

# Dissecting Idiosyncratic Income Risk

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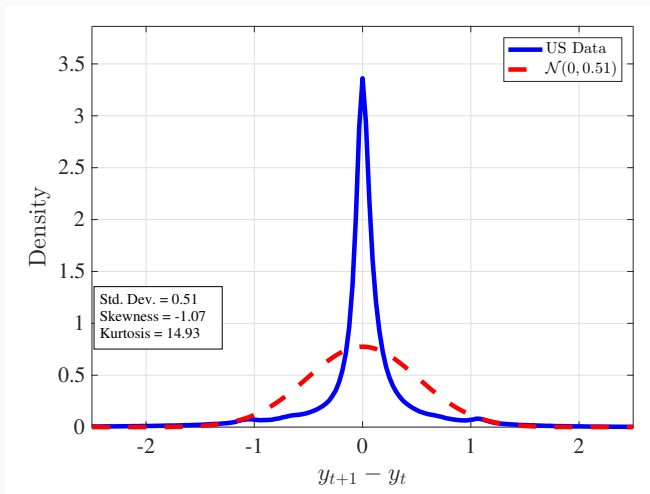
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# Nonlinear/Non-Gaussian Earnings Dynamics

- Sparked interest in income dynamics: Guvenen *et al.* (2014, 2015), Arellano *et al.* (2017) etc.
- Non-Gaussian features of income shocks
  - Left skewness and excess kurtosis

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- Asymmetric/nonlinear mean reversion. Persistence differ by:
  - Current shocks change persistence of past ones (Arellano *et al.* (2017)).
  - positive vs negative changes; low vs high income workers

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- Asymmetric/nonlinear mean reversion. Persistence differ by:
  - Current shocks change persistence of past ones (Arellano *et al.* (2017)).
  - positive vs negative changes; low vs high income workers
- New findings make their way into the quantitative macro literature:
  - McKay (2014), Kaplan *et al.* (2016), Golosov *et al.* (2016), De Nardi *et al.* (2016) and Wang *et al.* (2016)

# Open Questions: Drivers of Non-Gaussian Features

Focus has been on **annual individual labor income** dynamics.

- What's driving skewness/kurtosis of earnings growth?  
**Wages** vs **Hours**?
- Does **hourly wage** dynamics exhibit non-Gaussian/ nonlinear features?
- What are the **real-life events** lead to large swings in earnings?

# Open Questions: Insurance Against Tail Shocks

How much insurance against large earnings losses/gains from spouse and government?

- Do non-Gaussian features extend to household (husband+wife) earnings? After public insurance?
- For some questions nature of household income risk—before and after tax—is key.
- How about consumption growth distribution?

# What Do We Do?

Use the Norwegian registry data to study above questions.

1. Show that patterns for annual earnings risk are remarkably similar to the US.
2. Study the role of wages vs hours in non-Gaussian properties of earnings changes.
  - Decompose earnings changes into hours and hourly wage growth.
  - Do **wage** and **hours** growth display non-Gaussian features?
3. Document the insurance against tail shocks of earnings through spouse's income and public insurance.
  - Distribution of after tax-after transfer household income growth.



# Today

1. Data and Empirical Methodology
2. Earnings Growth Distribution
3. Changes in Hours vs Wages
4. Household Income Dynamics
5. Conclusion

# **Data and Empirical Methodology**

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## **Norwegian Registry Data**

# Norwegian Registry Data

- Administrative data covering the whole Norwegian population.
  - Derived from a combination of administrative registers such as annual tax records and employment register
- High quality because
  - Third-party reported: employers, banks, brokers, etc.
  - No attrition (unless someone emigrates).
- Family identifiers from the population register.
  - includes cohabitant couples.

# Norwegian Registry Data: Base Sample

- Panel data between 1998 and 2014.
  - Income data goes back to 1993 but not hours.
- Today we focus on males.
  - We do the same analysis with women.
- We use ~20M year/individual observations in our analysis
- **Labor Earnings** for wage and salary workers including bonuses and other remunerations.
  - Business income for self-employed workers: no hours data.
- Deflate all values with the 2000 CPI.

# **Data and Empirical Methodology**

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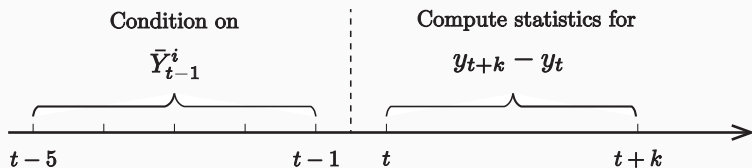
## **Methodology**

# Sample Selection

- Revolving panel of 25-60 year olds between 2003-2014.
- In year  $t$  select individuals participating in the labor market:
  - $Y_s^i > Y_s^{min}$  in  $t - 1$  and for 2 more years between  $t - 2$  and  $t - 5$ .
  - $Y_t^{min}$  is 5% of median earnings; approximately one quarter of full-time work at the half of the minimum wage.
- For every worker, compute recent wage earnings between  $t - 1$  and  $t - 5$ ,  $\bar{Y}_{t-1}^i \equiv (\frac{1}{5}) \sum_{s=t-5}^{t-1} \left( \frac{Y_s^i}{d_{h_{i,s}}} \right)$ .
  - $Y_s^i$  : Total earnings in year  $s$ .
  - $d_{h_{i,s}}$  : Average earnings in age  $h_{i,s}$ .

# A Graphical Construct

- Divide the population into 3 age groups in  $t - 1$ : 25–34, 35–44,..., 45–54.
- Within each age group rank individuals according to  $\bar{Y}_{t-1}$  into 10 RE deciles.
- Within each age group, against each quantile of  $\bar{Y}_{t-1}$  on the x-axis:
  - plot conditional distribution  $\mathbb{F}(y_{t+k} - y_t | \bar{Y}_{t-1})$  on the y-axis,  $k = 1, 5$ .



# Earnings Growth Distribution

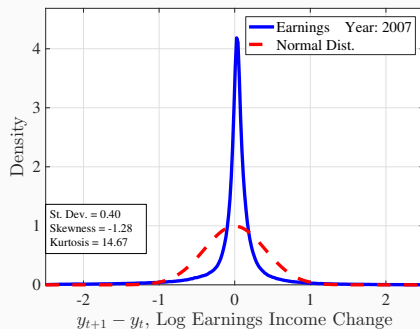
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Norway vs US

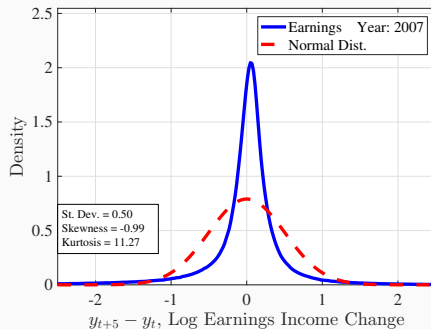


# Histogram of $y_{t+k} - y_t$

## 1-Year Growth



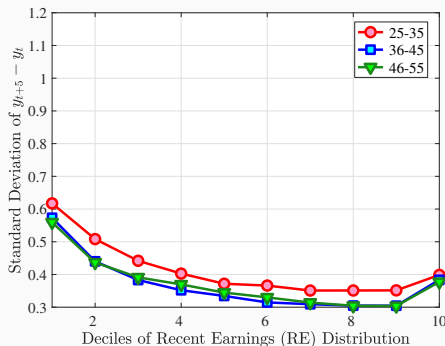
## 5-Year Growth



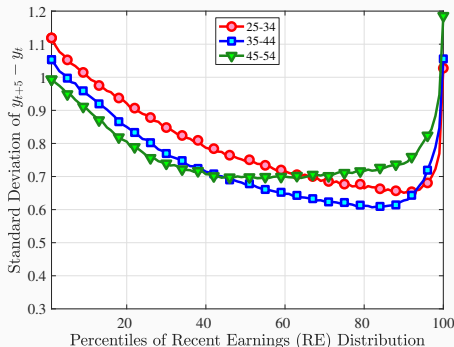
- Peak center, narrow shoulders, long tails  $\Rightarrow$  Excess kurtosis.
- Left tail longer than right tail  $\Rightarrow$  Left (Negative) Skewness.

# Standard Deviation of $y_{t+5} - y_t$

## Norway Data



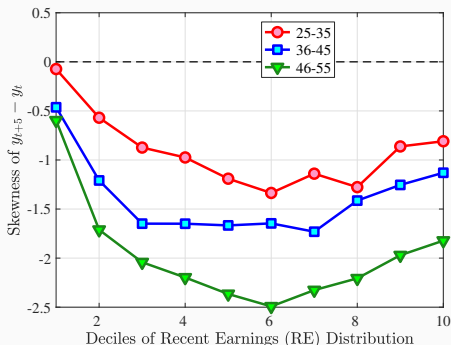
## US Data



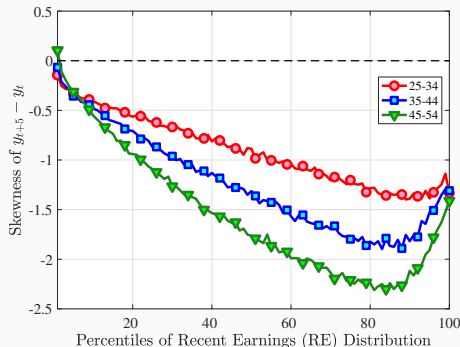
- Changes are smaller in Norway.
- RE and age variation are very similar in both countries.

# Skewness of $y_{t+5} - y_t$

## Norway Data



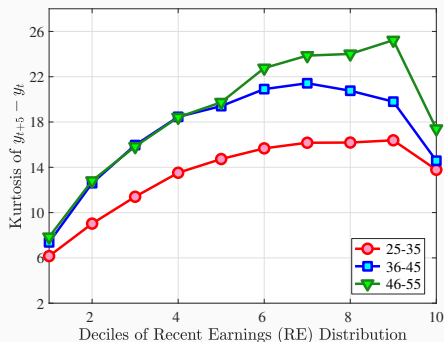
## US Data



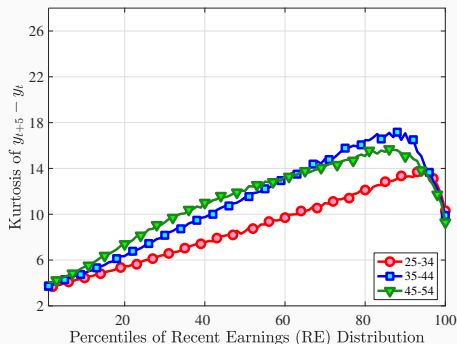
- In both economies, distributions are similarly left skewed.
- Left skewness increases by RE and age in a similar fashion.

# Kurtosis of $y_{t+5} - y_t$

## Norway Data



## US Data



- 5-year earnings distribution exhibits higher excess kurtosis in Norway.
- Excess kurtosis follows hump-shaped pattern over RE in both.

# Changes in Hours vs Wages

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## Hours Data

# Employment Register-Administrative Data

- Hours data reported by employers between 2003 and 2014
  - On contractual working hours per week
  - Only for wage and salary workers w/  $\geq 4$  hours/week contracts
  - No self-employed workers or freelancers
  - Cover 75% of population between 25 and 60.

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  - Cover 75% of population between 25 and 60.
- Measurement error in Employment register:
  - fail to report employment spells correctly or update hour changes,
  - overtime hours are not included,
  - employers with irregular employments are more prone.

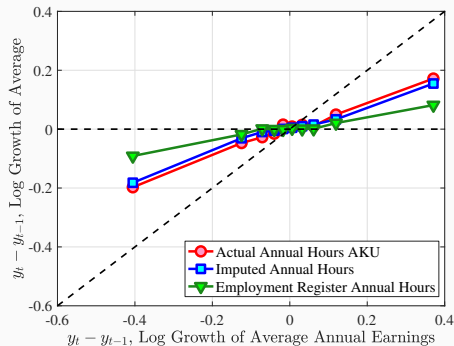
- Survey data on employment and work hours
  - Measure of actual hours worked last week.
  - Better quality than register data.
- 3200 working-age individuals interviewed 8 quarters in a row.
- Compute annual hours as  $h_{annual} = \sum_{t=1}^4 13 \times h_{actual}$
- Link observations to register data (data on annual wages, register hours, etc.)



# Imputation of Hours in the Register Data

- **Impute a better hours measure** in administrative register data.
- Link observations to register data (data on annual wages, register hours, etc.)
- Regress the AKU hours on observables in the register data, e.g., register hours, sick days, unemp. spells, parental leave, etc.
- Estimate an hour measure in register data using the estimates of this regression.

# Imputation of Hours in the Register Data



- Hours changes in register data are smaller than those from AKU.
- Imputation is doing fairly a good job in replicating the AKU measure.

# **Changes in Hours vs Wages**

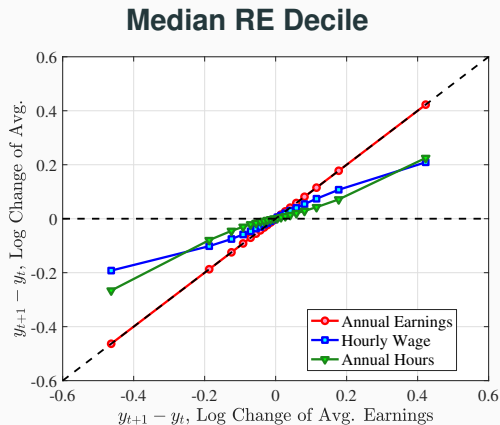
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**Earnings Growth: Hours vs Wage**

# Annual Hours vs Hourly Wage

- Decompose changes in earnings to **hourly wage** or **hours** components.
- Group workers w.r.t. annual wage growth between  $t - 1$  and  $t$ ,  $\Delta e_{t,1}$  into 20 equally sized bins.
  - On top of conditioning on age in  $t - 1$  (young vs prime age) and past 5-year income (RE) deciles  $\bar{Y}_{t-1}^i$ .
  - e.g., a group of prime age men with median past income who experience 25 log points decline in earnings between  $t - 1$  and  $t$ .
- How much hourly wage and hours growth each group experience?

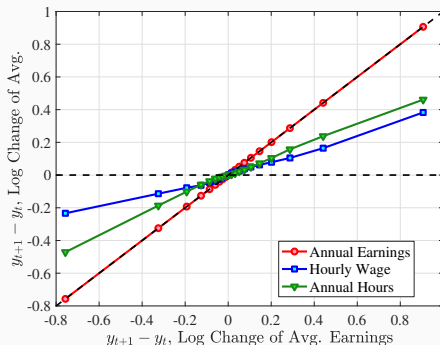
# Hours vs Wage: Median RE



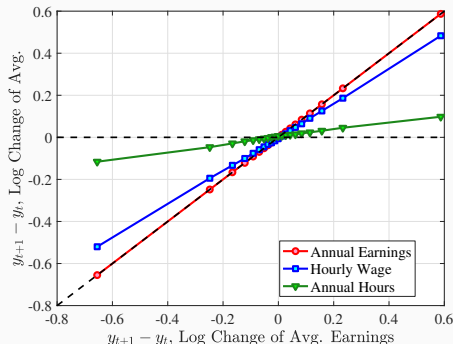
- Large earnings swings: hours and wage growth are equally important.
- Smaller earnings changes: wage growth is more important.

# Hours vs Wage: Bottom vs Top RE

## Bottom RE Decile



## Top RE Decile



- For bottom RE group hours growth plays a more important role.
- For higher RE groups wage changes are main drivers of earnings growth.

► More RE Groups

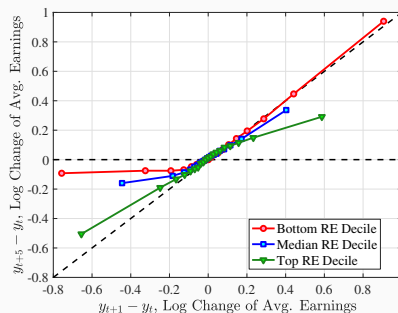
► Average of Log Growth

# **Changes in Hours vs Wages**

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## **Dynamics of Hours and Wage Growth**

# Asymmetric Mean Reversion: Dynamics of Earnings

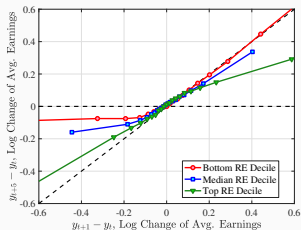


- For bottom (and median) RE group negative changes are transitory and positive changes are very persistent.
- The opposite is true for top RE group.

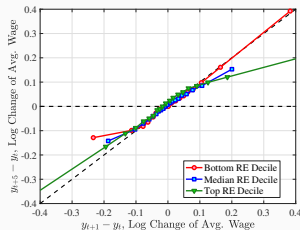


# Asymmetric Mean Reversion: Hours vs Wages

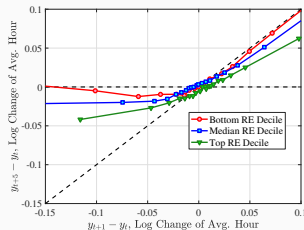
## Earnings Growth



## Wage Growth



## Hours Change



- Wage changes are very persistent (except for top RE).
- Declines in hours are transitory and increases persistent (not so much for top RE).

## **Changes in Hours vs Wages**

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**Distribution of Hours vs Wage Growth**

# Distribution of Hours vs Wage Growth

- Does **hourly wage** and **annual hours** growth distribution exhibit **non-Gaussian/nonlinear** features?
  - Plot their distributions and higher-order moments.
- How much of the left skewness and excess kurtosis of annual earnings growth are driven by changes in **hourly wages** vs **hours**?
  - Decompose skewness and kurtosis of earnings into hours and wage components.

# Decomposing Higher-Order Moments

$$\underbrace{e_{t+k} - e_t}_{\Delta e_{t,k}} = \underbrace{w_{t+k} - w_t}_{\Delta w_{t,k}} + \underbrace{h_{t+k} - h_t}_{\Delta h_{t,k}}$$

- $\Delta e_{t,k}$  : log **annual wage** growth between  $t$  and  $t + k$
- $\Delta w_{t,k}$  : log **hourly wage** growth between  $t$  and  $t + k$
- $\Delta h_{t,k}$  : log **annual hours** growth between  $t$  and  $t + k$

## Skewness Decomposition

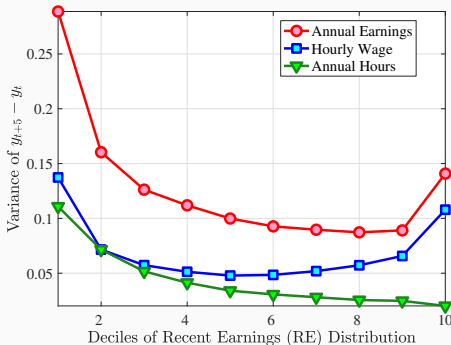
$$s_{\Delta e_{t,k}} = \left( \frac{\sigma_{\Delta w_{t,k}}}{\sigma_{\Delta e_{t,k}}} \right)^3 \times s_{\Delta w_{t,k}} + \left( \frac{\sigma_{\Delta h_{t,k}}}{\sigma_{\Delta e_{t,k}}} \right)^3 \times s_{\Delta h_{t,k}} + \text{CO-}s_{\Delta w_{t,k}, \Delta h_{t,k}}$$

## Kurtosis Decomposition

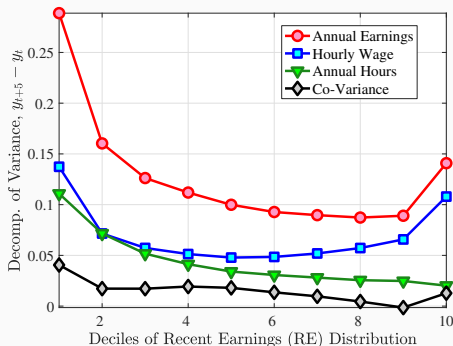
$$\kappa_{\Delta e_{t,k}} = \left( \frac{\sigma_{\Delta w_{t,k}}}{\sigma_{\Delta e_{t,k}}} \right)^4 \times \kappa_{\Delta w_{t,k}} + \left( \frac{\sigma_{\Delta h_{t,k}}}{\sigma_{\Delta e_{t,k}}} \right)^4 \times \kappa_{\Delta h_{t,k}} + \text{CO-}\kappa_{\Delta w_{t,k}, \Delta h_{t,k}}$$

# Variance of $y_{t+5} - y_t$ for Prime Age Male

## Variance



## Decomposition



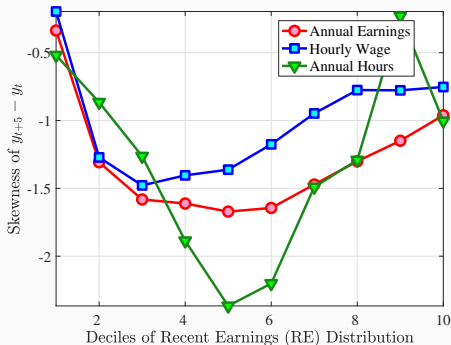
- Hourly wage is more volatile than hours especially above the median.
- Similar to the PSID (Heathcote *et al.* (2014)).

► 1-Year Growth Variance

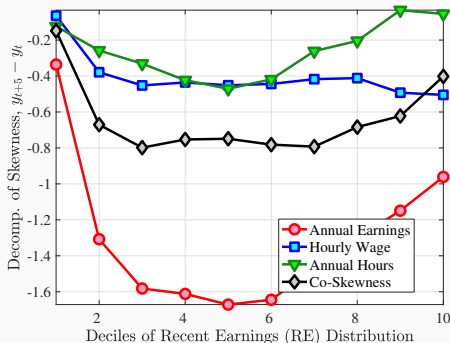
► 5-Year Growth Variance-Gaussian

# Skewness of $y_{t+5} - y_t$ for Prime Age Male

## Skewness



## Decomposition



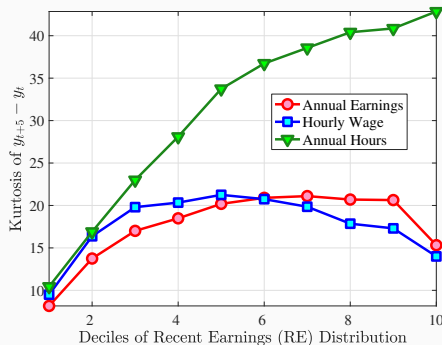
- Both hours and wage growth are left skewed.
- Wage growth and more importantly co-skewness are driving the left skewness of earnings growth.

► 1-Year Growth Skewness

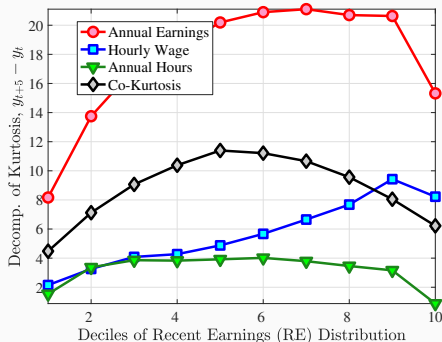
► 5-Year Growth Skewness-Gaussian

# Kurtosis of $y_{t+5} - y_t$ for Prime Age Male

## Kurtosis



## Decomposition



- Wage and hours growth are both leptokurtic (especially hours growth).
- Excess kurtosis due to hourly wage dominates the hours.

► 1-Year Growth Kurtosis

► 5-Year Growth Kurtosis-Gaussian

# **Changes in Hours vs Wages**

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**Earnings Swings and Important Life Cycle Events**



# Earnings Swings and Important Life Cycle Events

Event—in/out	1-Year Earnings Loss			1-Year Earnings Growth		
	> 0.5	[0.5, 0.25)	[0.25, 0.0)	[0.0, 0.25)	[0.25, 0.5)	≥ 0.5
Unemployment	8%	7%	2%	2%	7%	8%
Sickness	23%	21%	8%	8%	19%	20%
Part time	15%	13%	6%	8%	19%	23%
Parental leave	6%	9%	5%	6%	7%	5%
Firm change	19%	19%	10%	11%	21%	23%

# Household Income Dynamics

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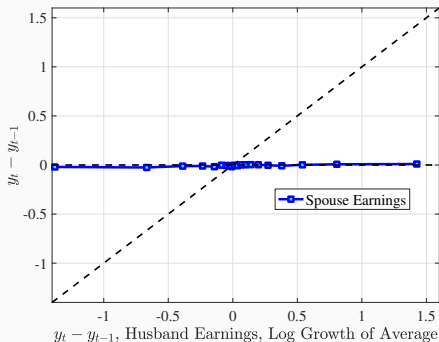
## Insurance Against Tail Shocks

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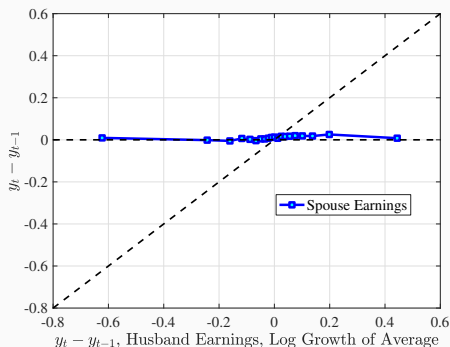
- How much insurance against tail shocks from
  - Spousal income & Government tax and transfers
  - After 1 year? After 5 years?
- **Capital income** includes positive interests, dividends and realized capital gains and losses.
  - excludes unrealized capital gains.
- **Tax and transfers** include UI, DI, SS pension, sickness benefits, paid maternity leave, money received on government activity program.
  - No in kind transfers: health care, daycare subsidies, schools, etc.
- **Imputed consumption** using the budget constraint of the household.

# Spousal Insurance

## Bottom RE Decile



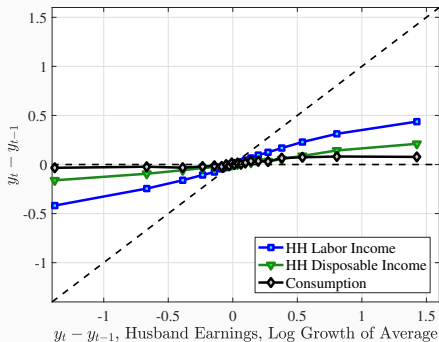
## Top RE Decile



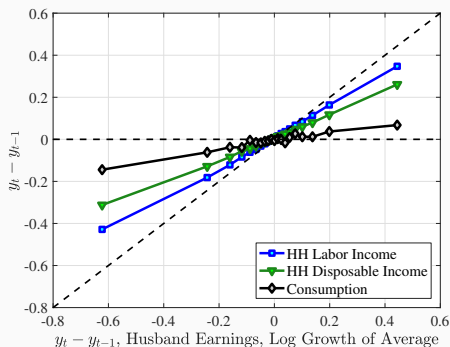
- No change in behavior of spouse or her earnings (not showing the SE income).

# Public Insurance

## Bottom RE Decile



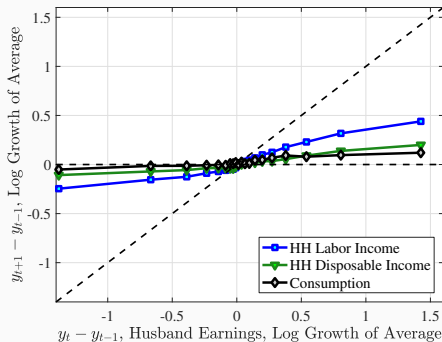
## Top RE Decile



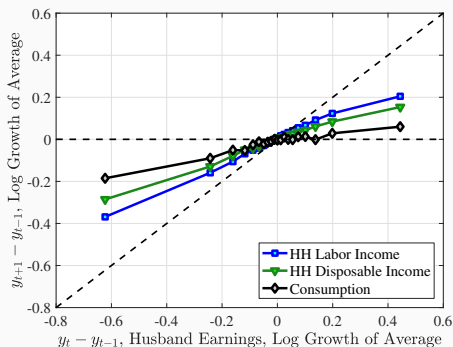
- Strong second earner effect (more so for low RE).
- Public insurance is much more helpful with tail shocks for low income.
- High RE can rely on self insurance for consumption.

# Public Insurance, 1 Year Later

## Bottom RE Decile



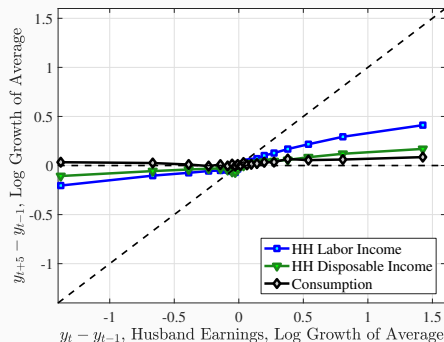
## Top RE Decile



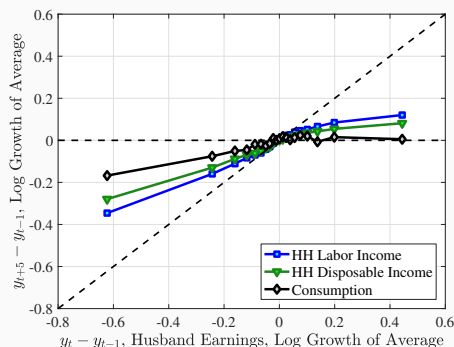
- After 1 year bottom RE see a very small decline in consumption (larger for top RE).
- Earnings losses are more persistent for top RE.

# Public Insurance, 5 Years Later

## Bottom RE Decile



## Top RE Decile



- Earnings changes are more persistent for top RE (especially negative changes).
- After 5 years, top RE still hasn't recovered the losses between  $t$  and  $t - 1$ .

# **Household Income Dynamics**

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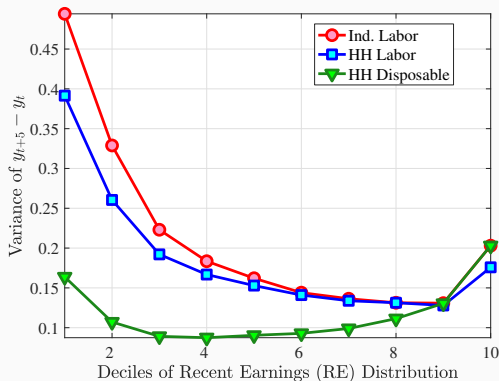
## **Distribution of Household Income Growth**



# Nature of Idiosyncratic Income Risk

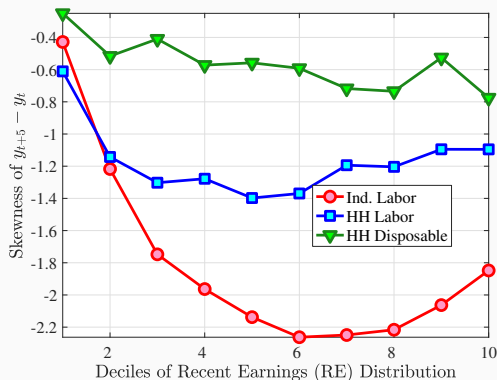
- Do non-Gaussian features of annual earnings growth distribution extend to
  - household (husband+wife) earnings?
  - After tax/after transfer disposable household income?
- For some questions nature of household income risk—before and after tax—is key.
- Plot their distributions and higher-order moments.

# Variance of 5-Year Income Growth, $y_{t+5} - y_t$



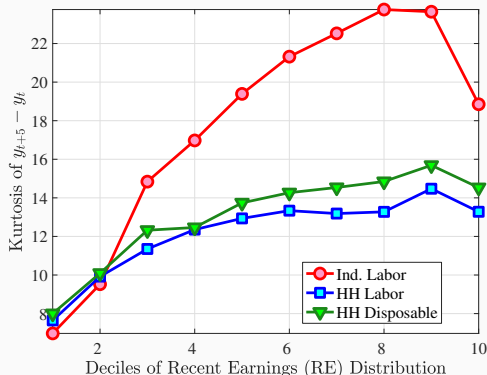
- HH labor is less volatile than individual labor.
- Taxes and transfers reduces variance substantially.

# Skewness of 5-Year Income Growth, $y_{t+5} - y_t$



- Spousal income reduces negative skewness due to second earner effect (similar for the US, Pruitt and Turner (2018)).
- Public insurance reduces left tail further.

# Kurtosis of 5-Year Income Growth, $y_{t+5} - y_t$



- HH labor and disposable income are still substantially leptokurtic, less so than individual earnings growth though.

# Summary of Findings

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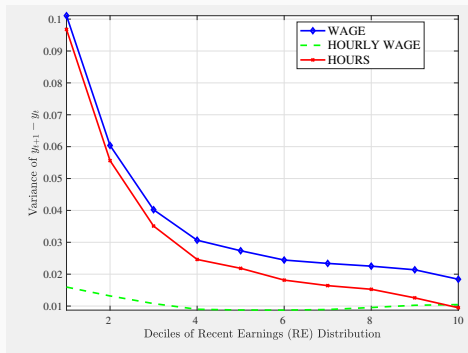
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3. Spousal inc. reduces the variance and skewness of earnings growth
  - mainly through second earner effect (no behavior change)
4. Taxes/transfers provide insurance against tail shocks—more for low RE groups
5. Even the disposable income growth exhibits long tails, less so than earnings.

## September Sample

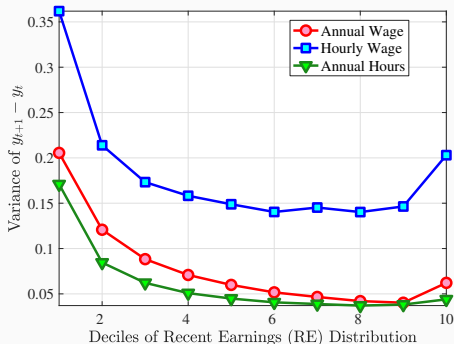
- Norway also surveys employers in **September** for more precise measure of hours.
  - An input to the annual wage negotiations between the unions and the employers,
  - For a sample of the largest private sector employers within each industry,
  - covering approximately 52% of firms and 70% of employees working in the private sector.
- Sample: Workers employed in a big firm two Septembers in a row and the past three Septs in the last 5 years.
  - no extensive margin in September
- Hourly wage=regular monthly wage/regular monthly hours

# Variance of $y_{t+1} - y_t$ for Prime Age Male

## September Sample



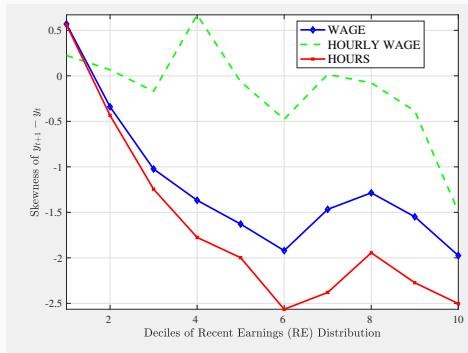
## Employment Register



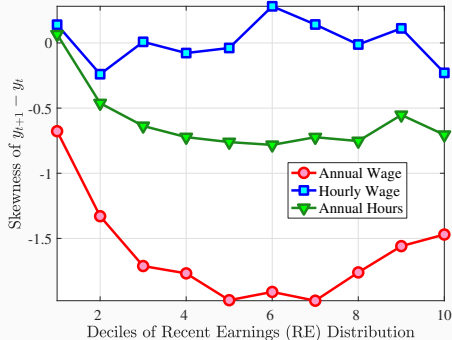
- Variance of annual and hourly wages are much smaller in September sample than Employment register.
- No overtime and bonuses are not included.

# Skewness of $y_{t+1} - y_t$ for Prime Age Male

## September Sample



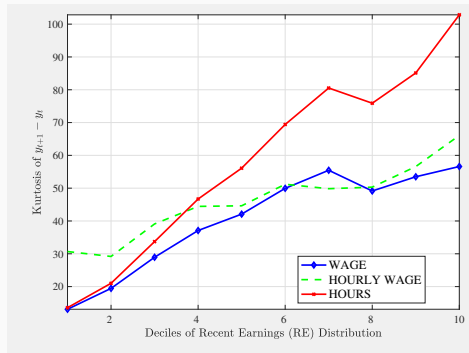
## Employment Register



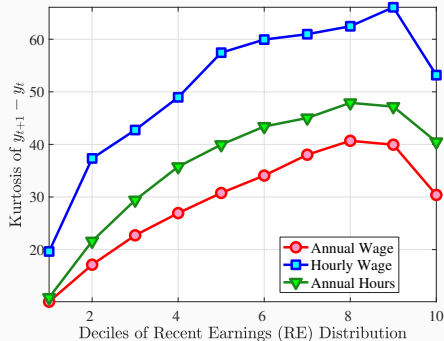
- Both samples display left skewness for hours growth and not so much for hourly wage growth.

# Kurtosis of $y_{t+1} - y_t$ for Prime Age Male

## September Sample



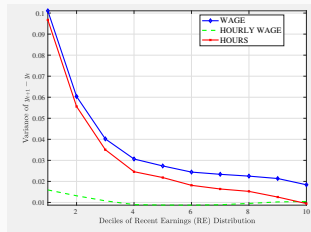
## Employment Register



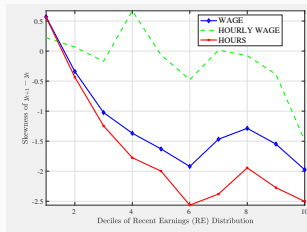
- September sample displays more excess kurtosis for both hours and hourly wage growth than employment register.

# Higher Order Moments in September Sample

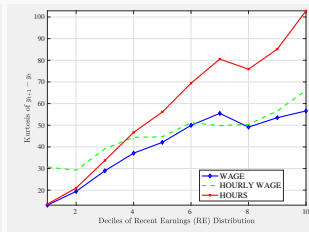
## Variance



## Skewness



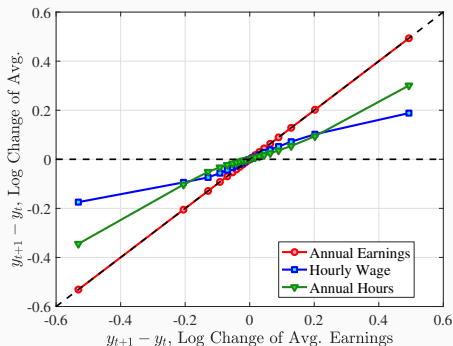
## Kurtosis



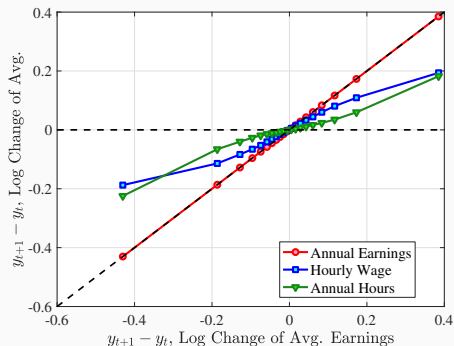
- Variance of annual and hourly wages are much smaller in September sample than Employment register.
- Both samples display left skewness and excess kurtosis for both hours and hourly wage growth.

# Hourly Wage vs Annual Hours: 3rd and 7th RE Groups

## 3rd RE Decile



## 7th RE Decile

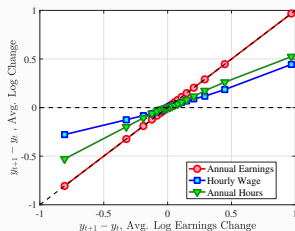


- Hourly wage growth plays a more important role for higher RE groups.

► Go back!

# Hourly Wage vs Annual Hours: Average of Log Change

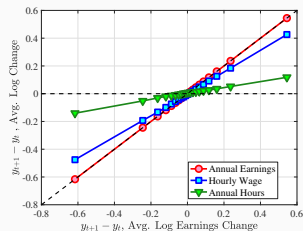
## 1st RE Decile



## 5th RE Decile



## 10th RE Decile



- Hourly wage growth plays a more important role lower RE groups.
- Wage changes drive earnings growth top RE groups. [▶ Go back!](#)



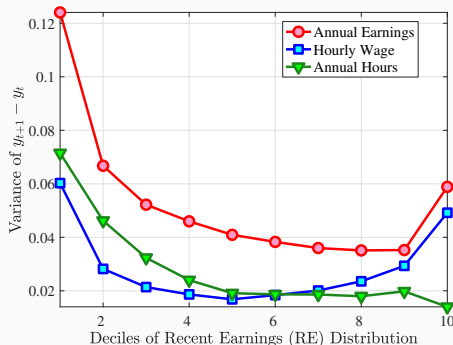
# Hourly Wage vs Annual Hours

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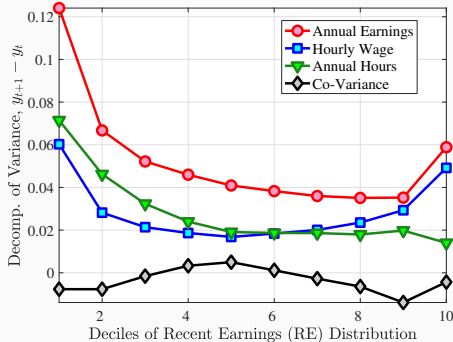
## 1-Year Moment Decomposition

# Variance of $y_{t+1} - y_t$ for Prime Age Male

## Variance



## Decomposition

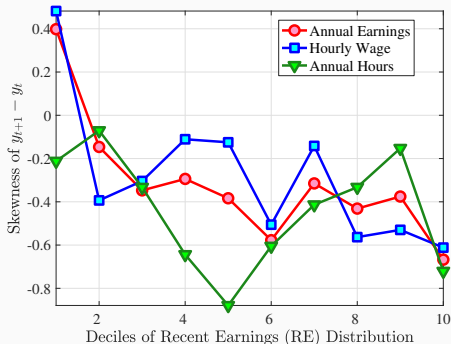


- Hourly wage is more volatile than hours above the median.

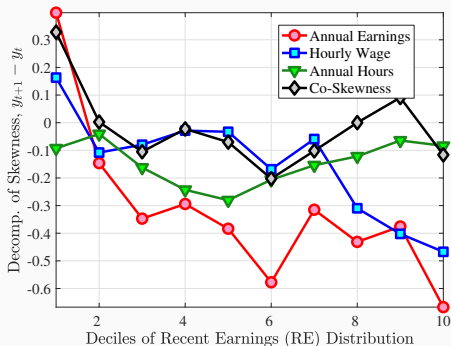
- Similar to the PSID (Heathcote *et al.* (2014)). ▶ 5-Year Growth Variance

# Skewness of $y_{t+1} - y_t$ for Prime Age Male

## Skewness



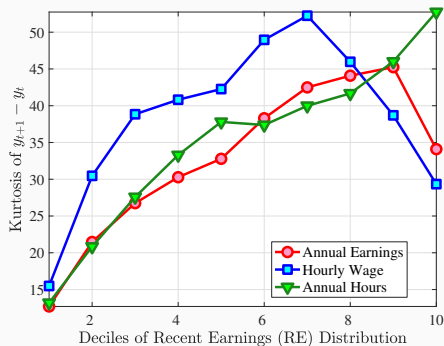
## Decomposition



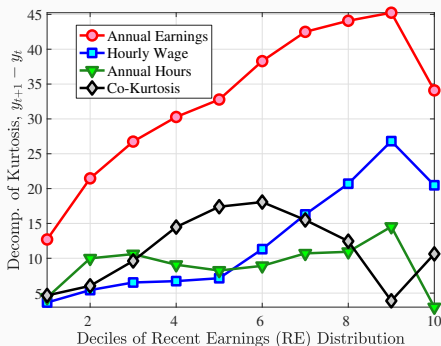
- Hours and wage growth are left skewed.
- For top earners wage growth is key for left skewness of earnings growth. ▶ 5-Year Growth Skewness

# Kurtosis of $y_{t+1} - y_t$ for Prime Age Male

## Kurtosis



## Decomposition



- Hourly wage and hours growth are both leptokurtic similar to earnings growth.
- Excess kurtosis due to hourly wage dominates the hours above the median. ▶ 5-Year Growth Kurtosis

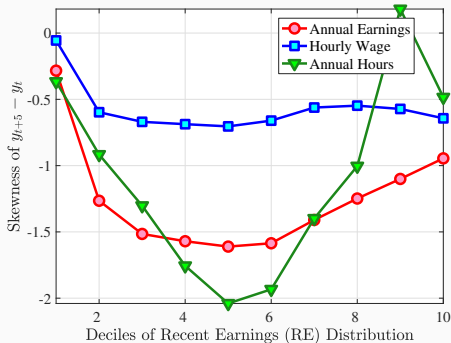
# **Hourly Wage vs Annual Hours**

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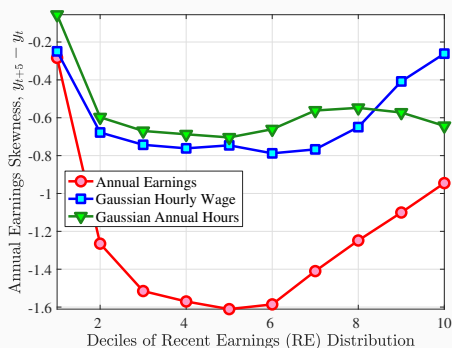
**Gaussian Decomposition: 5-Year Growth**

# Skewness of $y_{t+5} - y_t$ for Prime Age Male

## Skewness



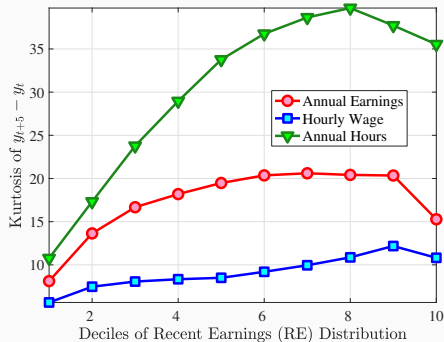
## Decomposition



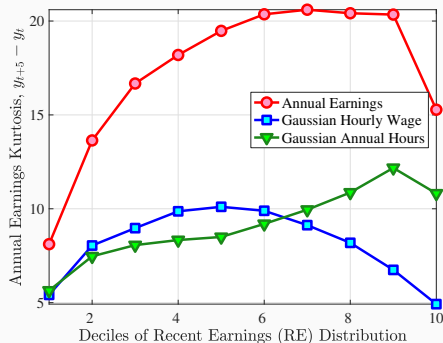
- Hours and wage growth are left skewed.
- For top earners wage growth is key for left skewness of earnings growth. ▶ 5-Year Growth Skewness

# Kurtosis of $y_{t+5} - y_t$ for Prime Age Male

## Kurtosis



## Decomposition



- Hourly wage and hours growth are both leptokurtic similar to earnings growth.
  - Excess kurtosis due to hourly wage dominates the hours above the median.
- 5-Year Growth Kurtosis

## **Hourly Wage vs Annual Hours**

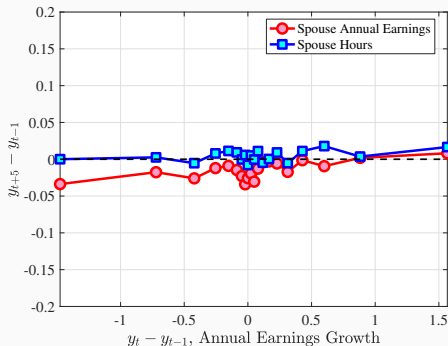
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**Spousal Insurance After 5 Years**

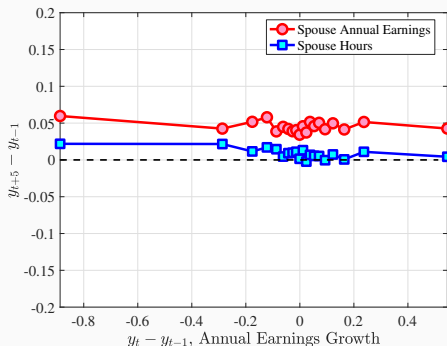


# Spousal Insurance, 5 Years Later

## Bottom RE Decile



## Top RE Decile



- Almost no change in behavior of spouse.
- For higher RE groups husband and wife's earnings changes are positively correlated.

## References i

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- , OZKAN, S. and SONG, J. (2014). The Nature of Countercyclical Income Risk. *Journal of Political Economy*, **122** (3), 621–660.
- HEATHCOTE, J., STORESLETTEN, K. and VIOLANTE, G. L. (2014). Consumption and labor supply with partial insurance: An analytical framework. *American Economic Review*.
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