

Calculus II: Project 1

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Problem 1

Choose a profile picture, which can be scanned from a drawing or desinged entirely on a computer. Each drawing must be unique and must be approved before proceeding to continue the project. The drawing must have an axis of symmetry. The design must be such that an application of Simpson's rule can be used to approximate the several integrals. Pixelated desings are also possible. The boundary must be a simple closed curve with (no holes, no self-crossing).

Solution

We chose an figure that when revolved, results in an innovative approach to lifesavers, as it provides a conforable space for placing one's arms and safely placing items that may be useful to one's survival. Our basic design is the following:

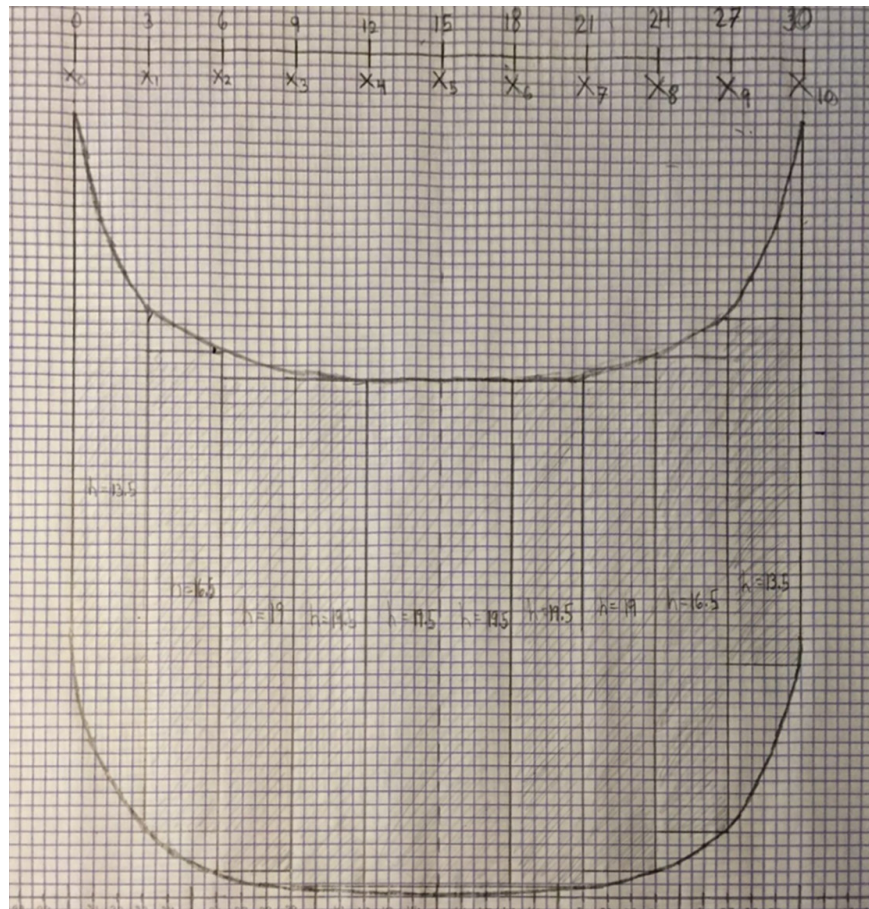


Figure 1: Cross section design

Problem 2

Choose a particular scale, origin and coordinate axes for your drawing.

Solution Our coordinate axis is the following:

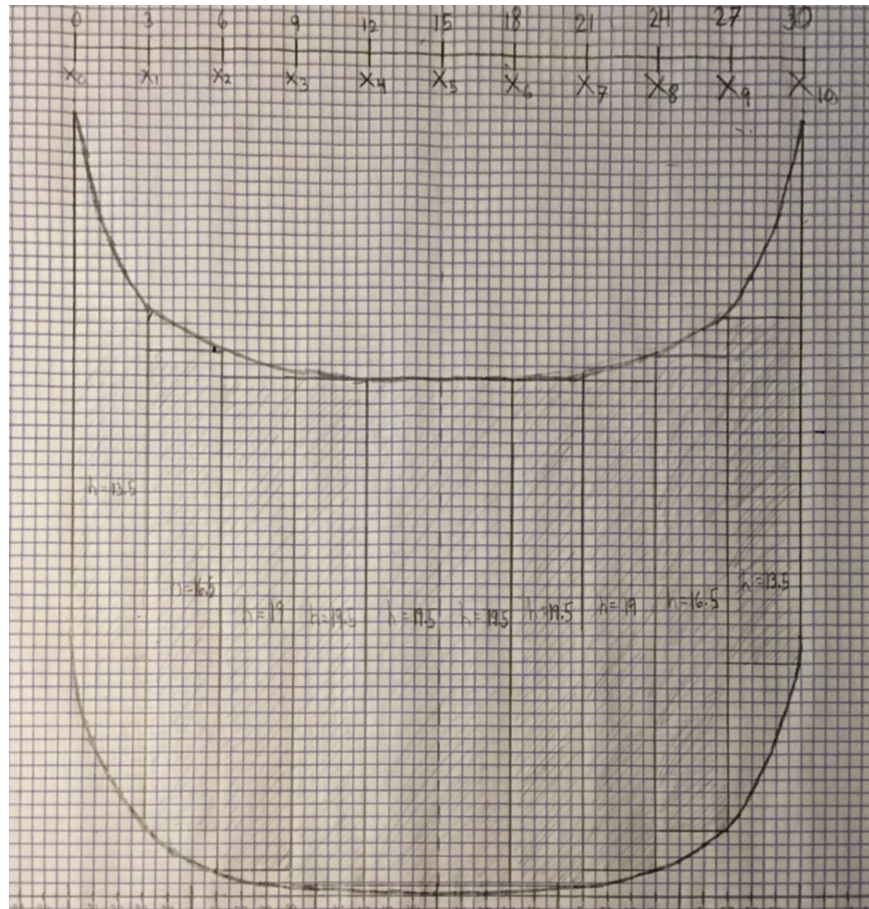


Figure 2: Cross section with axis

Problem 3

Numerically, and an approximation to the area of your drawing using Simpson's rule and the Trapezoidal rule. If your drawing allows it, and an exact answer also.

Solution First we present the samples and their respective heights:

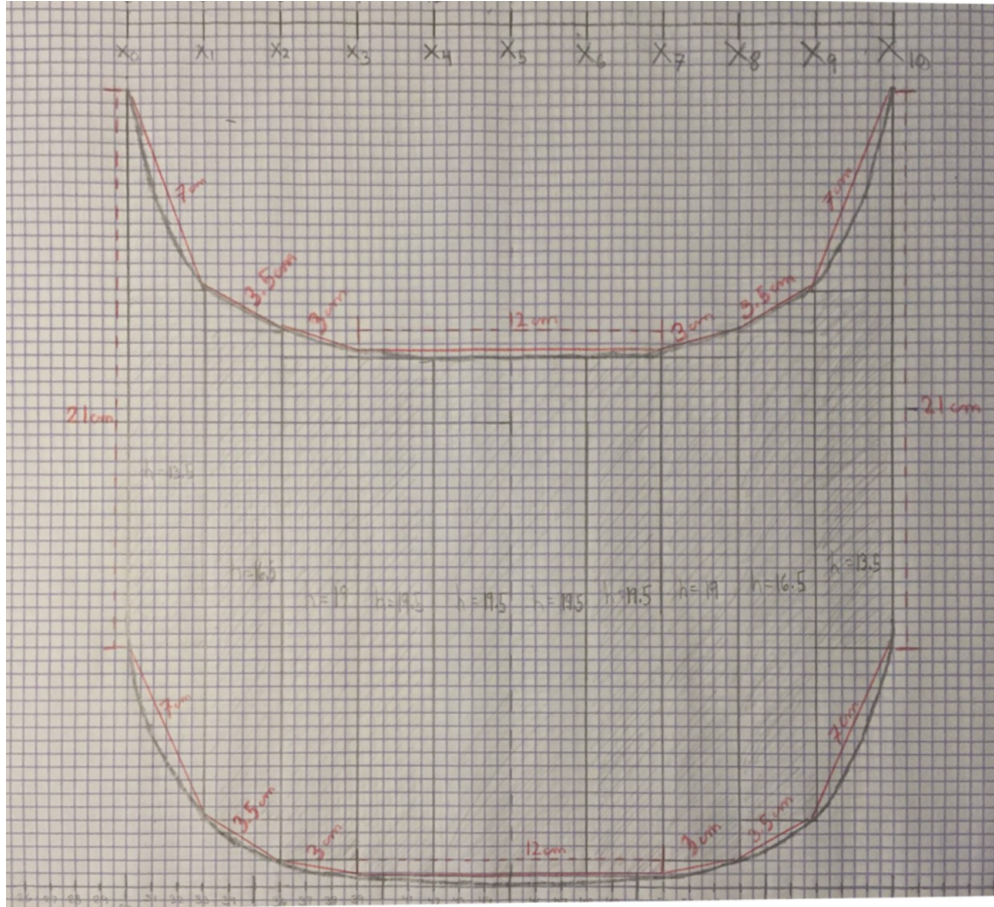


Figure 3: Cross section with measurements

Trapezoidal rule

Simpon's method By definition, we know that Simpon's method has the following form:

$$S_n = \frac{3}{h} [f(x_0) + 4f(x_1) + 2f(x_2) + 4f(x_3) + \cdots + 4f(x_{n-3}) + 2f(x_{n-2}) + 4f(x_{n-1}) + f(x_n)] \quad (1)$$

Problem 4

Numerically, and an approximation of the perimeter of your drawing approximating it using straight lines and adding the length.

Solution From 3, we can see that from our 16 measurements, we can approximate the perimeter as the sum:

$$P = 21 + 7 + 3.5 + 3 + 12 + 3 + 3.5 + 7 + 21 + 7 + 3.5 + 3 + 12 + 3 + 3.5 + 7$$

Which gives us a result of: $P \approx 120cm$

Problem 5

Choose an axis parallel to the axis of symmetry of your figure on which you will revolve your figure to produce a life saver with your figure as profile.

Problem 6

Investigate Pappus' Theorem for solids of Revolution, and use it to

- a) Compute the volume of the resulting solid of revolution.
- b) Compute the surface area of the resulting solid of revolution

Problem 7

Investigate Arquimedes' Theorem to And the boyance force of the life saver assuming it is completely submerged in water, and is filled with air.

Problem 8

Using Simpson's rule, and the volume of the solid of revolution without using Pappus' Theorem.

Problem 9

Make a real design of your life saver. You may 3d print it if you wish.