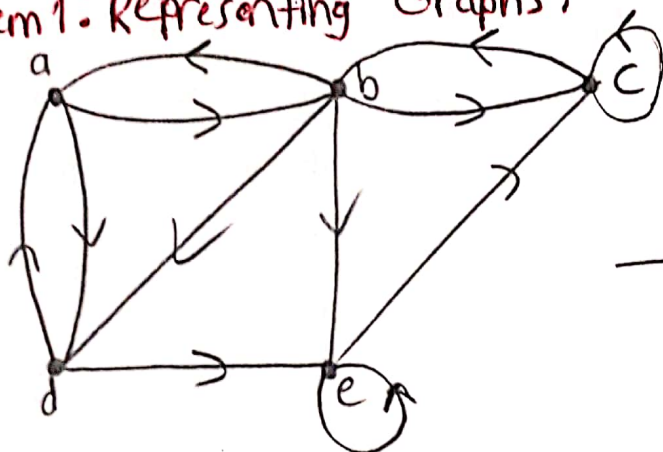


## Problem 1: Representing Graphs

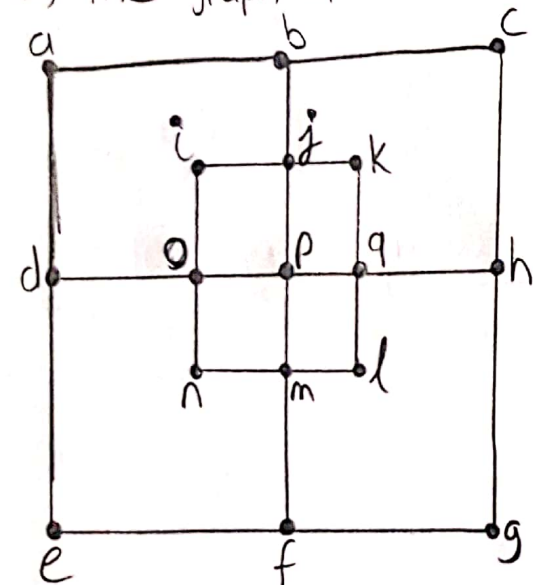


$$\begin{matrix}
 & \begin{matrix} a & b & c & d & e \end{matrix} \\
 \begin{matrix} a \\ b \\ c \\ d \\ e \end{matrix} & \begin{bmatrix} 0 & 1 & 0 & 1 & 0 \\ 1 & 0 & 1 & 1 & 1 \\ 0 & 1 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 & 1 \end{bmatrix}
 \end{matrix}$$

- If there is self loop I give the "1"
- If there is no edge I give the "0"
- If there is no self loop I give the "0" (it only applies to its connection with itself.)

## Problem 2: Hamilton Circuits

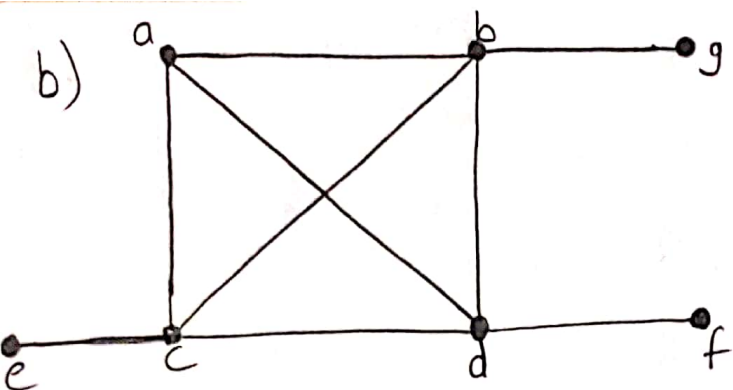
a) The graph  $G_1$



- we have 3 important items for a circuit to provide the Hamilton circuit.

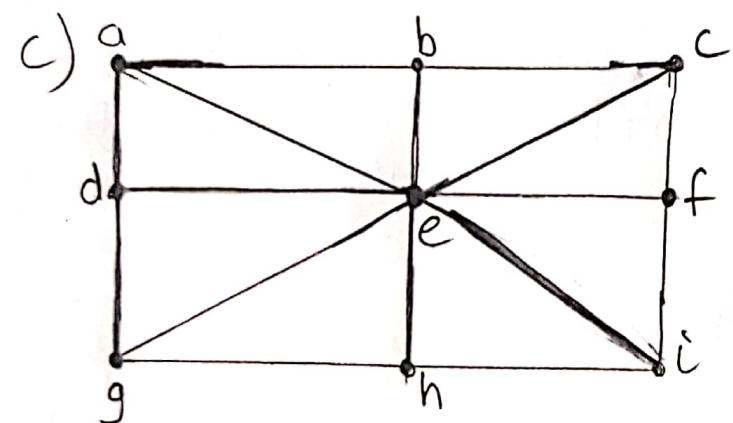
- 1- A graph with a vertex of degree one cannot have a Hamilton circuit.
- 2- Moreover, if a vertex in the graph has degree two, then both edges that are incident with this vertex must be part of any Hamilton circuit.
- 3- A Hamilton circuit cannot contain a smaller circuit within it.

a) This graph has not a Hamilton circuit because A Hamilton circuit cannot contain a smaller circuit within it.



→ Shape b has not Hamilton circuit because A graph with a vertex of edge one cannot have a Hamilton circuit.

The letters e, f and g do not follow this rule.

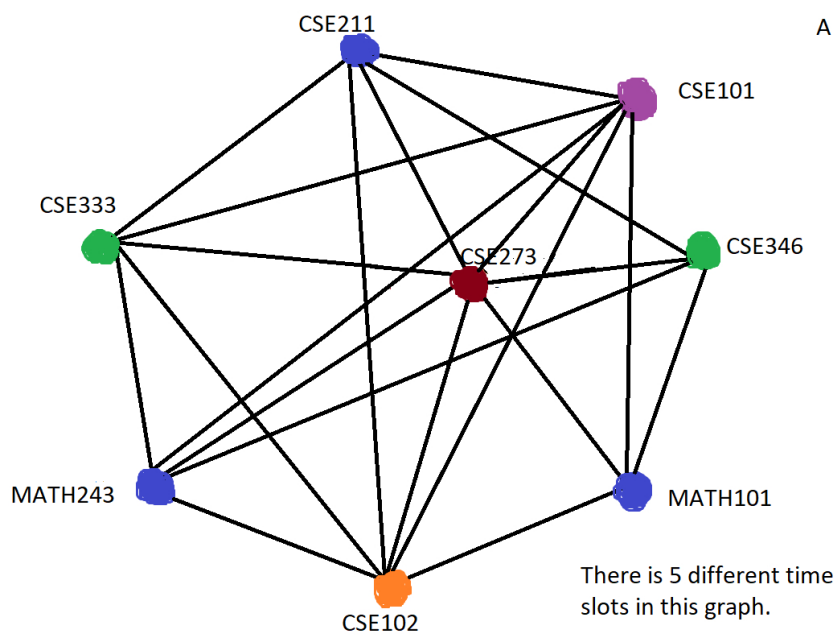


→ Yes, this shape has a Hamilton circuit.

And the Hamilton path is:  
a-d-g-h-i-f-c-e-b-a

**PROBLEM 3: APPLICATION ON GRAPHS?**  
If student can take both of these course I give the "+" otherwise I give the "-".

COURSE	CSE 101	CSE 102	CSE 273	CSE 211	CSE 333	CSE 346	MATH 101	MATH 243
CSE 101		+	+	+	+	-	+	+
CSE 102	+		+	+	+	-	+	+
CSE 273	+	+		+	+	+	+	+
CSE 211	+	+	+		+	+	-	-
CSE 333	+	+	+	+		-	-	+
CSE 346	-	-	+	+	-		+	+
MATH 101	+	+	+	-	-	+		-
MATH 243	+	+	+	-	+	+	-	



- A cse333,cse346
- B cse211,math243  
math101
- C cse273
- D cse101
- E cse102