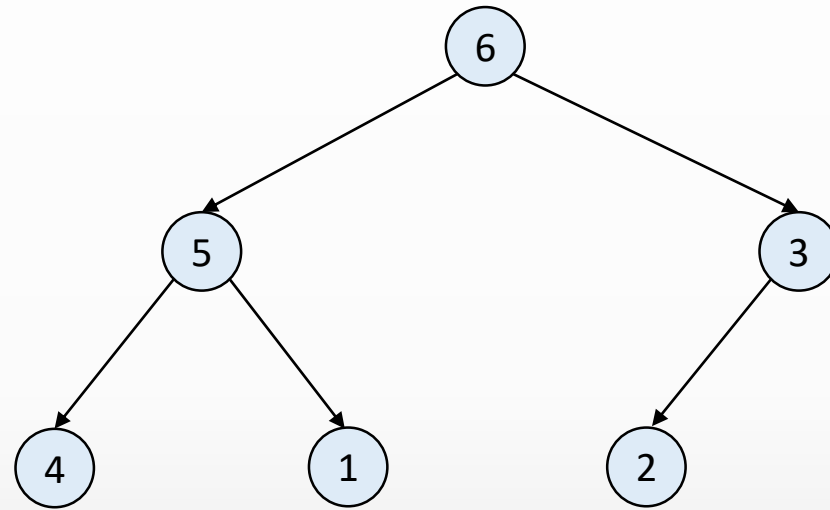
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ek1e(3)



ek1e(3)



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# Max Heap Ağacına Eleman Ekleme

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```



# Max Heap Ağacına Eleman Ekleme

```
MaxOK ok = new MaxOK(3);
```

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
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private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```



null	null	null	null
0	1	2	3
heap[]			

```
MaxOK ok = new MaxOK(3);
```

```
public void ekle(int x) {  
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	null	null	null
0	1	2	3

heap[]

```
MaxOK ok = new MaxOK(3);
```

```
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        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```



	null	null	null
--	------	------	------

0      1      2      3

heap[]

heap.length = 4

MaxOK ok = new MaxOK(3);

```
public void ekle(int x) {
    if (n == heap.length - 1) {
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    }
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    while (k > 1 && heap[k / 2] < heap[k]) {
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        heap[k] = heap[k / 2];
        heap[k / 2] = gecici;
        k = k / 2;
    }
}
```



	null	null	null
--	------	------	------

0      1      2      3

heap[]

n = 0

heap.length = 4

MaxOK ok = new MaxOK(3);

```
public void ekle(int x) {
    if (n == heap.length - 1) {
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        heap[k / 2] = gecici;
        k = k / 2;
    }
}
```



	null	null	null
--	------	------	------

0      1      2      3

heap[]

n = 0

heap.length = 4

ekle(4)

```
public void ekle(int x) {  
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	null	null	null
0	1	2	3

heap[]

n = 0  
heap.length = 4

ekle(4)

```
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```





	null	null	null
--	------	------	------

0

1

2

3

heap[]

x = 4

n = 0

heap.length = 4

ekle(4)

```
→ public void ekle(int x) {  
    if (n == heap.length - 1) {  
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0	1	2	3

heap[]

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ekle(4)



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0	1	2	3

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ekle(4)



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	null	null	null
--	------	------	------

0      1      2      3

heap[]

x = 4  
n = 1  
heap.length = 4

ekle(4)



```
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0	1	2	3

heap[]

x = 4  
n = 1  
heap.length = 4

ekle(4)



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0	1	2	3

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ekle(4)



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0	1	2	3

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ekle(4)

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        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
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}
```



	4	null	null
--	---	------	------

0      1      2      3

heap[]

k = 1  
x = 4  
n = 1  
heap.length = 4

ekle(4)

```
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	4	null	null
--	---	------	------

0      1      2      3

heap[]

k = 1  
x = 4  
n = 1  
heap.length = 4

ekle(4)

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0	1	2	3

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ekle(4)

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	4	null	null
--	---	------	------

0

1

2

3

heap[]

k = 1

x = 4

n = 1

heap.length = 4

ekle(4)

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0	1	2	3

heap[]

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heap.length = 4

ekle(4)



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	4	null	null
--	---	------	------

0

1

2

3

heap[]

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ekle(4)



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	4	null	null
--	---	------	------

0      1      2      3

heap[]

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heap.length = 4

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	4	null	null
--	---	------	------

0

1

2

3

heap[]

n = 1

heap.length = 4

ekle(5)

```
public void ekle(int x) {
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private void yuzdur(int k) {
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```



	4	null	null
0	1	2	3

heap[]

x = 5  
n = 1  
heap.length = 4

ekle(5)

```
→ public void ekle(int x) {  
    if (n == heap.length - 1) {  
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	4	null	null
0	1	2	3

heap[]

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ekle(5)



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```



	4	null	null
0	1	2	3

heap[]

x = 5  
n = 2  
heap.length = 4

ekle(5)



```
public void ekle(int x) {  
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        heap[k / 2] = gecici;  
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    }  
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```



	4	5	null
0	1	2	3

heap[]

x = 5  
n = 2  
heap.length = 4

ekle(5)



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```



	4	5	null
0	1	2	3

heap[]

x = 5  
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ekle(5)



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        k = k / 2;  
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}
```



	4	5	null
0	1	2	3

heap[]

k = 2  
x = 5  
n = 2  
heap.length = 4

ekle(5)

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
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        heap[k / 2] = gecici;  
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}
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	4	5	null
--	---	---	------

0

1

2

3

heap[]

k = 2

x = 5

n = 2

heap.length = 4

ekle(5)

```
public void ekle(int x) {  
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        k = k / 2;  
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}
```



	4	5	null
0	1	2	3

heap[]

$k/2 = 1$

$k = 2$

$x = 5$

$n = 2$

heap.length = 4

ekle(5)

```
public void ekle(int x) {  
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	4	5	null
0	1	2	3

heap[]

```
gecici = 5  
k/2 = 1  
k = 2  
x = 5  
n = 2  
heap.length = 4
```

```
ekle(5)
```

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public void ekle(int x) {  
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	4	4	null
0	1	2	3

heap[]

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gecici = 5  
k/2 = 1  
k = 2  
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```
ekle(5)
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	5	4	null
0	1	2	3

heap[]

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gecici = 5  
k/2 = 1  
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x = 5  
n = 2  
heap.length = 4
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```
ekle(5)
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	5	4	null
0	1	2	3

heap[]

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ekle(5)

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    }  
}
```






	5	4	null
0	1	2	3

heap[]

k = 1  
x = 5  
n = 2  
heap.length = 4

ekle(5)

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```





	5	4	null
0	1	2	3

heap[]

x = 5  
n = 2  
heap.length = 4

ekle(5)



```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```



	5	4	null
0	1	2	3

heap[]

x = 5  
n = 2  
heap.length = 4

ekle(5)

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```



	5	4	null
0	1	2	3

heap[]

n = 2  
heap.length = 4

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
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    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```



	5	4	null
--	---	---	------

0

1

2

3

heap[]

n = 2

heap.length = 4

ekle(2)

```
public void ekle(int x) {
    if (n == heap.length - 1) {
        buyut(2 * heap.length);
    }
    n++;
    heap[n] = x;
    yuzdur(n);
}

private void yuzdur(int k) {
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        k = k / 2;
    }
}
```





	5	4	null
0	1	2	3

heap[]

x = 2  
n = 2  
heap.length = 4

ekle(2)

```
→ public void ekle(int x) {  
    if (n == heap.length - 1) {  
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```



	5	4	null
0	1	2	3

heap[]

x = 2  
n = 2  
heap.length = 4

ekle(2)



```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
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    }  
}
```



	5	4	null
--	---	---	------

0

1

2

3

heap[]

x = 2

n = 3

heap.length = 4

ekle(2)



```
public void ekle(int x) {
    if (n == heap.length - 1) {
        buyut(2 * heap.length);
    }
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    heap[n] = x;
    yuzdur(n);
}

private void yuzdur(int k) {
    while (k > 1 && heap[k / 2] < heap[k]) {
        int gecici = heap[k];
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        heap[k / 2] = gecici;
        k = k / 2;
    }
}
```



	5	4	2
0	1	2	3

heap[]

x = 2  
n = 3  
heap.length = 4

ekle(2)



```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
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        k = k / 2;  
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heap[]

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ekle(2)



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ekle(2)

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    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```



	5	4	2
0	1	2	3

heap[]

k = 3  
x = 2  
n = 3  
heap.length = 4

ekle(2)

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
→ private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```



	5	4	2
0	1	2	3

heap[]

k = 3  
x = 2  
n = 3  
heap.length = 4

ekle(2)

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
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    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```





	5	4	2
0	1	2	3

heap[]

$k/2 = 1$

$k = 3$

$x = 2$

$n = 3$

heap.length = 4

ekle(2)

```
public void ekle(int x) {
    if (n == heap.length - 1) {
        buyut(2 * heap.length);
    }
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    heap[n] = x;
    yuzdur(n);
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heap[]

$k/2 = 1$

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ekle(2)

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}
```





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heap[]

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ekle(2)



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ekle(2)

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```



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0	1	2	3

heap[]

n = 3  
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```
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        int gecici = heap[k];  
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        k = k / 2;  
    }  
}
```



	5	4	2
0	1	2	3

heap[]

n = 3  
heap.length = 4

ekle(6)

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```



	5	4	2
0	1	2	3

heap[]

x = 6  
n = 3  
heap.length = 4

ekle(6)

```
→ public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
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```



	5	4	2
0	1	2	3

heap[]

x = 6  
n = 3  
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ekle(6)



```
public void ekle(int x) {  
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        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```





	5	4	2
0	1	2	3

heap[]

x = 6  
n = 3  
heap.length = 4

ekle(6)



```
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    heap[n] = x;  
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private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```



	5	4	2	null	null	null	null
0	1	2	3	4	5	6	7

heap[]

x = 6  
n = 3  
heap.length = 8

ekle(6)



```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
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        k = k / 2;  
    }  
}
```



	5	4	2	null	null	null	null
0	1	2	3	4	5	6	7

heap[]

x = 6  
n = 4  
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ekle(6)



```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
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    n++;  
    heap[n] = x;  
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private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```



	5	4	2	6	null	null	null
0	1	2	3	4	5	6	7

heap[]

x = 6  
n = 4  
heap.length = 8

ekle(6)



```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
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```



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0	1	2	3	4	5	6	7

heap[]

x = 6  
n = 4  
heap.length = 8

ekle(6)



```
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private void yuzdur(int k) {  
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        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
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        k = k / 2;  
    }  
}
```



	5	4	2	6	null	null	null
0	1	2	3	4	5	6	7

heap[]

x = 6  
n = 4  
heap.length = 8

ekle(6)

```
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        int gecici = heap[k];  
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        k = k / 2;  
    }  
}
```



	5	4	2	6	null	null	null
0	1	2	3	4	5	6	7

heap[]

k = 4  
x = 6  
n = 4  
heap.length = 8

ekle(6)

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
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        int gecici = heap[k];  
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    }  
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```



	5	4	2	6	null	null	null
0	1	2	3	4	5	6	7

heap[]

$k/2 = 2$

$k = 4$

$x = 6$

$n = 4$

heap.length = 8

ekle(6)

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
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heap[]

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$n = 4$

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ekle(6)

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    }  
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```



	5	4	2	6	null	null	null
0	1	2	3	4	5	6	7

heap[]

gecici = 6  
 $k/2 = 2$   
 $k = 4$   
 $x = 6$   
 $n = 4$   
 $\text{heap.length} = 8$

ekle(6)

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public void ekle(int x) {  
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```



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0	1	2	3	4	5	6	7

heap[]

gecici = 6  
k/2 = 2  
k = 4  
x = 6  
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heap.length = 8

ekle(6)



```
public void ekle(int x) {  
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0	1	2	3	4	5	6	7

heap[]

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 $k/2 = 2$   
 $k = 4$   
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ekle(6)



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0	1	2	3	4	5	6	7

heap[]

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 $k/2 = 2$   
 $k = 2$   
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ekle(6)

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0	1	2	3	4	5	6	7

heap[]

k = 2  
x = 6  
n = 4  
heap.length = 8

ekle(6)

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
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    heap[n] = x;  
    yuzdur(n);  
}  
  
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    while (k > 1 && heap[k / 2] < heap[k]) {  
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0	1	2	3	4	5	6	7

heap[]

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heap.length = 8

ekle(1)

```
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    heap[n] = x;  
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private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
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heap[]

x = 1  
n = 5  
heap.length = 8

ekle(1)



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public void ekle(int x) {  
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    }  
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heap[]

x = 3  
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heap.length = 8

ekle(3)

```
→ public void ekle(int x) {  
    if (n == heap.length - 1) {  
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    }  
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    heap[n] = x;  
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$n = 6$

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ekle(3)

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}  
  
private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```



	6	5	2	4	1	3	null
0	1	2	3	4	5	6	7

heap[]

$k/2 = 3$   
 $k = 6$   
 $x = 3$   
 $n = 6$   
 $\text{heap.length} = 8$

ekle(3)

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```



	6	5	2	4	1	3	null
0	1	2	3	4	5	6	7

heap[]

gecici = 3  
k/2 = 3  
k = 6  
x = 3  
n = 6  
heap.length = 8

ekle(3)

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```





	6	5	2	4	1	2	null
0	1	2	3	4	5	6	7

heap[]

gecici = 3  
k/2 = 3  
k = 6  
x = 3  
n = 6  
heap.length = 8

ekle(3)



```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```



	6	5	3	4	1	2	null
0	1	2	3	4	5	6	7

heap[]

gecici = 3  
k/2 = 3  
k = 6  
x = 3  
n = 6  
heap.length = 8

ekle(3)



```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```



	6	5	3	4	1	2	null
0	1	2	3	4	5	6	7

heap[]

gecici = 3  
k/2 = 3  
k = 3  
x = 3  
n = 6  
heap.length = 8

ekle(3)

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```





	6	5	3	4	1	2	null
0	1	2	3	4	5	6	7

heap[]

k = 3  
x = 3  
n = 6  
heap.length = 8

ekle(3)

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```



	6	5	3	4	1	2	null
0	1	2	3	4	5	6	7

heap[]

$k/2 = 1$

$k = 3$

$x = 3$

$n = 6$

heap.length = 8

ekle(3)

```
public void ekle(int x) {
    if (n == heap.length - 1) {
        buyut(2 * heap.length);
    }
    n++;
    heap[n] = x;
    yuzdur(n);
}

private void yuzdur(int k) {
    while (k > 1 && heap[k / 2] < heap[k]) {
        int gecici = heap[k];
        heap[k] = heap[k / 2];
        heap[k / 2] = gecici;
        k = k / 2;
    }
}
```



	6	5	3	4	1	2	null
0	1	2	3	4	5	6	7

heap[]

$k/2 = 1$

$k = 3$

$x = 3$

$n = 6$

heap.length = 8

ekle(3)

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```



	6	5	3	4	1	2	null
0	1	2	3	4	5	6	7

heap[]

$k/2 = 1$

$k = 3$

$x = 3$

$n = 6$

heap.length = 8

ekle(3)

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```





	6	5	3	4	1	2	null
0	1	2	3	4	5	6	7

heap[]

x = 3  
n = 6  
heap.length = 8

ekle(3)



```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```





	6	5	3	4	1	2	null
0	1	2	3	4	5	6	7

heap[]

x = 3  
n = 6  
heap.length = 8

ekle(3)

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```



	6	5	3	4	1	2	null
0	1	2	3	4	5	6	7

heap[]

n = 6  
heap.length = 8

```
public void ekle(int x) {  
    if (n == heap.length - 1) {  
        buyut(2 * heap.length);  
    }  
    n++;  
    heap[n] = x;  
    yuzdur(n);  
}  
  
private void yuzdur(int k) {  
    while (k > 1 && heap[k / 2] < heap[k]) {  
        int gecici = heap[k];  
        heap[k] = heap[k / 2];  
        heap[k / 2] = gecici;  
        k = k / 2;  
    }  
}
```



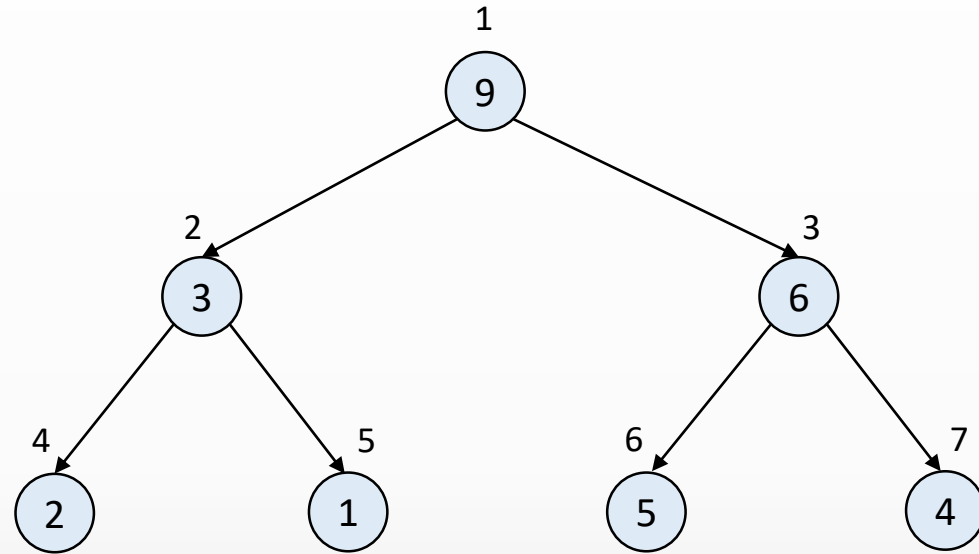
# Yukarıdan Aşağıya Heap Ağacına Dönüştürme



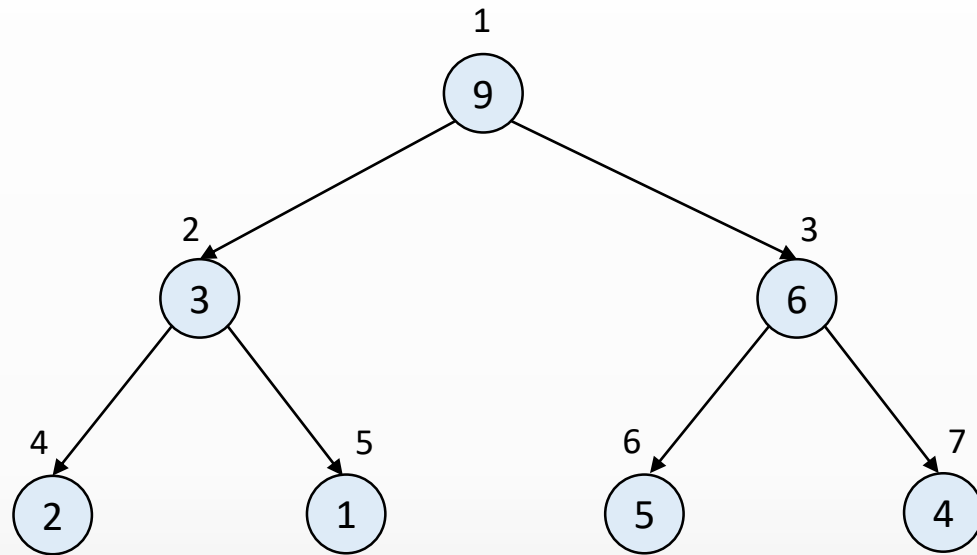
# Yukarıdan Aşağıya Heap Ağacına Dönüştürme

- Max heap ikili ağacının her bir düğümünün değeri, çocuklarının değerlerinden büyük olma özelliğini taşır.
- Ancak heap ağacında bir eleman silindikten sonra bu özellik bozulabilir.
- Bu nedenle elemanların yerlerini yukarıdan aşağıya değiştirerek yeniden heap ağacına dönüştürme işlemi (batır - sink) gerçekleştirilir (top-down heapify).

silMax()



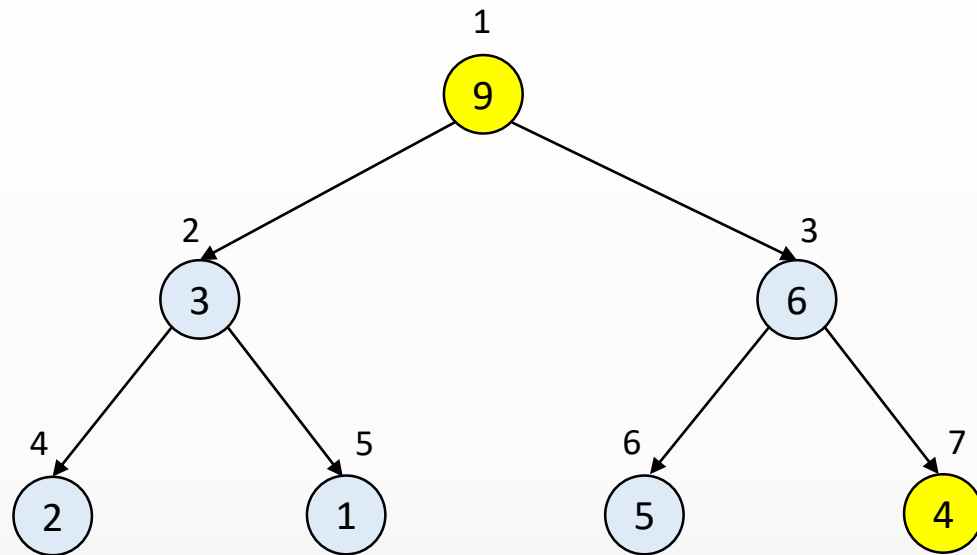
silMax()



max = 9



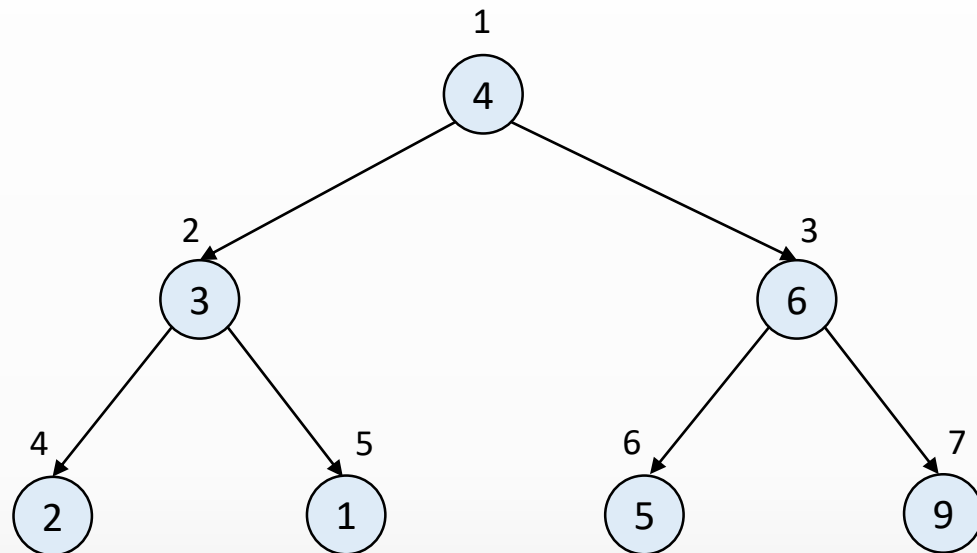
silMax()



max = 9



silMax()

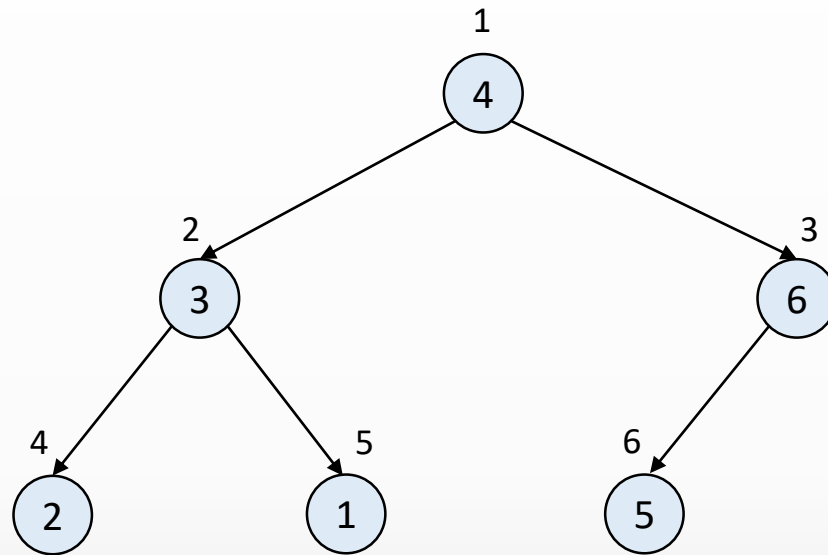


max = 9





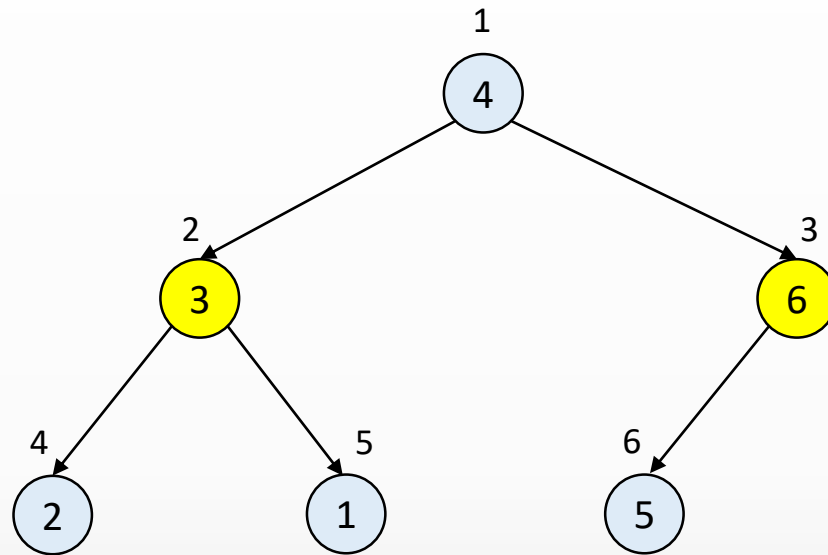
silMax()



max = 9



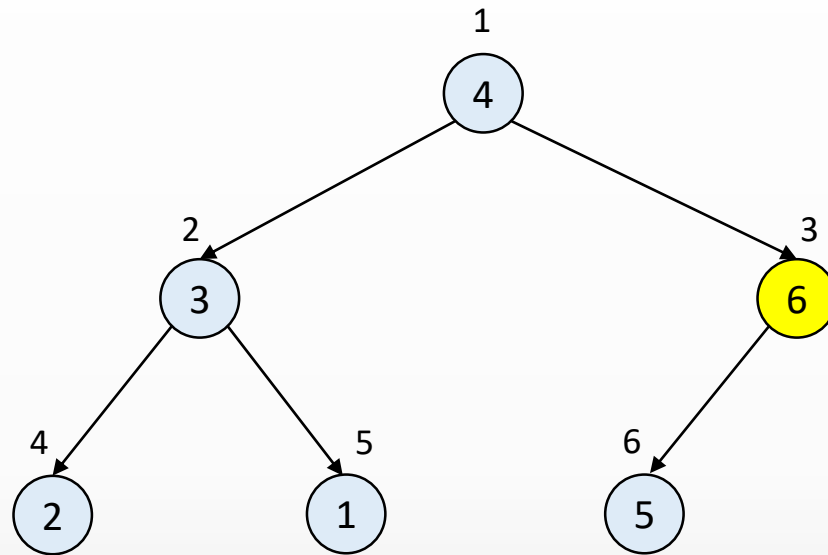
silMax()



max = 9



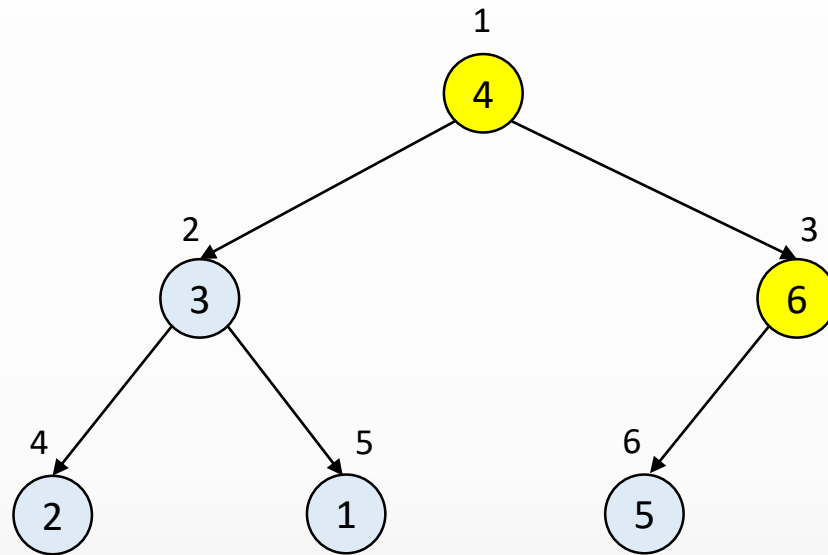
silMax()



max = 9



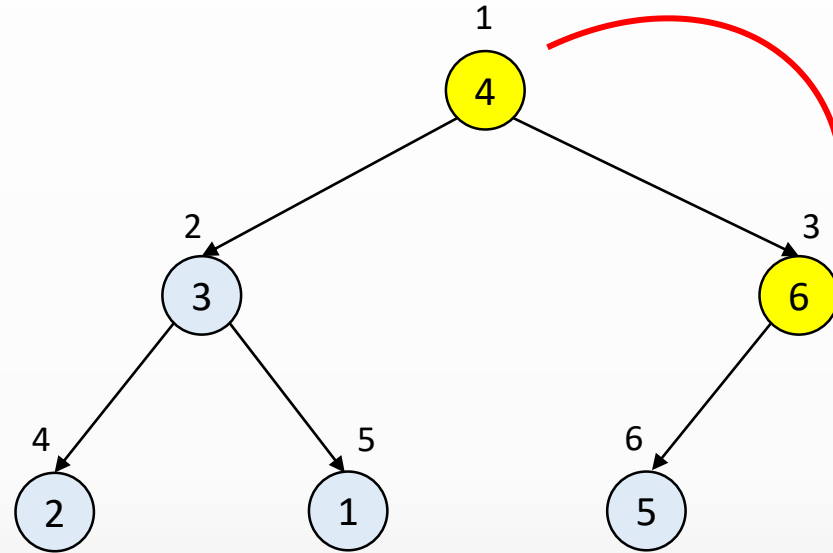
silMax()



max = 9



silMax()

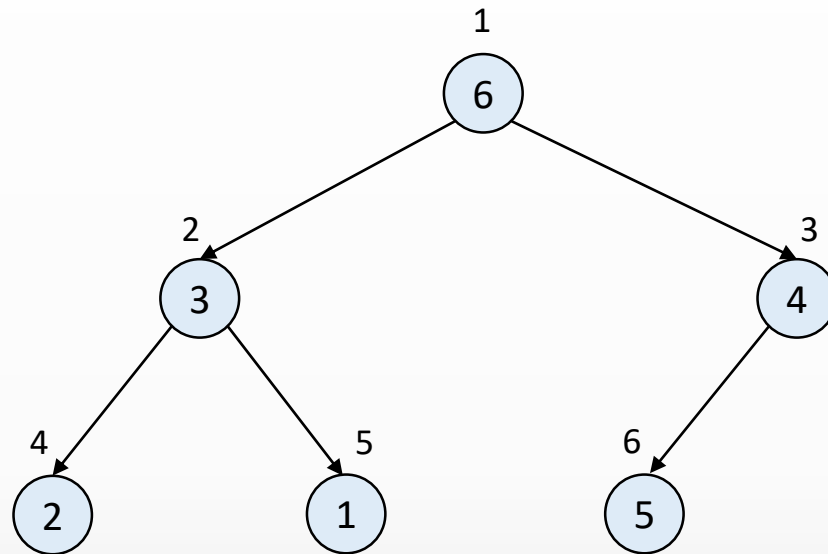


Aşağı taşı

max = 9



silMax()

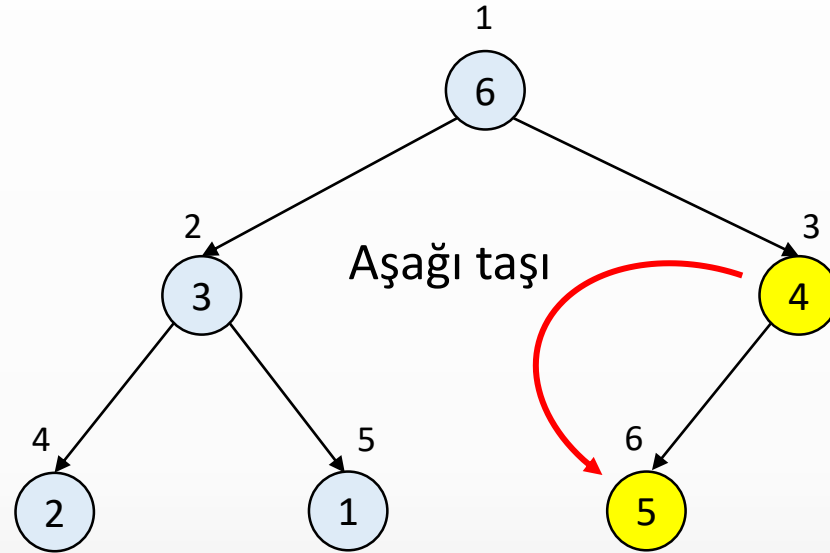


max = 9

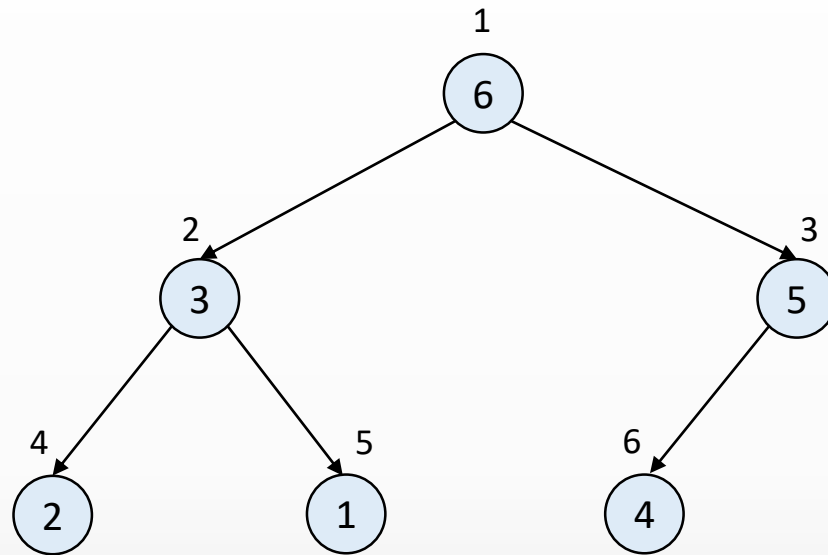


silMax()

max = 9



silMax()



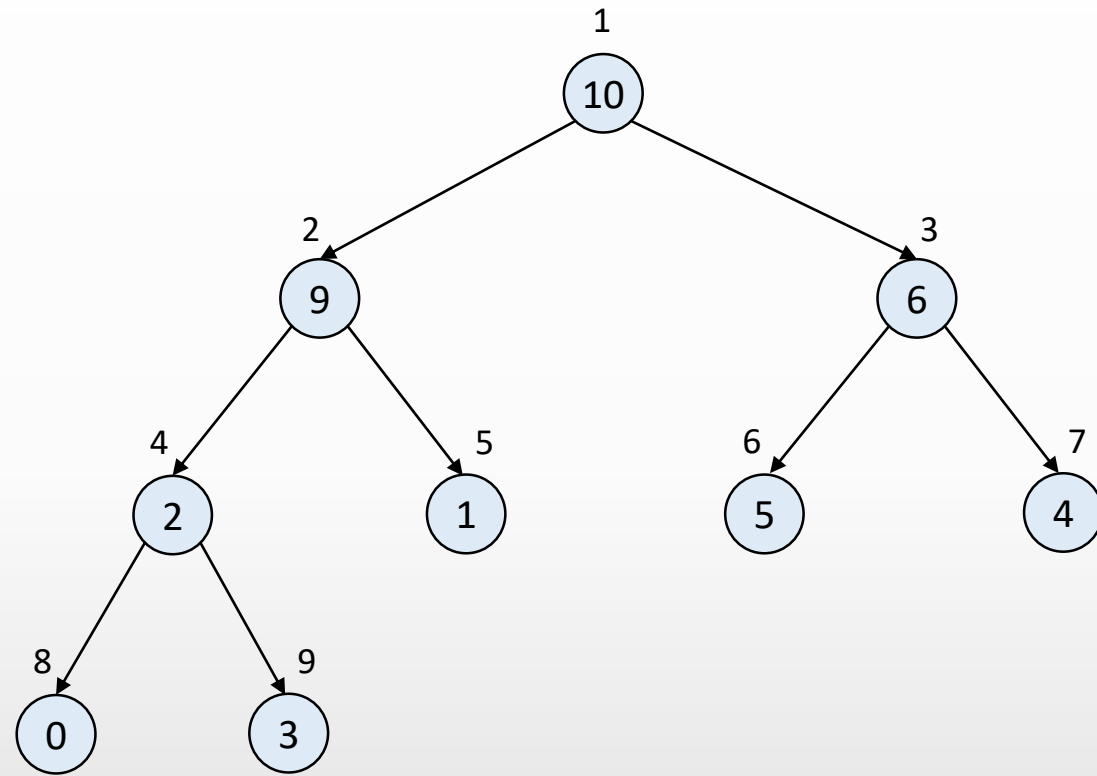
max = 9



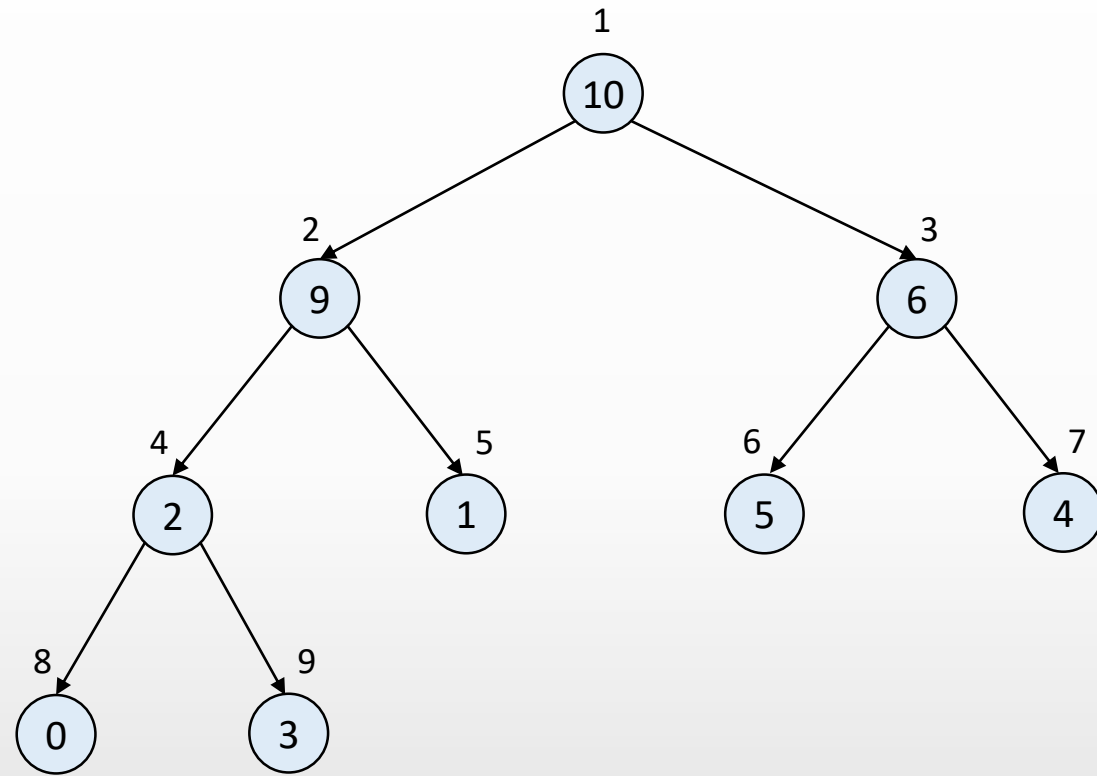




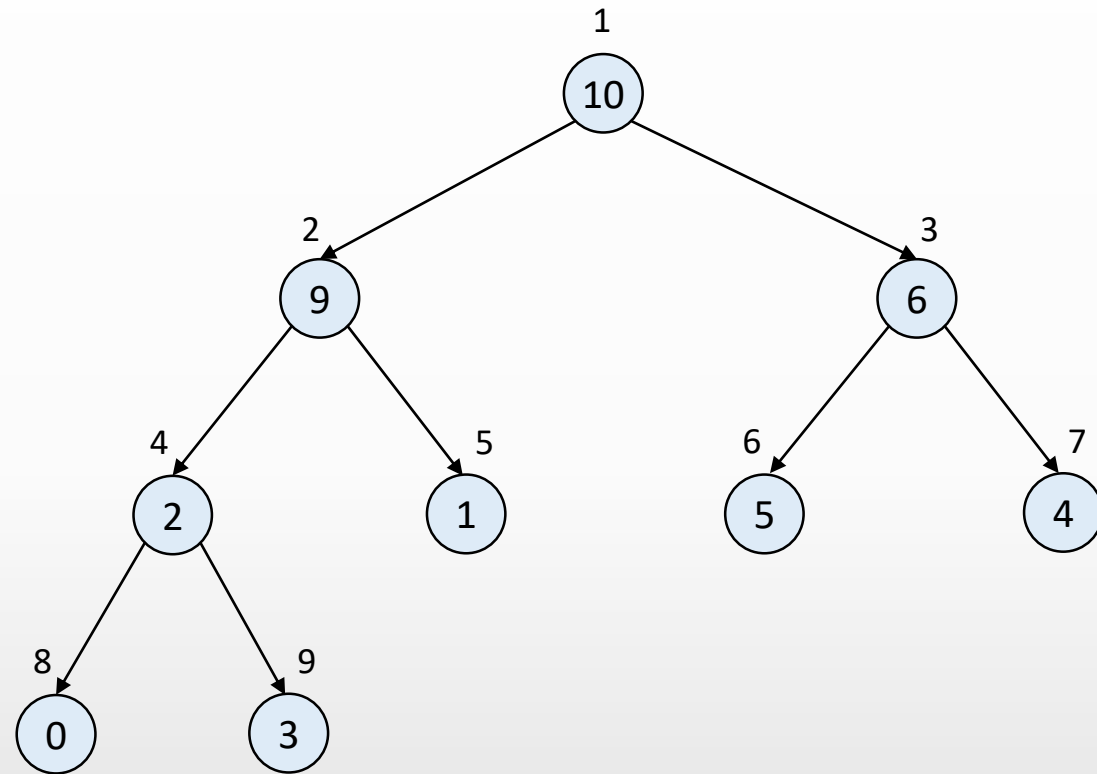
# Yukarıdan Aşağıya Heap Ağacına Dönüştürme



silMax()



silMax()

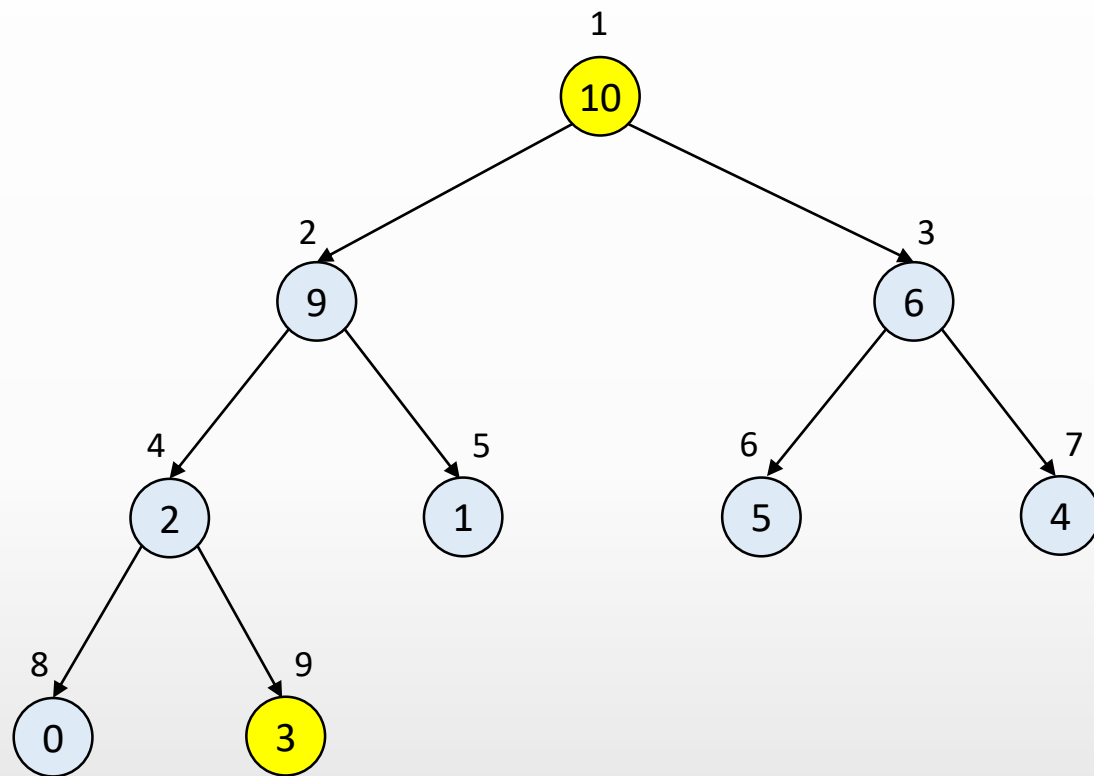


max = 10



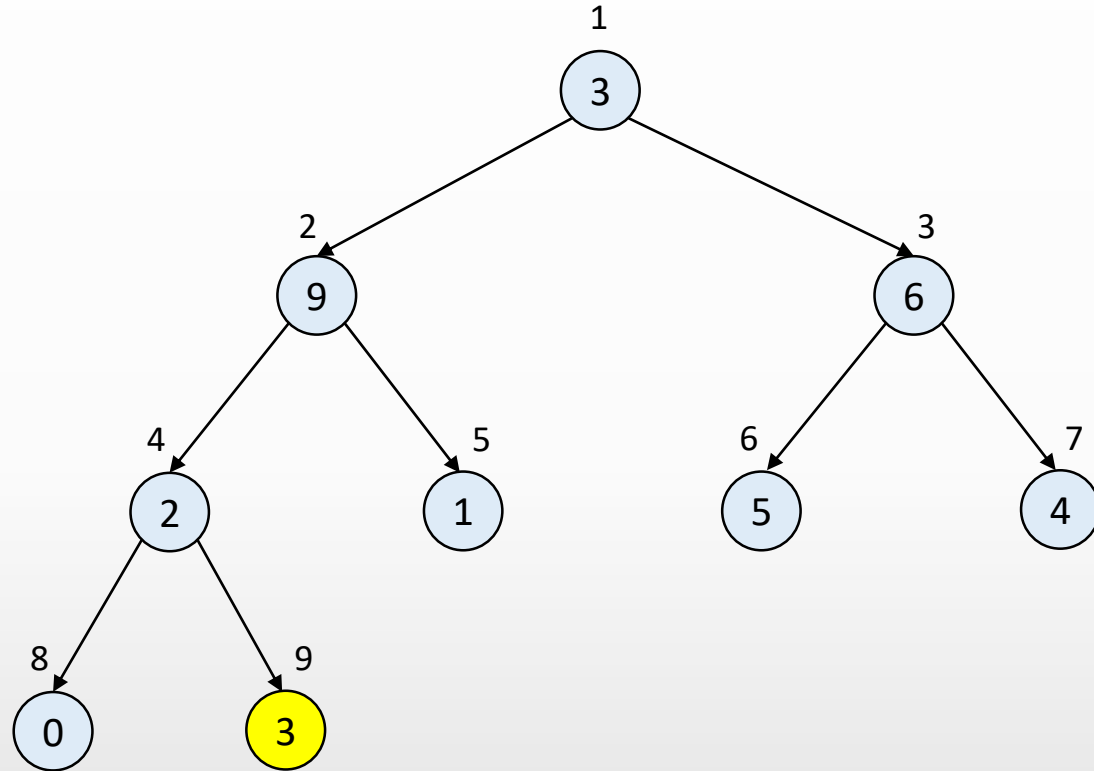
silMax()

max = 10



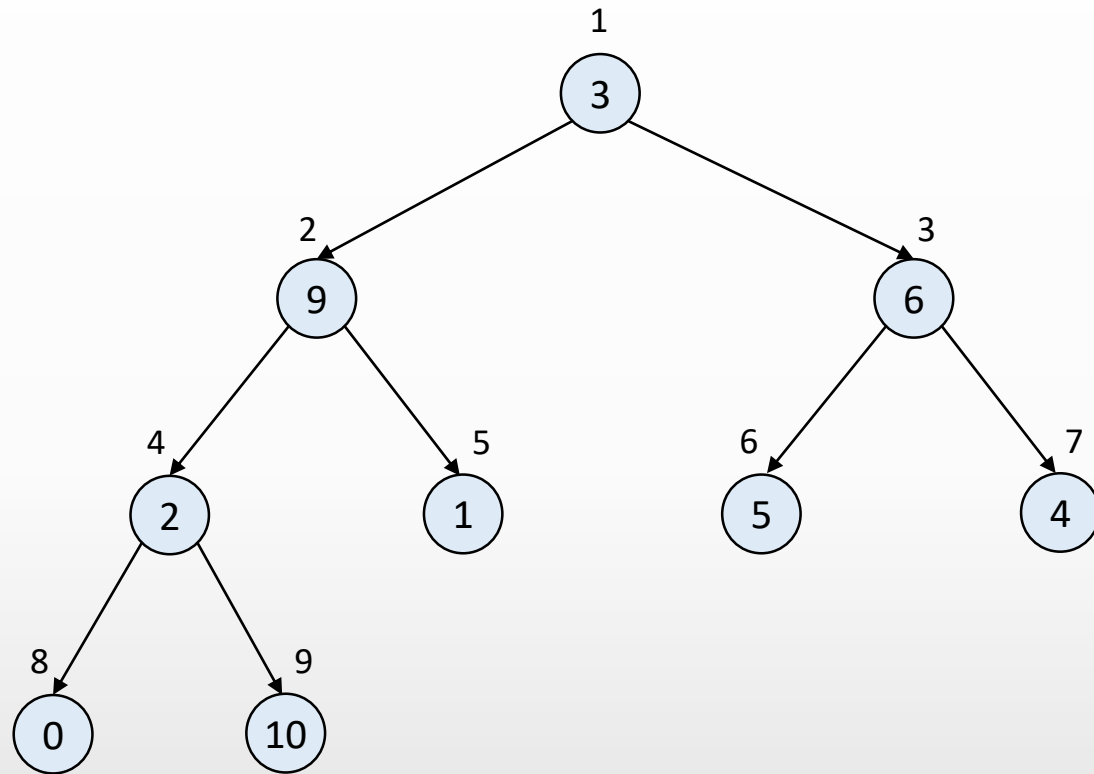
silMax()

max = 10

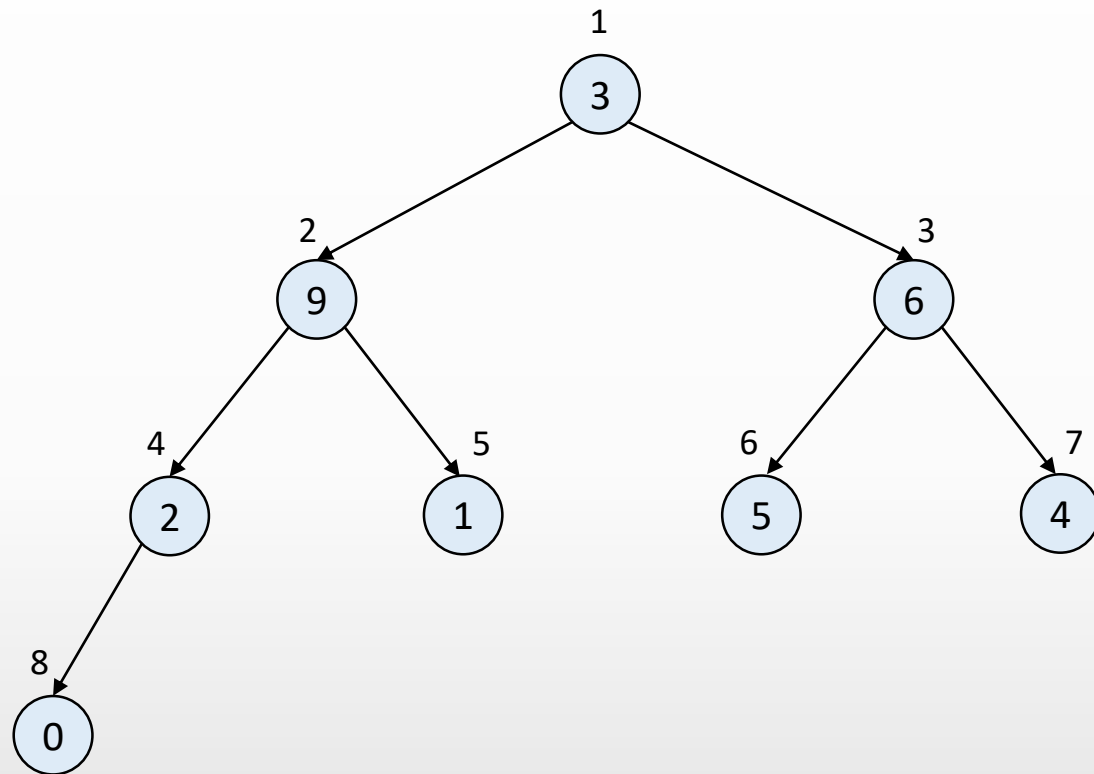


silMax()

max = 10



silMax()

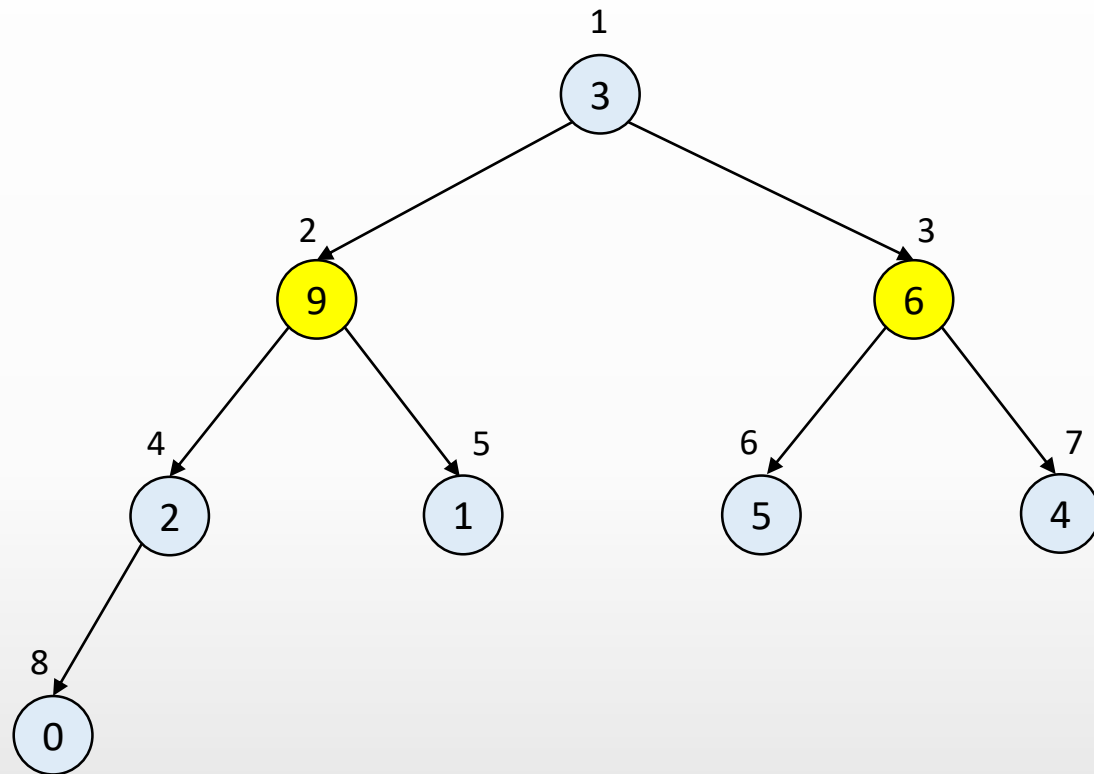


max = 10





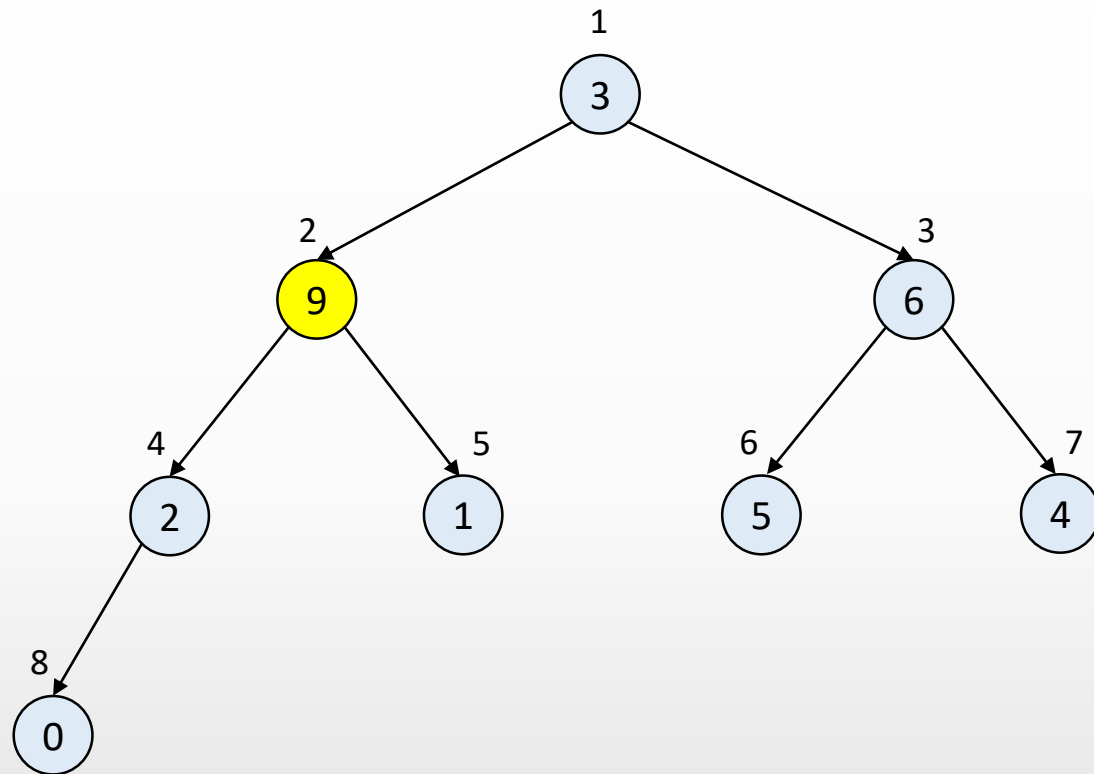
silMax()



max = 10



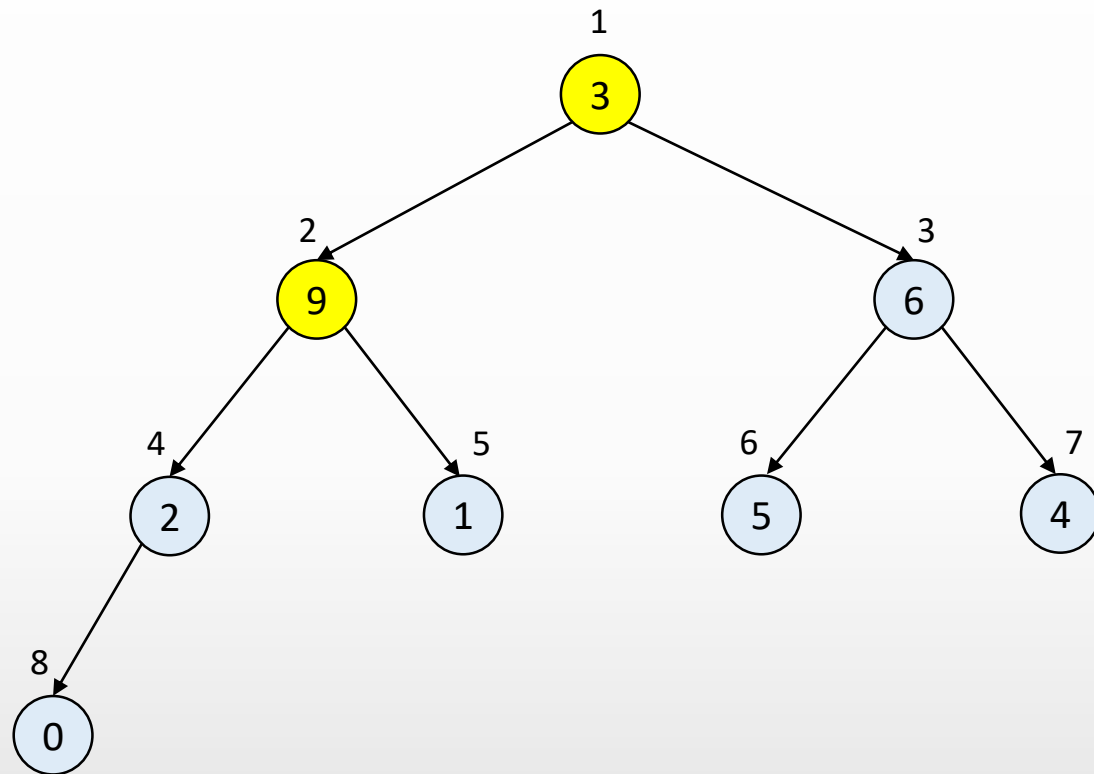
silMax()



max = 10




silMax()

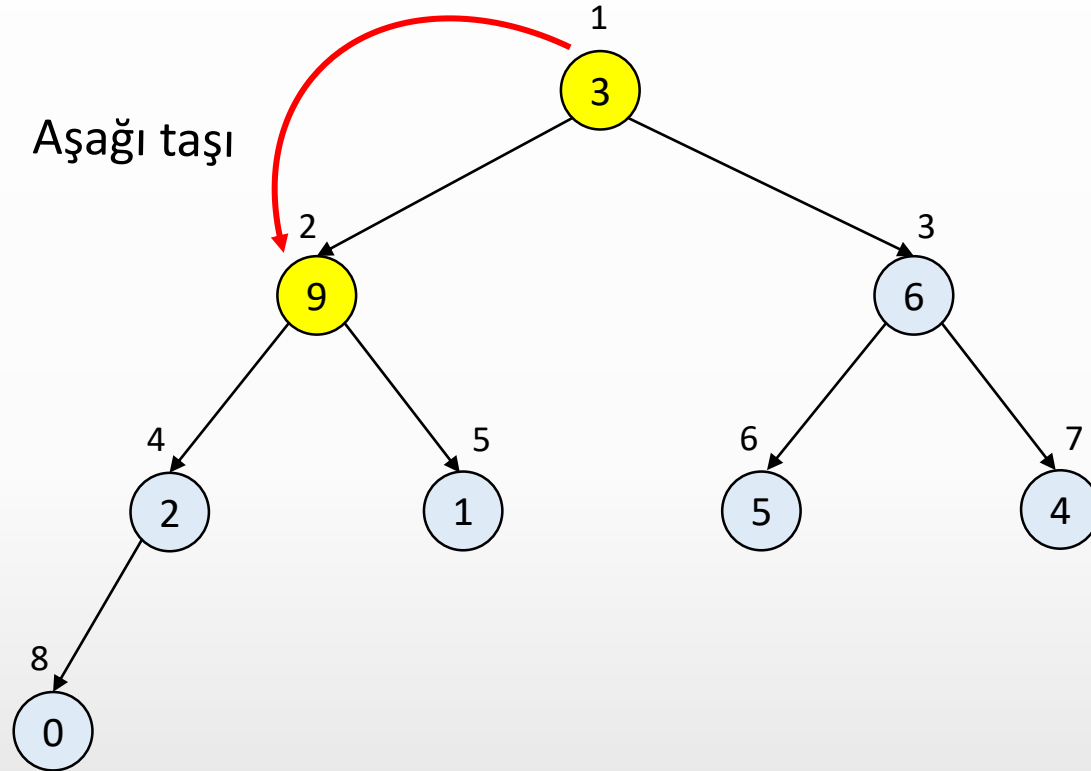


max = 10



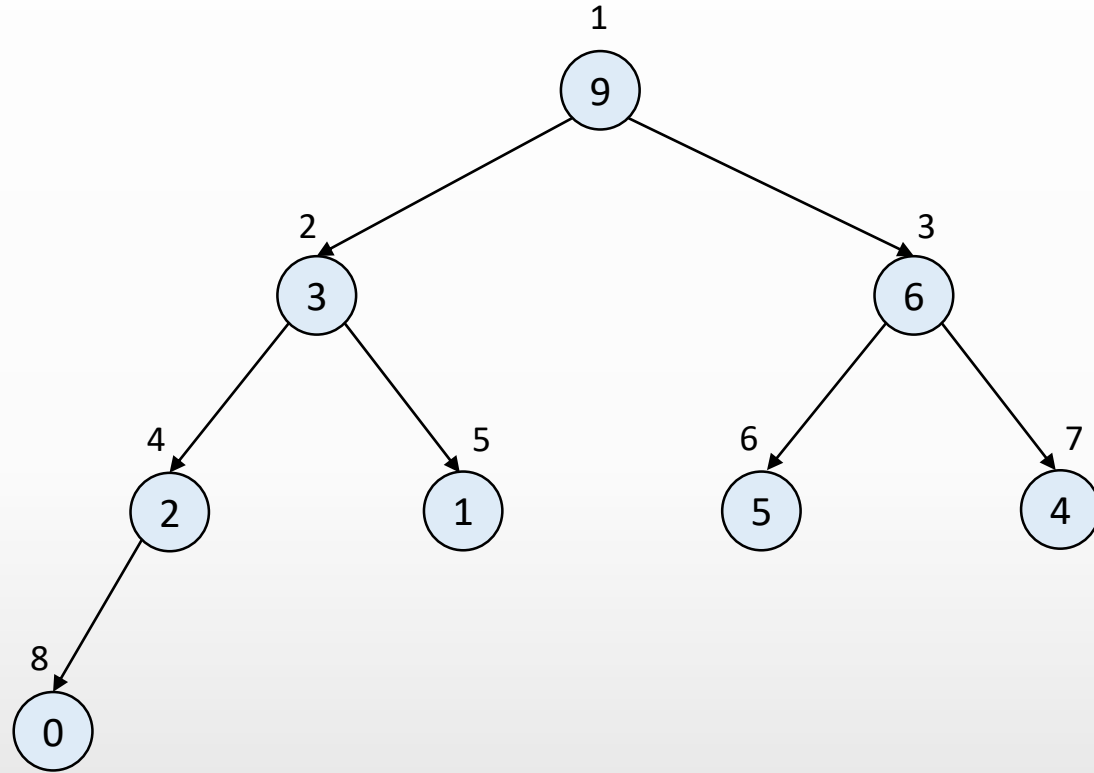
silMax()

max = 10 



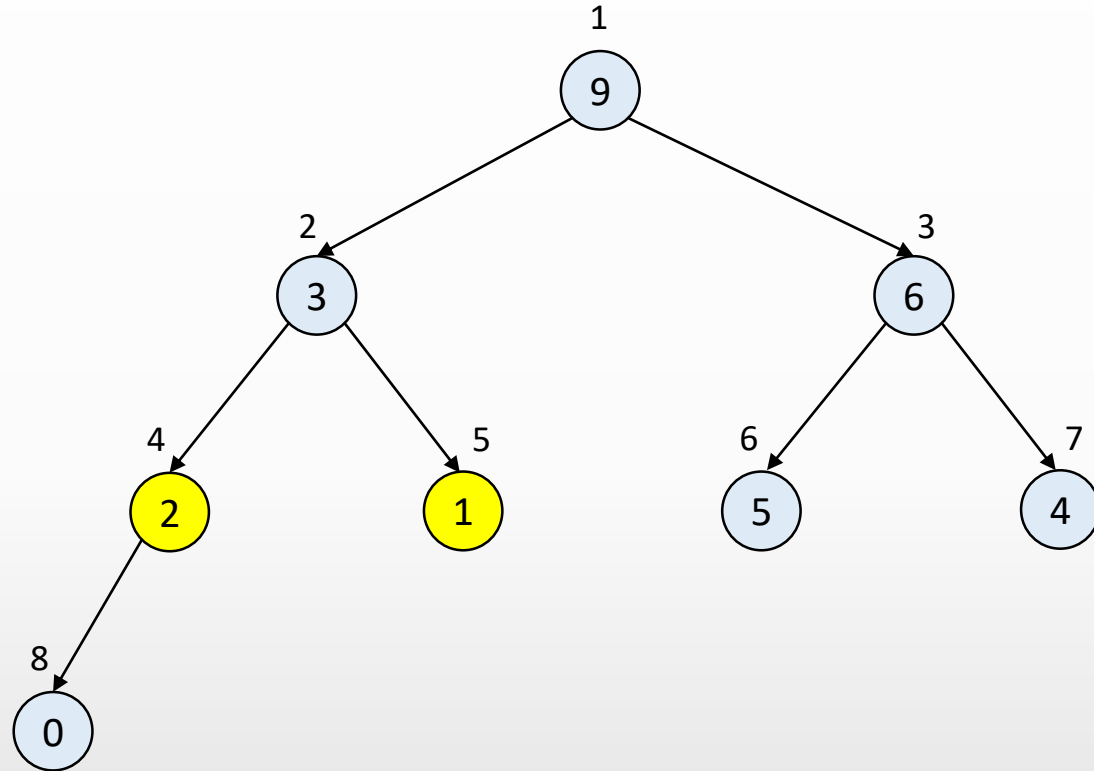
silMax()

max = 10



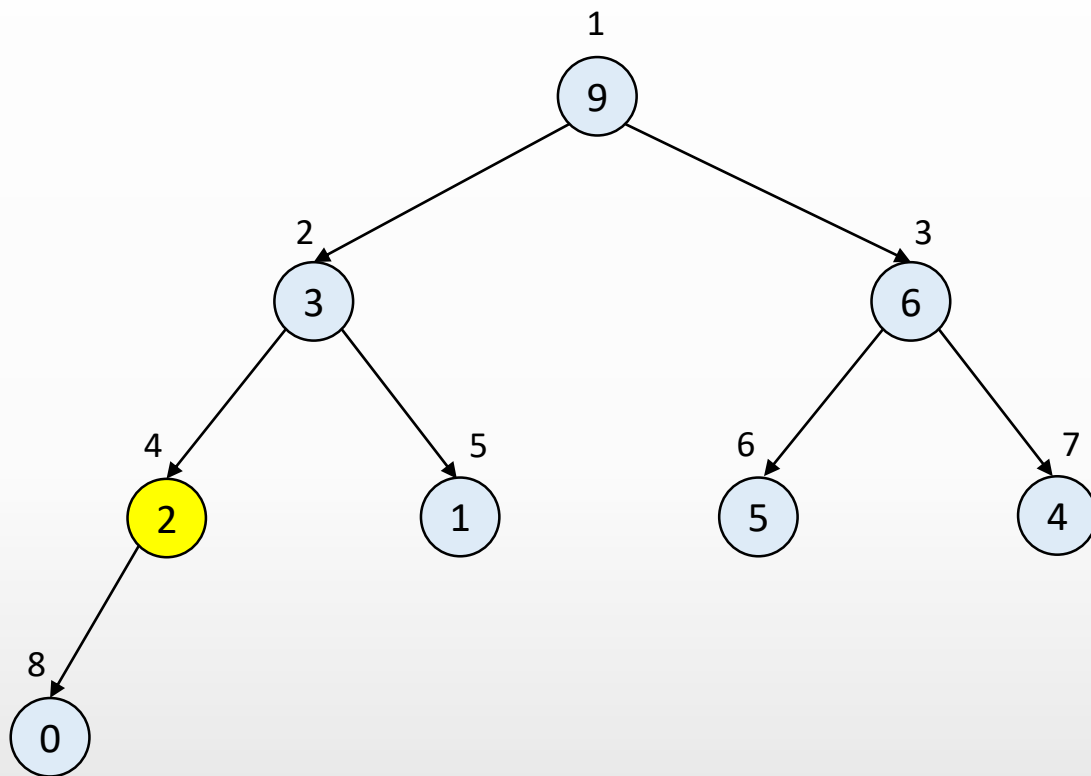
silMax()

max = 10

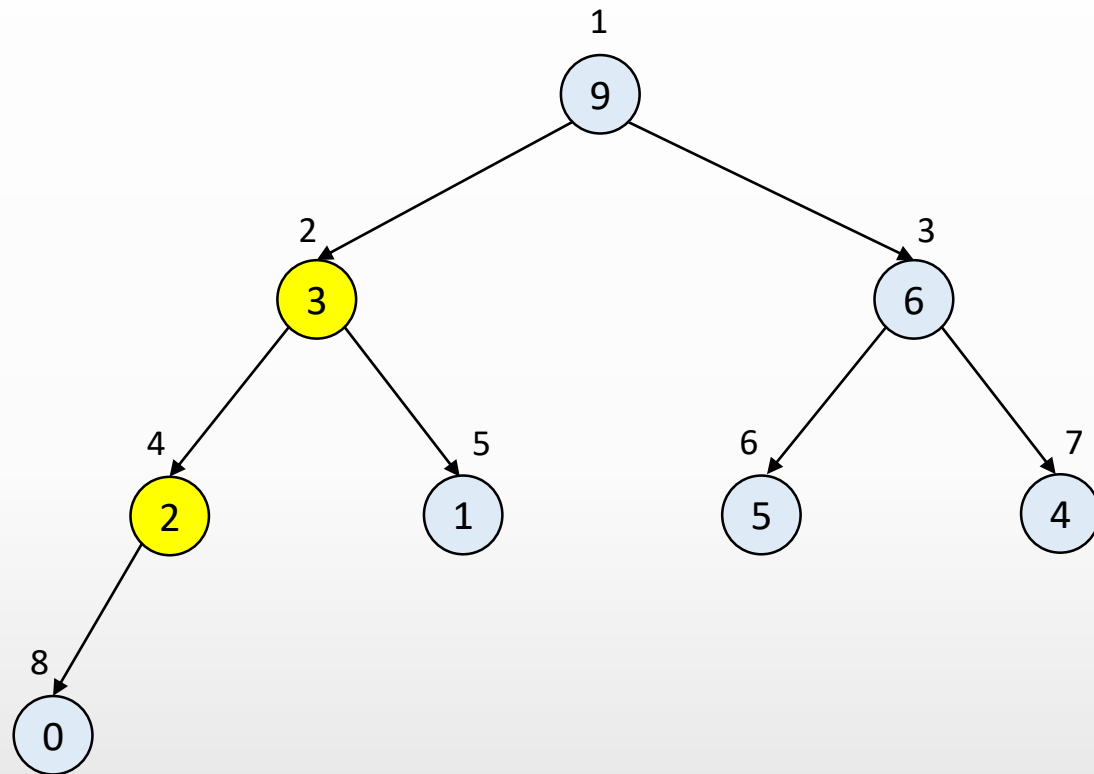


silMax()

max = 10



silMax()



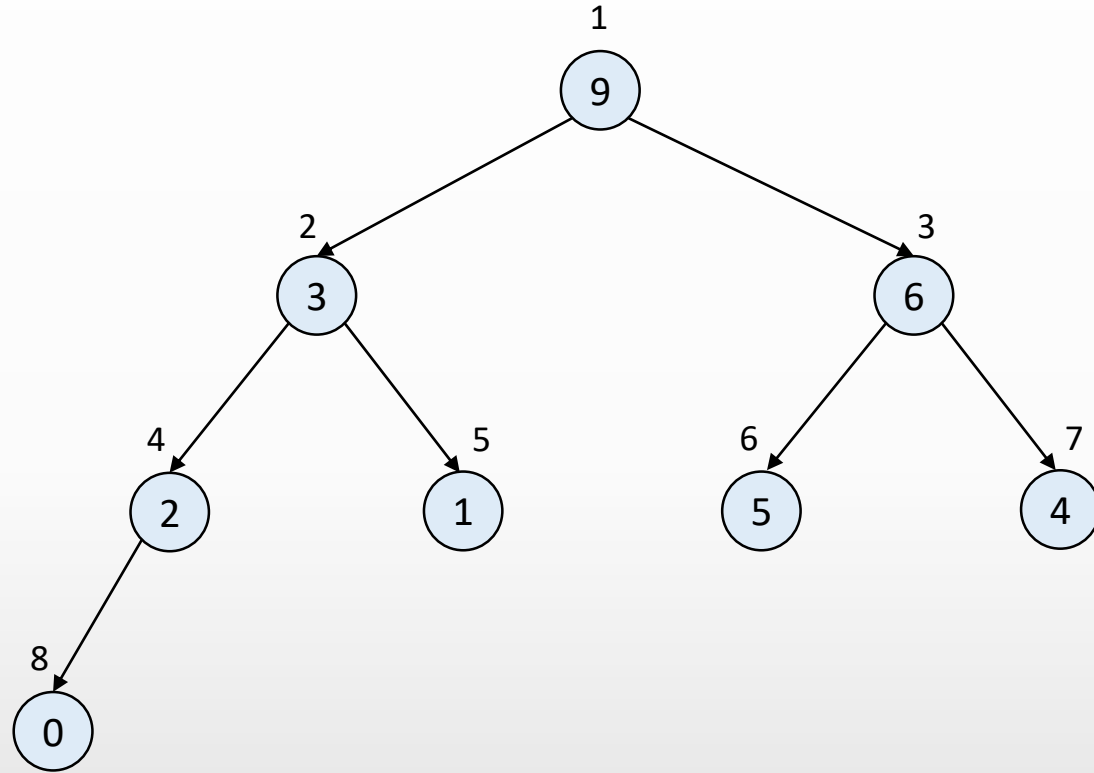
max = 10



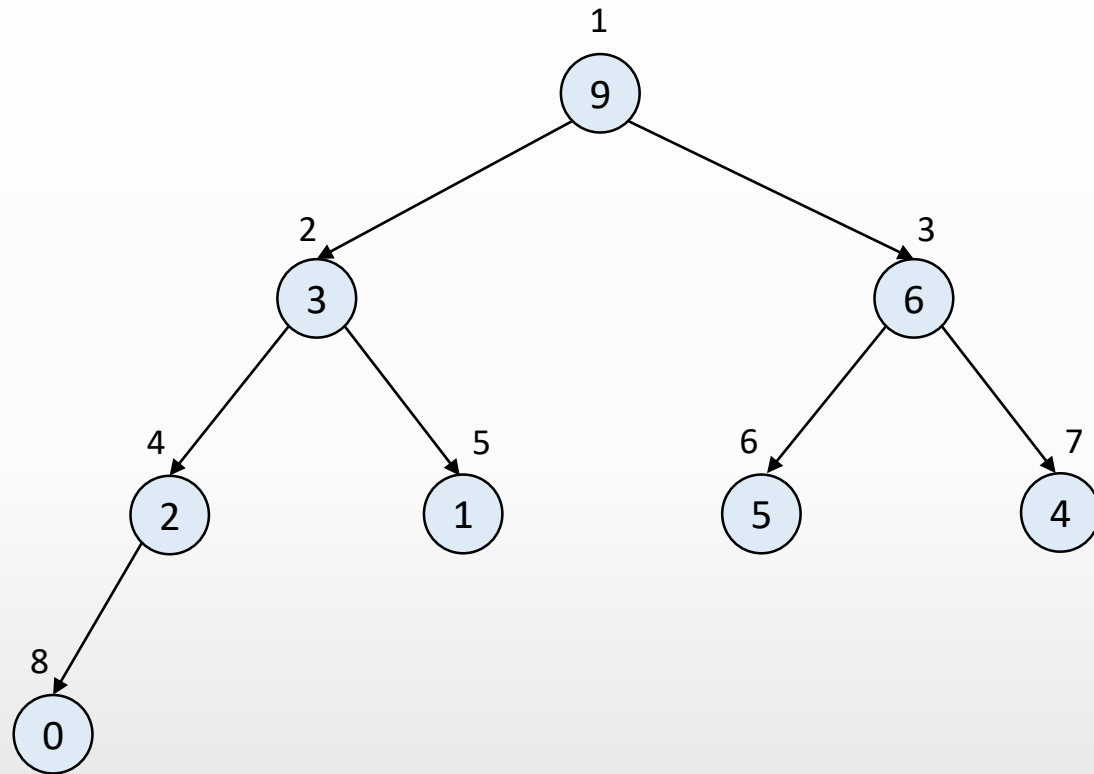


silMax()

max = 10



silMax()

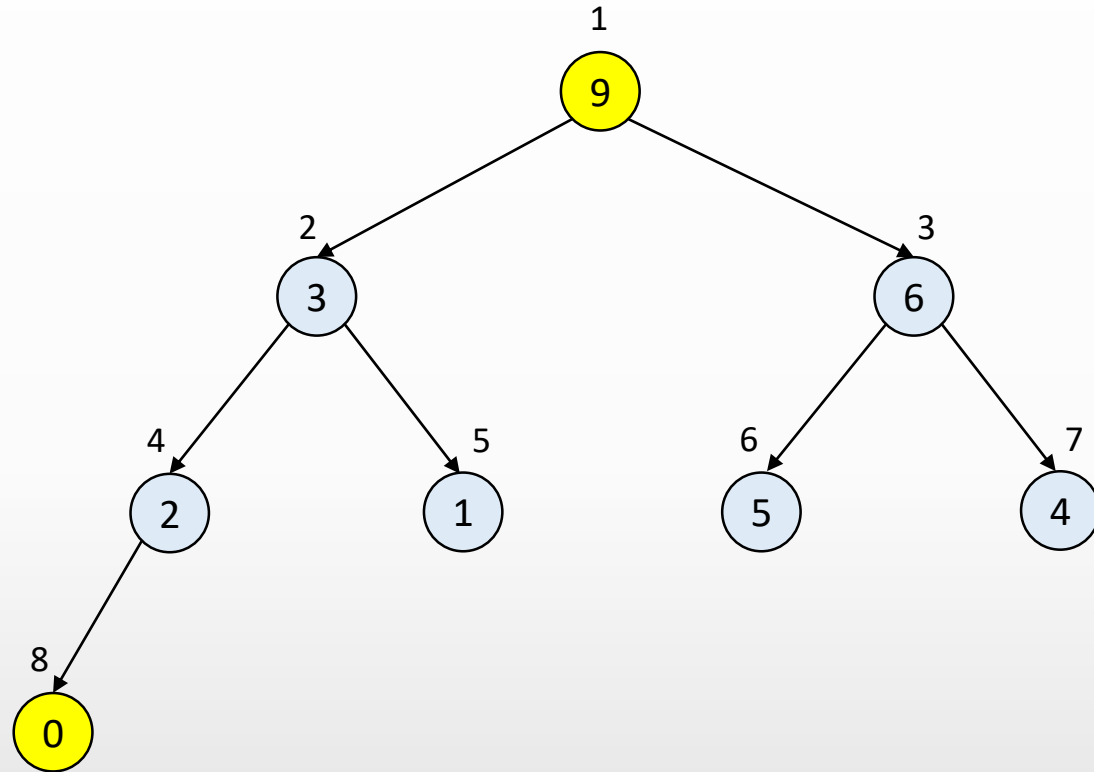


max = 9



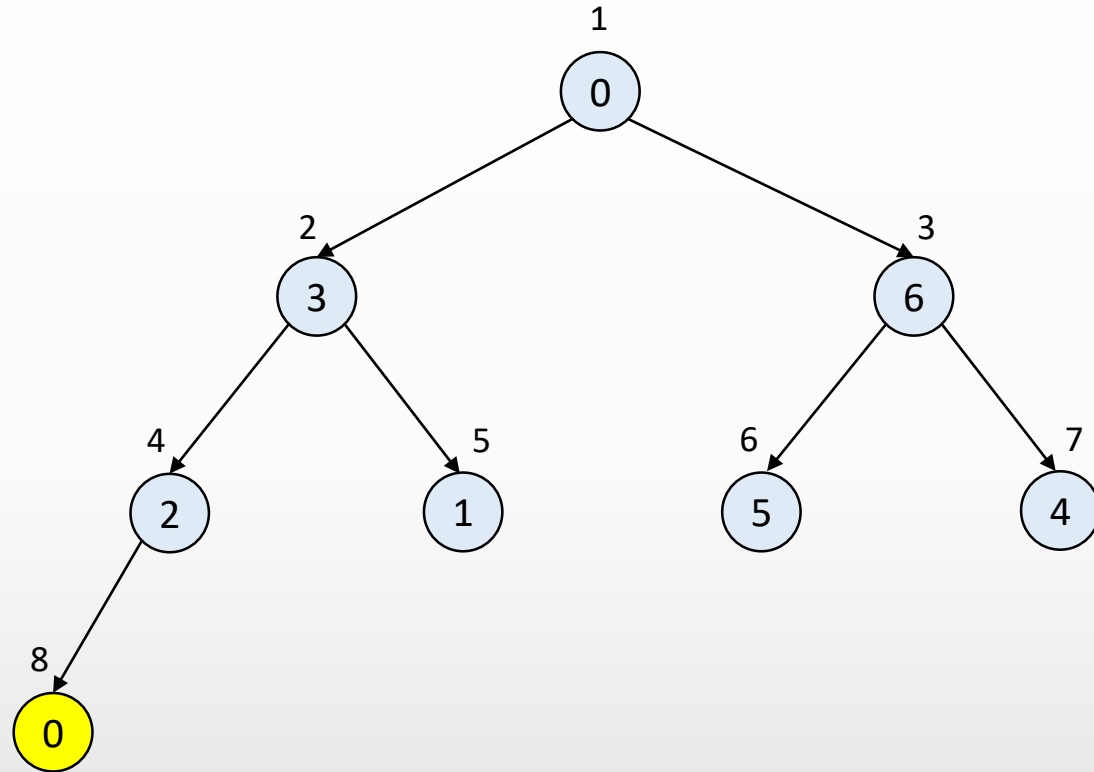
silMax()

max = 9

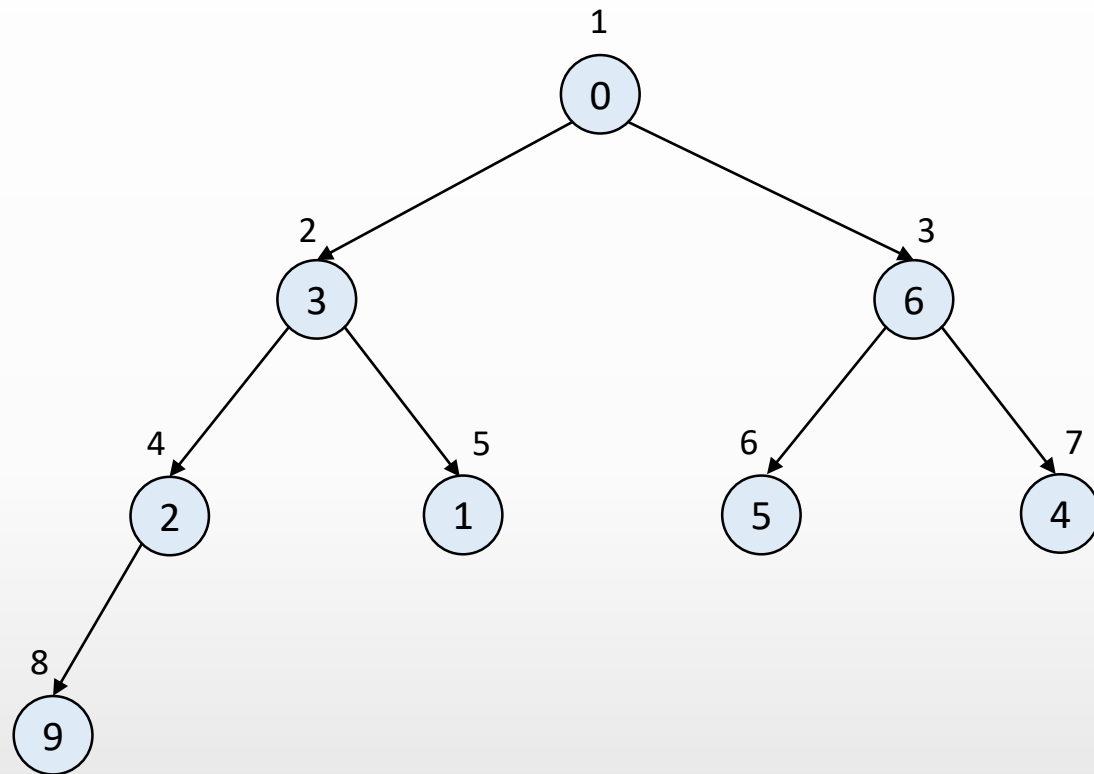


silMax()

max = 9



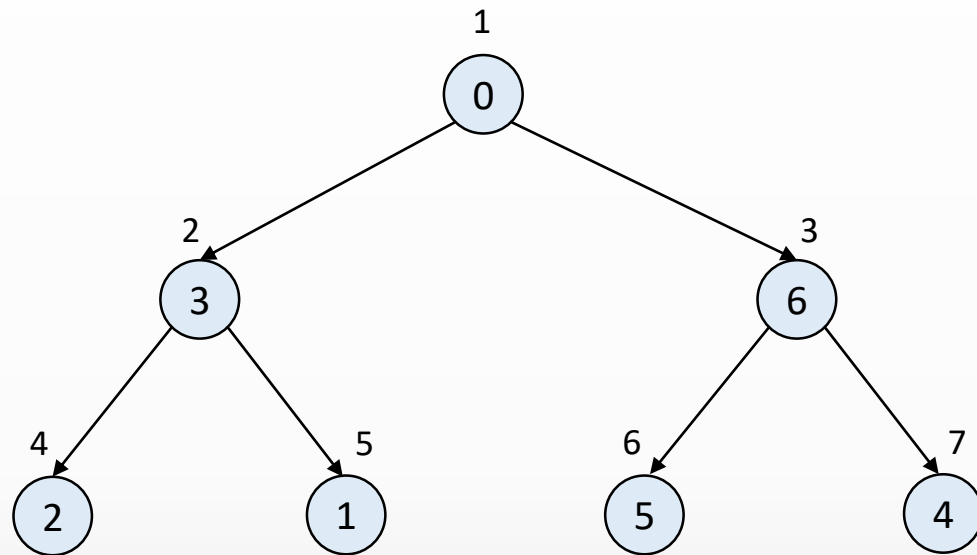
silMax()



max = 9



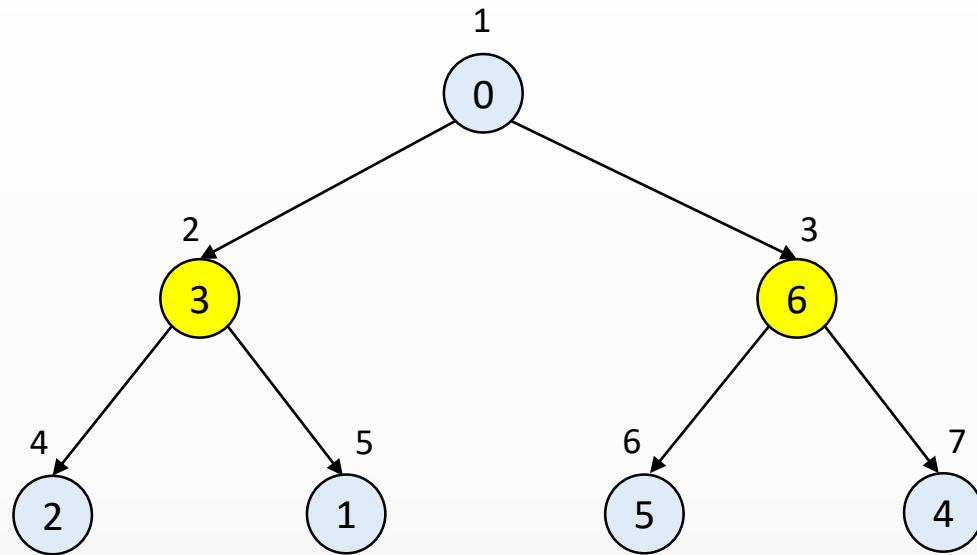
silMax()



max = 9



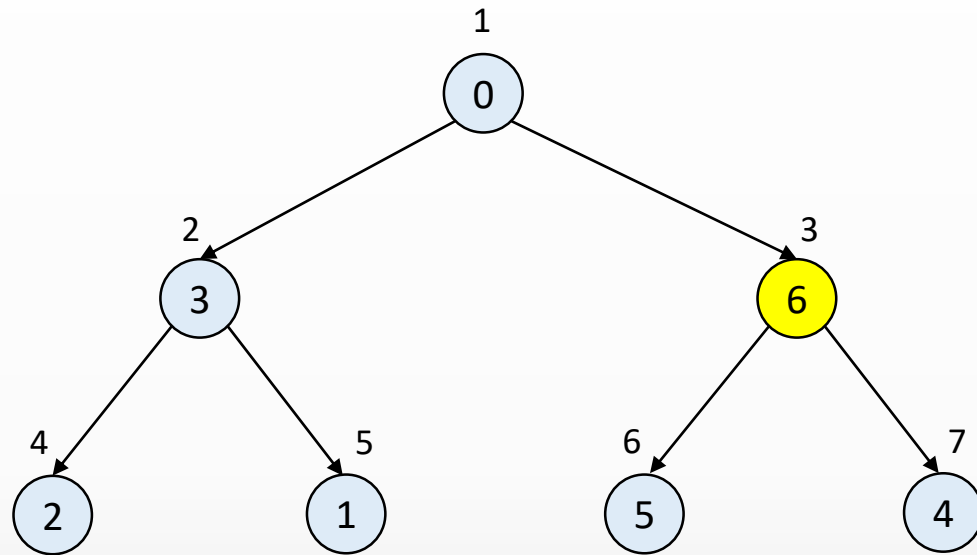
silMax()



max = 9



silMax()

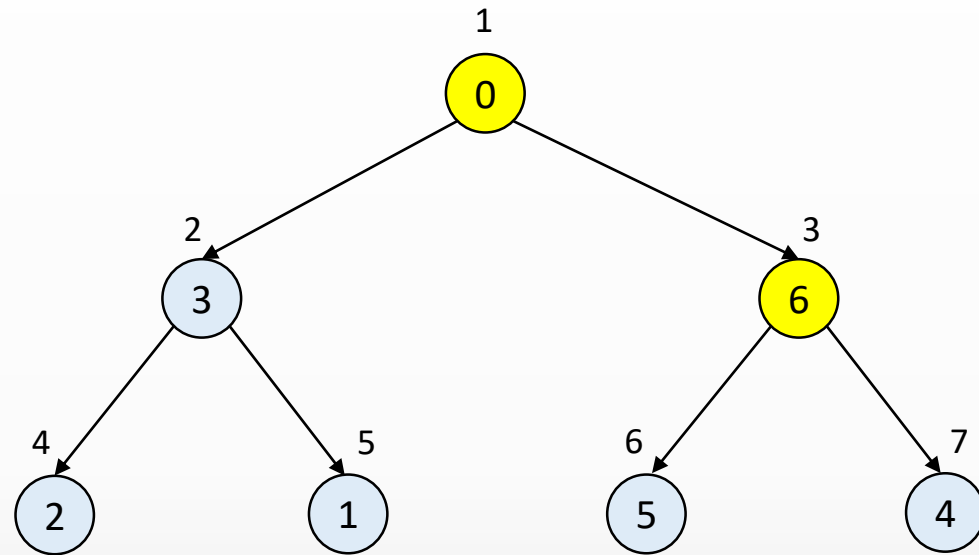


max = 9





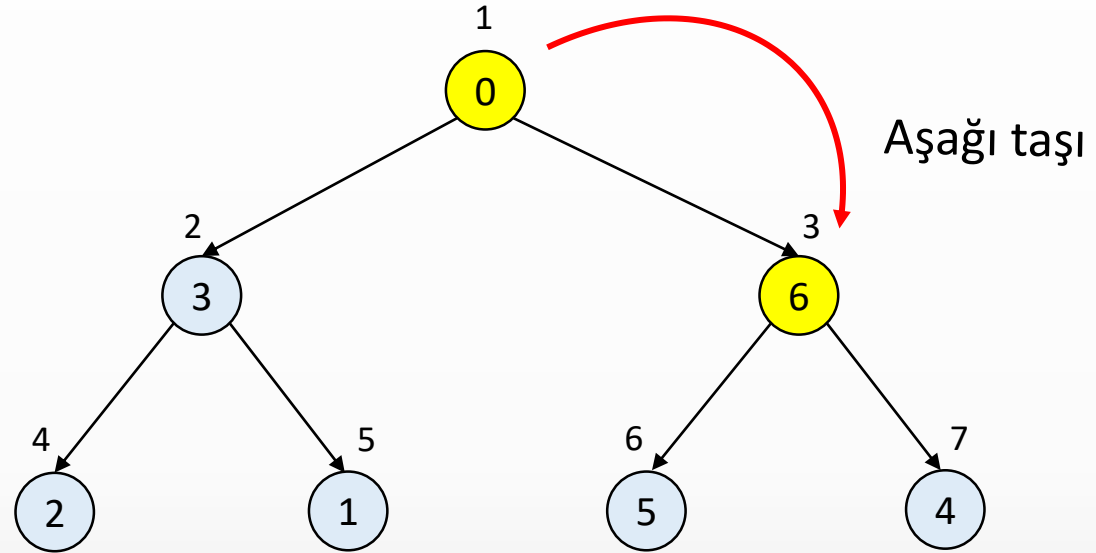
silMax()



max = 9



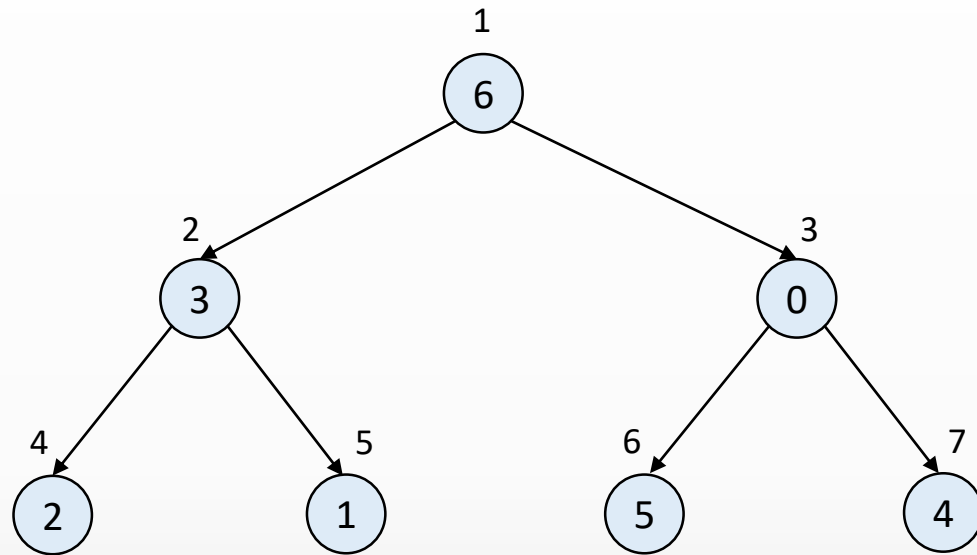
silMax()



max = 9



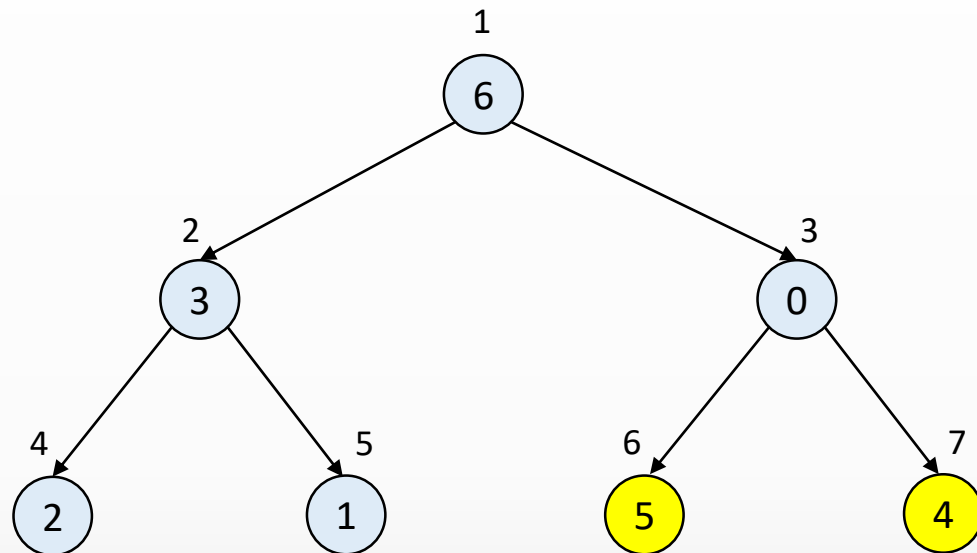
silMax()



max = 9



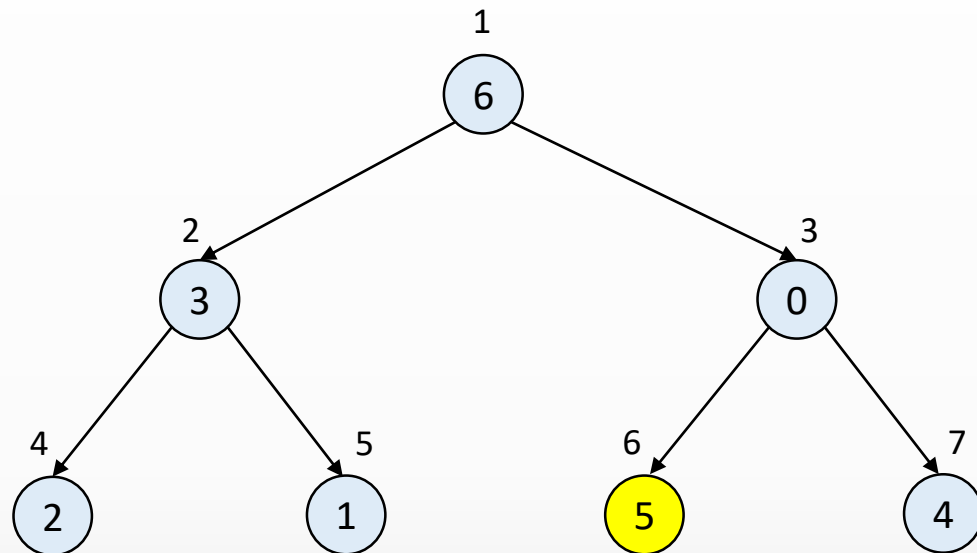
silMax()



max = 9



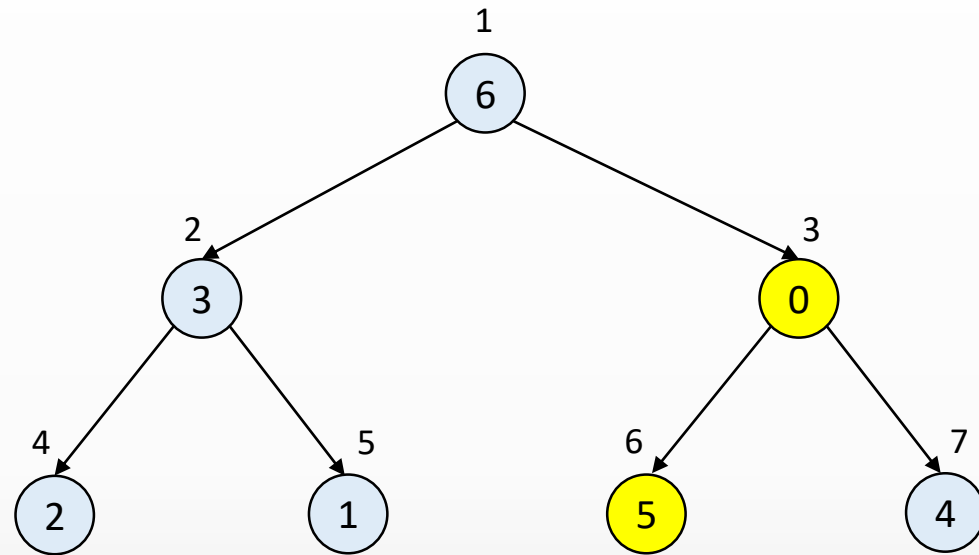
silMax()



max = 9



silMax()

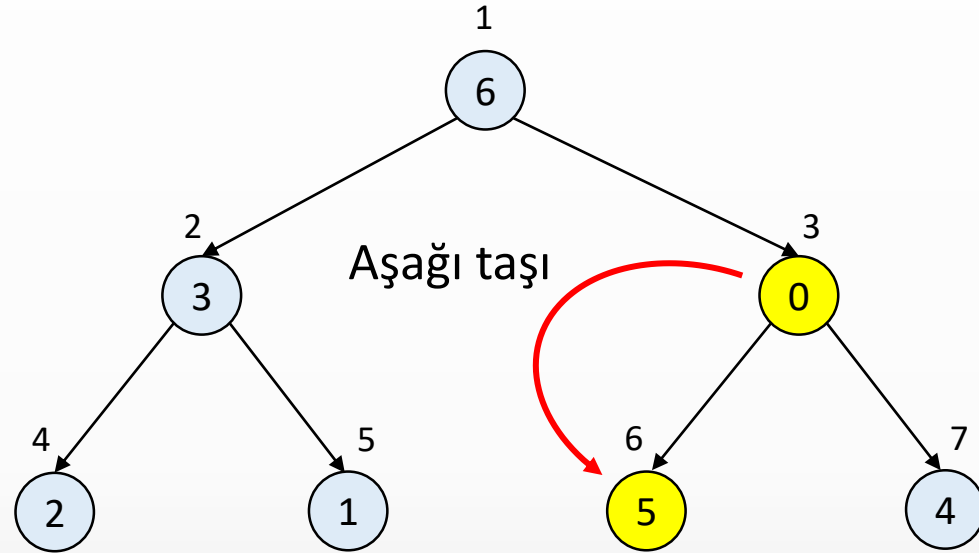


max = 9

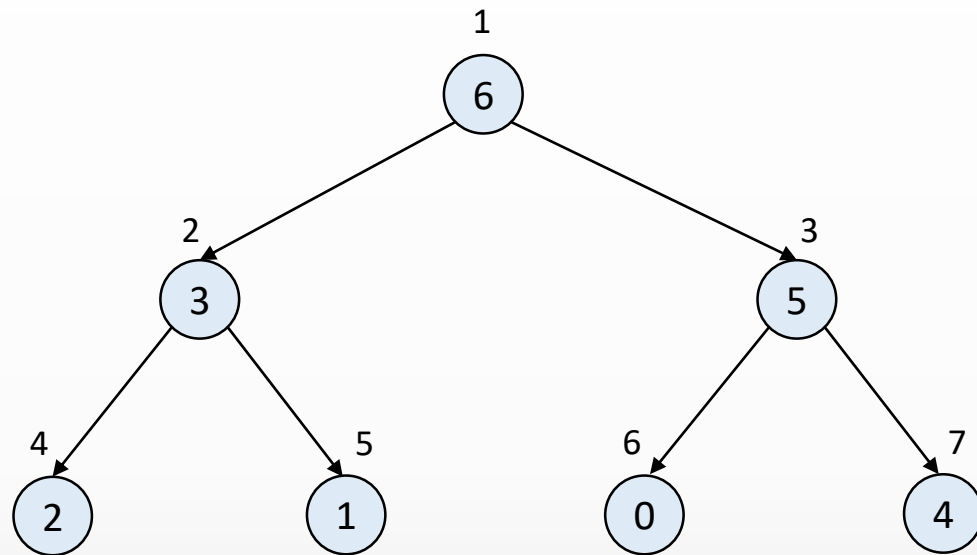


silMax()

max = 9



silMax()



max = 9







# Max Heap Ağacında En Büyük Elemanı Silme



	9	3	6	2	1	5	4	null
0	1	2	3	4	5	6	7	8

heap[]

```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



	9	3	6	2	1	5	4	null
0	1	2	3	4	5	6	7	8

heap[]

n  
↓

n = 7

```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



	9	3	6	2	1	5	4	null
0	1	2	3	4	5	6	7	8

heap[]

n = 7

silMax()

```
public int silMax() {
    int max = heap[1];
    yerDegistir(1,n);
    n--;
    batir(1);
    heap[n + 1] = null;
    if(n > 0 && (n == (heap.length - 1) / 4)) {
        kucult(heap.length / 2);
    }
    return max;
}

public void yerDegistir(int a, int b) {
    int gecici = heap[a];
    heap[a] = heap[b];
    heap[b] = gecici;
}
```



							n ↓	
	9	3	6	2	1	5	4	null
0	1	2	3	4	5	6	7	8

heap[]

n = 7

silMax()

```
→ public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



							n ↓	
	9	3	6	2	1	5	4	null
0	1	2	3	4	5	6	7	8

heap[]

max = 9

n = 7

silMax()



```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



							n ↓	
	9	3	6	2	1	5	4	null
0	1	2	3	4	5	6	7	8

heap[]

max = 9

n = 7

silMax()



```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



	9	3	6	2	1	5	4	null
0	1	2	3	4	5	6	7	8

heap[]

max = 9

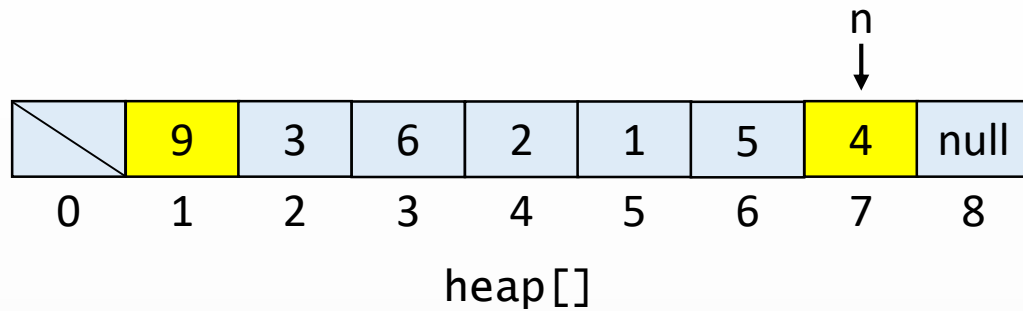
n = 7

silMax()

```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}
```

```
→ public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```





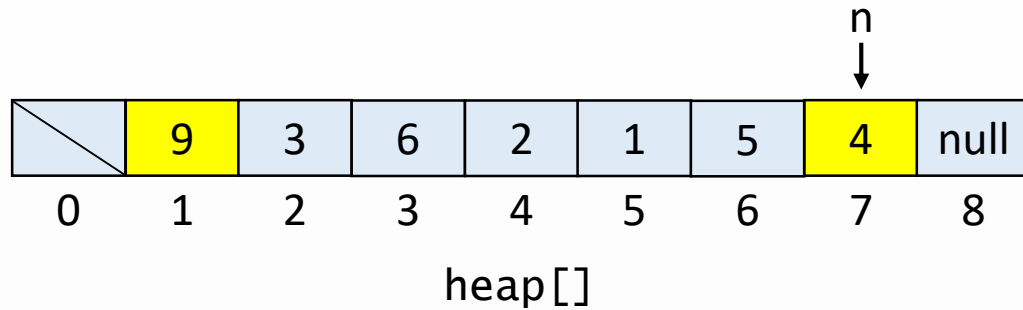
b = 7  
a = 1  
max = 9  
n = 7

silMax()

```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}
```

→ 

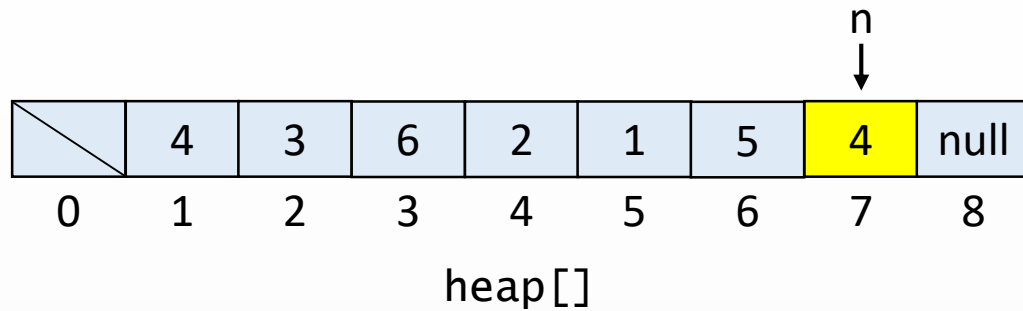
```
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



```
gecici = 9  
b = 7  
a = 1  
max = 9  
n = 7
```

```
silMax()
```

```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



```
gecici = 9  
b = 7  
a = 1  
max = 9  
n = 7
```

```
silMax()
```

```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



	4	3	6	2	1	5	9	null
0	1	2	3	4	5	6	7	8

heap[]

```
gecici = 9
b = 7
a = 1
max = 9
n = 7
```

silMax()

```
public int silMax() {
    int max = heap[1];
    yerDegistir(1,n);
    n--;
    batir(1);
    heap[n + 1] = null;
    if(n > 0 && (n == (heap.length - 1) / 4)) {
        kucult(heap.length / 2);
    }
    return max;
}

public void yerDegistir(int a, int b) {
    int gecici = heap[a];
    heap[a] = heap[b];
    heap[b] = gecici;
}
```



	4	3	6	2	1	5	9	null
0	1	2	3	4	5	6	7	8

heap[]

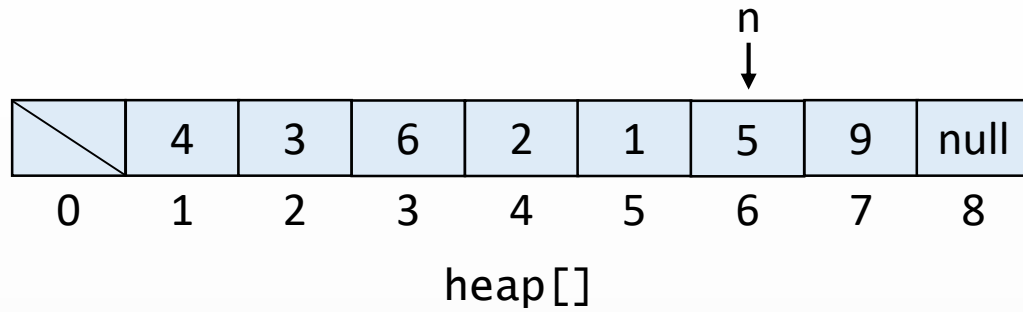
max = 9

n = 7

silMax()



```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



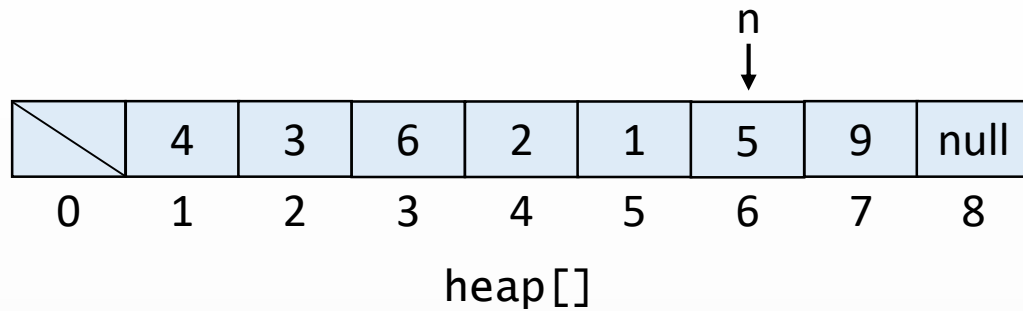
max = 9

n = 6

silMax()



```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



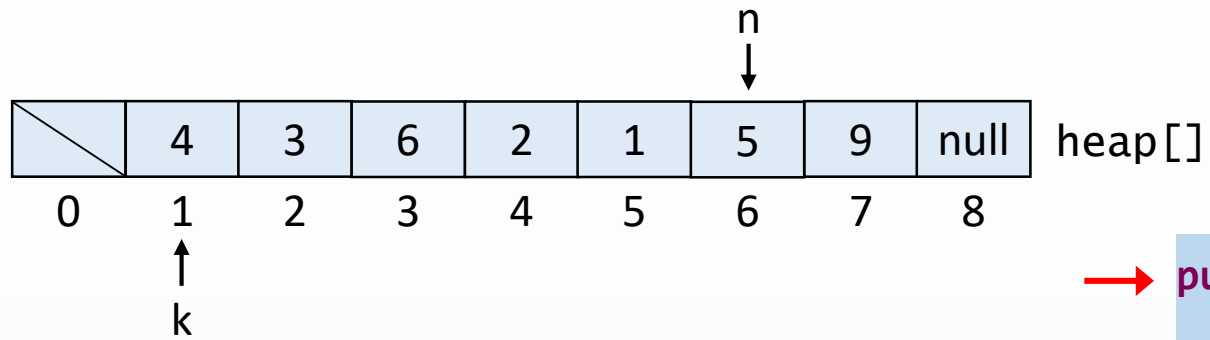
max = 9

n = 6

silMax()



```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```

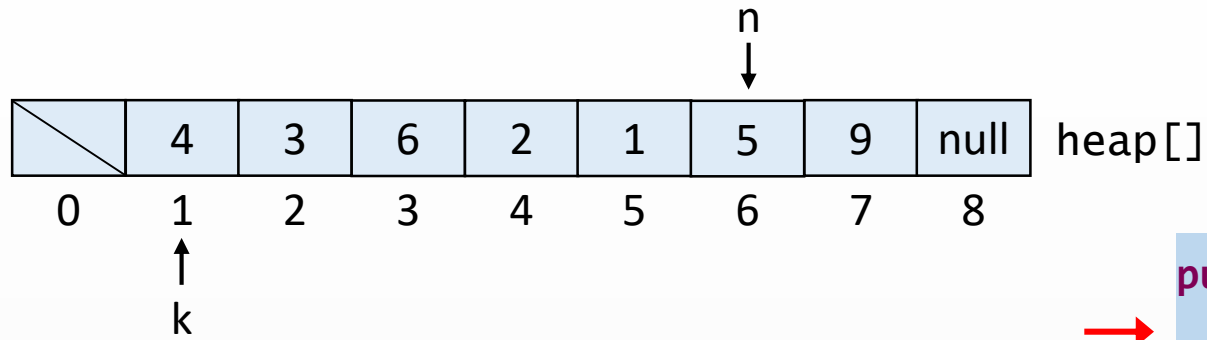


$k = 1$   
 $\text{max} = 9$   
 $n = 6$

silMax()

```
→ public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```





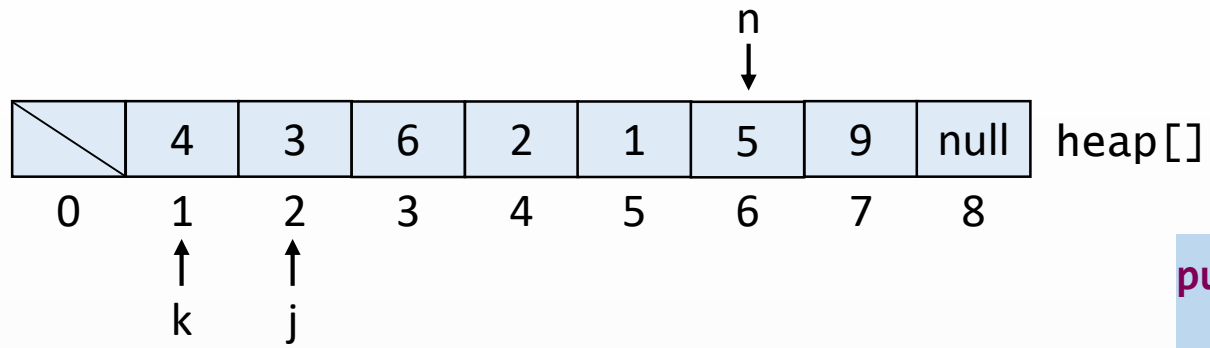
$k = 1$   
 $\text{max} = 9$   
 $n = 6$

`silMax()`



```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}
```

```
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```

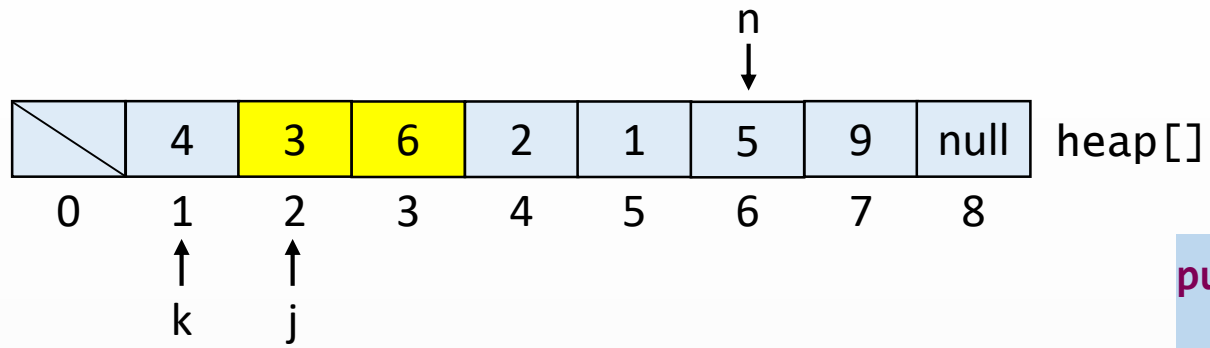


j = 2  
k = 1  
max = 9  
n = 6

silMax()



```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



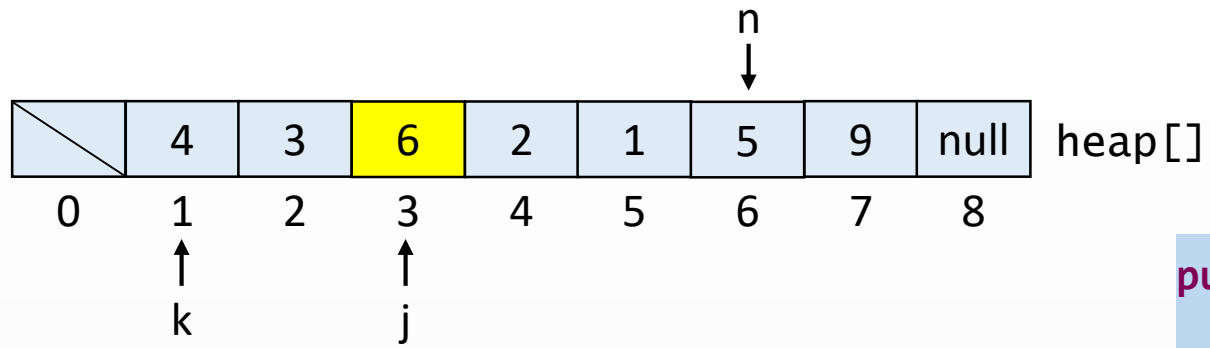
`j = 2`  
`k = 1`  
`max = 9`  
`n = 6`

`silMax()`



```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}
```

```
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



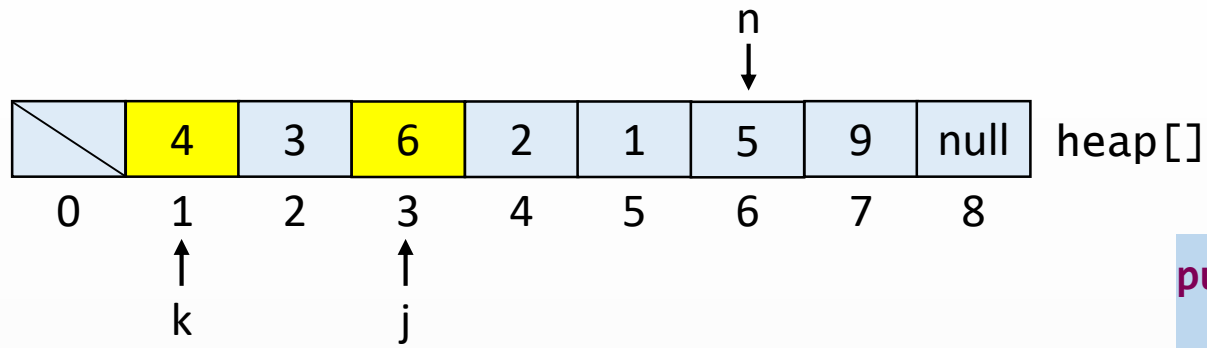
`j = 3`  
`k = 1`  
`max = 9`  
`n = 6`

`silMax()`



```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}
```

```
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



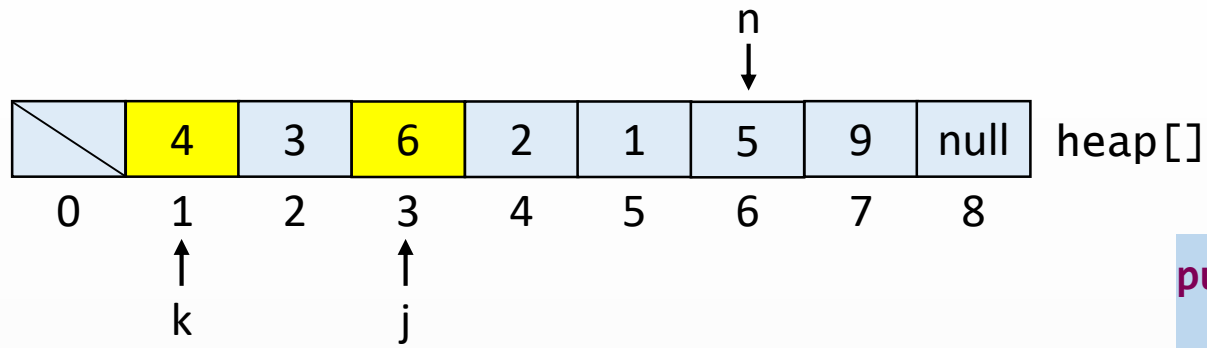
`j = 3`  
`k = 1`  
`max = 9`  
`n = 6`

`silMax()`



```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}
```

```
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```

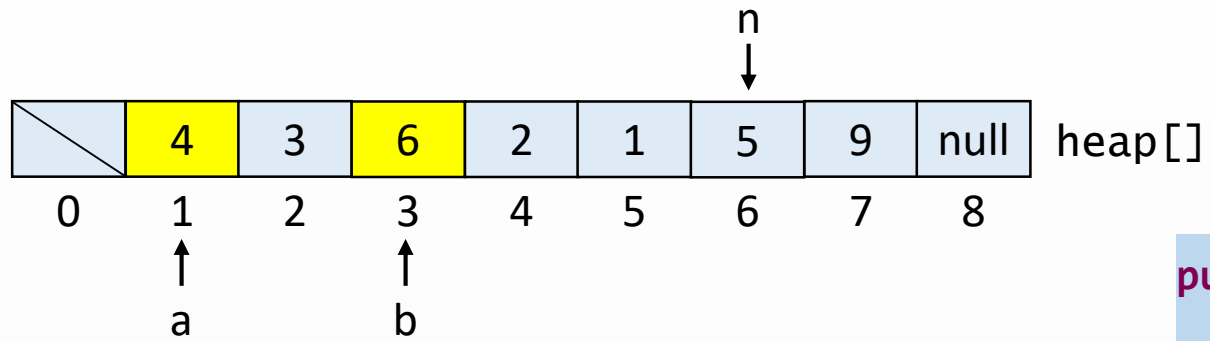


$j = 3$   
 $k = 1$   
 $\text{max} = 9$   
 $n = 6$

silMax()



```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```

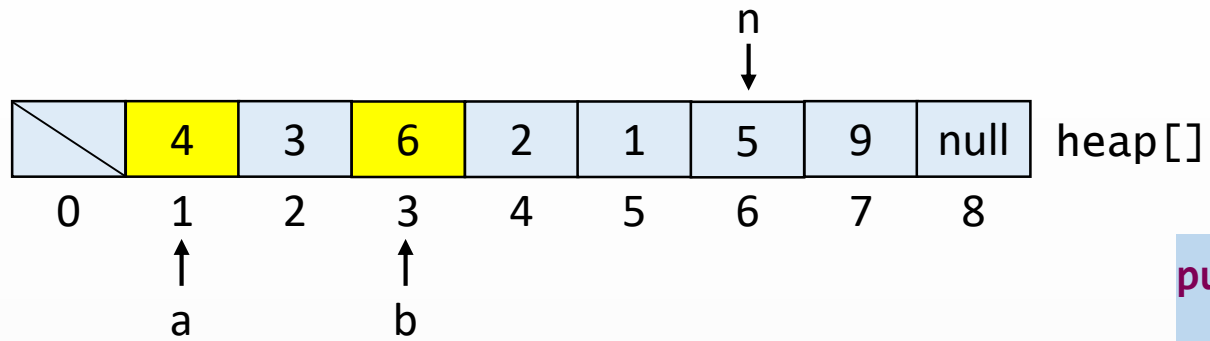


b = 3  
a = 1  
j = 3  
k = 1  
max = 9  
n = 6

silMax()

```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}
```

```
→ public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



gecici = 4  
b = 3  
a = 1  
j = 3  
k = 1  
max = 9  
n = 6

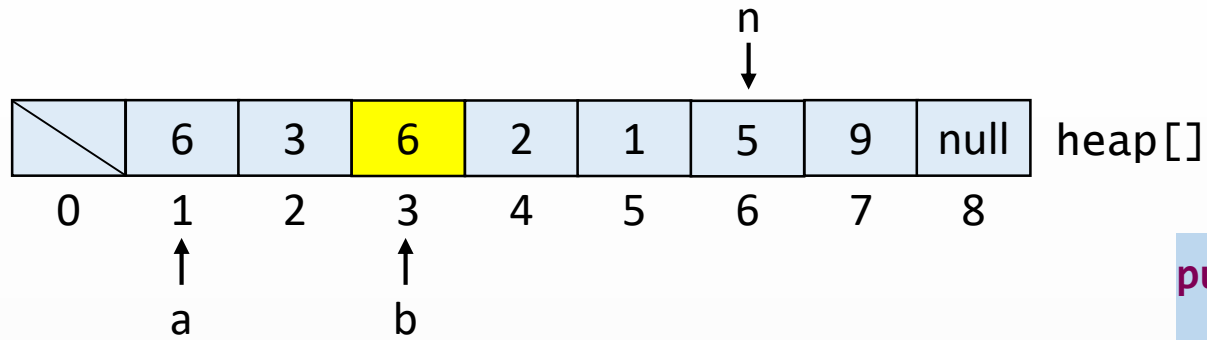
silMax()

```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}
```



```
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```





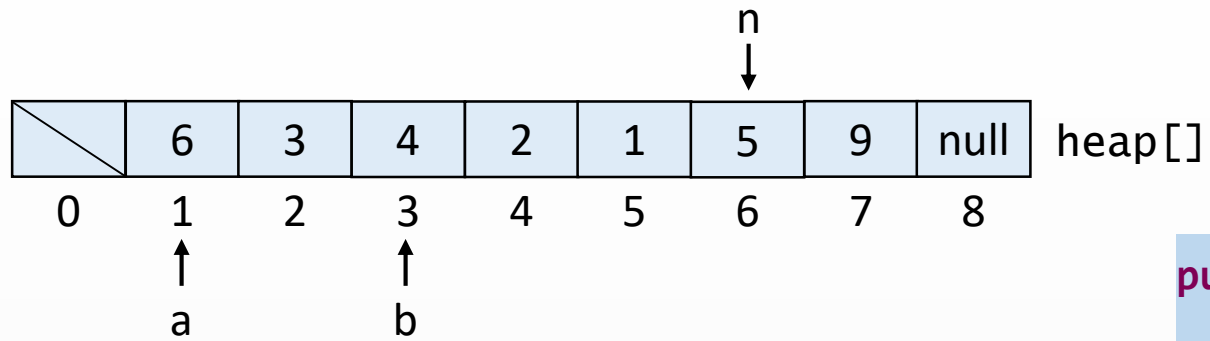
gecici = 4  
b = 3  
a = 1  
j = 3  
k = 1  
max = 9  
n = 6

silMax()

```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}
```

```
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```





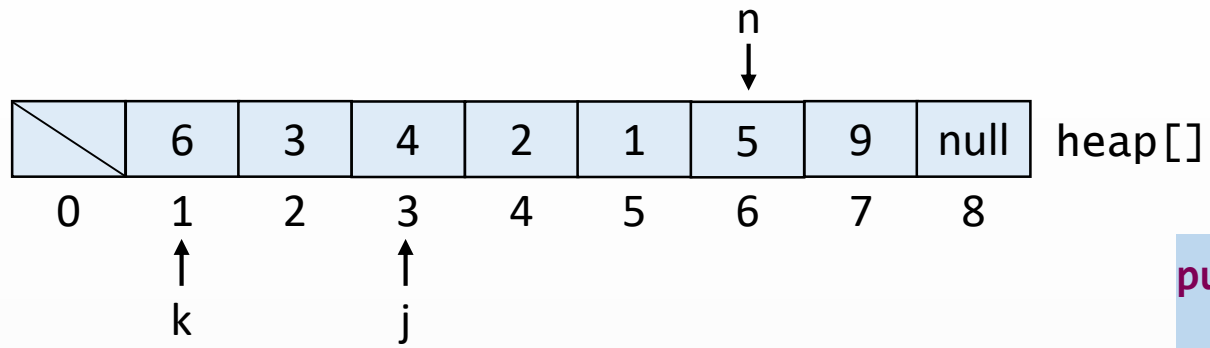
gecici = 4  
b = 3  
a = 1  
j = 3  
k = 1  
max = 9  
n = 6

silMax()

```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}
```

```
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



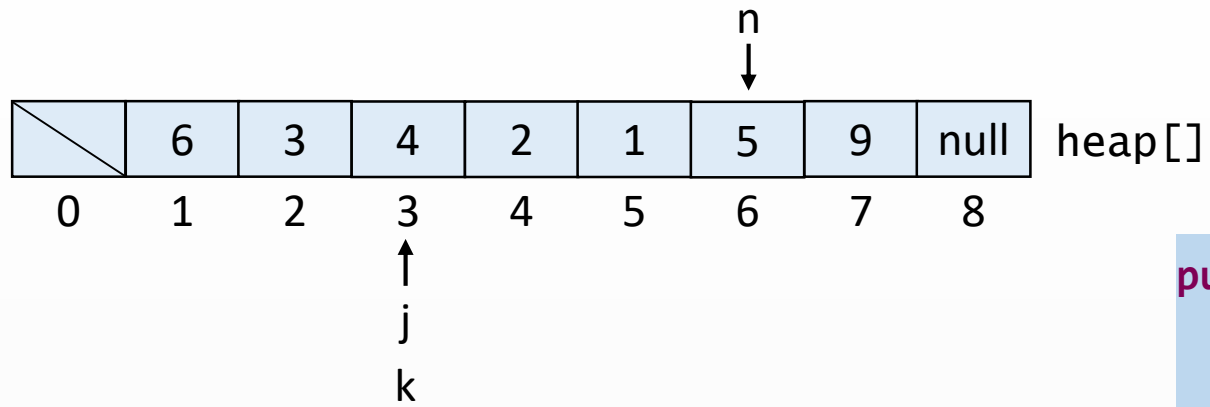


j = 3  
k = 1  
max = 9  
n = 6

silMax()



```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```

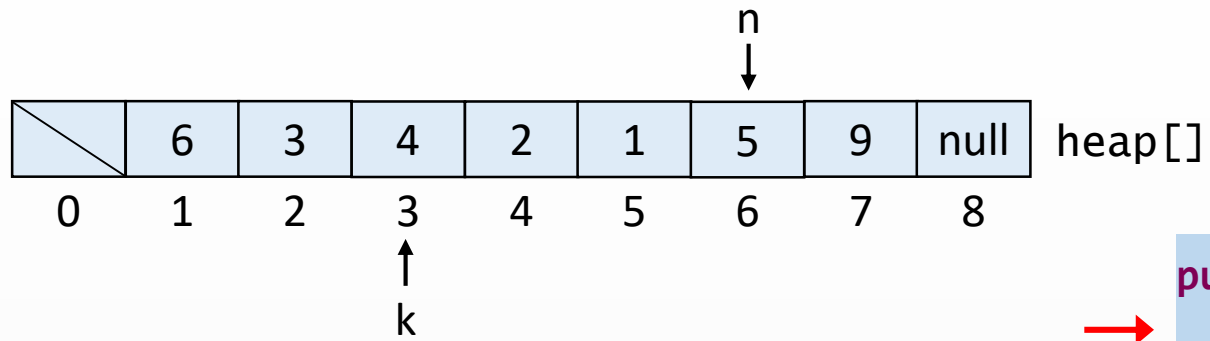


$j = 3$   
 $k = 3$   
 $\text{max} = 9$   
 $n = 6$

silMax()



```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```

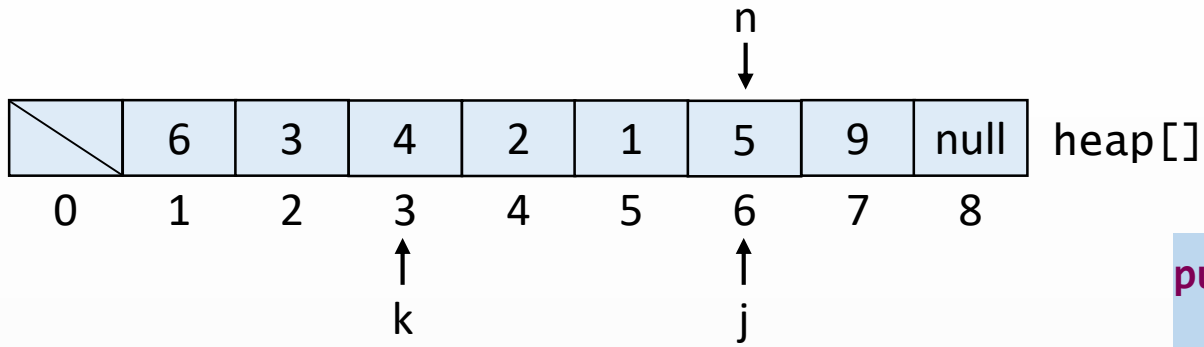


$k = 3$   
 $\text{max} = 9$   
 $n = 6$

`silMax()`



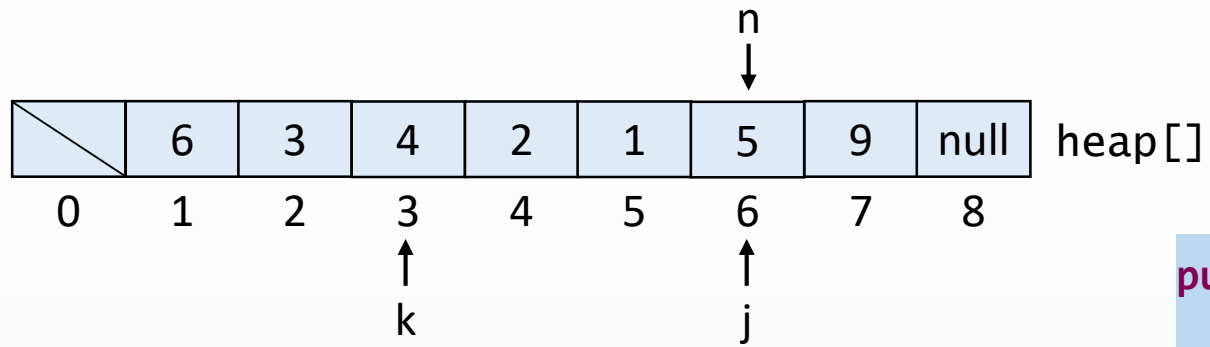
```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



## silMax()

```
public void batir(int k) {
    while(2*k <= n) {
        int j = 2*k;
        if(j < n && heap[j] < heap[j+1]) {
            j++;
        }
        if(heap[k] >= heap[j]) {
            break;
        }
        yerDegistir(k, j);
        k = j;
    }
}

public void yerDegistir(int a, int b) {
    int gecici = heap[a];
    heap[a] = heap[b];
    heap[b] = gecici;
}
```



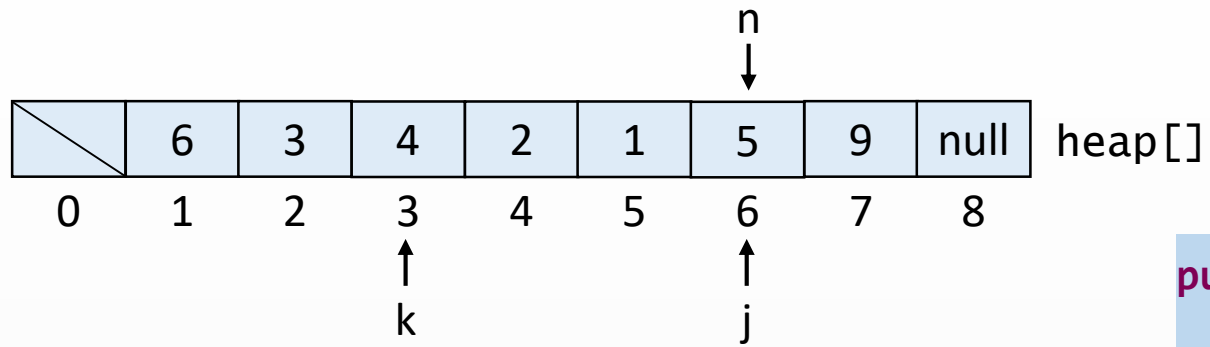
$j = 6$   
 $k = 3$   
 $\text{max} = 9$   
 $n = 6$

silMax()



```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}
```

```
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



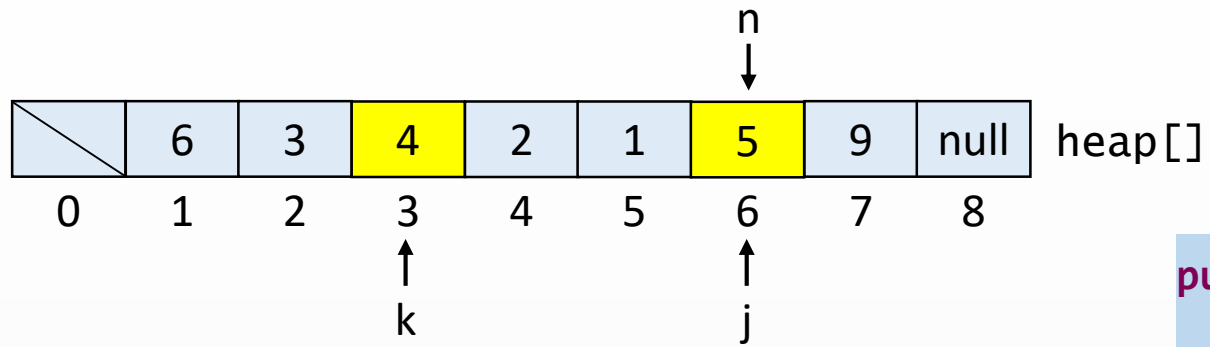
j = 6  
k = 3  
max = 9  
n = 6

silMax()



```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```





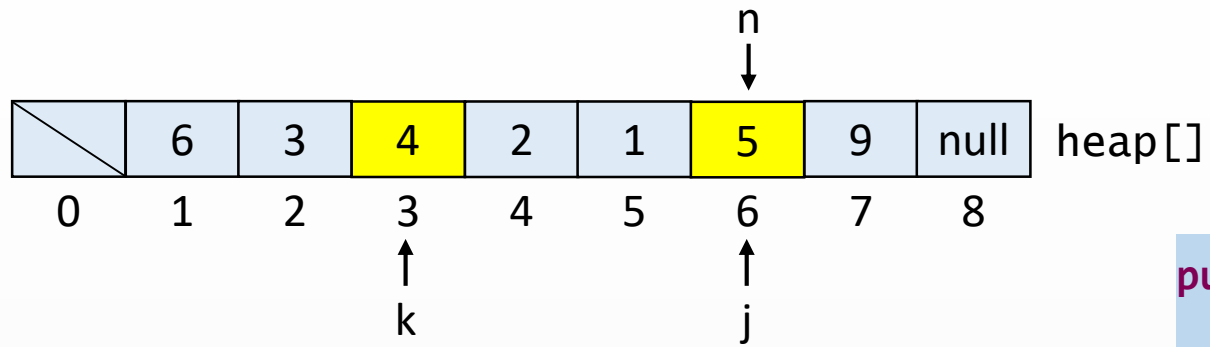
`j = 6`  
`k = 3`  
`max = 9`  
`n = 6`

`silMax()`



```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}
```

```
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```

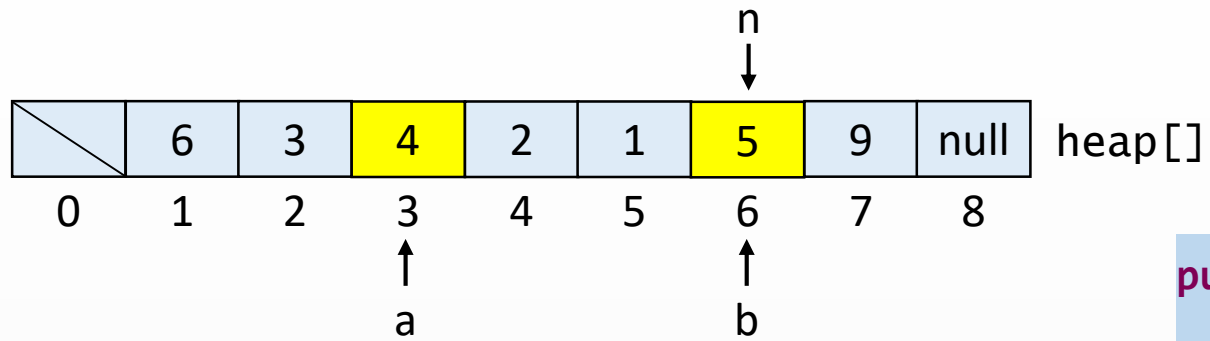


j = 6  
k = 3  
max = 9  
n = 6

silMax()



```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```

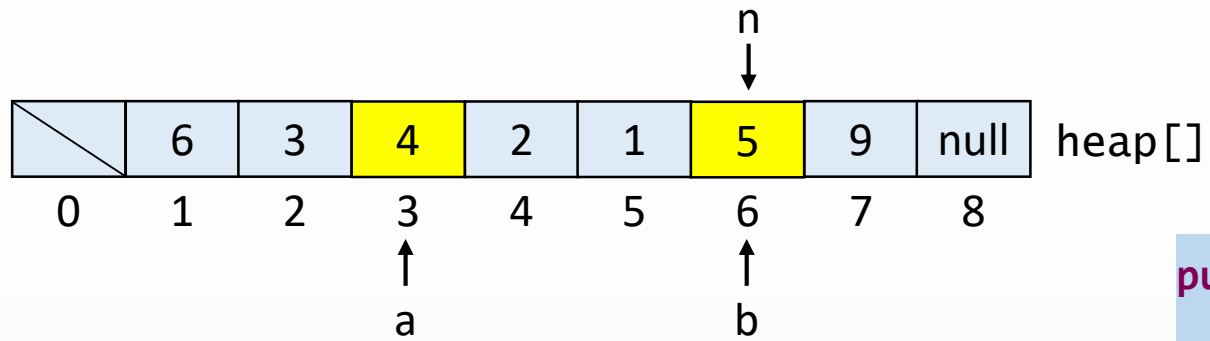


`b = 5`  
`a = 4`  
`j = 6`  
`k = 3`  
`max = 9`  
`n = 6`

`silMax()`

```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}
```

```
→ public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



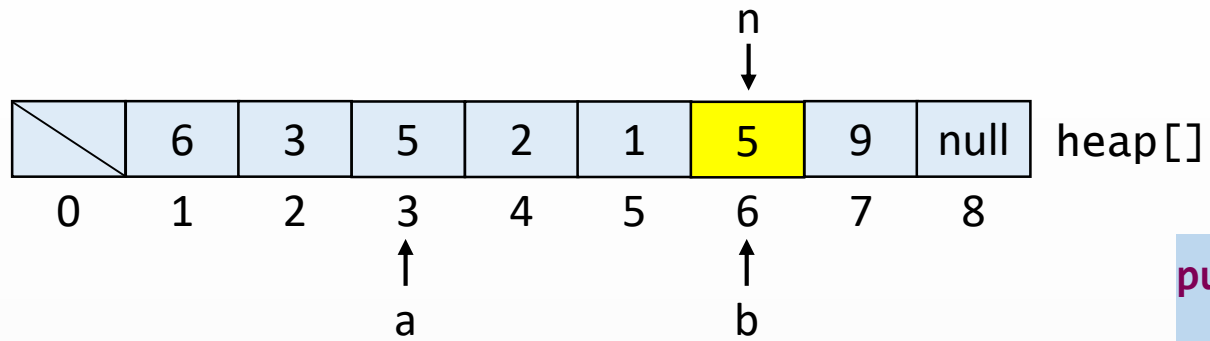
gecici = 4  
b = 5  
a = 4  
j = 6  
k = 3  
max = 9  
n = 6

silMax()

```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}
```

→

```
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



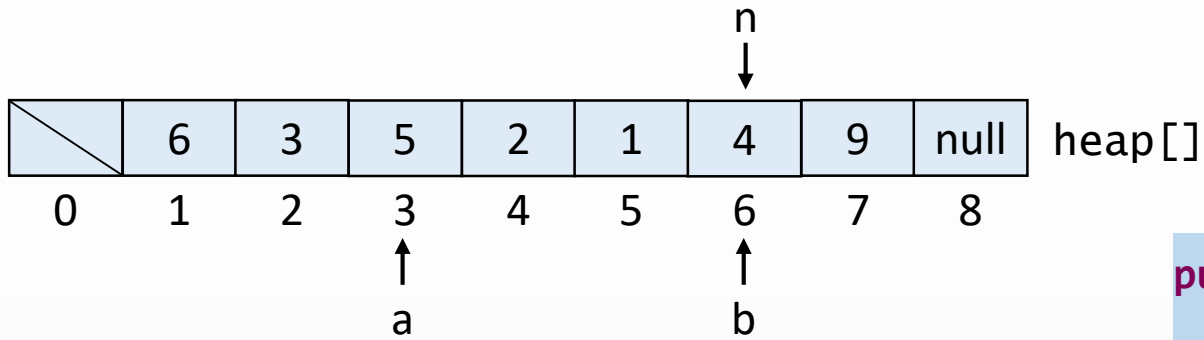
gecici = 4  
b = 5  
a = 4  
j = 6  
k = 3  
max = 9  
n = 6

silMax()

```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}
```

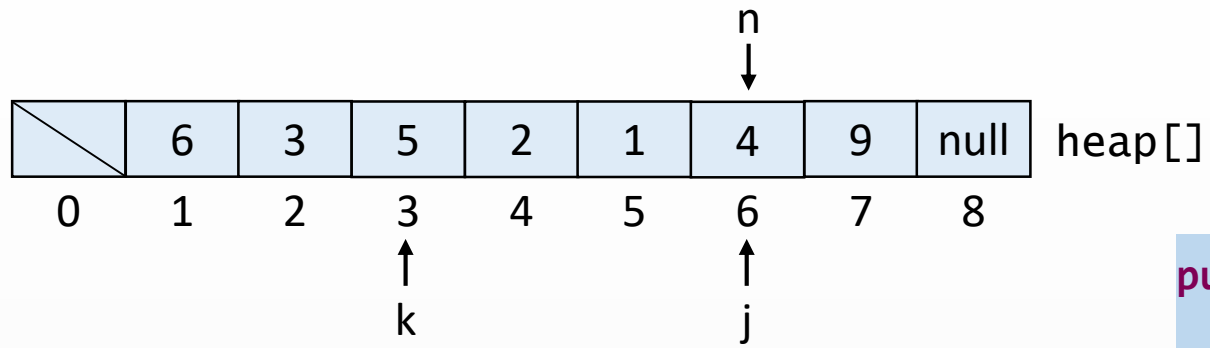
```
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```





## silMax()

```
public void yerDegistir(int a, int b) {
    int gecici = heap[a];
    heap[a] = heap[b];
    heap[b] = gecici;
}
```

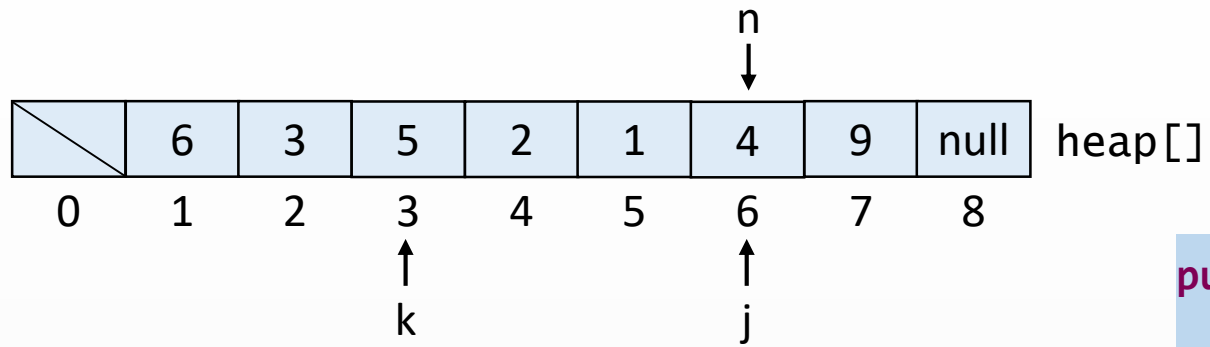


j = 6  
k = 3  
max = 9  
n = 6

silMax()



```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



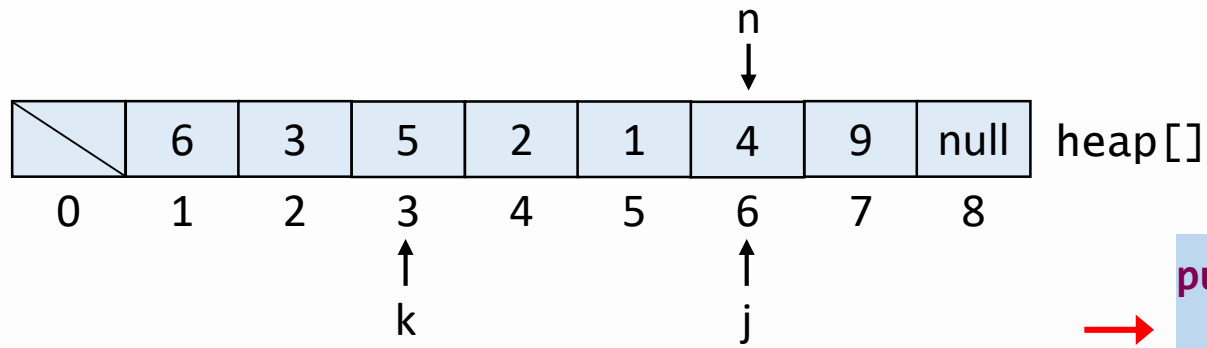
$j = 6$   
 $k = 6$   
 $\text{max} = 9$   
 $n = 6$

silMax()

```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}
```

```
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```





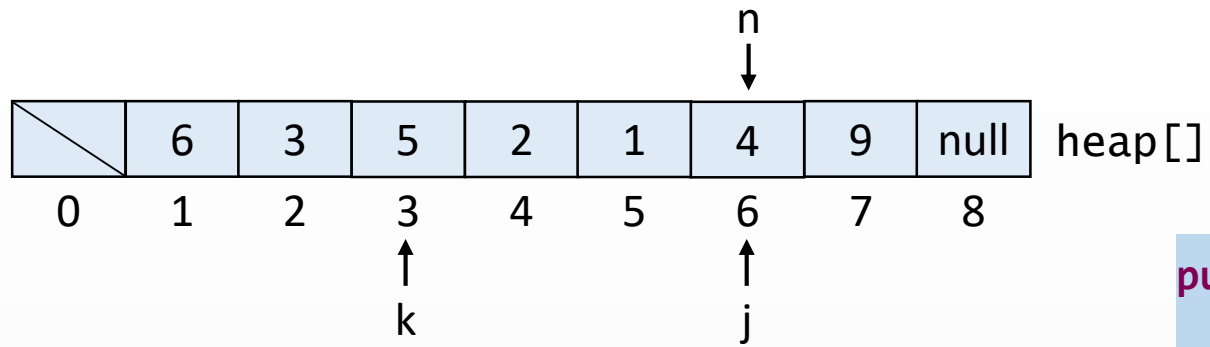
`j = 6`  
`k = 6`  
`max = 9`  
`n = 6`

`silMax()`



```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}
```

```
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```

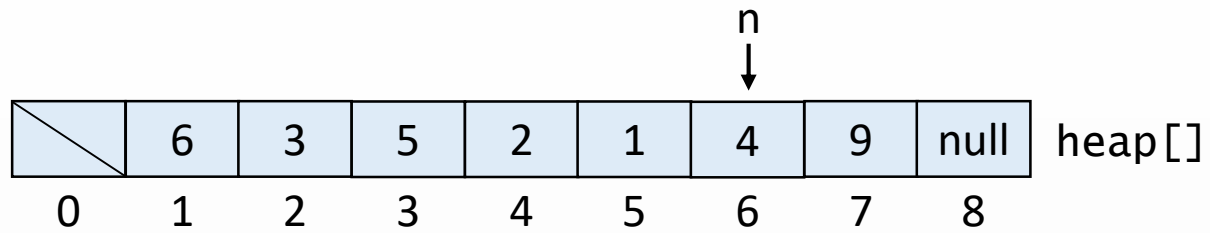


`j = 6`  
`k = 6`  
`max = 9`  
`n = 6`

`silMax()`

```
public void batir(int k) {  
    while(2*k <= n) {  
        int j = 2*k;  
        if(j < n && heap[j] < heap[j+1]) {  
            j++;  
        }  
        if(heap[k] >= heap[j]) {  
            break;  
        }  
        yerDegistir(k, j);  
        k = j;  
    }  
}
```

```
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



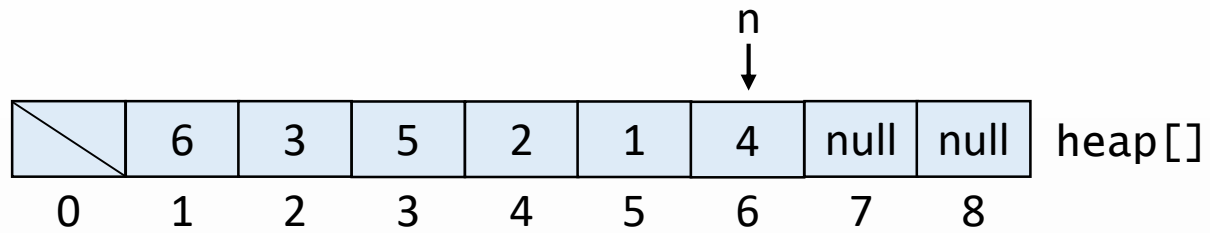
`max = 9`

`n = 6`

`silMax()`



```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



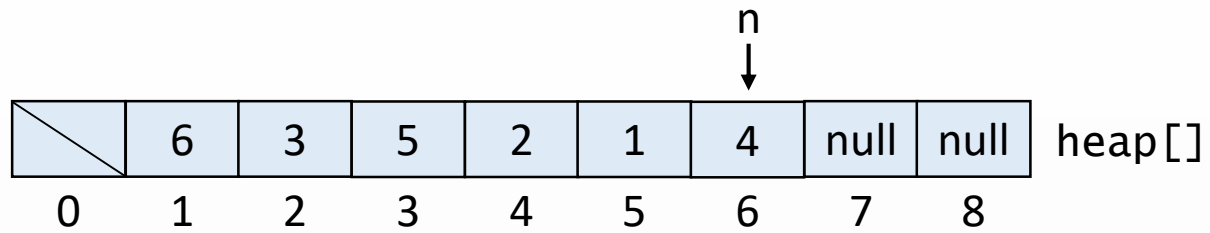
max = 9

n = 6

silMax()



```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



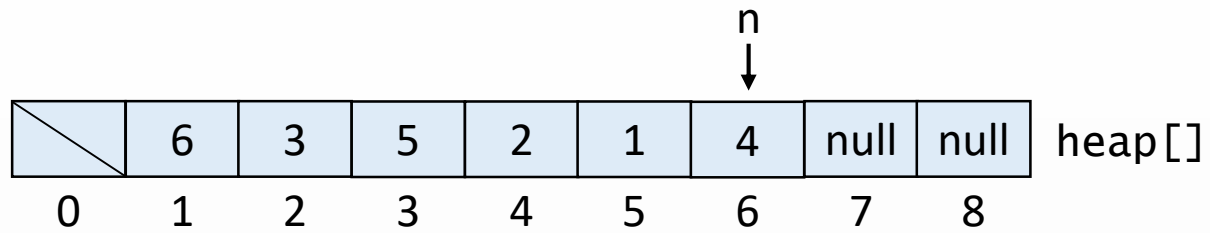
`max = 9`

`n = 6`

`silMax()`



```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```

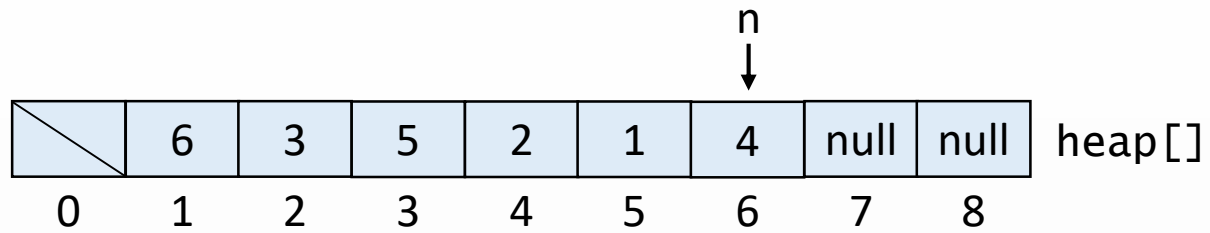


`max = 9`

`n = 6`

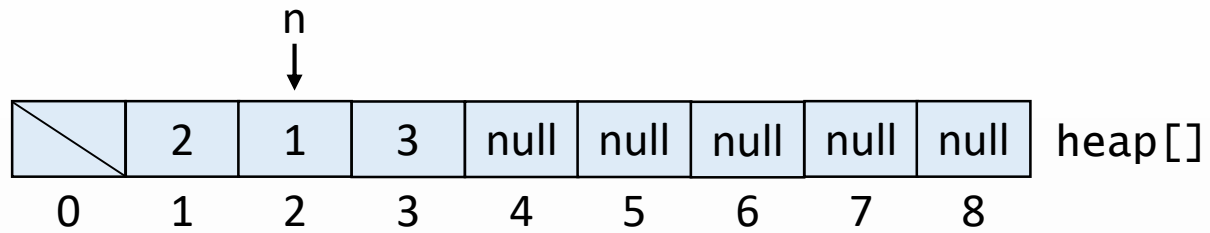
`silMax()`

```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



`n = 6`

```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```

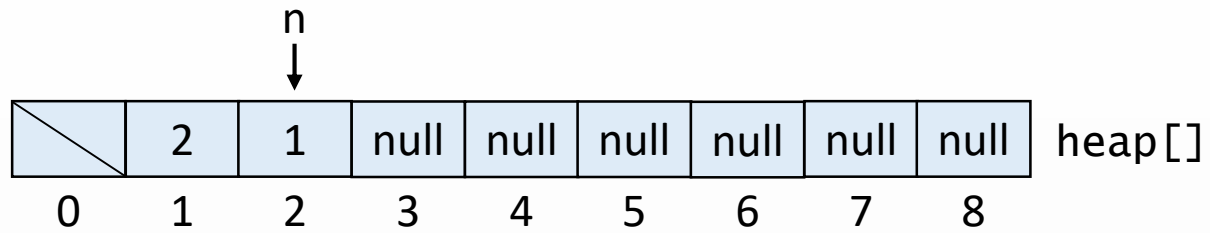


max = 3  
n = 2



```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



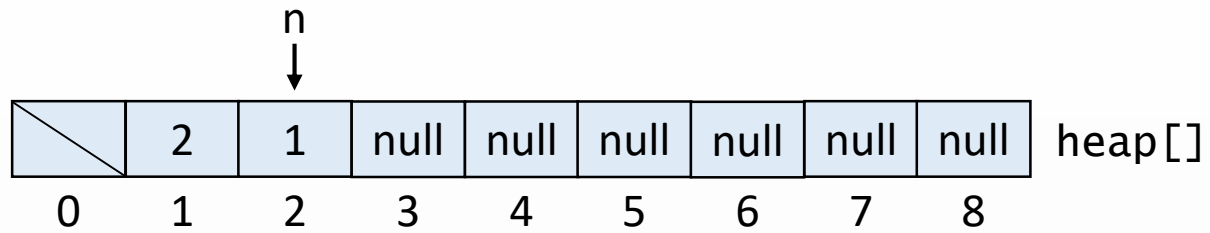


`max = 3`

`n = 2`



```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```

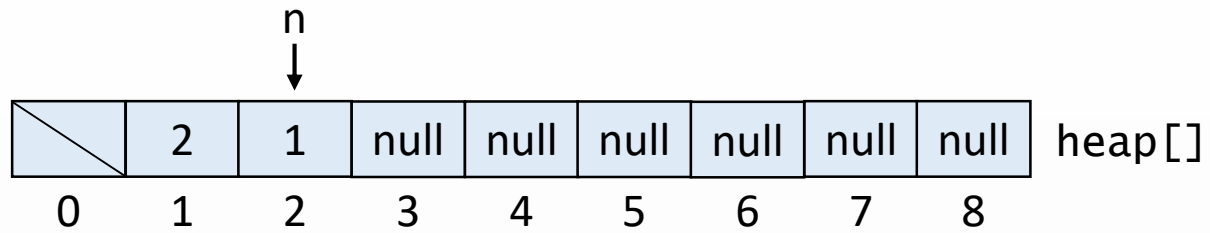


`max = 3`

`n = 2`



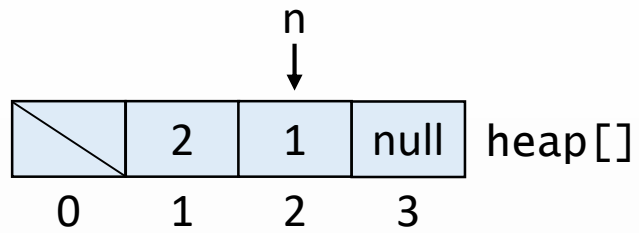
```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



`max = 3`  
`n = 2`



```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```

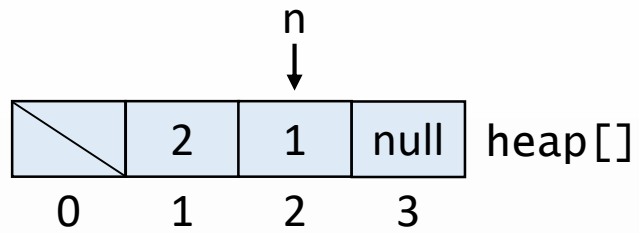


max = 3

n = 2



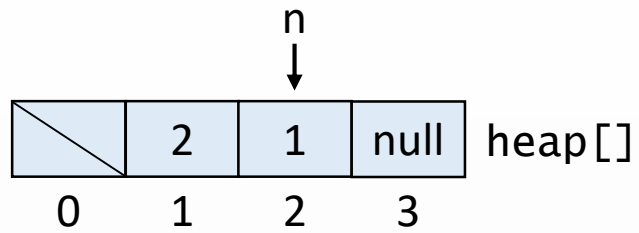
```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



max = 3

n = 2

```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```



n = 2

```
public int silMax() {  
    int max = heap[1];  
    yerDegistir(1,n);  
    n--;  
    batir(1);  
    heap[n + 1] = null;  
    if(n > 0 && (n == (heap.length - 1) / 4)) {  
        kucult(heap.length / 2);  
    }  
    return max;  
}  
  
public void yerDegistir(int a, int b) {  
    int gecici = heap[a];  
    heap[a] = heap[b];  
    heap[b] = gecici;  
}
```





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