

Question 2:

$$\text{Given that: } \begin{cases} \vec{a}^{(1)} = W^{(1)} \vec{a}^{(0)} + \vec{b}^{(1)} \\ \vec{a}^{(2)} = W^{(2)} \vec{a}^{(1)} + \vec{b}^{(2)} \\ \vec{a}^{(3)} = W^{(3)} \vec{a}^{(2)} + \vec{b}^{(3)} \end{cases}$$

$$\begin{aligned} \vec{a}^{(3)} &= W^{(3)} \vec{a}^{(2)} + \vec{b}^{(3)} \\ &= W^{(3)} (W^{(2)} \vec{a}^{(1)} + \vec{b}^{(2)}) + \vec{b}^{(3)} \\ &= W^{(3)} [W^{(2)} (W^{(1)} \vec{a}^{(0)} + \vec{b}^{(1)}) + \vec{b}^{(2)}] + \vec{b}^{(3)} \end{aligned}$$

$$\text{Thus, } \vec{a}^{(3)} = W^{(3)} W^{(2)} W^{(1)} \vec{a}^{(0)} + W^{(3)} W^{(2)} \vec{b}^{(1)} + W^{(3)} \vec{b}^{(2)} + \vec{b}^{(3)}$$

$$\text{for } \vec{a}^{(3)} \approx \tilde{W} \vec{a}^{(0)} + \tilde{b}$$

$$\begin{cases} \tilde{W} \approx W^{(3)} W^{(2)} W^{(1)} \\ \tilde{b} \approx W^{(3)} W^{(2)} \vec{b}^{(1)} + W^{(3)} \vec{b}^{(2)} + \vec{b}^{(3)} \end{cases}$$