Download Data

```
!wget http://www2.aueb.gr/users/ion/data/lingspam_public.tar.gz
!tar -zxf lingspam_public.tar.gz
--2021-11-01 19:27:09-- http://www2.aueb.gr/users/ion/data/lingspam_public.tar.gz
Resolving www2.aueb.gr (www2.aueb.gr)... 195.251.255.138
Connecting to www2.aueb.gr (www2.aueb.gr)|195.251.255.138|:80... connected.
HTTP request sent, awaiting response... 200 OK
Length: 11564714 (11M) [application/x-gzip]
Saving to: 'lingspam_public.tar.gz'
lingspam_public.tar 100%[==========================]] 11.03M 1.73MB/s in 7.0s
2021-11-01 19:27:17 (1.59 MB/s) - 'lingspam_public.tar.gz' saved [11564714/11564714]
```

Feature selection using information gain(IG) matrix

```
import os
 1
 2
    import re
 3
    import math
 4
    import numpy as np
 5
6
    from collections import Counter
7
8
    # Copy from readme.txt
9
    # Each one of the 10 subdirectories contains both spam and legitimate
    # messages, one message in each file. Files whose names have the form
10
    # spmsg*.txt are spam messages. All other files are legitimate messages.
11
12
    path = "lingspam public/lemm stop"
13
    word_filter = re.compile(r'^[a-z]+-?[a-z]+[0-9]*$')
14
15
16
    spam words = []
17
    ham_words = []
18
    train X = []
19
    train_Y = []
20
    spam_num = 0
21
    ham num = 0
22
23
    # Build IG and training dataset
24
    for dir in [os.path.join(path, 'part' + str(i)) for i in range(1, 10)]:
25
         mails = [(os.path.join(dir, file_name), 'spmsg' in file_name) for file_name in os.li
26
        for file path, spam in mails:
```

```
28
             with open(file path) as f:
                 content = f.readlines()[2]
29
                 words = content.split()
30
31
                 filtered words = list(set([w for w in words if (len(w) > 1 and re.match(word
32
                 # Add words to training set
33
                 train X.append(filtered words)
                 # Label spam as 1, ham as 0
34
35
                 if spam:
36
                     train Y.append(1)
37
                     spam_words += filtered_words
                     spam_num += 1
38
39
                 else:
40
                     train Y.append(0)
                     ham words += filtered words
41
42
                     ham num += 1
43
44
45
    train all counter = Counter(spam words + ham words)
46
    train spam counter = Counter(spam words)
47
    train ham counter = Counter(ham words)
48
49
    print(f'Loading {spam num + ham num} emails, {spam num} of them are spam, \
    and {ham num} of them are ham.')
50
    print(f'Within the total of {len(train all counter)} words, \
51
52
    getting {len(train spam counter)} words occur in spam, \
    and {len(train ham counter)} words occur in ham email.')
53
     Loading 2602 emails, 432 of them are spam, and 2170 of them are ham.
    Within the total of 48583 words, getting 8657 words occur in spam, and 45091 words occu
 1 print(train X[0])
     ['letter', 'establish', 'convert', 'participate', 'start', 'customer', 'simple', 'inter
                                                                                            •
1 # Build test data set
 2 test X = []
3 test Y = []
 5 test path = 'lingspam public/lemm stop/part10'
6 test_mail_path = [(os.path.join(test_path, file_name), 'spmsg' in file_name) for file_name
7 for file path, spam in test mail path:
      with open(file path) as f:
8
9
          content = f.readlines()[2]
10
          words = content.split()
11
          filtered_words = list(set([w for w in words if (len(w) > 1 and re.match(word_filte
12
          # Add words to test set
          test X.append(filtered words)
13
14
          # Label spam as 1, ham as 0
```

```
15
           if spam:
16
               test Y.append(1)
17
           else:
18
               test_Y.append(0)
 1 # Helper parameter and function for IG
 2 def Log(i):
       return np.log(i) if i != 0 else 0
 3
 4
 5
 6 total num = spam num + ham num
 7 P_SPAM = spam_num / total_num
 8 P HAM = 1 - P SPAM
 9 \ HC = -P \ SPAM * \ Log(P_SPAM) - P_HAM * \ Log(P_HAM)
 1 # Generating IG for all words
 2
 3 IG = \{\}
 4
 5 for word in train all counter:
       all_occur = train_all_counter[word]
 6
 7
       spam occur = train spam counter[word]
 8
       ham occur = train ham counter[word]
 9
10
       \# X=1, C = ham
11
       P1h = (ham_occur / ham_num) * P_HAM
       \# X=0, C = ham
12
13
       P0h = (1 - (ham occur / ham num)) * P HAM
14
       \# X=1, C = spam
       P1s = (spam occur / spam num) * P SPAM
15
       \# X=0, C = spam
16
       P0s = (1 - (spam occur / spam num)) * P SPAM
17
18
       \# P(X=1)
      P1 = all_occur / total_num
19
      \# P(X=0)
20
       P0 = 1 - P1
21
22
23
      # Note: H(C|X) = -sum(P(X,C) \log(C|X))
       # But it is easier to do addition operation here :)
24
25
      HCX = P1h*Log(P1h/P1) + P0h*Log(P0h/P0) + P1s*Log(P1s/P1) + P0s*Log(P0s/P0)
26
       IG[word] = HC + HCX
27
28 top_words = [k for k, v in sorted(IG.items(), key=lambda item: -item[1])]
29 top 10 = top words[:10]
30 top 100 = top words[:100]
31 top_1000 = top_words[:1000]
 1 print(top_10)
```

```
['language', 'remove', 'free', 'linguistic', 'university', 'money', 'click', 'market',
```

Classifiers Implementation

→ Generate Feature Matrix

```
def get_feature(N, dataset, term_frequency=False):
1
         """Generate feature matrix based on top N words."""
 2
 3
         # print(term_frequency)
         top n = {v:i for i,v in enumerate(top words[:N])}
4
5
         feature_matrix = np.zeros((len(dataset), N))
         for j, content in enumerate(dataset):
6
7
             for word in content:
8
                 if word in top n:
9
                     if term frequency:
10
                         feature_matrix[j, top_n[word]] += 1
                     else:
11
12
                         feature matrix[j, top n[word]] = 1
13
14
         return feature matrix
```

▼ Bernoulli NB Classifier

```
1 class BNB:
      """Naive Bayes classifier for multivariate Bernoulli models."""
 2
 3
       def __init__(self, alpha=1.0):
           self.alpha = alpha # Actually, no need in this homework :)
4
 5
           self.spam_num = 0
6
           self.ham num = 0
7
           self.P_X_spam = []
           self.P_X_ham = []
8
9
10
11
       def fit(self, train_x, train_y):
           """Fit Naive Bayes classifier according to train_x, train_y."""
12
           self.spam_num = sum(train_y)
13
           self.ham num = len(train y) - sum(train y)
14
15
           rows, feature_num = train_x.shape
16
17
           self.P_X_spam = np.zeros(feature_num)
           self.P_X_ham = np.zeros(feature_num)
18
           for i in range(feature num):
19
```

```
20
               x spam = 0
               x ham = 0
21
22
               for j in range(rows):
23
                   if train_x[j,i]:
24
                       if train_y[j]:
25
                           x spam += 1
26
                       else:
27
                           x ham += 1
28
               self.P \ X \ spam[i] = (1 + x \ spam) / (self.spam \ num + 2)
29
               self.P_X_ham[i] = (1 + x_ham) / (self.ham_num + 2)
30
31
32
      def _row_predict(self, one_sample):
           """Predict one record of the data set."""
33
34
           prob = 1
           for i, feature in enumerate(one sample):
35
               p0 = self.P_X_ham[i]
36
               p1 = self.P_X_spam[i]
37
38
               prob *= (p1 / p0) if feature == 1 else (1 - p1) / (1 - p0)
39
           return prob * self.spam_num / self.ham_num
40
41
42
       def predict(self, test x):
43
           """Perform classification on an array of test vectors test x."""
44
           pred = np.zeros((test_x.shape[0]))
           for i in range(test x.shape[0]):
45
               pred[i] = int(self._row_predict(test_x[i]) > 1)
46
47
           return pred
48
49
      def score(self, test x, test y):
50
           """Return the mean accuracy on the given test data and labels."""
51
52
           y pred = self.predict(test x)
53
           count = 0
54
           for i in range(len(test_y)):
               count += 1 if y pred[i] == test y[i] else 0
55
56
           return count / len(test_y)
57
```

Multinominal NB Classifier

```
1 class MNB:
2    """Naive Bayes classifier for multinomial models."""
3    def __init__(self, alpha=1.0):
4        self.alpha = alpha
5        self.spam_num = 0
6        self.ham_num = 0
7        self.P_X_spam = []
8        self.P X ham = []
```

```
9
10
11
       def fit(self, train x, train y):
12
           """Fit Naive Bayes classifier according to train x, train y."""
13
           self.spam_num = sum(train_y)
           self.ham num = len(train y) - sum(train y)
14
           rows, feature num = train x.shape
15
16
17
           self.P X spam = np.zeros(feature num)
18
           self.P_X_ham = np.zeros(feature_num)
           for i in range(feature num):
19
               x spam = 0
20
21
               x ham = 0
22
               for j in range(rows):
23
                   if train_x[j,i]:
24
                       if train y[j]:
25
                           x spam += 1
26
                       else:
27
                           x ham += 1
28
               self.P_X_spam[i] = (1 + x_spam) / (self.spam_num + 2)
29
               self.P \ X \ ham[i] = (1 + x \ ham) / (self.ham \ num + 2)
30
31
32
       def row predict(self, one sample):
           """Predict one record of the data set."""
33
34
           prob = 1
35
           for i, feature in enumerate(one_sample):
36
               p0 = self.P_X_ham[i]
37
               p1 = self.P X spam[i]
38
               prob += (Log(p1) - Log(p0)) if feature == 1 else 0
39
           return prob + Log(self.spam num) - Log(self.ham num)
40
41
42
       def predict(self, test_x):
           """Perform classification on an array of test vectors test x."""
43
44
           pred = np.zeros((test x.shape[0]))
45
           for i in range(test x.shape[0]):
               pred[i] = int(self. row predict(test x[i]) > 0)
46
47
           return pred
48
49
50
       def score(self, test x, test y):
           """Return the mean accuracy on the given test data and labels."""
51
52
           y_pred = self.predict(test_x)
           count = 0
53
54
           for i in range(len(test_y)):
55
               count += 1 if y pred[i] == test y[i] else 0
56
           return count / len(test y)
```

Classifiers Comparison

```
1 from sklearn.naive bayes import MultinomialNB, BernoulliNB
2 from sklearn.metrics import classification report
3
4 \text{ top N} = [10, 100, 1000]
5 result accuracy = []
7 for N in top_N:
      Xprint = get_feature(N, train_X)
8
9
      # X label with term frequency
10
      X tf = get feature(N, train X, term frequency=True)
11
      Y = np.array(train Y)
12
13
      X_test = get_feature(N, test_X)
14
      # X label with term frequency
15
      X test tf = get feature(N, test X, term frequency=True)
16
      Y_test = np.array(test_Y)
17
18
      model1 = BNB()
19
      model2 = MNB()
20
      model3 = MNB()
21
      # train models
22
23
      model1.fit(X, Y)
24
      model2.fit(X, Y)
25
      model3.fit(X_tf, Y)
26
27
      # predict
      y_1 = model1.predict(X_test)
28
      y 2 = model2.predict(X test)
29
30
      y_3 = model3.predict(X_test_tf)
31
      print(f'----')
32
      print( '-----')
33
      print(classification report(Y test,y 1, target names = ["ham", "spam"]))
34
35
      print('--- Multinominal Naive Bayes with binary features ---')
      print(classification_report(Y_test,y_2, target_names = ["ham", "spam"]))
36
      print('---- Multinominal Naive Bayes with term frequency ---')
37
38
      print(classification_report(Y_test,y_3, target_names = ["ham", "spam"]))
39
40
      N_accuray = [model1.score(X_test,Y_test),
                  model2.score(X test,Y test),
41
                  model3.score(X_test_tf,Y_test)]
42
43
      result_accuracy.append(N_accuray)
      ------ Using top 10 features ------
    ----- Bernoulli Naive Bayes ------
                 precision
                             recall f1-score
                                               support
             ham
                      0.96
                               0.98
                                         0.97
                                                   242
```

spam	0.89	0.82	0.85	49
accuracy			0.95	291
macro avg	0.93	0.90	0.91	291
_		0.95	0.95	291
weighted avg	0.95	0.95	0.95	291
Multinomi	nal Naive E	Bayes with	binary fea	atures
	precision	recall	f1-score	support
ham	0.98	0.95	0.97	242
spam	0.80	0.92	0.86	49
accuracy			0.95	291
macro avg	0.89	0.94		291
weighted avg	0.85	0.95	0.95	291
weighted avg	0.93	0.93	0.95	291
Multinom	inal Naive	Raves with	term free	niency
riatetiioii		recall		
	p. cc1310		. 1 300. 0	зарро. с
ham	0.98	0.95	0.97	242
spam	0.80	0.92	0.86	49
- F -				
accuracy			0.95	291
macro avg	0.89	0.94	0.91	291
weighted avg	0.95	0.95	0.95	291
0 0				
	Using to	op 100 feat	ures	
	Bernoul	li Naive Ba	ayes	
	precision	recall	f1-score	support
ham	0.94	1.00	0.97	242
_	1.00	0.67	0.80	49
spam	1.00	0.67	0.80	49
accuracy			0.95	291
macro avg	0.97	0.84	0.89	291
weighted avg	0.95	0.95		291
weighted avg	0.55	0.55	0.54	271
Multinomi	nal Naive N	Baves with	binary fea	atures
		recall	-	
	,			
ham	1.00	0.98	0.99	242
spam	0.89	1.00	0.94	49
accuracy			0.98	291
macro avg	0.95	0.99	0.96	291
weighted avg	0.98	0.98	0.98	291
Multinom		-		
	precision	recall	f1-score	support
	_			_
ham	1.00		0.99	242
spam	0.89	1.00	0.94	49
			0.00	201
acciiracv			0 92	291

▼ Spam precision and spam recall

Params	Spam Precision	Spam Recall
Top 10 Words, Bernoulli Naive Bayes	0.89	0.82
Top 10 Words, Multinominal Naive Bayes with binary features	0.80	0.92
Top 10 Words, Multinominal Naive Bayes with term frequency	0.80	0.92
Top 100 Words, Bernoulli Naive Bayes	1.00	0.67
Top 100 Words, Multinominal Naive Bayes with binary features	0.89	1.00
Top 100 Words, Multinominal Naive Bayes with term frequency	0.89	1.00
Top 1000 Words, Bernoulli Naive Bayes	1.00	0.61
Top 1000 Words, Multinominal Naive Bayes with binary features	1.00	1.00
Top 1000 Words, Multinominal Naive Bayes with term frequency	1.00	1.00

Compare with sklearn

```
1 result_accuracy_sk = []
   2
   3 for N in top N:
                       model1_sk = BernoulliNB()
   5
                       model2 sk = MultinomialNB()
   6
                       model3_sk = MultinomialNB()
   7
   8
                       X = get_feature(N, train_X)
   9
                       X_tf = get_feature(N, train_X, term_frequency=True)
                       Y = np.array(train_Y)
10
11
12
                       X_test = get_feature(N, test_X)
                       X_test_tf = get_feature(N, test_X, term_frequency=True)
13
14
                       Y_test = np.array(test_Y)
15
16
                       # train models
17
                       model1 sk.fit(X, Y)
                       model2_sk.fit(X, Y)
18
                        model3_sk.fit(X_tf, Y)
19
20
21
                        # predict
22
                       N_accuray = [model1_sk.score(X_test,Y_test),
                                                                       model2_sk.score(X_test,Y_test),
23
                                                                       model3_sk.score(X_test_tf,Y_test)]
24
25
                       result accuracy sk.append(N accuray)
26
27
28 print(result_accuracy)
29 print(result accuracy sk)
                 [[0.9518900343642611,\ 0.9484536082474226,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.945017182130584],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.9484536082474226],\ [0.9450171821305842,\ 0.94845360824,\ 0.94845360824,\ 0.948454084,\ 0.948454084,\ 0.948454084,\ 0.948454084,\ 0.948454084,\ 0.948454084,\ 0.948454084,\ 0.948454084,\ 0.948454084,\ 0.948454084,\ 0.
```

 $\lceil \lceil 0.9518900343642611, 0.9518900343642611, 0.9518900343642611 \rceil, \lceil 0.9450171821305842, 0.9618900343642611 \rceil$

SVM based spam filter

```
1 from sklearn.model_selection import GridSearchCV
 2 from sklearn.model selection import train test split
 3 from sklearn.svm import SVC
4 from sklearn.preprocessing import MinMaxScaler
5 from sklearn.base import clone
6
7
8 feature sizes = [10, 100, 200]
9 modes = ["bf", "tf"]
10 \text{ gamma} = [1, 0.1, 0.01, 0.001]
11 C = [0.1, 1, 10, 100]
12 degree = [2,3,10]
13 tuned parameters = [{'kernel': ['rbf','sigmoid'], 'gamma': gamma,'C': C},
14
                       {'kernel': ['linear'], 'C': C},
15
                       {'kernel': ['poly'], 'gamma': gamma, "degree" : degree, 'C':C}
16
                       ]
17 now best = {}
18 now score = 0
19 best_clf = SVC()
20 for N in feature sizes:
       for mode in modes:
21
           X = get feature(N, train X, term frequency=(mode=='tf'))
22
           X_test = get_feature(N, test_X, term_frequency=(mode=='tf'))
23
          Y = np.array(train Y)
24
25
           if mode == 'tf':
26
               ss = MinMaxScaler()
               X = ss.fit transform(X)
27
               X test = ss.transform(X test)
28
           clf = GridSearchCV(SVC(), tuned_parameters, cv = 5, scoring='recall_macro', verbos
29
30
           clf.fit(X, Y)
31
32
           if clf.best_score_ > now_score:
33
               now score = clf.best score
               now_best = {"size":N, "mode":mode, "score":clf.best_score_, "params":clf.best_
34
35
               best_clf = clone(clf.best_estimator_)
36
               print (now best)
37
38 N = now_best["size"]
39 mode = now best["mode"]
40 X = get feature(N, train X, term frequency=(mode=='tf'))
41 X_test = get_feature(N, test_X, term_frequency=(mode=='tf'))
42 Y = np.array(train Y)
43 Y_test = np.array(test_Y)
44
45 if mode == "tf":
```

```
46
      ss = MinMaxScaler()
47
      X = ss.fit transform(X)
48
      X test = ss.transform(X test)
49
50 best_clf.fit(X, Y)
51 pred y = best clf.predict(X test)
52 print (now best)
53 print (classification_report(Y_test, pred_y, target_names = ["ham", "spam"]))
     {'size': 10, 'mode': 'bf', 'score': 0.9333773098447026, 'params': {'C': 1, 'gamma': 1,
    {'size': 100, 'mode': 'bf', 'score': 0.9611211300362037, 'params': {'C': 1, 'gamma': 0.
    {'size': 200, 'mode': 'bf', 'score': 0.9699466122688307, 'params': {'C': 10, 'gamma': 0
    {'size': 200, 'mode': 'bf', 'score': 0.9699466122688307, 'params': {'C': 10, 'gamma': 0
                   precision
                                recall f1-score
                                                    support
              ham
                        0.98
                                  1.00
                                             0.99
                                                        242
                        0.98
                                  0.88
                                             0.92
                                                         49
             spam
                                             0.98
                                                        291
         accuracy
        macro avg
                        0.98
                                  0.94
                                             0.96
                                                        291
    weighted avg
                        0.98
                                  0.98
                                             0.98
                                                        291
```

Methodology

I use GridSearchCV to help me find the best parameters for SVM. Also, we've see that higher Information Gain feature matrix can have a better result in prediction. So I compare the score between "BF" and "TF" and the score among "N={10, 100, 200}". The result shows that using **top 200** words, **binary features**, and {'C': 10, 'gamma': 0.1, 'kernel': 'rbf'} as the SVM parameter can get the best result.

→ Adversarial Classification

Attacker

```
1 class Attacker:
2   def __init__(self):
3     self.Lo = []
4     self.Lo0 = []
5     self.Lo1 = []
6
7
8   def cal_Lo(self, train_x, train_y):
9     rows, feature_num = train_x.shape
```

```
self.Lo = np.zeros(feature num)
10
           self.Lo0 = np.zeros(feature num)
11
           self.Lo1 = np.zeros(feature num)
12
13
14
           for i in range(feature_num):
15
               x spam = 0
               x_ham = 0
16
               for j in range(rows):
17
18
                   if train x[j,i]:
19
                        if train_y[j]:
20
                            x spam += 1
21
                        else:
22
                            x ham += 1
23
               P X1 ham = x ham / ham num
               P_X1_{spam} = x_{spam} / spam_{num}
24
25
               P X0 ham = 1 - P X1 ham
               P_X0_{spam} = 1 - P_X1_{spam}
26
               self.Lo1[i] = Log(P_X1_spam/P_X1_ham)
27
28
               self.Lo0[i] = Log(P X0 spam/P X0 ham)
29
               self.Lo[i] = self.Lo1[i] - self.Lo0[i]
30
31
       def row attack(self, one sample):
32
           sort_Lo = sorted(range(len(self.Lo)), key=lambda i: self.Lo[i])
33
34
35
           cost = 0
           sigmaLoX = 0
36
           for i,v in enumerate(one sample):
37
               sigmaLoX += self.Lo1[i] if v==1 else self.Lo0[i]
38
39
           if sigmaLoX < 0:
               return 0, one sample
40
41
           for i in sort Lo:
42
43
               if(self.Lo[i] >= 0):
44
                   return cost, one_sample
45
               if one sample[i]:
46
                   continue
47
               one sample[i] = 1
48
               sigmaLoX += self.Lo[i]
49
               cost += 1
50
               if (sigmaLoX < 0):</pre>
51
                    return cost, one_sample
52
53
54
       def attack(self, test_x, test_y):
55
           costs = []
56
           new test x = []
           rows, feature num = test x.shape
57
58
           for i in range(rows):
59
               if test_y[i]:
60
                   cost, changed = self. row attack(test x[i])
```

▼ Defender

```
1 class Defender:
 2
       def __init__(self):
           self.P X1 ham = []
3
4
           self.P_X1_spam = []
           self.P_X0_ham = []
5
           self.P X0 spam = []
6
7
           self.Lo = []
8
           self.Lo0 = []
9
           self.Lo1 = []
           self.result = []
10
11
12
      def fit(self, train_x, train_y):
           rows, feature num = train x.shape
13
14
           self.P_X1_ham = np.zeros(feature_num)
           self.P X1 spam = np.zeros(feature num)
15
           self.P X0 ham = np.zeros(feature num)
16
17
           self.P_X0_spam = np.zeros(feature_num)
           self.Lo = np.zeros(feature num)
18
19
           self.Lo0 = np.zeros(feature_num)
           self.Lo1 = np.zeros(feature num)
20
21
22
           for i in range(feature_num):
23
               x spam = 0
24
               x ham = 0
               for j in range(rows):
25
                   if train_x[j,i]:
26
27
                       if train_y[j]:
28
                            x spam += 1
29
                       else:
30
                           x ham += 1
               self.P_X1_ham[i] = x_ham / ham_num
31
               self.P_X1_spam[i] = x_spam / spam_num
32
33
               self.P X0 ham[i] = 1 - self.P X1 ham[i]
34
               self.P_X0_spam[i] = 1 - self.P_X1_spam[i]
               self.Lo1[i] = Log(self.P X1 spam[i] / self.P X1 ham[i])
35
               self.Lo0[i] = Log(self.P_X0_spam[i] / self.P_X0_ham[i])
36
               self.Lo[i] = self.Lo1[i] - self.Lo0[i]
37
38
```

```
39
40
       def row attack(self, one sample):
           sort Lo = sorted(range(len(self.Lo)), key=lambda i: self.Lo[i])
41
42
43
           cost = 0
44
           sigmaLoX = 0
           for i,v in enumerate(one sample):
45
               sigmaLoX += self.Lo1[i] if v==1 else self.Lo0[i]
46
47
           if sigmaLoX < 0:</pre>
               return 0, one_sample
48
49
           for i in sort_Lo:
50
51
               if(self.Lo[i] >= 0):
52
                   return cost, one sample
53
               if one_sample[i]:
                   continue
54
55
               one_sample[i] = 1
               sigmaLoX += self.Lo[i]
56
57
               cost += 1
58
               if (sigmaLoX < 0):</pre>
59
                   return cost, one sample
60
61
62
       def defence(self, model, attacked x):
63
           for sample in attacked_x:
               if model. row predict(sample):
64
                   self.result += [1]
65
                   continue
66
67
               new matrix = [[]]
68
               for i in sample:
                   if i:
69
                        new\_row = [(x + [0]) for x in new\_matrix] + [(x + [1]) for x in new\_matrix]
70
71
                   else:
72
                        new_matrix_f = [(x + [0]) for x in new_matrix]
                   new_matrix = new_matrix_f
73
74
               new matrix = [np.asarray(x) for x in new matrix]
75
               realFroms = []
76
               for origin in new matrix:
77
                   _, attacked = self._row_attack(origin)
                   if np.array equal(attacked, sample):
78
79
                        if model. row predict(origin):
80
                            realFroms += [origin]
               if len(realFroms):
81
82
                   P_spam = 0
                   P ham = 0
83
                   for origin in realFroms:
84
85
                        for i in origin:
                            P spam *= self.P X1 spam[i] if i else self.P X0 spam[i]
86
87
                            P_ham *= self.P_X1_ham[i] if i else self.P_X0_ham[i]
88
                        P_spam += 1
89
                        P ham += 1
```

Adversarial attack analysis

```
1 from sklearn.metrics import confusion matrix
3 N = 10
4 X = get_feature(N, train_X)
5 Y = np.array(train Y)
6 X_test = get_feature(N, test_X)
7 Y_test = np.array(test_Y)
9 # Use original model to predict Y_test
10 botnet = BNB()
11 botnet.fit(X, Y)
12 Y pred origin = botnet.predict(X test)
13 print("Original classification report before attack")
14 print(classification_report(Y_test, Y_pred_origin, target_names = ["ham", "spam"]))
15 print("Confusion Matrix")
16 print(confusion_matrix(Y_test, Y_pred_origin))
17
18 # Assume that Attacker knows
19 # - original model's result: Y_pred_origin
20 # - original test words list: test X
21 # - oringinal test label: test_Y
22 # Using 'Add-Words' attack
23 hacker = Attacker()
24 hacker.cal_Lo(X, Y)
25 cost, X test attacked = hacker.attack(X test, Y test)
26 Y_pred_attacked = botnet.predict(X_test_attacked)
27 print("Original classification report after attack")
28 print(classification_report(Y_test, Y_pred_attacked, target_names = ["ham", "spam"]))
29 print("Confusion Matrix")
30 print(confusion matrix(Y test, Y pred attacked))
31 print(f"Average cost = {cost}")
32
33 # Denfender
34 antispam = Defender()
35 antispam.fit(X, Y)
36 Y_pred_defence = antispam.defence(botnet, X_test_attacked)
37 print("Original classification report after defence")
38 print(classification_report(Y_test, Y_pred_defence, target_names = ["ham", "spam"]))
39 print("Confusion Matrix")
```

```
40 print(confusion_matrix(Y_test, Y_pred_defence))
41 print(f"Average cost = {cost}")
```

```
Original classification report before attack
```

	precision	recall	†1-score	support
ham	0.96	0.98	0.97	242
spam	0.89	0.82	0.85	49
accuracy			0.95	291
macro avg	0.93	0.90	0.91	291
weighted avg	0.95	0.95	0.95	291

Confusion Matrix

[[237 5] [9 40]]

Original classification report after attack

	precision	recall	f1-score	support
ham	0.83	0.98	0.90	242
spam	0.29	0.04	0.07	49
accuracy			0.82	291
macro avg	0.56	0.51	0.49	291
weighted avg	0.74	0.82	0.76	291

Confusion Matrix

[[237 5] [47 2]]

Average cost = 1.7959183673469388

Original classification report after defence

	precision	recall	f1-score	support
ham	0.00	0.00	0.00	242
spam	0.17	1.00	0.29	49
accuracy			0.17	291
macro avg	0.08	0.50	0.14	291
weighted avg	0.03	0.17	0.05	291

Confusion Matrix

[[0 242]

[0 49]]

Average cost = 1.7959183673469388

/usr/local/lib/python3.7/dist-packages/sklearn/metrics/_classification.py:1272: Undefin _warn_prf(average, modifier, msg_start, len(result))

∢

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