

Design of Modular Cell Systems for Biocatalysis with Multi-Objective Optimization

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Abstract

Modular design has been the cornerstone of contemporary engineering, enabling efficient production of exchangeable parts that interact in a reproducible manner to constitute functional systems. In this proposed thesis, we transfer engineering modular design principles to the emerging fields of synthetic biology and metabolic engineering, that have promising applications to address problems related to health, energy, security, and the environment. In particular, we focus on microbial biocatalysis which has the potential to become a renewable and lower-cost replacement of traditional chemical synthesis processes. The thesis begins with an interdisciplinary review and perspective of the concepts, methodology, and applications of modular design. Then, a conceptual, mathematical, and algorithmic framework based on multi-objective optimization is developed to design modular cell biocatalysts. Genome-scale metabolic models that account for all known metabolic reactions of industrially-relevant organisms such as *Escherichia coli* and *Clostridium thermocellum* are used as a basis for simulation of biocatalytic strain phenotypes. In combination with these models, the proposed framework is used to design modular cell systems for renewable production of diverse biofuels and biochemicals. Overall this contribution addresses the current interest in modular design in synthetic biology through novel systematic principles and quantitative tools. We anticipate this modular cell design approach not only brings whole-cell biocatalysis closer to being an industrially competitive technology, but also provides tools to understand the natural modular architectures of metabolic networks designed by evolution for billions of years under physical and biological constraints.

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Chapter 1

Introduction

Vitalism was the notion that life arises from an essential principle that cannot be explained in terms of physical and chemical phenomena. Eduard Buchner's discovery of what would later be called enzymes during the late 19th century provided the final blow to vitalism, opening the door to great developments in our mechanistic understanding of living systems throughout the 20th century. However, it was not until the last few decades that bioengineers began to manipulate cellular DNA for diverse applications ranging from renewable chemical production to medical treatment. Despite recent success stories, such applied fields remain highly constrained by a lack of models with sufficient predictive and explanatory power to bridge the gap between first principles and emerging phenomena. Finding such models for biological systems might be an unprecedented challenge, and remains a remarkable opportunity for scientific discovery. In addition to this scientific challenge, our increasing capabilities to engineer biological systems need to be complemented by design principles and methods that will ensure efficient development of predictable devices. Among potential applications, biocatalysis technologies can broaden the accessibility of essential goods, such as food and medication, and reduce global warming, two issues that will likely become the major drivers of civil conflict during the 21st century [11, 94, 56].

The successful development of biocatalysis technologies depends on the use of genetic engineering techniques in combination with abstract systems engineering approaches. The most important concept is modern engineering is modular design. Computers, vehicles, factories, and many other complex devices are often assembled from exchangeable units

of self-contained functionality known as modules. By analogy with electrical engineering, synthetic biologist have aimed to build biological parts that enable modular assembly and re-usability in different contexts. However, most modularization efforts in this field have been applied qualitatively and in isolation to specific cellular components (e.g., modular metabolic pathways [14] or modular proteins [153]) rather than treating the cell as a chassis and enablers of desirable functions as modules. Hence, such approaches are difficult to generalize and do not explore the potential advantages of building whole-cell modular systems, such as platform strains for diverse chemical production. The primary aim of this thesis is to advance modular design principles in synthetic biology and metabolic engineering with emphasis on biocatalysis applications. Unlike previous modularization approaches, this work considers modular design at the system level and provides quantitative tools for its application. Chapter 2 reviews the engineering and bioengineering literature in depth to develop this overall view.

The contribution of this thesis is divided into three aspects: i) The development of general modular cell design principles and associated mathematical models (Chapters 2, 3); ii) the development of scalable algorithms to solve the mathematical models (Chapters 4, 5, 7); and iii) the application of the resulting modular cell design tool to understand driving principles of natural biological modularity and to design modular biocatalyst strains based on industrially-relevant hosts and production modules (Chapters 3, 5, 6, 7). In conclusion, the outcome of this research is to bring modularity principles proven in conventional engineering to metabolic engineering, leading to increased robustness and efficiency, thereby accelerating the strain engineering process that remains the major roadblock for widespread industrial application of microbial catalysis.

Chapter 2

Modular design: Concepts, methods, and applications in engineering, biology, and biotechnology

This chapter is based on the publication *Modular design: Implementing proven engineering principles in biotechnology*. Garcia, S., and Trinh, C. T. *Biotechnology Advances*, 2019. As first author I lead the development, implementation, and writing of this study.

Abstract

Modular design is at the foundation of contemporary engineering, enabling rapid, efficient, and reproducible construction and maintenance of complex systems across applications. Remarkably, modularity has recently been discovered as a governing principle in natural biological systems from genes to proteins to complex networks within a cell and organism communities. The convergent knowledge of natural and engineered modular systems provides a key to drive modern biotechnology to address emergent challenges associated with health, food, energy, and the environment. Here, we first present the theory and application of modular design in traditional engineering fields. We then discuss the significance and impact of modular architectures on systems biology and biotechnology. Next, we focus on the very recent theoretical and experimental advances in modular cell engineering that seeks to enable

rapid and systematic development of microbial catalysts capable of efficiently synthesizing a large space of useful chemicals. We conclude with an outlook towards theoretical and practical opportunities for a more systematic and effective application of modular engineering in biotechnology.

2.1 Introduction

Complex engineered systems such as computers, vehicles, or factories can be assembled from exchangeable units of self-contained functionality known as modules. Modular design enables efficient production, maintenance, and customization across modern engineering technologies. The inception of modular design has had a revolutionary impact on many industries. For instance, the first modular computer, named IBM System/360 and built in the 1960s, allowed to use the same software for different application-dependent hardware, shaping information technology as we know it today [179]. Undoubtedly, modular design will continue to drive innovation in both established and emergent fields of engineering.

Among trending engineering disciplines, biotechnology is encompassing far-reaching applications driven by the recent development of enabling technologies in interdisciplinary areas of genome engineering [12], systems and synthetic biology [105], metabolic engineering [172], and bioprocessing [46, 178]. Amid many applications to address issues related to health, energy, and the environment, the chemical industry will benefit from metabolic reprogramming of microbes as cell factories to catalyze the synthesis of therapeutics, chemicals, and fuels, from renewable and sustainable feedstocks (e.g., lignocellulosic biomass, sugar cane) or waste products (e.g., waste gas from steel manufacturing, plastic waste). Even though there exists a naturally large space of molecules that can be synthesized by metabolically engineered microorganisms [131], fewer than a dozen molecules are industrially produced [172]. A major roadblock is attributed to the very laborious and costly strain engineering process partly arising from the lack of standardization and repetition of genetic manipulation tasks [118, 263]. Recently, modular cell engineering has been proposed as an innovative approach to accelerate strain engineering process, harnessing a large space

of molecules derived from rich and diverse cellular metabolism and thus pushing whole-cell biocatalysis towards an industrially competitive technology [242].

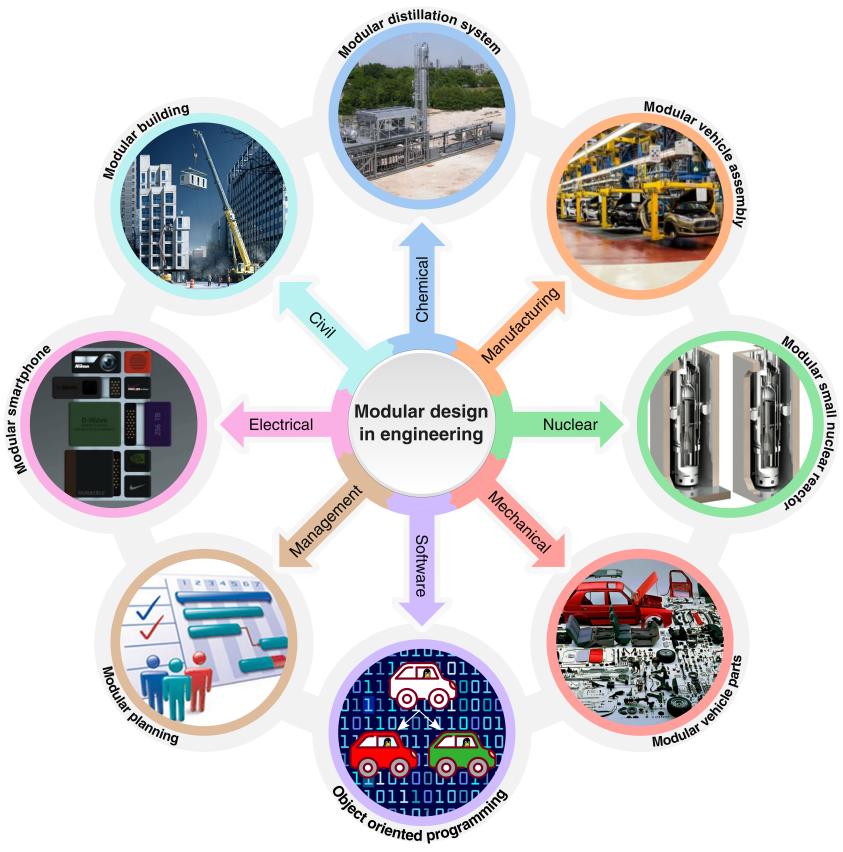
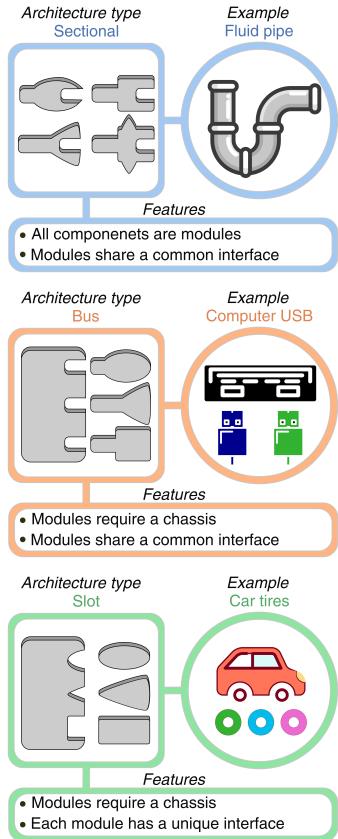
In this paper, we first examine the theory and application of modular design in conventional engineering disciplines, such as mechanical, chemical, nuclear, and civil engineering, with the aim to provide perspectives and innovative methods that can be transferred to biotechnology. We next present the importance of modularity that exists in natural biological systems. Finally, we highlight the most recent theoretical and experimental developments in modular cell design for synthetic biology and metabolic engineering applications.

2.2 Modularity in engineered systems

2.2.1 Basic concepts

Based on the definition by Miller and Elgard [162], a module is "an essential and self-contained functional unit relative to the product of which it is part. The module has, relative to a system definition, standardized interfaces and interactions that allow composition of products by combination". We find this definition, out of the many available [202], to be general yet descriptive enough to illustrate the topics in this paper. Based on the above definition, modules must have a standardized interface and exchangeability in order to enable rapid and systematic assembly of components into a system with various types of modular architectures [248]. A fully modular or sectional architecture has all the components to be modules, for instance, fluid pipes or sectional couches, while an integral architecture lacks any type of modules (Figure 2.1 A). Chassis-based architectures are also common in modular design, including bus and slot. The bus modular architecture uses the same interface for all modules, e.g., universal serial bus (USB) and peripheral component interconnect (PCI) ports found in computers, while the slot modular architecture has specific interfaces for corresponding modules, e.g., tires in an automobile. The chassis-based architectures enable the use of alternative chasses that can be combined with the same modules to efficiently generate a variety of products or vice versa [102].

A. Types of modular architecture B. Applications of modular design in engineering



C. General mathematical models for modular product design

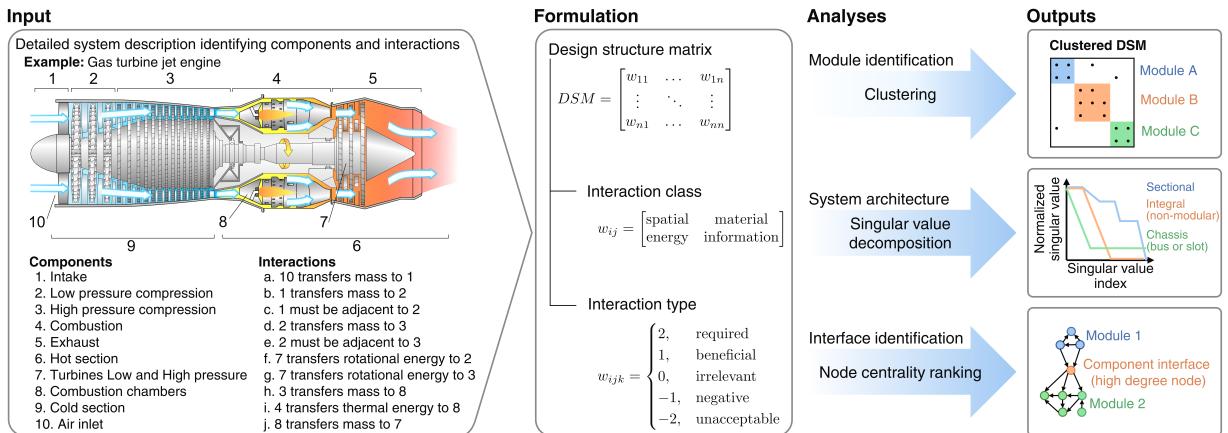


Figure 2.1: Modular design in engineering. (A) Common types of modular architectures. (B) Current applications of innovative modular design. (C) General mathematical framework of modular design. The input is illustrated with a gas turbine jet engine, that intakes air through the front section for heating and compression followed by air expansion to generate thrust. The interaction between system components can be formalized in a DSM model and analyzed to identify the most effective modules and interfaces.

2.2.2 Driving forces and potential tradeoffs of modular design

The driving forces for system modularization are to achieve increased efficiency and robustness, reduced complexity and cost, and better customization and maintenance options [20, 162]. Modular design has been the core of many innovative technologies across engineering disciplines (Figure 2.1 B). For instance, modularized plants in chemical engineering allow faster and more cost-effective deployment, making small operations viable and hence providing economic and environmental advantages [10, 115]. Likewise, modular buildings in civil engineering enable more rapid and economical construction [108]. In nuclear engineering, the use of small modularized reactors overcomes potential hazards of traditional large-scale operations, allows plant customization to energetic demand, and reduces construction and manufacturing costs [252]. The emerging area of highly automated manufacturing also implements modular production systems [258]. In addition, modular design principles have been applied with great success in abstract engineering disciplines such as software [2, 70] and management engineering [27]. The decomposition of software elements into modules of defined functionality is essential to manage complexity, ensure robustness, and allow for concurrent development. Similarly, organizations and projects can be structured into modules to accomplish parallel task execution and avoid repetition.

Even though modular design is ubiquitous, it may not be desirable or feasible in every circumstance. The disadvantages and limitations of modularity tend to be field specific. When modularity is part of an innovative approach, such as modular chemical plants, a lack of experience and higher upfront costs are regarded as common drawbacks [10]. Design constraints may also limit the applicability of modularity; for example, a quantitative study [97] suggested that the portability requirements of cell phones and laptops makes them less modular than their static counterparts. In the case of buildings and chemical plants, the size of components may prevent off-site modular manufacturing if transportation is unfeasible. Thus, when choosing modular design for engineering applications, it is important to ensure that advantages outweigh disadvantages.

2.2.3 Theoretical frameworks of modular design

Modular product design is complex and field-specific but can be generally formulated using the language of graph theory. The Design Structure Matrix (DSM) [23] is a commonly used technique to model a system as a graph, where nodes represent basic components and links between nodes describe their functional interactions. Component interactions can be represented in a binary manner (i.e., whether a relationship exists or not) or in a detailed complex fashion with multiple dimensions and values to increase model accuracy. For example, with a complex interaction, a metric can be used to quantitatively assign interaction desirability between two components, i.e., a high desirability score if they require each other to work or a negative desirability score otherwise. In some cases, detailed interaction types can also be classified and integrated in the modular design; for example, a cooling system with a radiator and a fan is required to have not only a *spatial* interaction (i.e., both elements need to be in close proximity) but also a *material* interaction (i.e., the fan provides airflow across the radiator) (Figure 2.1 C) [91].

DSM can reveal properties of the system through different analyses, including singular value decomposition to capture the modular architecture type (e.g. integral, chassis-based, bus, or slot) [97], node centrality ranking to identify key interactions between modules and interfaces [218], and most importantly, clustering to identify modules (Figure 2.1 C). While many approaches exist to cluster a DSM, not all can successfully identify modules due to underlying design conflicts in product modularization; for these scenarios, integrated use of a highly descriptive DSM model to account for complex interactions and multi-objective optimization to identify Pareto optimal solutions is needed to accurately design modular systems [91].

2.3 Modularity in biological systems

In the high-throughput and quantitative era of biology, modularity has become a fundamental abstraction in understanding and redesigning biological systems that have existed and evolved for billions of years [87, 254]. A variety of definitions of biological modules co-exist, arising from the multi-scale and multi-interaction nature of biological systems. From a

mathematical perspective, two general approaches are commonly used to define modules: (i) modules as clusters of highly interconnected nodes in a biological interaction network, and (ii) modules as programmable circuits that can be described with laws of mass and energy conservation and control theory. These paradigms differ in that network modules provide a holistic and simplified description, while circuit modules provide a reductionistic and detailed description. Despite their differences, both approaches seek to understand the evolutionary origin of modules, their role in fundamental biological properties such as robustness and evolvability, and their biotechnological applications.

2.3.1 Modularity exists across all scales of biology

Modularity is a ubiquitous organizing principle across all scales of biology. Within a scale, modules often interact in a hierarchical manner (Figure 2.2). At the molecular level, DNA transcription activation and rate can be controlled by a variety of modular promoter elements [58]. Additionally, certain proteins are highly modular, such as enzymes (e.g., polyketide synthase and non-ribosomal peptide synthetase [95]) with modular substrate identification elements that enable biosynthesis of a large space of secondary metabolites [113]. At the cellular level, modularity is present in all biomolecule interaction networks [164], including RNAs [221], proteins [219], and metabolites [193]. In all cases, modules are associated with specific cellular functions or pathways, which often interact in a hierarchical manner [193]. At the multi-cellular level, organs and tissues are also structured modularly. For example, in the human brain, neuron interaction networks contain modules associated with specific cognitive functions [220]. These modules are hierarchically organized into submodules to integrate and contextualize specialized functions of the brain [160]; for instance, visual perception that requires the functional integration of multiple neuron clusters in the cortical columns [183]. At the ecological scale, organism communities can be represented by networks, where nodes are species or subpopulations and links are interactions such as consumption, pollination, or competition [82]. The capability of ecological networks to avoid global failure due to small perturbations has been attributed to their modular structure both theoretically [82] and experimentally [79].

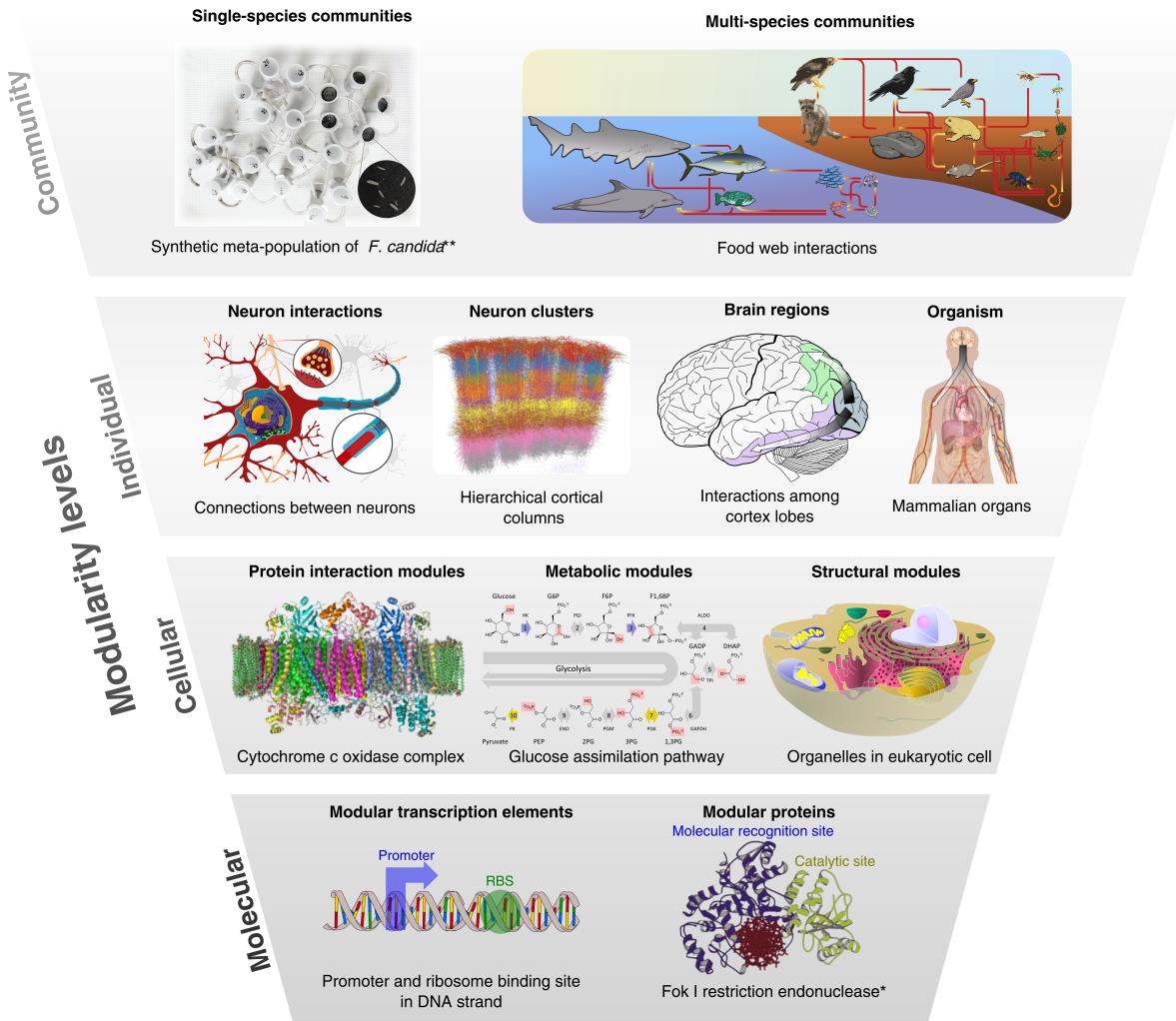


Figure 2.2: Hierarchical modularity across all scales of biology. Images marked with * and ** are adapted from Khosla and Harbury [113] and Gilarranz *et al.* [79], respectively.

2.3.2 Modularity explains functions of components and interactions of biological systems

Prior to the systems biology era, the view of modular biological systems can be traced back as early as the late 19th century with the initial study of what later became known as glycolysis to investigate how yeast fermentation made wine have a good taste. Throughout the first half of the 20th century, the complete knowledge of many major metabolic pathways of well-defined functionality across organisms, including the EMP pathway, the Entner-Doudoroff

pathway, Krebs cycle, pentose phosphate pathway, and so on, was established. These pathways were mapped to qualitatively describe the modular interconnection of functional elements within a cell, i.e., cellular metabolism that governs cell physiology. Pioneering work in the 1980s, including the comprehensive description of measurable bacterial cellular components [168] and constraint-based simulations of microbial metabolism [64], helped establish a foundation for quantitative modular analysis of cell physiology. With the explosion of high-throughput ‘omics technologies in the late 90’s, complex biological systems with thousands of interacting elements can now be studied holistically and quantitatively at multiple levels from genes to proteins and metabolites within the cell and microbial communities [198, 145, 184, 262]. Graphs (or networks) can represent these systems [5] and their complex interactions, e.g., metabolites-enzymes [149, 193], genes-diseases [80], protein-protein [223], or a combination of all known protein and genetic interactions [33]. Module analysis of biological networks can provide two insights: (i) identification of modules that represent transferable and self-contained functions [164], for example, a *cis*-regulatory element and its associated genes [176], the subunits of a protein complex [83, 88], and the genes associated with a disease phenotype [80], and (ii) interactions among modules of a system. For example, by analyzing the metabolic networks of 43 organisms, Ravasz *et al.* [193] identified a hierarchical modular architecture containing hubs of highly connected metabolites and modules with specific metabolic functions. Remarkably, the identified architecture overlaps with the known primary and secondary metabolic pathways. Likewise, by analyzing metabolic networks of 63 organisms, Ma and Zeng [149] could identify a bow-tie architecture of the network containing a core of highly interconnected components linking input and output node clusters. Graph-based analysis of metabolic networks also revealed a small-world architecture (i.e., a small number of reactions between any two metabolites) that was hypothesized to confer cellular metabolism with the capability to quickly adapt to perturbations [253].

2.3.3 Modularity is a foundational tool to control programmable cells

Genetic circuits are modules that define a universal programming language of cells, such as logical gates [22, 172], and can be widely found in natural biological systems. Classical examples of genetic circuits are the lac operon that enables carbon catabolite repression in bacteria and the MAPK/ERK signaling pathway in mammalian cells that controls cell division among other cellular functions. Modularity of natural signaling pathways can be harnessed for novel functions [139, 189], including the production of valuable metabolites, synthesis of nanomaterials, treatment of disease, and sensors to detect hazardous molecules [22]. The laws of mass and energy conservation and principles of control theory that have been well developed in traditional engineering disciplines can be applied to enable modular design of synthetic biological systems. For instance, Del Vecchio *et al.* [53] developed a mathematical model of retroactivity that captures the impact of a downstream module on the function of an upstream module, and used this model to enhance module insulation. Even though synthetic genetic circuit modules operate correctly and reliably in an isolated environment, it remains challenging to integrate these modules into complex systems [190].

2.3.4 Modularity enables evolutionary advantage and robustness

Biological robustness is the ability of a system to maintain its function upon genetic and environmental perturbations. Both the graph- and circuit-based descriptions of modules [259] can help explain their contributions to system robustness. For example, the bow-tie architecture of biological networks [68] has been suggested [119] to enhance the biological robustness of chassis-based modularity, where the essential core processes belong to the conserved chassis and adaptable modules allow for evolution to experiment safely. This view, however, raises the question of the evolutionary origin and function of modules. It has been hypothesized that modules may arise due to natural selection or biased mutational mechanisms. Computational studies on the topic are abundant but compatible with both hypotheses [254]. Several models have suggested that when a single fitness goal is present, a modular architecture does not emerge since it does not provide a fitness advantage. However,

when multiple fitness goals are pursued, either sequentially [110] or simultaneously [39], a modular architecture is favored. Additionally, it has been demonstrated that macroscopic [216] and molecular [208] phenotypes are weighted combinations of optimal phenotypes specialized for single tasks. This view is important in the context of modular cell engineering that can be formulated as a multi-objective optimization problem [73], where each fitness goal corresponds to a module for making a desirable chemical. Thus, modular cell engineering can harness the existing features of biological modularity instead of creating entirely synthetic properties.

2.4 Modular cell engineering

Diverse and complex cellular metabolism encompasses a large space of molecules, providing a potential path towards broader industrialization of biology [45]. To realize this potential, rapid development of novel microbial biocatalysts to efficiently synthesize these molecules is critical but faces multiple challenges due to laborious and costly requirement of extensive strain optimization cycles [172, 242]. Effective exploitation of modular design as seen in natural and engineered systems for biocatalyst development can offer innovative strategies to tackle these challenges.

To date, modular cell engineering has been mostly applied at the pathway level, where enzyme module expression is adjusted to increase target metabolite production. This topic has been extensively reviewed [14, 100, 147, 266] and will not be elaborated in detail here. At the cellular level, platform strains engineered to eliminate common byproducts and increase availability of important precursors for overproduction of target molecules have been reported with some success by implementing the conventional “push-and-pull” metabolic engineering strategy [172]. More recently, a system-level modular cell design method has been developed to systematically and simultaneously design both the chassis cell and production modules for the synthesis of various target chemicals [73, 241]. Unlike conventional strain optimization methods that target one product, modular cell design seeks to enable rapid and predictable creation of multiple production strains to achieve superior performance with minimal strain optimization cycle where each synthesizes a different product. Each

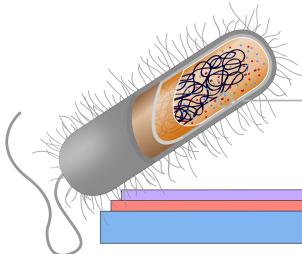
optimal production strain is obtained by assembling a reusable modular (chassis) cell with an exchangeable production module(s) in a plug-and-play fashion, resembling the advantages of modular design in traditional engineering disciplines. Specifically, a modular cell contains core metabolic phenotypes shared among production modules (Figure 2.3 A). The chassis interfaces with the modules through enzyme synthesis machinery and precursor metabolites (Figure 2.3 B). Modules contain auxiliary regulatory and metabolic pathways (Figure 2.3 C) that enable a desired phenotype for optimal biosynthesis of a target molecule, such as growth-coupled-to-product formation (*GCP* design) or stationary-phase product synthesis (*NGP* design) (Figure 2.3 D). These design principles are formulated to integrate state-of-the-art techniques developed in the fields of synthetic biology and metabolic engineering, including, (1) computational models that identify genetic interventions towards desirable phenotypes, (2) rapid discovery and optimization of metabolic pathways for target product synthesis (i.e., production modules), and (3) design of minimal cells and orthogonal pathways to generate a toolkit of parts that can be assembled into various functional systems.

In the following sections, we highlight the recent advancements in modular cell engineering that capture: (1) design principles and computational tools to enable construction of a modular cell and associated production modules, (2) discovery and optimization of metabolic pathways as production modules both theoretically and experimentally, and (3) experimental implementation of modular cell design principles.

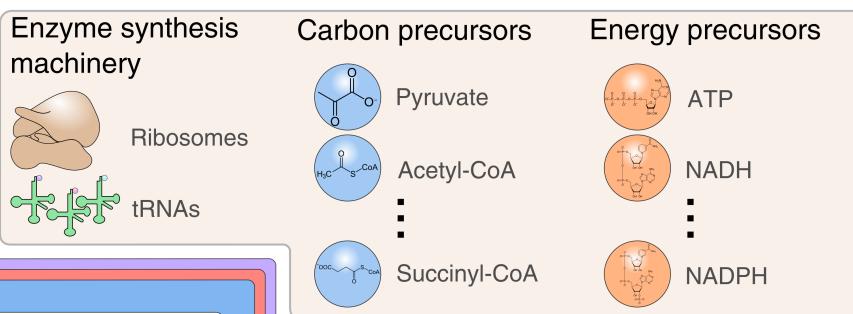
2.4.1 Recent developments in mathematical formulation of modular cell design

The primer for the modular cell design principles started with the observation [238] that the optimal design of the n-butanol- and isobutanol-producing *E. coli* cells, based on constraint-based modeling [180] and conventional strain design methods [244], exhibited the same core metabolism (Figure 2.4 A-B). To systematically explore this property, the first modular cell design method, called MODCELL, was proposed and used to design an *E. coli* modular cell for alcohol and ester production [241] (Figure 2.4 E). In Chapter 3 a new formulation of the modular cell design problem, ModCell2, based on multi-objective optimization will be

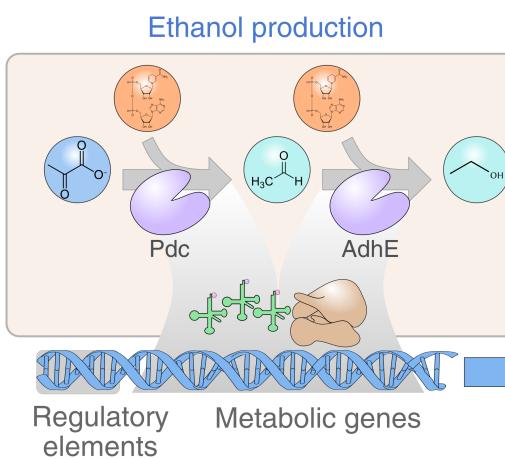
A. Chassis



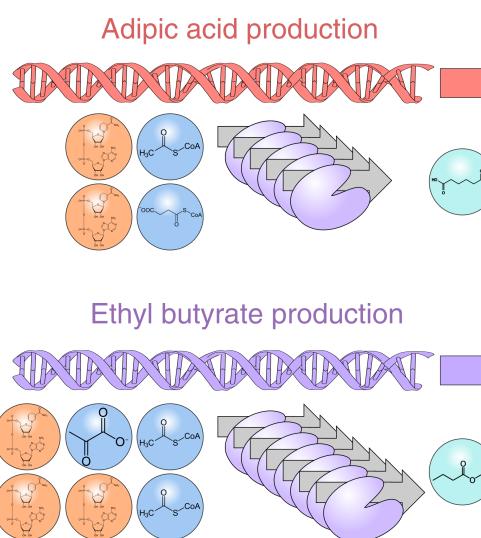
B. Interfaces



C. Modules



D. Production strains



Common design phenotypes:

- **GCP design:** growth-coupled to product formation
- **NGP design:** non-growth phase production

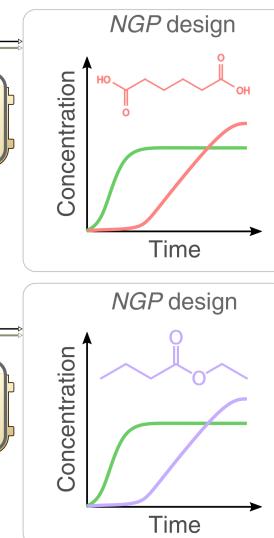
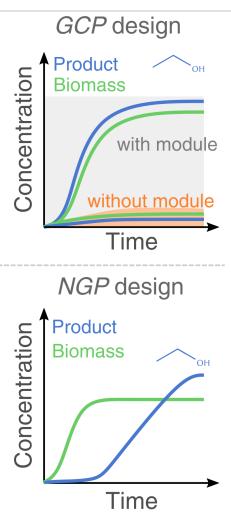


Figure 2.3: Generalized concept of modular cell design. **(A)** Modular (chassis) cell. **(B)** Interfaces. **(C)** Production modules. **(D)** Production strains. A modular cell is designed to provide the necessary precursors for biosynthesis pathway modules that are independently assembled with the modular cell to generate production strains exhibiting desirable phenotypes.

developed to design strains with minimal trade-off between compatibility, performance, and robustness (Figure 2.4 H).

While ModCell2 is to our knowledge the only tool that involves simultaneous design of chassis, modules, and interfaces, other recently developed computational tools can be applied to design these elements individually. For example, MinGenome [257] is used to design genomes of minimal cells that can serve as chassis whereas ValveFind [181] enables design of orthogonal pathways to build production modules. Topics on model-guided strain design techniques for “integral” strains, .i.e, strains optimized for production of only a single product, can be found in recent excellent reviews. [144, 152, 170].

Future development of modular cell design tools will incorporate enzyme kinetics of cellular metabolism [117, 175] to account for potential metabolic burdens [264] in the design of modular cells and exchangeable production modules (Figure 2.4 I). Enzyme cost analysis is also particularly useful for identifying robust strategies for adaptive laboratory evolution that prevent an unintended pathway(s) to be optimized instead of a targeted pathway(s) [55]. The lack of experimental data on enzyme catalytic efficiencies needed for these modeling approaches can be addressed through random parameter sampling [55], *omics* integration [59, 112], and machine learning [89]. Recently developed models that predict *in-vivo* enzyme concentrations from the genetic sequence help bridge the gap between metabolic model predictions and experimental implementation [61, 159, 201].

2.4.2 Recent advances in discovery and optimization of metabolic pathways as production modules

With the arrival of quantitative ‘omics era in mid 1990s, we started to gain a deeper understanding of complex biological systems and categorize them into the functional biological parts, i.e., regulatory and functional genes for retrieval through development of biological databases (e.g., Registry of Standard Biological Parts (<https://parts.igem.org>), KEGG [109], Biocyc [30], Brenda [205], among many others). Synergistically, the interdisciplinary areas of bioinformatics, synthetic biology, metabolic and protein engineering have also emerged, advanced, and now enabled rapid and systematic identification and

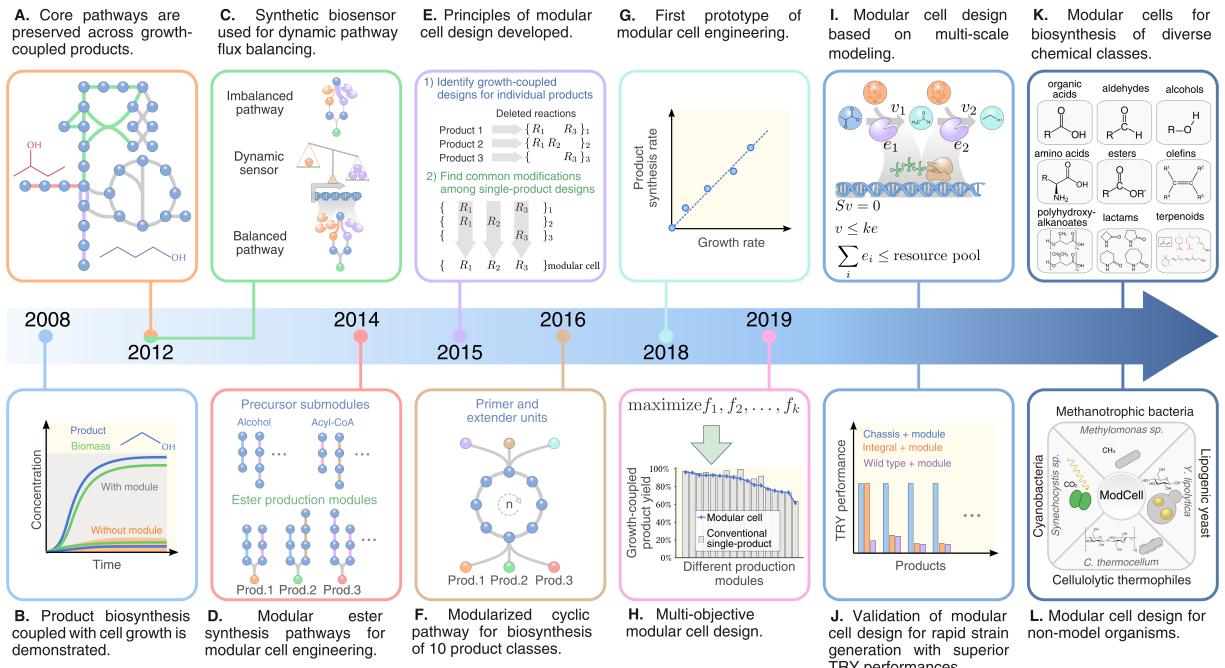


Figure 2.4: Key advances and opportunities in the design and implementation of modular cells and exchangeable production modules. (A) The same core metabolic pathways were revealed for butanol and isobutanol growth-coupled production based on elementary mode analysis [238]. (B) An *E. coli* cell with minimal metabolic functionality designed to require product (ethanol) synthesis for cell growth was experimentally validated [243]. (C) A dynamic sensor-regulator system was designed and implemented to balance metabolic fluxes for enhanced biosynthesis of fatty acid-derived molecules [275]. (D) A modular ester fermentative pathway platform derived from alcohol and acyl-CoA pathway submodules was designed and experimentally demonstrated in a chassis strain [127]. (E) First modular cell design method, named MODCELL, was proposed and used to design 3 modular cells for the production of a group of alcohols and derived esters [241]. (F) Carbon and energy efficient cyclic pathway was developed to synthesize 10 product classes from a variety of primer and extender precursors [36]. (G) Prototypes of modular cell engineering were demonstrated for growth-coupled to product synthesis predicted by MODCELL [241] and pathway optimization by adaptive laboratory evolution [261]. (H) Multi-objective optimization-based modular cell design method, named ModCell2, will be developed in Chapter 3 and used to reveal negligible trade-offs between modular and integral designs. (I) Next-generation of modular cell design framework is proposed to account for enzyme biosynthesis cost using metabolism and expression (ME) or kinetic models with enzyme constraints. (J) Experimental demonstration of rapid and systematic generation of modular production strains with many different types of production modules to achieve superior performances over the wildtype and single-product (integral) strains in terms of titer, rate, and yield (TRY). (K) Design of a universal modular cell compatible with a large and diverse space of production modules. (L) Future demonstration of modular cell design is proposed for industrially-relevant, non-model organisms with difficult-to-transfer phenotypes, such as efficient assimilation of CO₂, CH₄, or cellulose.

assembly of these biological parts into production modules to probe a large space of molecules that are only limited by one's imagination. Nowadays, development of production modules can start by using computational tools with increasing scope and accuracy [125, 256], that help identify metabolic steps, associated enzymes, and genetic parts (i.e., promoters, terminators, ribosome binding sites, regulatory/sensory elements, and so on) using a combination of elementary reaction rules, yield, thermodynamic, and biophysical analyses [57, 125]. Next, the genetic parts can be synthesized, assembled, and characterized for accuracy in a rapid manner to build production modules to make desirable molecules in a target host [6, 17, 18, 34, 43, 78, 122, 137, 134, 213, 245, 247, 276]. Some recent achievements, highlighting innovations in retrofitting cellular metabolism for novel biocatalysis from sustainable feedstocks, include: (i) redirection of central metabolism to make environmentally friendly, non-natural bioplastics [194], (ii) redesign of fermentative pathways to produce a large space of designer bioesters used as flavors, fragrances, biofuels, and solvents [127, 198] (Figure 2.4 D), (iii) repurposing of the beta-oxidation pathway for combinatorial biosynthesis of alcohols, dicarboxylic acids, hydroxyl acids, and lactones as industrial platform chemicals [36] (Figure 2.4 F), and (iv) refactoring of polyketide and isoprenoid pathways to explore a large space of secondary metabolites as drugs [3, 69, 156].

While the design, construction, and characterization of production modules can be streamlined, compatibility between the modules and a target host has always posed a significant challenge mainly due to the intricate flux imbalance resulting in low product titers, rates, and yields [172]. In the case of heterologous enzyme expression, undesirable regulatory interactions at the transcriptional and metabolic levels might hinder the pathway operation in a new host. This problem can be addressed by refactoring pathways into isolated orthogonal modules that are independent of the source organism regulation and do not interfere with heterologous host regulation [69, 203, 225, 227]. In most design scenarios, even after regulatory issues are addressed, metabolic flux imbalance is likely to occur due to the differences in expression and catalytic efficiencies of pathway enzymes. Metabolic flux balancing of engineered pathways is a combinatorial optimization problem that requires modification of gene expression elements (e.g., promoters, ribosome binding sites, etc.) and enzyme engineering to achieve the desired fluxes. Currently, this combinatorial problem

is often tackled in two ways: (i) identification of key design variables and screening and (ii) pathway selection. The search space in variable screening approaches can be reduced by pathway-level modularization, known as Multivariate Modular Metabolic Engineering [14, 100, 266]. Screening approaches can be effort-intensive and impractical for certain scenarios due to the extensive strain characterizations required to effectively sample the design space. Additionally, these approaches may not be able to solve poor pathway-host interactions where precursor metabolite(s) of the pathway of interest becomes the bottleneck. Alternatively, simultaneous host and pathway optimization can be accomplished by adaptive laboratory evolution, provided that a simple selectable phenotype such as growth is tightly coupled with the desirable product synthesis phenotype. For example, Wilbanks *et al.* [261] recently demonstrated a linear correlation between growth rate and product synthesis rate for computationally designed growth-coupled strains [241] (Figure 2.4 G). Pathway optimization through growth-coupled design has been applied successfully [66], and a recent computational study suggest its applicability to many different products and organisms. [250] Modular cell design is compatible with the two described module optimization tools; particularly, the design of a chassis growth-coupled to its production modules can enable rapid optimization of diverse pathways.

2.4.3 Recent advances in the experimental implementation of modular cell design

Experimental implementation of modular cell design is still at infancy of validation. Construction of modular cells can be implemented by two methods: (i) top-down approach that aims to remove undesired phenotypes from a naturally existing organism under defined environmental conditions [243, 239] and (ii) bottom-up approach that seeks to create a new organism derived from a synthetic minimal cell. [96] These two methods draw the same analogy as those in the engineering modular design, classified as “product modularization” and “design with modules” [20]. In the “product modularization” approach like the “top-down” approach, the chassis, modules, and interfaces are simultaneously designed either by defining functional carriers and interfaces as part of the design (*ex ante* design) or by

clustering existing functions into modules (*ex post* design). Alternatively, in the “design with modules” approach like the “bottom-up” approach, a product is designed out of a collection of predefined compatible parts; for example, the design of a personal computer that is assembled from the existing modules, including a motherboard, a graphic card, a monitor, etc., with standard interfaces. In the modular cell design context, a minimal cell can function as chassis whereas orthogonal refactored pathways that function as modules are independently designed and combined with the chassis to build modular production strains with desirable phenotypes.

To date, all recent computational [73, 241] and experimental [127, 261] efforts in implementing modular cell design have been focused on the top-down approach, since it is more feasible and accessible with the current knowledge and available genetic tools. Even though the bottom-up approach is much more challenging [96], the design principles developed for top-down construction can be applied to create bottom-up minimal modular cells, which would be less prone to failure due to their simpler architecture. Regardless of which approach is chosen, the underlying genotypes essential to target product synthesis appear to be conserved, according to the recent surveys of over two decades of metabolic engineering reports [118, 263]. This suggests that modular cell design can serve as a unifying platform for rapid strain engineering (Figure 2.4 J).

An anticipated challenge of modular cell design is that the chassis must provide enough precursor metabolites and enzyme synthesis machinery to support the target flux through each module. This issue may become increasingly difficult as the biochemical diversity and number of products supported by a single chassis expands (Figure 2.4 K). Recent developments in biosensors coupled with gene expression regulation tools [142, 161, 166, 268, 275] can achieve tunable control over the host metabolism to meet the requirements of each production module (Figure 2.4 C). In practice, such regulatory elements may be implemented in the host or as a part of specific modules.

2.5 Conclusions

Inspired by natural and conventional engineering modularity, bioengineers have started applying modular design principles to engineer biological systems at genetic, enzymatic, and cellular levels. Modular cell design aims to integrate all three levels for rapidly creating novel microbial biocatalysts in a plug-and-play fashion with minimal strain optimization cycles. Advancements in genome reading [81], writing [29, 123], and editing [12] will provide a unique opportunity to streamline modular cell engineering that effectively harnesses a large space of molecules from cellular metabolism using single organisms or microbial consortia, especially from non-model organisms with industrially-relevant but not-easy-to-transfer traits (Figure 2.4 L) [1, 28, 107, 148, 230]. Particularly, these advancements help streamline the construction of modular cells and exchangeable production modules from both top-down and bottom-up approaches. To further advance modular cell engineering, it is important not only to optimize the interfaces between production modules and modular cell but also to account for robustness and evolvability towards desirable engineered phenotypes. By combining proven engineering methods rooted in the physical and chemical laws with system modeling frameworks (e.g., Pareto optimality theory, graph theory), we can elucidate the modular design principles in biology from natural systems to engineered ones, leading towards fundamental understanding of essential rules of life and broader industrialization of biology.

Chapter 3

Formulation of conceptual and mathematical framework to design modular cells

This chapter is based on the publication *Multiobjective strain design: A framework for modular cell engineering.* Garcia, S., and Trinh, C. T. *Metabolic Engineering*, 2019. As first author I lead the development, implementation, and writing of this study. Supplementary Files S1 and S2 are provided in Appendix A and B respectively, while Supplementary Files S3, S4, and S5 are provided as attachments.

Abstract

Diversity of cellular metabolism can be harnessed to produce a large space of molecules. However, development of optimal strains with high product titers, rates, and yields required for industrial production is laborious and expensive. To accelerate the strain engineering process, we have recently introduced a modular cell design concept that enables rapid generation of optimal production strains by systematically assembling a modular cell with an exchangeable production module(s) to produce target molecules efficiently. In this study, we formulated the modular cell design concept as a general multi-objective optimization problem with flexible design objectives derived from mass action. We developed algorithms and an

associated software package, named ModCell2 to implement the design. We demonstrated that ModCell2 can systematically identify genetic modifications to design modular cells that can couple with a variety of production modules and exhibit a minimal tradeoff among modularity, performance, and robustness. Analysis of the modular cell designs revealed both intuitive and complex metabolic architectures enabling modular production of these molecules. We envision ModCell2 provides a powerful tool to guide modular cell engineering and sheds light on modular design principles of biological systems.

3.1 Introduction

Engineering microbial cells to produce bulk and specialty chemicals from renewable and sustainable feedstocks is becoming a feasible alternative to traditional chemical methods that rely on petroleum feedstocks [172]. However, only a handful of chemicals, out of the many possible molecules offered by nature, are industrially produced by microbial conversion, mainly because the current strain engineering process is laborious and expensive for profitable biochemical production [242]. Thus, innovative technologies to enable rapid and economical strain engineering are needed to harness a large space of industrially-relevant molecules [45].

The modular organization of biological systems has been a source of inspiration for synthetic biology and metabolic engineering [190, 204]. Modular pathway engineering breaks down target pathways into tractable pathway modules that can be finely tuned for optimal production of desirable chemicals [14, 266]. Harnessing combinatorial pathways (e.g., fatty acid biosynthesis, reverse beta oxidation, polyketide or isoprenoid biosynthesis) is one excellent example of modular pathway engineering. These pathways contain metabolic similarity (or combinatorial characteristics) such as a group of common specific enzymes capable of catalyzing linear reaction steps [198] and/or elongation cycles [36, 246, 265] and hence are capable of producing a large library of unique molecules [169]. Since these molecules are derived from a common precursor metabolite(s), the optimal production strains often share common genotypes and phenotypes, and hence, the costly strain optimization process is only performed once for these molecules. Remarkably, this advantageous strain optimization

strategy can be applied even for production of molecules derived from different precursors, using the concept of modular cell (ModCell) design [241, 242, 261].

With the arrival of steady-state, constraint-based stoichiometric models of cellular metabolism, various computational algorithms have been developed to guide strain engineering [38, 144, 267]. These methods have featured the design of strains capable of growth-coupled product synthesis (*GCP*), enabling adaptive laboratory evolution of these designed strains to enhance product titers, rates, and yields [66, 266, 244, 261]. Two approaches on growth-coupled production have been formulated - one based on the coexistence of maximum growth and product synthesis rates during the growth phase [24] and the other based on the obligate requirement of optimal product synthesis in any growth phase [243]. The distinction between these two types of growth coupling are also referred to weak coupling (*wGCP*) and strong coupling (*sGCP*) [120, 267].

Development of most strain design algorithms has been focused on overproduction of only one target molecule. The first algorithm proposed for modular cell design compatible for overproduction of multiple target molecules is MODCELL [241], which guided several experimental studies [128, 127, 129, 260, 261]. It works by generating *sGCP* strain designs for each target product based on elementary mode analysis [237], and then comparing the design strategies of different products to identify common genetic modifications among them. A similar approach was adapted in a subsequent work [103]. For MODCELL to find optimal solutions for multiple target products, it requires: 1) enumerating all possible designs above a predefined minimum product yield and with minimal reaction deletion sets for each production network, which might lead to a large number of solutions for each network and hence make the problem computationally intractable, and 2) the resulting designs for all products must be compared to identify common interventions, which is a computationally-hard, set-covering problem. Thus, the current enumerative approach of MODCELL might become intractable very quickly, especially for large-scale metabolic networks and potentially generate non-optimal designs, i.e., requiring more knock-outs than necessary or including fewer products than possible.

In this study, we generalized the concept of modular cell design and addressed the computational limitation of implementing it. We developed a novel computational platform

(ModCell2), based on multi-objective optimization and analysis of mass action of cellular metabolism, to guide the design of modular cells for large-scale metabolic networks. We demonstrated that ModCell2 can systematically identify genetic modifications to design modular cells that can couple with a variety of production modules and exhibit a minimal tradeoff among modularity, performance, and robustness. By analyzing these designs, we further revealed both intuitive and complex metabolic architectures enabling modularity in modular cell and production modules required for efficient biosynthesis of target molecules.

3.2 Methods

3.2.1 Design principles of modular cell engineering

In the conventional strain engineering approach, a parent strain is genetically modified to yield an optimal production strain to make only a target product. To produce each new molecule, the design-build-test cycles of strain engineering must be repeated, which is laborious and expensive (Figure 3.1). To minimize the cycles, modular cell engineering is formulated by genetically transforming a parent strain into a modular (chassis) cell that must be assembled with exchangeable modules to create optimal production strains [241]. A modular cell is designed to contain core metabolic pathways shared across designed optimal production strains. Exchangeable modules are production pathways designed to synthesize desirable chemicals. A combination of a modular cell and a production module(s) is required to balance redox, energy, and precursor metabolites for sustaining cellular metabolism during growth and/or stationary phases and exhibiting only desirable phenotypes. Practically, modular cell engineering can be applied to monocultures and polycultures, where a production module(s) can be embedded in a modular cell and activated by intracellular and/or extracellular cues such as light and/or signaling molecules.

Features	Conventional strain engineering	Modular cell engineering
Parent strain		
Modular cell	Absent	
Exchangeable modules	1	k
Optimal production strains		
Design-build-test cycle	Repeated for every new product	One time for many products

Figure 3.1: Comparison between the conventional single-product strain design and modular cell engineering. In the conventional approach, each target product requires to go through the iterative optimization cycle. The modular cell engineering approach exploits common phenotypes associated with high product titers, rates, and yields; and hence, the strain optimization cycle only needs to be performed once for multiple products, which helps reduce the cost and time of strain development.

3.2.2 Multi-objective strain design framework for modular cell engineering

For modular cell engineering, we seek to design a chassis cell compatible with as many production modules as possible to achieve only desirable production phenotypes while requiring minimal genetic modifications. Since all production modules must leverage cellular resources of the modular cell (e.g. precursor metabolites, cofactors, and energy), they form competing objectives. Therefore, the framework of modular cell engineering can be formulated as a multi-objective optimization problem, named ModCell2, as described below.

$$\underset{y_j, z_{jk}}{\text{maximize}} \quad (f_1, f_2, \dots, f_{|\mathcal{K}|})^T \quad \text{subject to} \quad (3.1)$$

$$f_k \in \arg \max \left\{ \sum_{j \in \mathcal{J}_k} c_{jk} v_{jk} \quad \text{subject to} \right. \quad (3.2)$$

$$\sum_{j \in \mathcal{J}_k} S_{ijk} v_{jk} = 0 \quad \text{for all } i \in \mathcal{I}_k \quad (3.3)$$

$$l_{jk} \leq v_{jk} \leq u_{jk} \quad \text{for all } j \in \mathcal{J}_k \quad (3.4)$$

$$l_{jk} d_{jk} \leq v_{jk} \leq u_{jk} d_{jk} \quad \text{for all } j \in \mathcal{C} \quad (3.5)$$

$$\left. \begin{array}{l} \text{where } d_{jk} = y_j \vee z_{jk} \\ \end{array} \right\} \quad \text{for all } k \in \mathcal{K}$$

$$z_{jk} \leq (1 - y_j) \quad \text{for all } j \in \mathcal{C}, k \in \mathcal{K} \quad (3.6)$$

$$\sum_{j \in \mathcal{C}} z_{jk} \leq \beta_k \quad \text{for all } k \in \mathcal{K} \quad (3.7)$$

$$\sum_{j \in \mathcal{C}} (1 - y_j) \leq \alpha \quad (3.8)$$

where i , j , and k are indices of metabolite i , reaction j , and production network k , respectively; f_k is a design objective for network k ; c_{jk} represents the cellular objective for reaction j in network k associated with a design objective defined in (3.9 - 3.11); v_{jk} (mmol/g DCW/h) is metabolic flux of reaction j bounded by l_{jk} and u_{jk} in network k , respectively; y_j and z_{jk} are binary design variables for deletion reaction j and module reaction j in network k , respectively; α and β_k are design parameters for deletion and module reactions, respectively; S_{ijk} is a stoichiometric coefficient of metabolite in reaction j of network k ; and C (3.5) is the candidate reaction set (Supplementary File S1). The goal of the optimization problem is to simultaneously maximize all design objectives f_k .

Steady-state mass balance constraint of cellular metabolism

Quasi steady-state flux balance of cellular metabolism (3.3) is used as metabolic constraints for (3.1).[188]. A model corresponding to each modular production strain (i.e. production network k) will be derived from a parent strain (i.e. parent network) by adding necessary

reactions (e.g., a production module) to produce a target molecule. A feasible flux distribution for each production network is described by mass balance (3.3) and reaction flux bounds (3.4-3.5). For a given production network, the phenotypic space can be illustrated by the gray area that is projected onto the two-dimensional space spanned by product synthesis and growth rates (Figure 3.2).

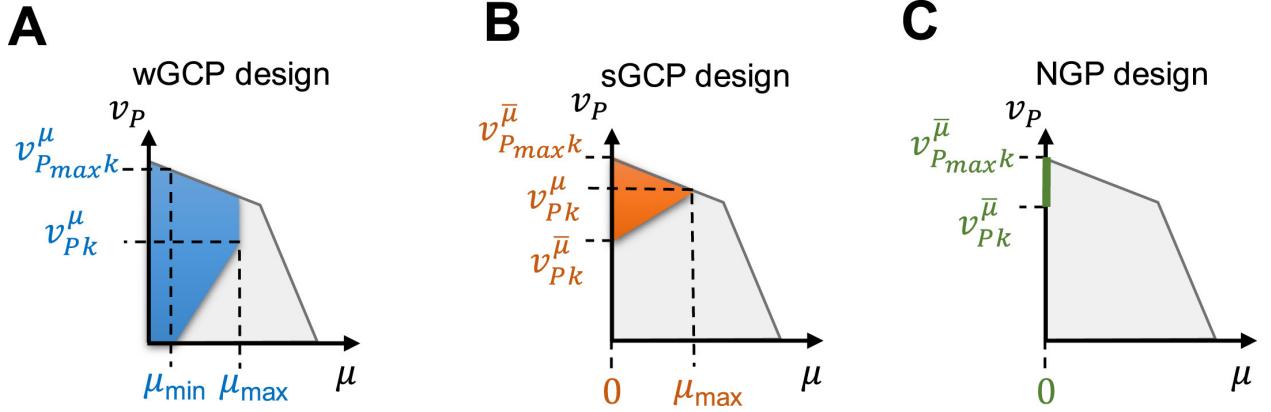


Figure 3.2: Graphical representation of phenotypic spaces for different strain design objectives including (A) weak growth coupling (*wGCP*), (B) strong growth coupling (*sGCP*), and (C) no-growth production (*NGP*). $v_{P_k}^\mu$ is the minimum product formation rate at the maximum growth rate for production network k , and $v_{P_{max}k}^\mu$ is the maximum product secretion rate attainable. $v_{P_k}^{\bar{\mu}}$ and $v_{P_{max}k}^{\bar{\mu}}$ are the minimum and maximum product formation rates for production network k during the stationary phase, respectively.

Design variables

In our formulation for modular cell engineering, we introduced two design variables: binary reaction deletions (y_j) inherent to the modular cell and module-specific reaction insertions (z_{jk}) (3.5). These variables can be experimentally manipulated to constrain the desirable phenotypes of production strains as shown in Figure 3.2. Specifically, $y_j = 0$ if reaction j is deleted from the modular cell; otherwise, $y_j = 1$. Deleting metabolic reactions removes undesired functional states of the network and leaves those with high design objectives. Likewise, $z_{jk} = 1$ if reaction j is present in the production network k ; otherwise, $z_{jk} = 0$. These module reactions are endogenous reactions removed from the parent network (3.6), but are added back to a specific production module to enhance the compatibility of a

modular cell. The maximum number of reaction deletions (α) and module-specific reaction insertions (β_k) are user-defined parameters.

Design objectives

To generalize ModCell2 design, we allow three different types of design objectives (f_k , (3.1)) that determine production phenotypes for each production network. Depending on the application, a phenotype can be designed to be weak coupling ($wGCP$), strong coupling ($sGCP$), and/or non-growth production (NGP) (Figure 3.2). The constrained phenotypic spaces based on these design objectives are shown in color; any point within these spaces is a feasible physiological state of the cell that can be represented by a metabolic flux distribution.

The $wGCP$ design seeks to achieve a high product rate at maximum growth rate (Figure 3.2A). The $wGCP$ design objective, $f_k^{wGCP} \in \{0, 1\}$, is calculated as follows:

$$f_k^{wGCP} = \frac{v_{Pk}^\mu}{v_{P_{maxk}}^\mu} \quad (3.9)$$

where v_{Pk}^μ is the minimum synthesis rate of the target product P at the maximum growth rate for production network k and $v_{P_{maxk}}^\mu$ is the maximum synthesis rate of P (Supplementary File S1). This $wGCP$ design formulation is equivalent to RobustKnock [228] or OptKnock with a tilted objective function [24, 63, 267]. In (3.9), f_k^{wGCP} is scaled from 0 to 1 for proper comparison among products. The $wGCP$ design is appropriate for applications where growth rate is not limited by the nutrients, and the product is formed during the growth phase.

The $sGCP$ design seeks to achieve a high product rate not only at optimal growth rate but also during non-growth phase (Figure 3.2B). The $sGCP$ design objective, $f_k^{sGCP} \in \{0, 1\}$, is calculated as follows:

$$f_k^{sGCP} = \frac{v_{Pk}^\mu}{v_{P_{maxk}}^\mu} \frac{v_{Pk}^{\bar{\mu}}}{v_{P_{maxk}}^{\bar{\mu}}} \quad (3.10)$$

where $v_{Pk}^{\bar{\mu}}$ and $v_{P_{maxk}}^{\bar{\mu}}$ are the minimum and maximum product formation rates for production network k in the stationary phase, respectively (Supplementary File S1). The $sGCP$ design objective is comparable to the one implemented in MODCELL [241]. Different from $wGCP$,

sGCP requires high product synthesis rate for any growth phase. However, the additional constraint of optimal product synthesis during the stationary phase requires more genetic manipulations or specific experimental conditions (e.g., anaerobic growth condition, supply of intermediate metabolites). Both *wGCP* and *sGCP* designs enable fast growth selection to attain the optimum product rates by adaptive laboratory evolution [66, 237].

The *NGP* design aims to maximize the minimum product rate during the non-growth phase by eliminating carbon fluxes directed to biomass synthesis (Figure 3.2C). The *NGP* design objective, $f_k^{\text{NGP}} \in \{0, 1\}$, is calculated as follows:

$$f_k^{\text{NGP}} = \frac{v_{P_k}^{\bar{\mu}}}{v_{P_{\max k}}^{\bar{\mu}}} \quad (3.11)$$

While the *NGP* design is not suitable for growth selection, it can be derived from a *wGCP* (or *sGCP*) design by imposing additional genetic modifications. Practically, *NGP* design strains can be activated during cell culturing using a regulatory genetic circuit to toggle switch between production phases.

Design solutions

Optimal solutions for (3.1-3.8) are a Pareto set (\mathcal{PS}) that correspond to design variables, including reaction deletions (y_j) and module reaction insertions (z_{jk}). Each solution constitutes a design of a modular cell:

$$\mathcal{PS} = \{x \in \Omega : \nexists t \in \Omega, F(t) \prec F(x)\} \quad (3.12)$$

Here, $\mathbf{F}(\mathbf{t}) \prec \mathbf{F}(\mathbf{x})$ means $\mathbf{F}(\mathbf{t})$ dominates $\mathbf{F}(\mathbf{x})$ if and only if $f_i(\mathbf{t}) \geq f_i(\mathbf{x})$ for all i , and $\mathbf{F}(\mathbf{t})$ differs from $\mathbf{F}(\mathbf{x})$ in at least one entry. The feasible space of design variables, Ω , is defined by the problem constraints (3.2-3.8), also see Supplementary File S1). Phenotypes of modular cells will be the image of the Pareto set in the objective space, known as the Pareto front (\mathcal{PF}):

$$\mathcal{PF} = \{F(x) : x \in \mathcal{PS}\} \quad (3.13)$$

For the multi-objective strain design framework, the input parameters include α (3.8), β_k (??) , and the production networks as input metabolic models. Each model contains a production module to produce one target chemical. The output is a Pareto set (genetic modifications) and its respective Pareto front (desirable production phenotypes). For a special case with no trade-off among the design objectives, an optimal solution, named a utopia point, exists where each objective achieves its maximum value. The multi-objective strain design formulation presented is general and can be applied to design modular cells for any organism.

3.2.3 Algorithm and implementation

ModCell2 algorithm

To solve the multi-objective optimization problem for modular cell engineering, we used multi-objective evolutionary algorithms (MOEAs) [42]. MOEAs were selected because they can efficiently handle linear and non-linear problems and do not require preferential specification of design objectives [155]. MOEAs start by randomly generating a population of individuals (a vector of design variables), each of which is mapped to a design objective vector (i.e., a fitness vector). In ModCell2 (Supplementary File S1), the objective values of an individual are calculated by solving the linear programming problems for each production network. Next, individuals are shuffled to generate an offspring, from which the most fit individuals are kept. This process was repeated until the termination criteria was reached, for instance, either the solutions cannot be further improved or the simulation time limit is reached.

ModCell2 implementation

To streamline the modular cell design, we developed the ModCell2 software package based on three core classes (Figure S1 in Supplementary File S2). The Prodnet class parses and pre-processes production network models, and computes production phenotypes. The MCdesign class serves as an interface between the MOEA optimization method and metabolic models.

Finally, the ResAnalysis class loads the Pareto set computed by MCdesign and identifies the most promising modular cell designs.

The code was written in MATLAB 2017b (The Mathworks Inc.) using the function gamultiobj() from the MATLAB Optimization Toolbox that implements the NSGA-II algorithm [51] to solve the multi-objective optimization problem. The solution and analysis methods were parallelized using the MATLAB Parallel Computing Toolbox. The linear programs to calculate metabolic fluxes were solved using the GNU Linear Programming Kit (GLPK). The COBRA toolbox [90, 207] and F2C2 0.95b [126] were also used for COBRA model preprocessing and manipulation.

Metabolic models

In our study, we used three parent models including i) a small metabolic network to illustrate the modular cell design concept [241], ii) a core metabolic network of *Escherichia coli* to compare the performance of ModCell2 with respect to the conventional single-product strain design strategy and the first-generation modular cell design platform MODCELL [241], and iii) a genome-scale metabolic network of *E. coli* (i.e., iML1515 [63]) for biosynthesis of a library of endogenous and heterologous metabolites, including 4 organic acids, 6 alcohols, and 10 esters (Figures S2 in Supplementary File S2) \cite{RN197, 126, 81, 198, 83, 127, 136, 80, 110, 1045}.

Simulation protocols

Anaerobic conditions were imposed by setting oxygen exchange fluxes to be 0, and the glucose uptake rate was constrained to be at most 10 mmol/gCDW/h, as experimentally observed for *E. coli*. When using the genome-scale model iML1515 to simulate *wGCP* designs, the commonly observed fermentative products (acetate, CO₂, ethanol, formate, lactate, succinate) were allowed for secretion as described elsewhere [250]. For simulation of *sGCP* and *NGP* designs, the glucose uptake rate was fixed (i.e., -10 mmol/gCDW/h); otherwise, the flux is not active during the no-growth phases, resulting in the product synthesis rate of 0 regardless of genetic manipulations. To compare ModCell2 with Optknock, we applied the OptKnock algorithm with a tilted objective function [154] to generate *wGCP* designs for

each production network, using the open-source algebraic modeling language Pyomo [85]. The MILP problems were solved using CPLEX 12.8.0 with a time limit of 10,000 seconds set for each product. ModCell2 is provided as an open-source software package and is freely available for academic research. The software package and documentation can be downloaded via either <https://web.utk.edu/~ctrinh> or Github <https://github.com/TrinhLab>.

3.2.4 Analysis methods for design solutions

Compatibility

The compatibility, C , of a design is defined as the number of products that are coupled with a modular cell and has objective values above a specified cutoff value θ . As a default, we set $\theta = 0.6$ for the *wGCP* and *NGP* design objectives and $\theta = 0.36$ (0.6^2) for the *sGCP* design objective. For example, a *wGCP* design for 3 products that has the design objective values of 0.4, 0.9, and 0.6 has a compatibility of 2, given a cutoff value of $\theta \geq 0.6$.

Compatibility difference and loss

Robustness is the ability of a system to maintain its function against perturbations, and hence is very important of designing biological and engineered systems [119]. To evaluate the robustness of modular cell designs, we defined two metrics, the compatibility difference (CD) and compatibility loss ($CL \in \{0, 1\}$) as follows:

$$CD = C_{\text{initial}} - C_{\text{final}} \quad (3.14)$$

$$CL = \frac{C_{\text{initial}} - C_{\text{final}}}{C_{\text{initial}}} \quad (3.15)$$

where C_{initial} and C_{final} are the compatibilities of a modular cell design before and after a single reaction deletion, respectively. The value $CD > 0$ (or $CL > 0$) means the modular gains fitness while $CD < 0$ (or $CL < 0$) means that it loses its fitness. In the analysis, we did not consider essential and blocked reactions for our single-deletion analysis; for instance, there are only 1139 potential reaction deletions in the iML1515 model.

Metabolic switch design

A metabolic switch design is a modular cell that can possess multiple production phenotypes (i.e., *wGCP*, *sGCP*, and *NPG*), activated by an environmental stimulus (e.g. metabolites, lights). The metabolic switch design is enforced to have a set of reaction (gene) deletions in one production phenotype to be a subset of the other. The metabolic switch design is beneficial for multiphase fermentation configurations that enable flexible genetic modification and implementation. Specifically, the metabolic switch design can exhibit the *wGCP* phenotype during the growth phase and the *NPG* (or *sGCP*) phenotype during the stationary phase. The metabolic switches can be implemented using the genetic switchboard [25].

3.3 Results and discussion

3.3.1 Illustrating ModCell2 for modular cell design of a simplified network

An example parent network, adapted from [241], was used to illustrate ModCell2 (Figure 3.3A). Inputs for the multi-objective optimization problem include i) three production networks (Figure 3.3B), comprising of one endogenous production module (module 1) and two heterologous production modules (modules 2 and 3) and ii) design parameters (Figure 3.3C), containing design objective type, maximum number of deletion reactions (α), and maximum number of module reactions (β_k). The output of ModCell2 generated the Pareto set and the corresponding Pareto front for modular cell designs (Figure 3.3D). The 2-D plots of product yields versus growth rates presented the feasible phenotypic spaces of the wildtype (gray area) and the designed strain (blue area).

Using various α and β_k values, ModCell2 simulation generated three *wGCP*- α - β_k - d , four *sGCP*- α - β_k - d designs, and three *NPG*- α - β_k - d designs, where d is the design solution index (Figure 3.3D). For instance, by setting $\alpha = 3$ and $\beta_k = 0$, we found three *sGCP* designs including *sGCP*-3-0-1, *sGCP*-3-0-2, and *sGCP*-3-0-3. The first design *sGCP*-3-0-1 has a compatibility of 2 with the design objective values of 0.42 and 0.97 for the products P2 and

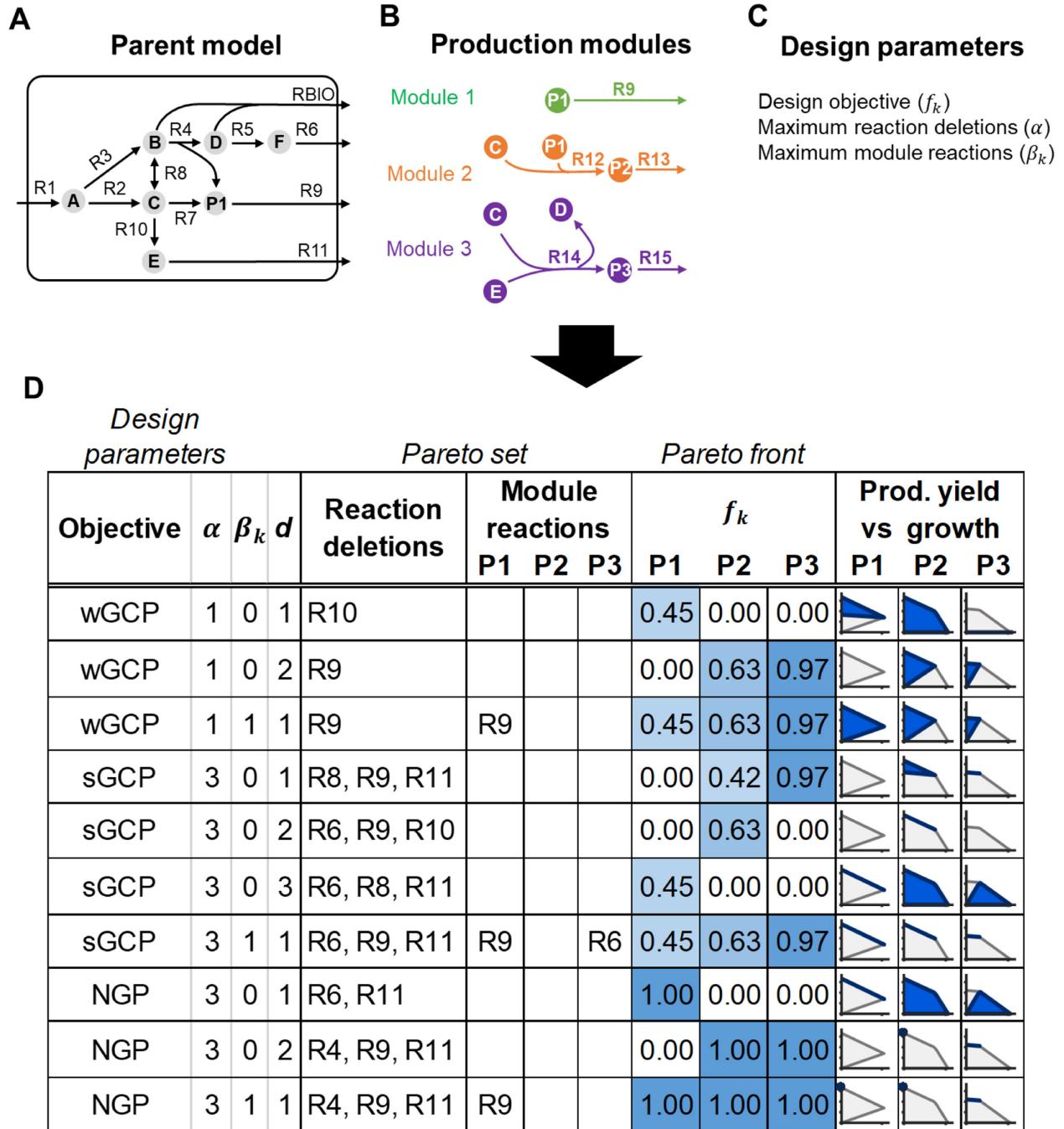


Figure 3.3: Illustration of ModCell2 workflow and analysis including (A) parent model, (B) production modules, (C) design parameters, and (D) simulation output for Pareto set and Pareto front based on design input.

P3, respectively. In contrast, the *sGCP*-3-0-2 and *sGCP*-3-0-3 designs have compatibilities of only 1 with the design objectives of 0.63 for P2 and 0.45 for P1, respectively.

Based on all designs, we can clearly see the trade-offs for optimization of different products for $\beta_k = 0$. However, setting $\beta_k \geq 1$ helps increase the compatibility of a modular cell with different production modules. In addition, we found that the Pareto front collapses into a utopia point as seen in the *wGCP*-1-1-1, *sGCP*-3-1-1, and *NGP*-3-1-1 designs. For instance, the modular cell, *sGCP*-3-1-1, is compatible with all three products. The three corresponding optimal production strains can couple growth and product formation during the growth phase. During the stationary phase, these strains produce the products at maximum theoretical yields. In theory, a universal modular cell always exists, provided that enough reaction deletions and module reactions are used. It might be more tractable to construct such a modular cell from a synthetic minimal cell using the bottom-up approach. However, construction of a universal modular cell from a host organism (e.g., *E. coli*, *S. cerevisiae*) using the top-down approach will require a significantly large number of genetic modifications, that might be challenging.

3.3.2 Comparing ModCell2 designs with first-generation MOD-CELL and single product designs

ModCell2 can generate more and better designs than the first-generation modular cell design platform

To evaluate the algorithms and performance of ModCell2, we directly compared it with MODCELL [241] in two case studies, using the same core model of *E. coli* for production of five alcohols (ethanol, propanol, isopropanol, butanol, and isobutanol) and 5 derived butyrate esters (ethyl butyrate, propyl butyrate, isopropyl butyrate, butyl butyrate, and isobutyl butyrate) from glucose (Figure 3.4A).

In the first case study, we fixed the reaction module, i.e. $\beta_k = 2$ for ethanol dehydrogenase (FEM5) and ethanol export reaction (TRA1), in ModCell2 to emulate the same input as MODCELL (Supplementary File S3). The results showed that ModCell2 generated all the designs with the same *sGCP* objective values like MODCELL (Figure 3.4B, 4C, 4D)

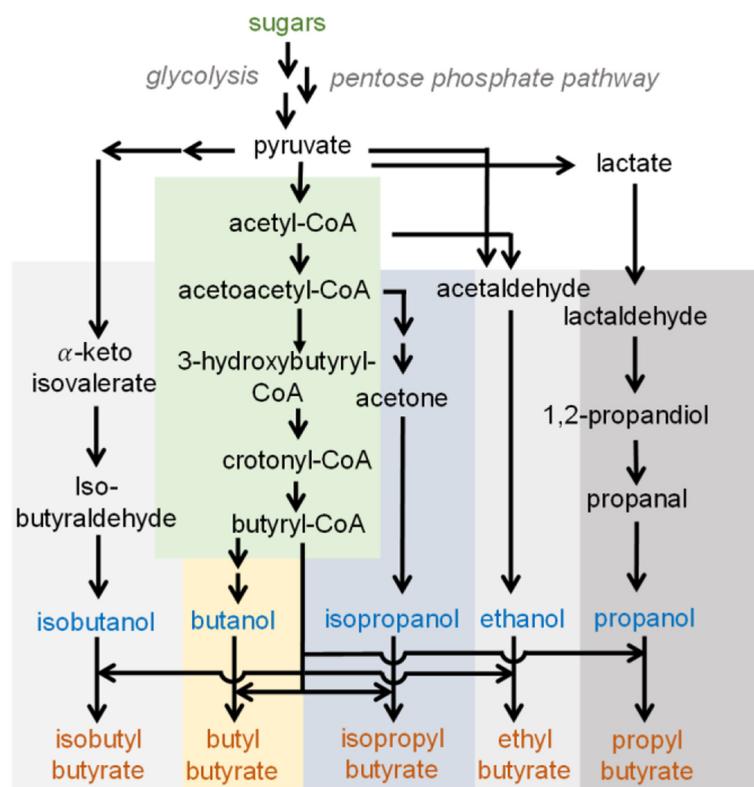
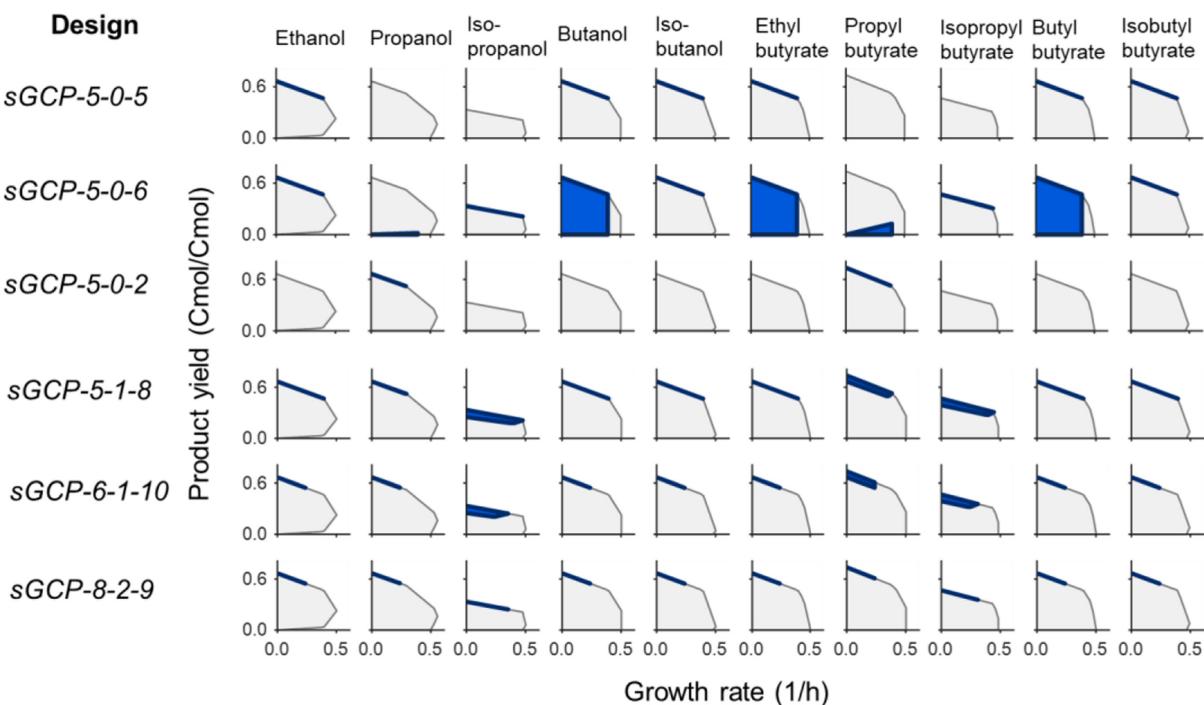
A**B**

Figure 3.4: The 2-D metabolic phenotypic spaces of different *sGCP* designs using the core metabolic model. (A) Metabolic map, (B) *sGCP-5-0-5* design, (C) *sGCP-5-0-6* design, (D) *sGCP-5-0-2* design, (E) *sGCP-5-1-8* design, (F) *sGCP-6-1-10* design, and (G) *sGCP-8-2-9* design. For each panel, the gray and blue areas correspond to the phenotypic spaces of the wildtype and the optimal production strain, respectively.

together with other alternative solutions (Supplementary File S3). Interestingly, ModCell2 only required 5 and 6 reaction deletions as opposed to 7 and 7 for the *sGCP-5-0-5* and *sGCP-5-0-6* designs, respectively. By setting the maximum reaction deletions to $\alpha \geq 6$, ModCell2 could find better design solutions with fewer deletion reaction requirement and higher objective values (Supplementary File S3).

In the second case study, we used the same model configuration but did not enforce the module reactions. By setting $\alpha = 5$ and $\beta_k = 1$, we found the *sGCP-5-1-8* design that is compatible with all products and achieves the same objective values for products found in *sGCP-5-0-5*, *sGCP-5-0-6*, and *sGCP-5-0-2* (Figure 3.4E). The desirable phenotypic spaces can be further constrained for many products if α is increased from 5 to 6 (Figure 3.4F). Remarkably, by setting $\alpha = 8$ and $\beta_k = 2$, we found a utopia point design, *sGCP-8-2-9*, without any trade-off among design objectives (Figure 3.4G). This utopia point design could not be achieved with $\alpha < 8$ regardless of any β_k value.

Overall, the results demonstrate that ModCell2 can efficiently compute the Pareto front of modular cell designs. It can find better designs with fewer reaction deletion and module reaction requirements, improve design objective values, and enhance compatibility.

ModCell2 can identify designs with more compatibility than the conventional single-product designs

To evaluate if the conventional, single-product design strategy is suitable for modular cell engineering, we first used OptKnock to generate *wGCP* designs for the same 10 target molecules independently with various allowable reaction deletions ($\alpha = 2, 3, \dots, 7$). Likewise, we employed ModCell2 to produce *wGCP* designs using the same α and various β . To directly compare OptKnock and ModCell2 solutions, we calculated the *wGCP* design objective values for all products based on each OptKnock solution (Supplementary File S3). As expected, our result showed that ModCell2 and OptKnock designs have the same highest objective values for each product (Figure 5A). However, several OptKnock solutions were always dominated by ModCell2 solutions in all parameter configurations (Figure 3.5B). With $\alpha \geq 4$, ModCell2 could identify *wGCP- $\alpha-1$* designs with the maximum compatibility of 10,

while the best OptKnock designs only achieved the highest compatibility of 5 (Figure 3.5C, 5D).

Overall, ModCell2 can generate modular cells compatible with the maximum number of modules and achieve high objective values. Single-product designs might not be compatible with a large number of products, and the solutions might be far from Pareto optimality.

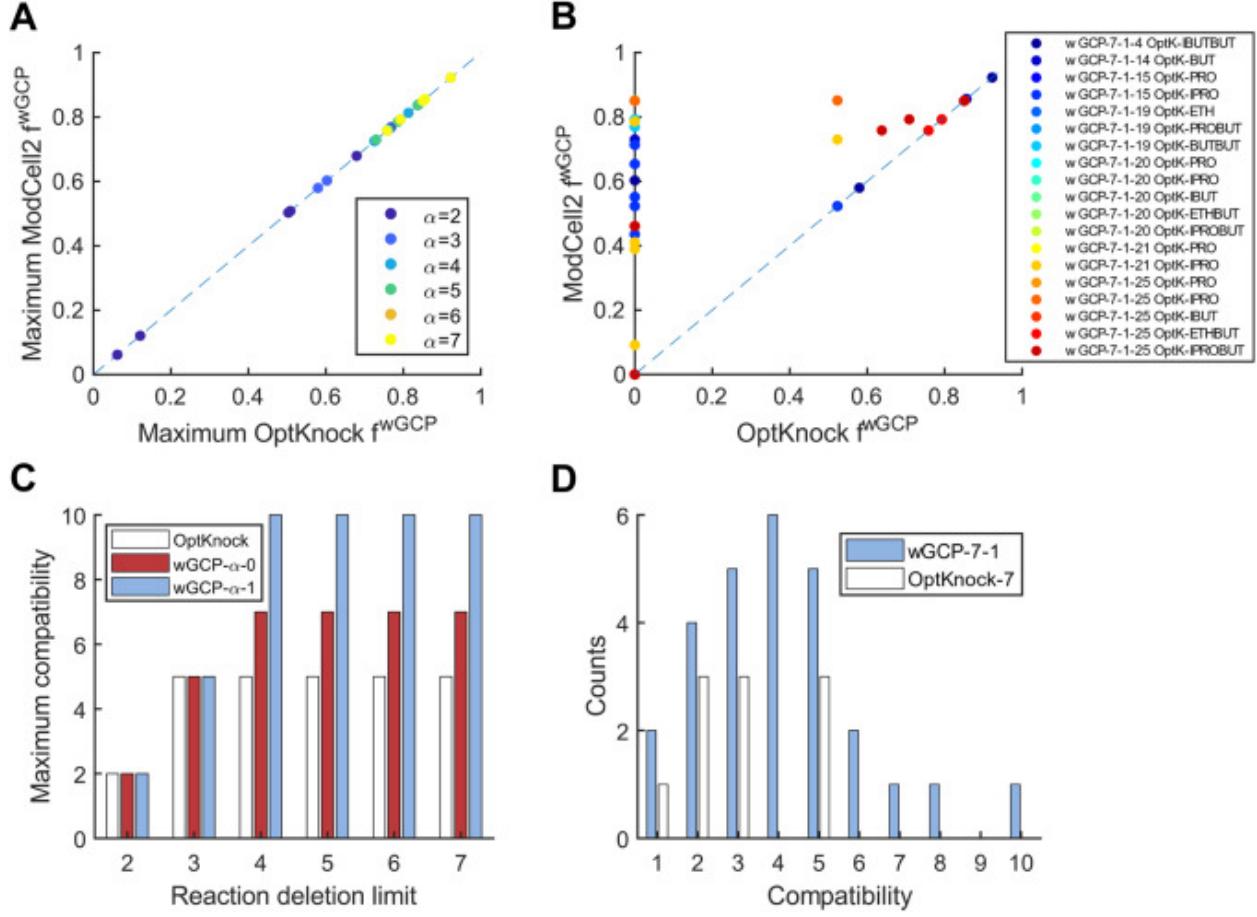


Figure 3.5: Comparison of strain design by OptKnock and Modcell2. **(A)** A correlation between the maximum objective values for each product generated by OptKnock and the equivalent values attained by ModCell2. Each point is colored based on the number of reaction deletions, with warmer colors corresponding to more reaction deletions. **(B)** A comparison between the Optknock objective vectors with at most 7 reaction deletions and the representative ModCell2 objective vector, $wGCP-7-1$ which dominates them. Each color circle represents a pair of dominating $wGCP$ design and dominated OptKnock solution (Supplementary File S3). **(C)** Maximum compatibility of OptKnock designs (blue), $wGCP$ designs ($\beta_k = 0$, orange), $wGCP$ designs ($\beta_k = 1$, yellow). **(D)** Compatibility distribution of Optknock ($\alpha = 7$, orange) and $wGCP-7-1$ (blue).

3.3.3 Exploring emergent features of modular cell design using an *E. coli* genome-scale network

Modcell2 can design modular cells using a large-scale metabolic network.

To demonstrate that ModCell2 can be applied for a genome scale metabolic network, we tested it to generate *wGCP* designs for 20 target molecules with $\alpha = 4$ and various β_k (Supplementary File S4). The α value was chosen because with 4 deletions, OptKnock could identify single product designs with objectives above 60% of the theoretical maximum (Supplementary File S5). With $\beta_k = 0$, ModCell2 could identify modular cell designs with compatibility of 17, for example, the *wGCP-4-0-50* design featuring deletion of ACALD (acetaldehyde dehydrogenase, *adhE*), ACKr/PTAr (acetate kinase, *ack*; phosphotransacetylase, *pta*), GLYAT (glycine C-acetyltransferase, *kbl*), and LDH_D (lactate dehydrogenase, *ldhA*) (Figure 3.6A, 6D, Supplementary File S4). By analyzing all *wGCP-4- β_k -d* designs (257 total for $\beta_k = 0, 1, 2$, and 3), we found that the ethanol and D-lactate production modules are most compatible with all modular cell designs (Figure 3.6A, 6C, Supplementary File S4). Among reaction deletions, *LdhA* (86% of designs), *Pta* (38%), and *AdhE* (25%) are the most frequent deletion reactions (Figure 3.6B). This finding is consistent with a comprehensive survey of metabolic engineering publications [263] showing that these deleted reactions appeared in most of *E. coli* engineered strains for production of fuels and chemicals. The result supports the potential use of modular cell engineering to systematically build modular platform strains.

ModCell2 designs can capture combinatorial characteristics of production modules.

To evaluate whether ModCell2 could capture the combinatorial properties among production modules, we analyzed the Pareto front of *wGCP-4-0-d* that have a total of 58 designs. Hierarchical clustering of this Pareto front revealed certain products with similar objective values across solutions, such as ethyl esters and butyrate esters (Figure 3.6A). These products together were compatible with different modular cells and exhibited metabolic similarity

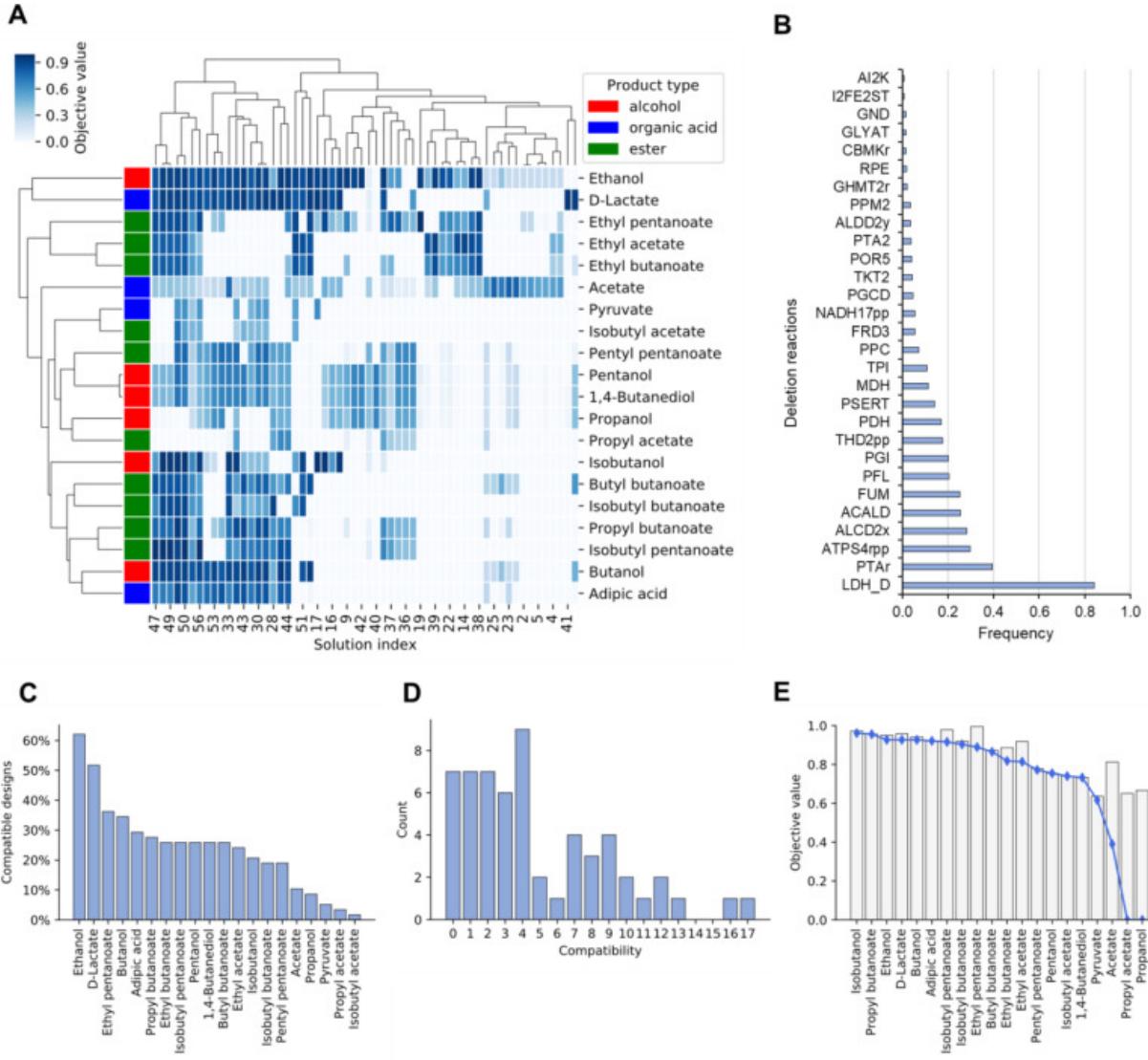


Figure 3.6: Analysis of *wGCP* designs with genome-scale model. **(A)** Pareto front of *wGCP-4-0-d*. The columns correspond to different designs labeled by their design index, d , where the rows correspond to different products. **(B)** Frequency of the top deletion reactions. **(C)** Product compatibility distribution across designs. **(D)** Design compatibility. **(E)** Tradeoff between modularity and performance. The bars correspond to the maximum objective values attainable for each product whereas the blue line represent the objective values of the *wGCP-4-0-48alternative* design.

in their production modules. Thus, ModCell2 could generate designs that capture the combinatorial properties useful for modular cell engineering.

ModCell2 can identify highly compatible modular cells

Analysis of compatibility shows that certain modular cells can couple with production modules that may not exhibit the combinatorial properties (Figure 3.6D). However, there exists a tradeoff between the number of feasible designs and degree of compatibility. Some modular cell designs are compatible with up to 17 out of 20 products, for instance, the most compatible design, *wGCP-4-0-48*, featuring deletions of ACALD (*adhE*), ACKr/PTAr (*ack*, *pta*), GND (phosphogluconate dehydrogenase, *gnd*) and LDH_D (*ldhA*) (Supplementary File S4). An alternative design *wGCP-4-0-48-alternative* also exists where deletion of G6PDH2r (glucose-6-phosphate dehydrogenase, *zwf*) is replaced by that of GND, the first step in the oxidative pentose phosphate pathway. The gene deletions in the design *wGCP-4-0-48-alternative* are a subset of the modular *E. coli* strain TCS095, whose modular properties have recently been validated experimentally [261].

To determine if modular cell design is a viable alternative to single-product design, we also analyzed a potential tradeoff between design performance and modularity by comparing the maximum value of each objective across all solutions in the Pareto front and the single-product design optima. If production modules exhibit competing phenotypes, a modular cell will not achieve the same performance in all modules as a single-product design strain. Analysis of the most compatible design *wGCP-4-0-48-alternative* showed that it could achieve objectives within 4% of the single-product optima in 14 products and within 10% in 3 products (Figure 3.6E). This result indicates that it is feasible to identify highly compatible modular cell designs without a significant tradeoff between performance and modularity.

Analysis of potential tradeoff between robustness and modularity can identify conserved metabolic features

To evaluate the robustness of modular cells, we analyzed the compatibility change (*CD*) of *wGCP-4-0* designs with compatibilities of 4 or greater (Figure S3 in Supplementary File 2). Remarkably, the result shows that only 7.5% of potential reaction deletions were detrimental

to the robustness of modular cells while the large remaining portion did not affect CD values. Out of the 85 reactions whose deletion affected compatibility, only a few appeared consistently across the designs. For instance, deletion of TPI (triose-phosphate isomerase, *tpi*) led to an average compatibility loss of 95%, inactivating most modular cell designs. Based on flux variability analysis, TPI must operate in the forward direction by converting glycerone phosphate (dhap) to glyceraldehyde-3-phosphate (g3p) to drive sufficient flux through glycolysis and hence preventing synthesis of undesired byproducts (D-lactate or 1,2-propanediol) from dhap. Likewise, deletion of carbon dioxide and water transport and exchange reactions caused compatibility loss across all designs. Pyruvate carboxylase (PPC) is an important reaction to channel carbon flux through the Krebs cycle [44], and hence, deletion of PPC reduces compatibility in most modular cell designs with an average CL of 43%.

While some reaction deletions are critical for modular cell robustness, others are associated with specific products. For example, deletion of PDH (pyruvate dehydrogenase complex, *lpd/aceEF*) removes compatibility in all butanol-derived designs, indicating PFL (pyruvate formate lyase, *pfl*) is not an appropriate route. To make heterologous butanol-derived molecules under anaerobic conditions, FDH (NADH-dependent formate dehydrogenase, *fdh*) is required in butanol-derived modules where enzymatic reaction pairs of PFL and FDH could substitute PDH known to be anaerobically inhibited.

Overall, analysis of tradeoff between modularity and robustness can identify not only the conserved metabolic features of modular cells but also potential bottlenecks in specific production modules.

Enabling metabolic switch among different design objectives using ModCell2

The ability to dynamically control growth and production phases can potentially enhance product titers, rates, and yields. For instance, two-phase fermentation can be employed where growth phase is optimized for biomass synthesis and stationary phase for chemical production [121]. Using ModCell2, we investigated the feasibility to design optimal strains to toggle switch desirable production phenotypes. To design a *wGCP*→*NPG* metabolic switch, we first used our reference *wGCP* design as a parent strain (Figure 3.7A) and then employed

ModCell2 to identify the most compatible $wGCP \rightarrow NPG$ designs. With 5 additional deletions, we could find $wGCP \rightarrow NPG$ designs that encompass both $wGCP$ and NPG phenotypes, for instance, the *sup-NGP-5-0-23* design featuring deletion of PGI (glucose-6-phosphate isomerase, *pgi*), MDH (malate dehydrogenase, *mdh*), ASPT (L-aspartase, *aspT*), Tkt2 (transketolase, *tktB*), and ATPS4rpp (ATP synthase, *atp*) (Figure 3.7B). The deletion reactions in the $wGCP \rightarrow NPG$ designs appear in both catabolic (PGI, ATPS4tpp) and anabolic (ASP, TKT2) processes, responsible for growth disruption and direction of carbon flow to the biosynthesis of target products.

Likewise, we used ModCell2 to design a $wGCP \rightarrow sGCP$ metabolic switch. We identified the most compatible $wGCP \rightarrow sGCP$ designs with 6 additional deletions, for instance, the *sup-sGCP-6-0-39* design featuring the deletion of MGSA (Methylglyoxal synthase, *mgsA*), ALCD2x (alcohol dehydrogenase, *adhE*), PFL, MDH, FADRx (FAD reductase, *fadI*), and GLUDy (NADP⁺ dependent glutamate dehydrogenase, *gdhA*) (Figure 3.7C). Different from the $wGCP \rightarrow NGP$ metabolic switch, all deletions in the $wGCP \rightarrow sGCP$ designs are involved the elimination of biosynthesis pathways of undesirable byproducts.

While it is feasible to metabolically switch among different production phenotypes, it not only requires more reaction deletions but also reduces the product compatibility. For instance, the $wGCP \rightarrow sGCP$ and $wGCP \rightarrow NGP$ designs are only compatible with 5 products while the $wGCP$ parent design have a compatibility of 17 out of 20 products with 4 deletions. The main reason is that both $wGCP \rightarrow sGCP$ and $wGCP \rightarrow NGP$ designs must eliminate all possible redundant pathways that result in biosynthesis of undesirable byproducts.

3.4 Conclusion

In this study, we developed a multi-objective strain design platform for modular cell engineering. With a new developed algorithm and computational platform, ModCell2 enables flexible design of modular cells that can couple with production modules to exhibit desirable production phenotypes. In comparison to the first-generation strain design platform, ModCell2 can handle large-scale metabolic networks and identify better solutions that require fewer genetic modifications and exhibit more product compatibility. Different from

the conventional single-product strain design, ModCell2 can find solutions that are Pareto optimal with negligible tradeoffs among modularity, performance, and robustness. We envision ModCell2 is a useful tool to implement modular cell engineering and fundamentally study modular designs in natural and synthetic biological systems.

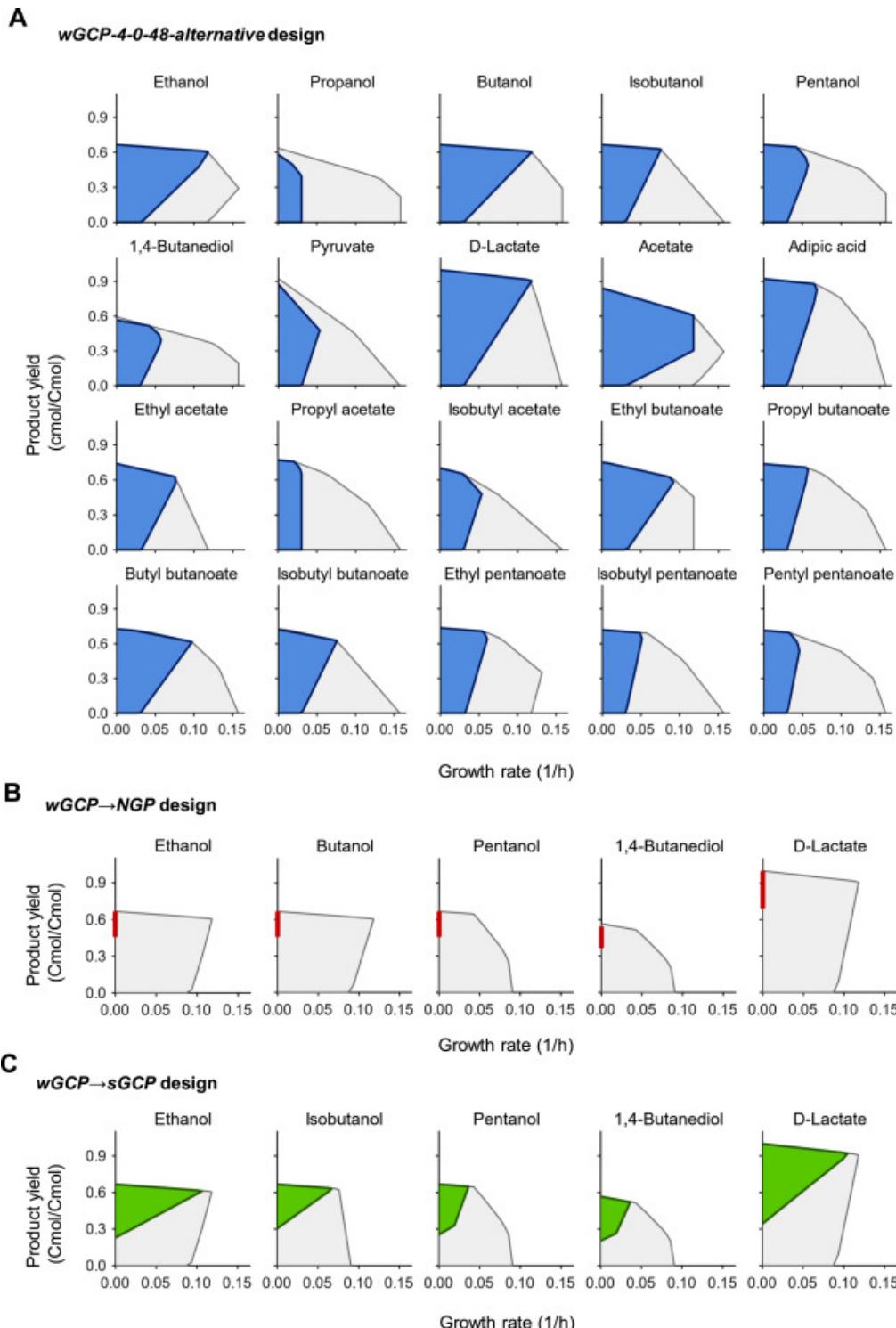


Figure 3.7: Production phenotypes of (A) the wild type (gray) and the representative, highly-compatible design *wGCP-4-0-48-alternative* (blue), (B) the *wGCP→NPG* design, *sup-NGP-5-0-23*, and (C) the *wGCP→sGCP* design, *sup-sGCP-6-0-39*.

Chapter 4

Comparison of multi-objective evolutionary algorithms to solve the modular cell design problem

This chapter is based on the publication *Comparison of Multi-Objective Evolutionary Algorithms to Solve the Modular Cell Design Problem for Novel Biocatalysis*. Garcia, S., and Trinh, C. T. *Processes*, 2019. As first author I lead the development, implementation, and writing of this study. Supplementary Material 1 is provided as an attachment.

Abstract

A large space of chemicals with broad industrial and consumer applications could be synthesized by engineered microbial biocatalysts. However, the current strain optimization process is prohibitively laborious and costly to produce one target chemical and often requires new engineering efforts to produce new molecules. To tackle this challenge, modular cell design based on a chassis strain that can be combined with different product synthesis pathway modules has been recently proposed. This approach seeks to minimize unexpected failure and avoid task repetition, leading to a more robust and faster strain engineering process. In our previous study, we mathematically formulated the modular cell design problem based on the multi-objective optimization framework. In this study, we evaluated a

library of state-of-the-art multi-objective evolutionary algorithms (MOEAs) to identify the most effective method to solve the modular cell design problem. Using the best MOEA, we found better solutions for modular cells compatible with many product synthesis modules. Furthermore, the best performing algorithm could provide better and more diverse design options that might help increase the likelihood of successful experimental implementation. We identified key parameter configurations to overcome the difficulty associated with multi-objective optimization problems with many competing design objectives. Interestingly, we found that MOEA performance with a real application problem, e.g., the modular strain design problem, does not always correlate with artificial benchmarks. Overall, MOEAs provide powerful tools to solve the modular cell design problem for novel biocatalysis.

4.1 Introduction

Multi-objective optimization is a powerful mathematical toolbox widely used in engineering disciplines to solve problems with multiple conflicting design objectives [40]. For example, in the field of chemical engineering, multi-objective optimization has been applied to balance design conflicts in the performance, material and energy requirements, and environmental sustainability of many different chemical processes [192]. In industrial biotechnology, with recent advancements in synthetic biology and metabolic engineering, microorganisms can be genetically modified to produce a large space of molecules with broad applications using renewable lignocellulosic biomass or waste products as feedstocks [242, 131]. However, the current strain design process is prohibitively laborious and expensive for broad industrial application [172]. To overcome this challenge, recent studies have proposed the application of modular design principles commonly used in engineering [20] to microbial biocatalysis [238, 241, 73, 72]. This modular cell design approach, known as ModCell, uses multi-objective optimization to account for the competing cellular objectives when cellular metabolism is (re)designed in a modular fashion to produce a diverse class of target chemicals. ModCell has been experimentally demonstrated for biosynthesis of alcohols [240, 238, 261] and esters [127, 128, 129, 260, 130] in *Escherichia coli*.

Despite the broad applicability of multi-objective optimization problems (MOPs) in engineering design, powerful solution algorithms remain elusive. Two approaches can be used to solve MOPs, including multi-objective evolutionary algorithms (MOEAs) and mixed integer linear programming (MILP) algorithms. Unlike MOEA, MILP can ensure that the identified MOP solutions are optimal. Nonetheless, MOEAs are widely used due to the following advantages over MILP: (i) computational scalability for large-scale networks by implementing efficient parallelization algorithms [41], (ii) compatibility with non-linear objectives and constraints, and (iii) unbiased sampling of Pareto optimal solutions without a need to pre-specify objective preference [155]. MOEAs are based on a more general type of optimization method known as evolutionary algorithms, where candidate solutions, that represent individuals of a population, are iteratively modified using heuristic rules to increase their fitness (i.e., objective function values). Recently, much attention has been placed in the development of MOEAs to solve many-objective problems (e.g., problems with 4 or more objectives) that often correspond to real-world applications, but can be very challenging to solve with conventional MOEAs [133]. For the case of ModCell problem, the popular MOEA NSGAII [Mathworks, 106] was used to design a modular cell under 20 different production modules [73]. Due to a large space of molecules that can potentially be synthesized by modular cells, scalability issues are expected to occur when constructing modular cells that are designed to be compatible with tenths or hundreds of products. Furthermore, using the best solver algorithm(s) allows to explore a more diverse design space, resulting in better choices for experimental implementation.

Many MOEAs have been proposed over the past two decades since the inception of landmark algorithms such as NSGAII [51] and SPEA2 [284]. New MOEAs are benchmarked against libraries of artificial problems with known solutions [283, 52], and are expected to show enhanced performance for a subset of these problems in terms of scalability, identification of Pareto optimal solutions, and number of simulation generations needed to converge. This benchmarking methodology does not always reflect MOEA performance for general problems, since specialized parameter configurations or heuristics are often used and can lead to drastically different performance towards a specific problem of interest. Thus, the best MOEA for a certain application problem needs to be determined empirically. In this

study, we evaluated a library of state-of-the-art MOEAs to solve the multi-objective ModCell problem, with the focus on many-objectives methods. Several cases study of increasing difficulty were examined using common performance indicators of solution optimality and diversity, and critical algorithm parameters that determine solution quality were also investigated.

4.2 Methods

4.2.1 Multi-objective modular cell design

Modular cell design enables rapid generation of optimal production strains with desirable phenotypes from a modular (chassis) cell [73], requiring minimal strain optimization cycles. These production strains are assembled from a modular cell and various compatible pathway modules. A modular cell is constructed by eliminating genes from a parent strain to maintain only core metabolic pathways shared across all pathway modules. Each module enables an optimized target product synthesis phenotype that leads to high yields, titers, and production rates. The different biochemical nature of each target metabolite can make the objectives compete with each other, turning the modular cell design problem into a multi-objective optimization problem known as ModCell2 [73]:

$$\max_{y_j, z_{jk}} (f_1, f_2, \dots, f_{|\mathcal{K}|})^T \quad \text{s.t.} \quad (4.1)$$

$$f_k \in \arg \max \left\{ \frac{1}{f_k^{max}} \sum_{j \in \mathcal{J}_k} c_{jk} v_{jk} \quad \text{s.t.} \quad (4.2) \right.$$

$$\sum_{j \in \mathcal{J}_k} S_{ijk} v_{jk} = 0 \quad \text{for all } i \in \mathcal{I}_k \quad (4.3)$$

$$l_{jk} \leq v_{jk} \leq u_{jk} \quad \text{for all } j \in \mathcal{J}_k \quad (4.4)$$

$$l_{jk} d_{jk} \leq v_{jk} \leq u_{jk} d_{jk} \quad \text{for all } j \in \mathcal{C} \quad (4.5)$$

$$\left. \begin{array}{ll} \text{where } d_{jk} = y_j \vee z_{jk} \\ \end{array} \right\} \quad \text{for all } k \in \mathcal{K}$$

$$z_{jk} \leq (1 - y_j) \quad \text{for all } j \in \mathcal{C}, k \in \mathcal{K} \quad (4.6)$$

$$\sum_{j \in \mathcal{C}} z_{jk} \leq \beta_k \quad \text{for all } k \in \mathcal{K} \quad (4.7)$$

$$\sum_{j \in \mathcal{C}} (1 - y_j) \leq \alpha \quad (4.8)$$

where \mathcal{I}_k , \mathcal{J}_k , and \mathcal{K} are the sets of metabolites, reactions, and associated production metabolic networks (i.e., the combination of the chassis organism with a specific product synthesis pathway), respectively. The optimization problem seeks to simultaneously maximize all objectives f_k (4.1). The desirable phenotype f_k for production module k is determined based on key metabolic fluxes v_{jk} (mmol/gDCW/h) predicted by the constraint-based metabolic model (4.2-4.5) [180]. For example, the weak growth coupled to product formation (*wGCP*), a common design objective, requires a high minimum product synthesis rate at the maximum growth-rate, enabling growth selection of optimal production strains. Thus, in *wGCP* design, the inner optimization problem seeks to maximize growth rate while calculating the minimum product synthesis rate through the linear objective function (4.2) (where c_{jk} is 1 and -0.0001 for j corresponding to the biomass and product reactions across all networks k , respectively, and 0 otherwise) subject to: (i) mass-balance constraints (4.3), where S_{ijk} represents the stoichiometric coefficient of metabolite i in reaction j of production network k , (ii) flux bound constraints (4.4) that determine reaction reversibility

and available substrates, where l_{jk} and u_{jk} are lower and upper bounds respectively, and (iii) genetic manipulation constraints (4.5), i.e., deletion of a reaction j in the chassis through the binary indicator y_j , or insertion of a reaction j in a specific production network k through the binary indicator z_{jk} . The maximum product synthesis rate of each production network k , f_k^{max} , is determined by maximizing the product synthesis reaction subject to (4.3-4.4), allowing to bound f_k in $wGCP$ between 0 and 1. Only a subset of all metabolic reactions, \mathcal{C} , are considered as candidates for deletion, since many of the reactions in the metabolic model cannot be manipulated to enhance the target phenotype. Certain reactions can be deleted in the chassis but inserted back to specific production modules, enabling the chassis to be compatible with a broader number of modules (4.6). The numbers of module-reaction additions and reaction deletions in the chassis are constrained by the parameters β_k (4.7) and α (4.8), respectively, to avoid unnecessary genetic manipulations that are generally time-consuming to implement and can lead to unforeseen phenotypes.

4.2.2 Optimal solutions for a multi-objective optimization problem

Optimal solutions for a MOP (4.1-4.8) are defined based on the concept of domination: A vector $a = (a_1, \dots, a_K)^T$ dominates another vector $b = (b_1, \dots, b_K)^T$, denoted as $a \prec b$ if and only if $a_i \geq b_i \forall i \in \{1, 2, \dots, K\}$ and $a_i \neq b_i$ for at least one i . Letting x be the design variables (i.e., y_j and z_{jk}) and X be the feasible set determined by the problem constraints (4.2-4.8), a feasible solution $x^* \in X$ of the MOP is called a Pareto optimal solution if and only if there does not exist a vector $x' \in X$ such that $F(x') \prec F(x^*)$. The set of all Pareto optimal solutions is called Pareto set:

$$PS := \{x \in X : \nexists x' \in X, F(x') \prec F(x)\} \quad (4.9)$$

The projection of the Pareto set in the objective space is denoted as Pareto front:

$$PF := \{F(x) : x \in PS\} \quad (4.10)$$

4.2.3 MOEA selection

To find the best MOEAs for ModCell2, we evaluated a recent and comprehensive set of MOEAs implemented in the PlatEMO platform [235]. From over 50 algorithms available in PlatEMO, we selected 2 methods for benchmark study, including NSGAII/gamultiobj and MOEAIGDNS, and 8 methods that have been specifically developed to tackle many-objective problems with discrete variables like ModCell2, including ARMOEA, EFRRR, MaOEADDFC, SPEAR, tDEA, BiGE, NSGAIID, and SPEA2SDE (Table 4.1). It should be noted that gamultiobj is an alternative implementation of the NSGAII algorithm available in Matlab.

Table 4.1: Summary of MOEAs used in this study

Abbreviation	Name	Notes	Reference
NSGAII	Non-dominated sorting genetic algorithm 2	Highly applied MOEA	[51]
gamultiobj	Matlab implementation of NSGAII	Used in the original ModCell2 study[73]	[Mathworks]
MOEAIGDNS	Multi-objective evolutionary algorithm based on an enhanced inverted generational distance metric	General MOEA with an implementation that works well with discrete variables	[236]
ARMOEA	Adaption to reference points multi-objective evolutionary algorithm	Many-objective EA based on MOEAIGDNS	[234]
EFRRR	Ensemble fitness ranking with ranking restriction	Many-objective EA	[274]
MaOEADDFC	Many-objective evolutionary algorithm based on directional diversity and favorable convergence	Many-objective EA	[35]
SPEAR	Strength Pareto evolutionary algorithm based on reference direction	Many-objective EA	[101]
tDEA	θ -dominance evolutionary algorithm	Many-objective EA	[273]
BiGE	Bi-goal evolution	Many-objective EA	[136]
NSGAIID	Non-dominated sorting genetic algorithm 3	Many-objective EA	[50]
SPEA2SDE	Strength Pareto evolutionary algorithm 2 with shift-based density estimation	Many-objective EA	[135]

4.2.4 Performance metrics

To evaluate the performance of different MOEAs for a given problem, each algorithm was ran for the same number of generations, and the resulting solutions, known as Pareto front approximations, are compared using functions that measure two qualities: (i) solution accuracy, i.e., to determine how similar the solution is to the true Pareto front and (ii) solution diversity, i.e., to evaluate how well distributed are the points in the solution. We selected the top 5 most used metrics according to a recent literature survey [196]. These include, in order of popularity, hypervolume (HV), generational distance (GD), epsilon indicator (ϵ), inverted generational distance (IGD), and coverage (C). Based on a recent study [209], we considered the average Hausdorff distance (Δ_p), that combines GD and IGD , and hence simplified the number of performance metrics to 4 in our study. These metrics are defined as follows:

HV : This metric measures the volume occupied by the union of the smallest hyperboxes formed by each point in the Pareto front approximation and the reference point. This Pareto front approximation corresponds to the solution of a specific MOEA (denoted as \mathcal{PF}) and the reference point is selected to be greater or equal to the maximum value attainable by any objective, which in our case is $\vec{1}$ (Figure 4.1a):

$$HV = \bigcup_{i \in I} \text{Volume}(\text{Box}(\mathcal{PF}_i, \vec{1})) \quad (4.11)$$

where I is the index set of \mathcal{PF} points.

GD : This metric measures the distance between the solution \mathcal{PF} and the best Pareto front approximation determined by combining non-dominated points from all MOEA solutions of a specific case study, denoted \mathcal{PF}^* . More specifically, GD corresponds to the average Euclidean distance between each point in \mathcal{PF} and the nearest point in \mathcal{PF}^* , denoted as $d_i = \min_{k \in K} \left(\sum_{j \in J} (\mathcal{PF}_{ij} - \mathcal{PF}_{kj}^*)^2 \right)^{\frac{1}{2}}$, where I ($i \in I$), K ($k \in K$), and J ($j \in J$) correspond to the index sets of \mathcal{PF} points, \mathcal{PF}^* points, and problem objectives, respectively (Figure 4.1b):

$$GD = \frac{\sum_{i \in I} d_i}{|I|} \quad (4.12)$$

IGD: This metric measures the distance between \mathcal{PF} and \mathcal{PF}^* . It is determined by the average Euclidean distance between each point in \mathcal{PF}^* and the nearest point in \mathcal{PF} denoted

$$\hat{d}_k = \min_{i \in I} \left(\sum_{j \in J} (\mathcal{PF}_{kj}^* - \mathcal{PF}_{ij})^2 \right)^{\frac{1}{2}} \text{ (Figure 4.1b):}$$

$$IGD = \frac{\sum_{k \in K} \hat{d}_k}{|K|} \quad (4.13)$$

Δ_p : This metric combines *GD* and *IGD* metric and thus has superior properties [209]:

$$\Delta_p = \max(GD, IGD) \quad (4.14)$$

C: This metric determines the fraction of \mathcal{PF}^* captured by the solution \mathcal{PF} (Figure 4.1c):

$$C = \frac{|\mathcal{PF} \cap \mathcal{PF}^*|}{|\mathcal{PF}^*|} = \frac{|\{k \in K : \exists i \in I \text{ such that } \mathcal{PF}_{kj}^* = \mathcal{PF}_{ij} \text{ for all } j \in J\}|}{|K|} \quad (4.15)$$

ϵ : This metric is the additive epsilon indicator [285] that measures the smallest value to be added to any point in \mathcal{PF} to make it non-dominated with respect to some point in \mathcal{PF}^* . In other words, it is the smallest value ϵ such that for any solution in \mathcal{PF}^* there is at least one solution in \mathcal{PF} that is not worse by a difference of ϵ (Figure 4.1d):

$$\epsilon = \inf \{ \epsilon \in \mathbb{R} : \text{for all } i \in I \exists k \in K \text{ such that } \mathcal{PF}_{ij} + \epsilon \geq \mathcal{PF}_{kj}^* \text{ for all } j \in J \} \quad (4.16)$$

Use of these metrics can be illustrated with a two-objective design example with 4 generations of improving Pareto front approximations, where the final Pareto front is used as a reference (i.e., \mathcal{PF}^*) (Figure 4.1e). As the Pareto fronts contain points that dominate the previous generations, all metrics decrease monotonically with the exception of *C* that increases to a value of 1 when both Pareto front approximation and reference are the same (Figure 4.1f).

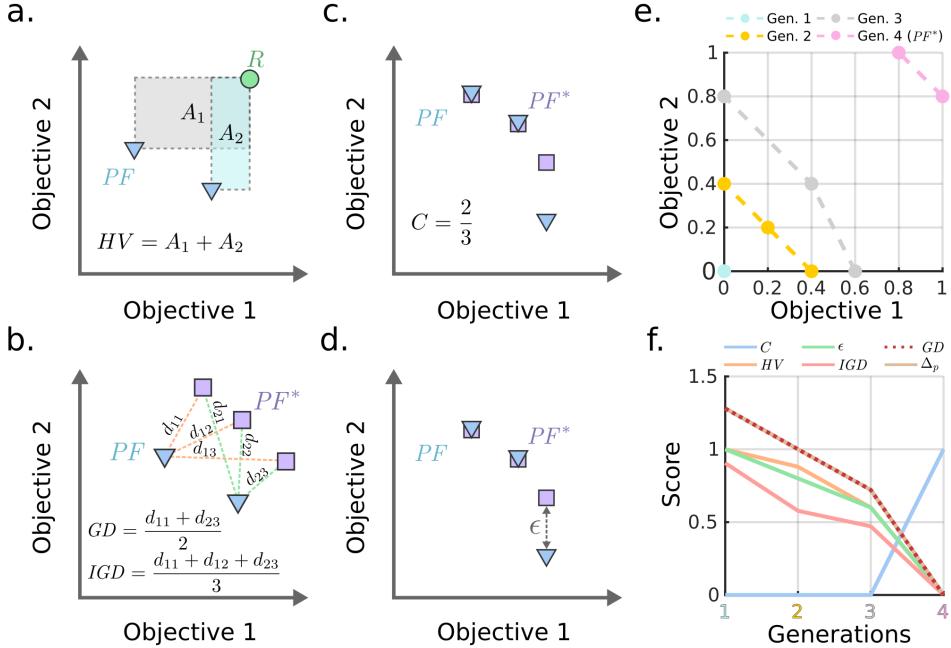


Figure 4.1: (a-d) Conceptual illustration of performance metrics of MOEAs for a two-objectives design problem. PF and PF^* correspond to the Pareto front approximation and the best Pareto front available, respectively. The reference point R must always dominate all solutions in PF . (e-f) An example of Pareto fronts with 2 dimensions and associated metrics. The 4th generation corresponds to \mathcal{PF}^* used as a reference for comparison.

4.2.5 Algorithm parameters

All parameters used in the simulations of this study were left as default except the following ones. The total number of generations was set to be 200, which was sufficient to reach high quality solutions for the problems of this study. In addition, the population size was set to be 100 for all algorithms unless noted otherwise. All problems were solved in triplicates with unique random number generator seeds.

4.2.6 Metabolic models

For all simulations, we used a core *E. coli* model, downloaded from the BiGG database (<https://bigg.ucsd.edu>) [117], that captures the most important metabolic pathways [180]. The product synthesis pathways for each module correspond to native *E. coli* pathways together with well-characterized heterologous pathways for the synthesis of propanol [246],

butanol [214], isobutanol [9], and pentanol [246]. The metabolic reactions associated with these pathways are described in the software implementation (Supplementary Material 1).

4.2.7 Implementation

The simulations were performed using the ModCell2 software framework [73]. The MOEAs are implemented in the PlatEMO Matlab library [235], except *gamultiobj* which is implemented as part of the Matlab Optimization Toolbox. *HV* was calculated using the *hv package* [67]. All computations were executed in a computer with the Arch Linux operative system, Intel Core i7-3770 processor, and 32 GB of random-access memory. The Matlab 2018b code used to generate the results of this manuscript is available in Supplementary Material 1 and <https://github.com/trinhlab/compare-moea>.

4.3 Results and Discussion

4.3.1 Case 1: A 3-objectives design problem

We first formulated a design problem that considers an *E. coli* core model and 3 production modules based on the endogenous acetate, D-lactate, and ethanol biosynthesis pathways (Figure 4.2a). We used all MOEAs to solve for the problem by setting the following design parameters: *wGCP* design objective, a maximum number of reaction deletions $\alpha = 3$, and no module reactions $\beta = 0$. These design parameters were sufficiently restrictive to generate conflicting objectives. A total coverage of \mathcal{PF}^* ($C = 1$) was reached within 20 generations by several algorithms (Figure 4.2b, e, h, i) and by *gamultiobj* after 150 generations (Figure 4.2k), while the remaining algorithms could not attain C values above 0.8 (Figure 4.2c, d, f, g, j, l). In particular, MaOEADDFC and BiGE obtained the worst C , ϵ , and Δ_p values (Figure 4.2m). Although C , ϵ , and Δ_p values of BiGE indicated inferior performance, this algorithm had the lowest *HV* since it generated only one point with a high objective value (Figure 4.2o). Due to the simplicity of the problem, every algorithm except MaOEADDFC, tDEA, and BiGE converged to very similar Pareto fronts (Figure 4.2n-x), and 5 of them reached $C = 1$, indicating convergence to the reference Pareto front (Figure 4.2y).

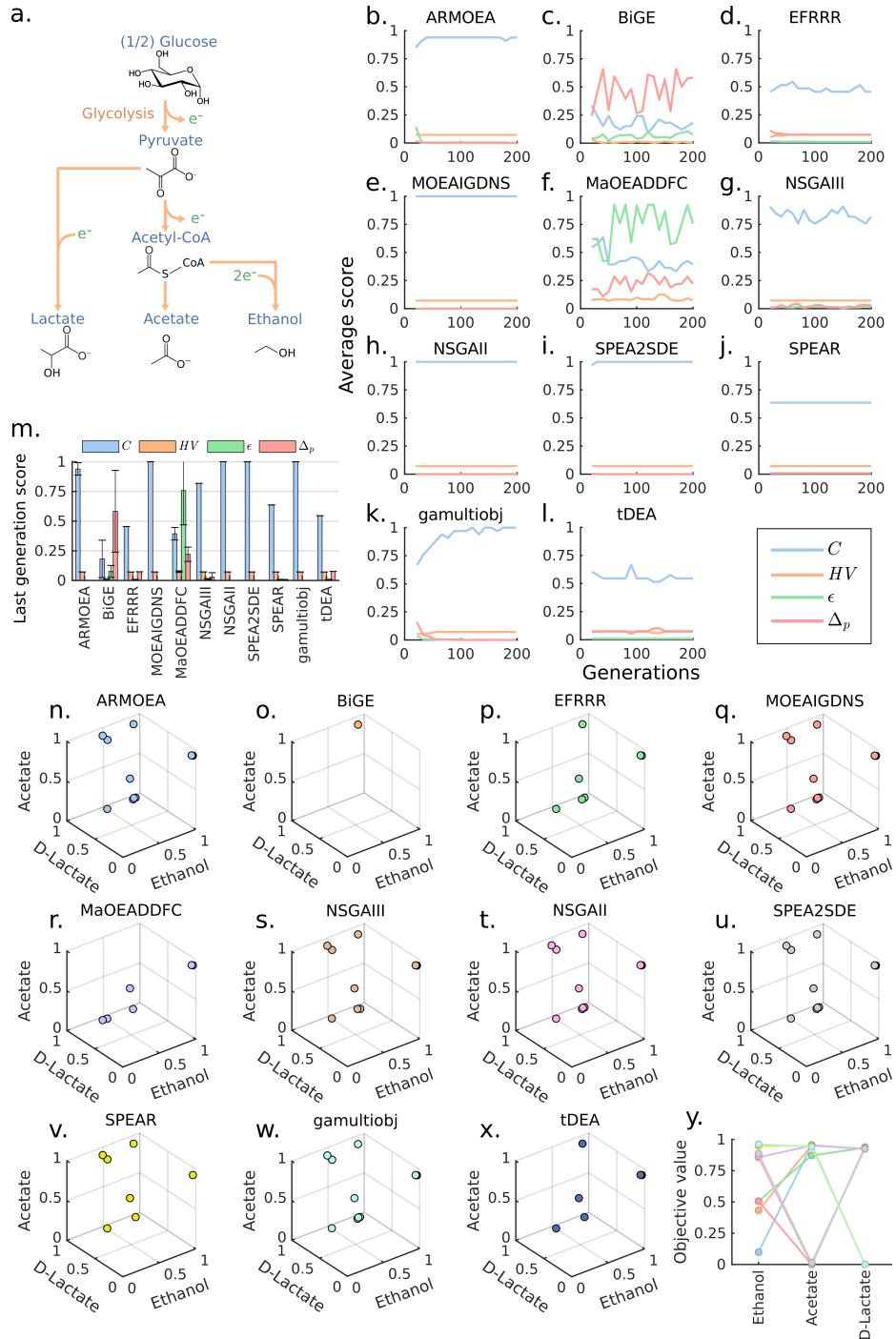


Figure 4.2: Comparison of MOEAs for a 3-objectives design problem. **(a)** The simplified metabolic pathways for conversion of glucose to the target products. Reducing equivalents are presented with e^- . **(b-l)** Generation-dependent performance metrics for various MOEAs. **(m)** Performance metrics for various MOEAs at the last generation. **(n-x)** Pareto fronts of various MOEAs at the last generation. It should be noted that only the first replicate is plotted for clear illustration. **(y)** Reference Pareto front ($\mathcal{P}\mathcal{F}^*$). Each line represents a solution.

4.3.2 Case 2: A 10-objectives design problem

Using the same model and design parameters as in Case 1, we expanded the number of objectives to represent a more realistic scenario. These objectives correspond to 6 endogenous pathways for biosynthesis of D-lactate, acetate, ethanol, formate, pyruvate and L-glutamate and 4 heterologous pathways for biosynthesis of propanol, butanol, isobutanol, and pentanol. The additional objectives increased the difficulty of the problem, leading to more notable difference among algorithm performances (Figure 4.3a-k). The SPEA2SDE algorithm displayed consistent improvement of C as generations progressed, and quickly reached the smallest values of ϵ and Δ_p (Figure 4.3h). Other algorithms, including ARMOEA and MOEAIGDNS, also improved their ϵ values with the increasing number of generations and reached the same final values of ϵ and Δ_p as SPEA2SDE (Figure 4.3a, d). However, SPEA2SDE approached $C \cong 0.6$, which is twice the value reached by the next best-performing methods (Figure 4.3l). Remarkably, SPEA2SDE outperformed every other algorithm in all metrics, except HV . The HV metric continues to show bias towards algorithms that generated a small number of points and scored poorly in other metrics.

4.3.3 Case 3: Use of large population size overcomes poor MOEA performance

Increasing the number of objectives often leads to a combinatorial explosion of the number of feasible Pareto optimal points and consequently causes poor MOEA performance. This problem can be alleviated by using a larger population size to sample a broader volume of solution space [98]. To test this strategy for the 10-objectives design problem above, we increased the population size from 100 to 1000 individuals while all other parameters remained unchanged. The result showed that ARMOEA, MOEAIGDNS, NSGAII, SPEA2SDE (the best performer in Case 2), and *gamultiobj*, could reach C of 0.7, ϵ of 0, and Δ_p of 0 in fewer than 50 generations (Figure 4.4a, d, g, h, j). These 5 algorithms also yielded very similar final values across all metrics (Figure 4.4l). The remaining algorithms converged to considerably lower C values (Figure 4.4b, c, e, f, i, k).

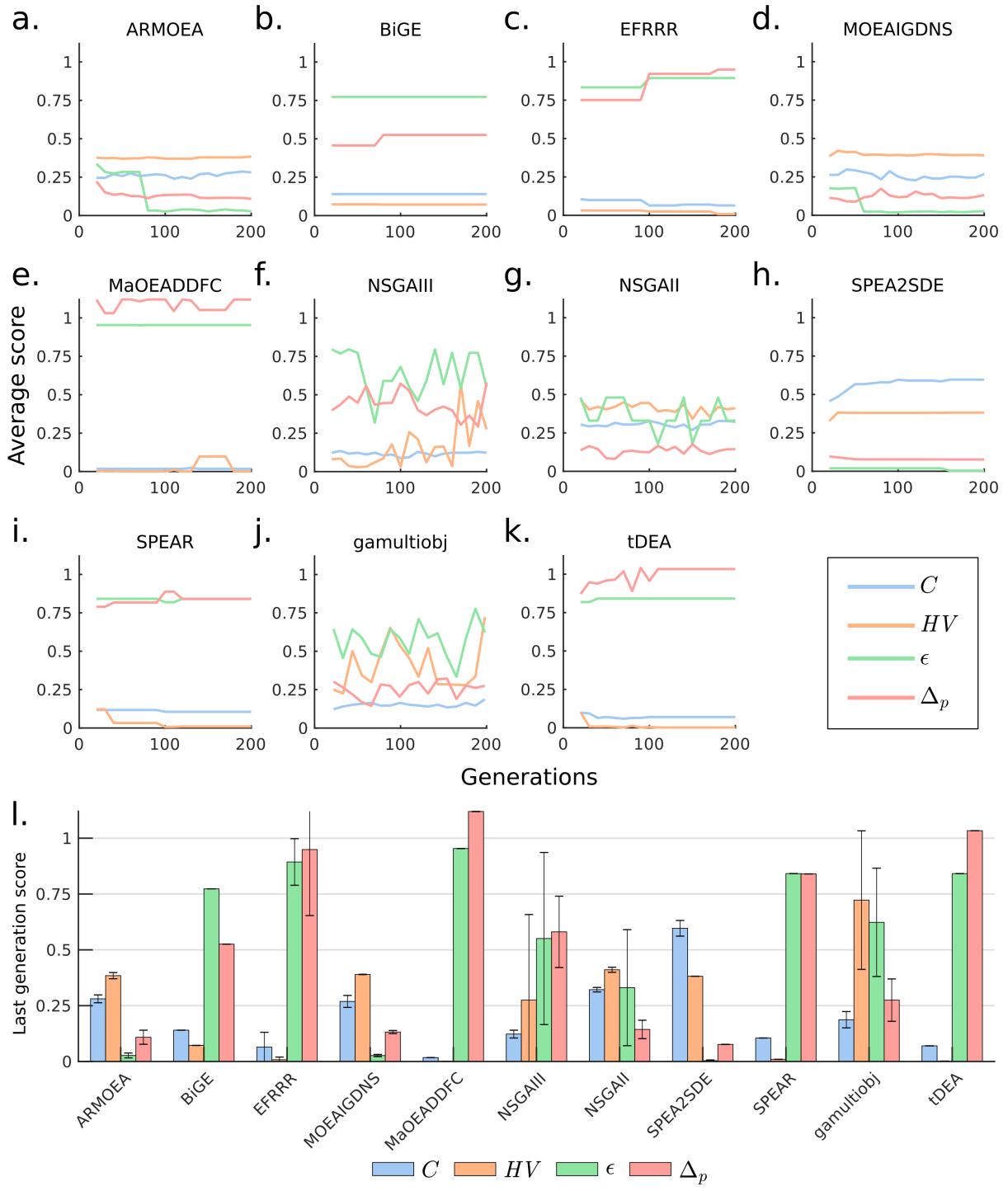


Figure 4.3: Comparison of MOEAs for a 10-objective design problem. (a-k) Generation-dependent performance metrics for various MOAEAs. (l) Performance metrics for various MOEAs at the last generation.

Remarkably, NSGAII/*gamultiobj*, that is not considered a many-objective solver, performed better than more recent many-objective algorithms such as NSGAIID.

One limitation of using larger populations is an increased cost in computational time. We observed that a 10-fold increase in population sizes resulted in a 10-fold increase in the run times (Figure 4.5). Nonetheless, all metrics reached a stable value in the top performing algorithms after 50 generations (out of 200 total), suggesting that fewer generations were needed by using a larger population size. Among the best performing algorithms with large population sizes, *gamultiobj*, implemented in the Matlab Optimization Toolbox, required the shortest run time, followed by NSGAII and SPEA2SDE implemented in PlatEMO.

4.4 Conclusions

In this study, we evaluated the performance of several MOEAs to solve the modular cell design problem. SPEA2SDE, the recently developed many-objectives method, was the best performing MOEA for limited population sizes in our study. However, for sufficiently large populations, several algorithms attained the best results, including the well-established NSGAII, which performed better than more recently developed many-objectives MOEAs. We used the most popular performance metrics to compare MOEAs and found that the coverage (C) metric is the most valuable indicator. This metric can provide an intuitive quantitative meaning and tends to increase monotonically with the number of generations simulated. In contrast, hypervolume (HV) generally did not differentiate algorithm performance and was misleading in some scenarios where an algorithm generated very few solutions. Overall, these results highlight the need for empirical testing of MOEAs towards specific problems and of the population size as a more important factor in performance than the unique heuristics commonly used by different algorithms. For the application of modular cell engineering, efficient MOEAs will enable the design of modular cell(s) compatible with many product synthesis modules for large-scale metabolic networks and the identification of more diverse and better solutions that will provide more viable options for practical implementation.

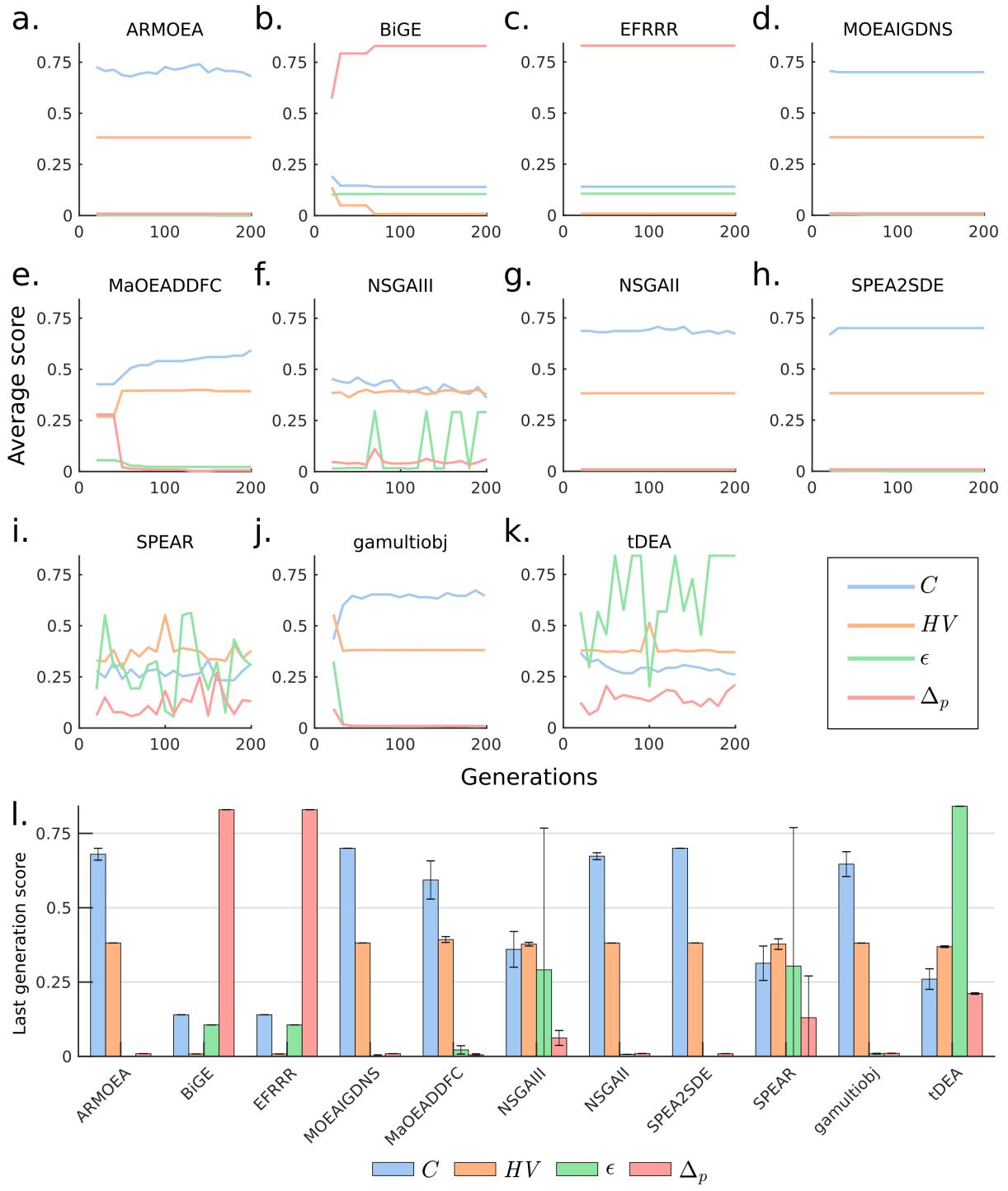


Figure 4.4: Comparison of MOEAs for a 10-objectives design problem with larger population sizes (a-k) Generation-dependent performance metrics for various MOAEs. (l) Performance metrics for various MOEAs at the last generation.

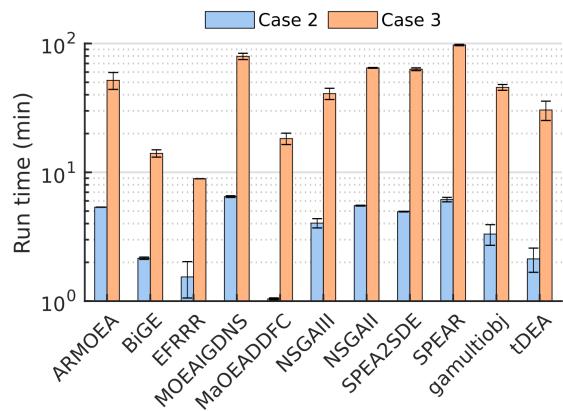


Figure 4.5: Wall-clock run times for the 10-objectives design problem with population sizes of 100 (Case 2) and 1000 (Case 3).

Chapter 5

Development of linear formulations to solve the modular cell problem and application to design a universal modular cell

This chapter is based on the publication *Harnessing natural modularity of cellular metabolism to design a modular chassis cell for a diverse class of products by using goal attainment optimization.* Garcia, S., and Trinh, C. T. In review, 2019. As first author I lead the development, implementation, and writing of this study. Supplementary Files S1 and S2 are provided as attachments.

Abstract

Modular design is key to achieve efficient and robust systems across engineering disciplines. Modular design potentially offers advantages to engineer microbial systems for biocatalysis, bioremediation, and biosensing, overcoming the slow and costly design-build-test cycles in the conventional cell engineering approach. These systems consist of a modular cell chassis compatible with modules that enable programmed functions such as overproduction of a desirable chemical. We previously proposed a multi-objective optimization framework

coupled with metabolic flux models to design modular cells and solved it using multi-objective evolutionary algorithms. However, such approach might not achieve solution optimality and hence limit design options for experimental implementation. In this study, we developed the goal attainment formulation compatible with optimization algorithms that guarantee solution optimality. We applied goal attainment to design an *Escherichia coli* modular cell capable of synthesizing all molecules in a biochemically diverse library at high yields and rates with only a few genetic manipulations. To elucidate modular organization of the designed cells, we developed a flux variance clustering (FVC) method by identifying reactions with high flux variance and clustering them to identify metabolic modules. Using FVC, we identified reaction usage patterns for different modules in the modular cell, revealing its broad pathway compatibility is enabled by the natural modularity and flexible flux capacity of endogenous core metabolism. Overall, this study not only sheds light on modularity in metabolic networks from their topology and metabolic functions but also presents a useful synthetic biology toolbox to design modular cells with broad applications.

5.1 Introduction

Microbial metabolism can be engineered to produce a large space of molecules from renewable and sustainable feedstocks [131]. Currently, only a handful of fuels and chemicals out of the many possible molecules offered by nature are industrially produced by microbial conversion, mainly because the strain engineering process is too laborious and expensive [172]. To overcome this roadblock and produce a more diverse range of molecules requires innovative technologies for rapid and economically competitive strain engineering [242, 172, 131]. The principles of modular design that have shown great success in traditional engineering disciplines can be adapted to construct modular cell biocatalysts in a plug-and-play fashion with minimal strain design-build-test cycles [72].

Multi-objective optimization is a powerful mathematical framework widely applied in engineering disciplines to tackle the optimal design of a complex system with multiple conflicting objectives [40, 192]. This framework has recently been used to design modular systems in conventional engineering [91], and to explain the modularity of natural biological

systems that enable cellular robustness and adaptability [119, 110, 39, 216, 208]. Using multi-objective optimization, microbial metabolism can be redirected to generate modular production strains that are systematically assembled from an engineered modular cell and exchangeable production modules, where each module synthesizes a target molecule [73]. This modular cell design approach, known as ModCell2, uses the principles of mass balance and thermodynamics of biochemical reaction networks to predict metabolic fluxes upon genetic manipulations [73, 71]. Based on such flux predictions, a multi-objective optimization problem is then formulated and solved with a multi-objective evolutionary algorithm (MOEA)[280, 51] to yield a sample of the Pareto front (i.e., the set of optimal solutions to the problem with minimal trade-offs among objectives) that a designer can explore genetic manipulation targets for modular cell engineering.

In this study, we developed ModCell2-MILP, a ModCell2-based formulation to be compatible with mixed integer linear programming (MILP) algorithms. This framework presents a significant advancement from ModCell2 in solving the multi-objective strain design problem for modular cell engineering. Specifically, ModCell2-MILP is developed to (i) guarantee optimal solutions, (ii) completely enumerate alternative solutions of a target design, and (iii) describe practical engineering goals more directly (e.g., design of a modular cell where all production modules lead to a product yield above 50% of the theoretical maximum). By applying ModCell2-MILP to analyze the genome-scale metabolic network of *Escherichia coli*, we could identify a universal modular cell that is compatible with a diverse class of production modules. To gain a mechanistic view into the modular organization of metabolic networks, we developed a flux variance clustering (FVC) method by identifying reactions with high flux variance and clustering them to identify metabolic modules. Using FVC, we found that broad pathway compatibility of the modular cell is facilitated by its natural modularity and flexible flux capacity of endogenous core metabolism. We anticipate ModCell2-MILP and FVC can serve as powerful tools for not only elucidating natural and synthetic metabolic modularity but also rationally designing modular cells for broad biotechnological applications in biocatalysis, bioremediation, and biosensing.

5.2 Materials and methods

5.2.1 Modular cell design

Design principles

ModCell design enables rapid assembly of production strains with desirable phenotypes from a modular (chassis) cell [241, 73, 72]. More specifically, a modular cell contains core metabolic pathways shared among production modules (Figure 5.1a). The chassis interfaces with the modules through enzymatic and genetic synthesis machinery and precursor metabolites (Figure 5.1b). Modules contain auxiliary regulatory and metabolic pathways (Figure 5.1c) that enable a desired phenotype for optimal biosynthesis of a target molecule, for example, *weak growth coupled to product formation (wGCP)*, where a positive correlation between growth and product synthesis rates is enforced (Figure 5.1d) [24, 120, 73]. The *wGCP* phenotype is useful because it enables rapid pathway optimization by adaptive laboratory evolution [66, 237] or high-throughput genetic library selection [74]. The design objective phenotypes are determined from cellular growth and product synthesis rates based on steady-state stoichiometric metabolic models [180]. A modular cell is said to be *compatible* with a module if the design objective of the resulting production strain is above a specified threshold. The different biochemical nature of production modules to synthesize target metabolites can make the design objectives compete with each other and also the cellular objectives (e.g., biomass formation) compete with the engineering objectives (e.g., product formation), turning the ModCell design problem into a multi-objective and multi-level optimization problem.

Multi-objective optimization formulation

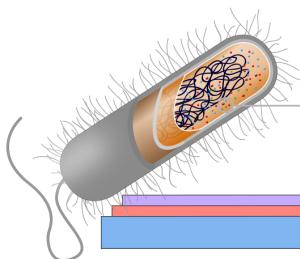
The modular cell design problem is stated as a general multi-objective optimization problem of the form:

$$\max_x \quad F(x) = (f_1(x), f_2(x), \dots, f_K(x))^\top \quad \text{s.t. } x \in X \quad (5.1)$$

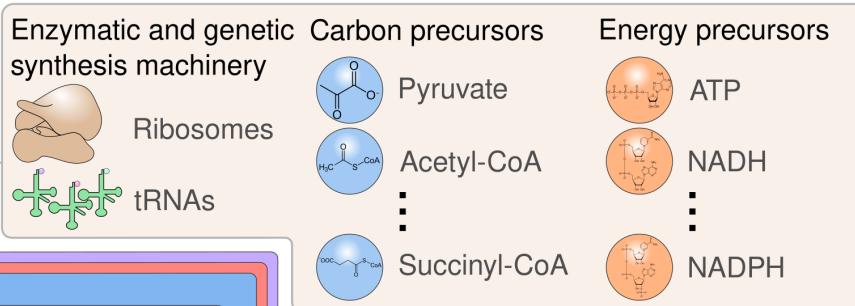
where f_k is the desirable phenotype for production module k , x are the problem variables including binary design variables corresponding to genetic manipulations, and X is the set of

Figure 5.1: Principles of modular cell design. (a) Modular cell chassis. (b) Interfaces. (c) Production modules. (d) Production strains. A modular cell is designed to provide the necessary precursors for biosynthesis pathway modules that are independently assembled with the modular cell to generate production strains exhibiting desirable phenotypes. The *wGCP* phenotype, one of the possible design objectives, enforces the coupling between the desirable product synthesis rate and the maximum cellular growth rate.

a. Chassis

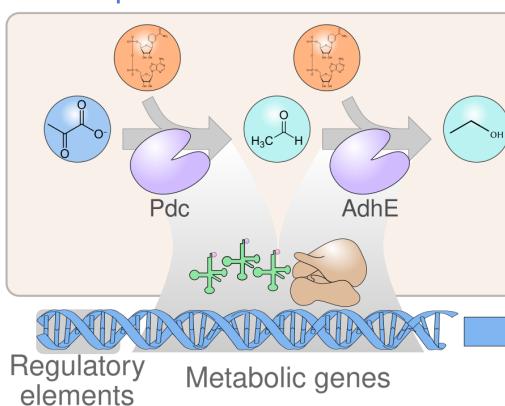


b. Interfaces

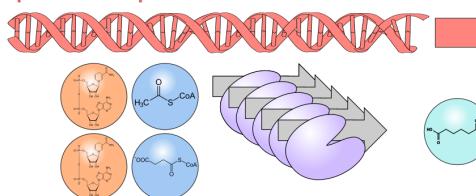


c. Modules

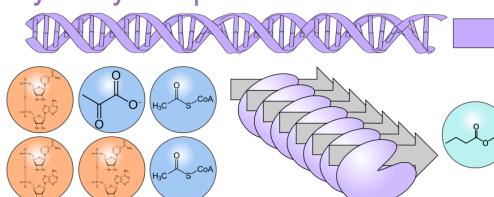
Ethanol production



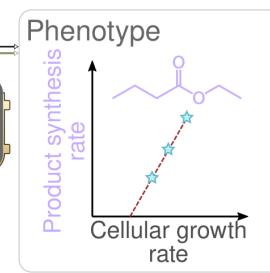
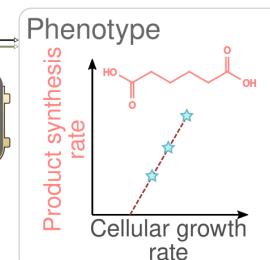
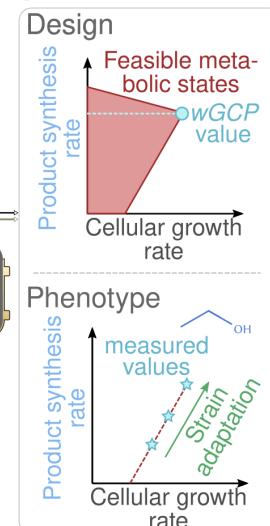
Adipic acid production



Ethyl butyrate production



d. Production strains



constraints including mass balance of metabolism. Optimal solutions for the multi-objective optimization problem (5.1) are defined using the concept of domination: A vector $a = (a_1, \dots, a_K)^\top$ *dominates* another vector $b = (b_1, \dots, b_K)^\top$, denoted as $a \prec b$, if and only if $a_i \geq b_i \forall i \in \{1, 2, \dots, K\}$ and $a_i \neq b_i$ for at least one i . A feasible solution $x^* \in X$ of the multi-objective optimization problem is called a Pareto optimal solution if and only if there does not exist a vector $x' \in X$ such that $F(x') \prec F(x^*)$. The set of all Pareto optimal solutions is called Pareto set:

$$PS := \{x \in X : \nexists x' \in X, F(x') \prec F(x)\} \quad (5.2)$$

The projection of the Pareto set in the objective space is denoted as Pareto front:

$$PF := \{F(x) : x \in PS\} \quad (5.3)$$

Different feasible points in PS (i.e., different genetic manipulations) which map to a single point in PF (i.e., the same phenotype) are denoted *alternative solutions*.

The design variables x in ModCell2 correspond to chassis reaction deletions, that remove undesired metabolic functions, and module reaction insertions, that allow to identify optimal module configurations without extensive prior knowledge of the product synthesis pathway. The constraint set X is comprised of two types: (i) flux simulation constraints (e.g., mass balance, reaction reversibility, and flux bound) that allow to predict fluxes in the design objectives upon genetic manipulations, and (ii) implementation constraints that involve the maximum number of reaction deletions in the chassis (denoted by α) and the maximum number of module reaction insertions per module (denoted by β). The following sections describe the problem formulation in detail using the definitions compiled in the Definitions Section.

Design objectives

Design objectives, f_k , that correspond to specific metabolic phenotypes within the space of feasible steady-state reaction fluxes, Π_{km} , of production network k (i.e., the combination of

the chassis network with the production module k) and metabolic state m , are defined as follows:

$$\Pi_{km}(e_{jk}) := \{v_{jkm} \in \mathbb{R} : \quad (5.4)$$

$$\sum_{j \in \mathcal{J}_k} S_{ijk} v_{jkm} = 0 \quad \forall i \in \mathcal{I}_k \quad (5.5)$$

$$l_{jkm} e_{jk} \leq v_{jkm} \leq u_{jkm} \quad \forall j \in \mathcal{J}_k \quad (5.6)$$

Here, v_{jkm} is the rate (mmol/gCDW/hr) of reaction j in production network k under metabolic state m . Constraint (5.5) enforces mass balance for all metabolites according to reaction stoichiometry given by the coefficients S_{ijk} , and constraint (5.6) imposes bounds, l_{jkm} and u_{jkm} , for the metabolic fluxes according to reaction reversibility, experimentally measured values, and specified metabolic state. The binary variable e_{jk} is used in the overall optimization problem to indicate whether reaction j in production network k is removed and thus cannot carry any flux. Two metabolic states m are considered, growth and non-growth, denoted μ and $\bar{\mu}$, respectively. These states are differentiated by their flux bounds l_{jkm} and u_{jkm} . For growth state, the lower bound of the biomass formation reaction that represents cell division, v_{Xkm} , is set to a minimum value of γ , i.e., $l_{Xk\mu} = \gamma$ ($\forall k \in \mathcal{K}$), while there is no upper limit to growth, i.e., $u_{Xk\mu} = \infty$ ($\forall k \in \mathcal{K}$). On the other hand, for the non-growth state both bounds are set to 0, i.e., $l_{Xk\bar{\mu}} = 0$ and $u_{Xk\bar{\mu}} = 0$ ($\forall k \in \mathcal{K}$).

Given the feasible metabolic flux space, Π_{km} , the following design objectives, based on the product synthesis rate reaction, v_{Pkm} , are of interest:

$$f_k^{wGCP} = \frac{v_{Pk\mu}}{v_{Pk\mu}^{\max}} \in [0, 1], \quad \forall k \in \mathcal{K} \quad (5.7)$$

$$f_k^{lsGCP} = b_\mu \frac{v_{Pk\mu}}{v_{Pk\mu}^{\max}} + b_{\bar{\mu}} \frac{v_{Pk\bar{\mu}}}{v_{Pk\bar{\mu}}^{\max}} \in [0, b_\mu + b_{\bar{\mu}}], \quad \forall k \in \mathcal{K} \quad (5.8)$$

$$f_k^{NGP} = \frac{v_{Pk\bar{\mu}}}{v_{Pk\bar{\mu}}^{\max}} \in [0, 1], \quad \forall k \in \mathcal{K} \quad (5.9)$$

The product synthesis fluxes, including $v_{P\bar{k}\mu}$, $v_{P\bar{k}\mu}^{max}$, $v_{P\bar{k}\bar{\mu}}$, and $v_{P\bar{k}\bar{\mu}}^{max}$, are computed by solving the following linear programming problems:

$$v_{P\bar{k}\mu} \in \arg \max \{v_{Xk\mu} - \epsilon v_{P\bar{k}\mu} : v_{k\mu} \in \Pi_{k\mu}(e_{jk})\} \quad (5.10)$$

$$v_{P\bar{k}\mu}^{max} \in \arg \max \{v_{P\bar{k}\mu} : v_{k\mu} \in \Pi_{k\mu}(e_{jk} = 1, \forall j \in \mathcal{J}_k)\} \quad (5.11)$$

$$v_{P\bar{k}\bar{\mu}} \in \arg \min \{v_{P\bar{k}\bar{\mu}} : v_{k\bar{\mu}} \in \Pi_{k\bar{\mu}}(e_{jk})\} \quad (5.12)$$

$$v_{P\bar{k}\bar{\mu}}^{max} \in \arg \max \{v_{P\bar{k}\bar{\mu}} : v_{k\bar{\mu}} \in \Pi_{k\bar{\mu}}(e_{jk} = 1, \forall j \in \mathcal{J}_k)\} \quad (5.13)$$

The maximum product synthesis fluxes (5.11) and (5.13) used for objective scaling are only calculated once by not using any deleted reactions ($e_{jk} = 1$), while the target phenotype fluxes (5.10) and (5.12) are functions of the deleted reactions e_{jk} . The design objectives, *wGCP* (5.7), *lsGCP* (5.8), and *NGP* (5.9), were previously proposed [73] and briefly described here. The weak growth coupled to product formation objective (*wGCP*) (5.7) seeks to maximize the minimum product rate at the maximum cellular growth, which is accomplished by a titled objective function[63] (5.10). The linearized strong growth coupled to product formation (*lsGCP*) (5.8) objective seeks to maximize the minimum product synthesis rate at the non-growth state $v_{P\bar{k}\bar{\mu}}$ in addition to the goal of *wGCP*. Finally, the non-growth production (*NGP*) (5.9) objective seeks to optimize the minimum product synthesis rate during the non-growth state.

Design constraints

All the constraints of the modular cell design problem are gathered as follows:

$$\Omega := \{f'_k \in \mathbb{R}, y_j, z_{jk}, d_{jk}, w_k, e_{jk} \in \{0, 1\} : \quad (5.14)$$

$$\sum_{j \in \mathcal{C}} (1 - y_j) \leq \alpha \quad (5.15)$$

$$\sum_{j \in \mathcal{C} - \mathcal{N}_k} z_{jk} \leq \beta_k \quad \forall k \in \mathcal{K} \quad (5.16)$$

$$z_{jk} \leq 1 - y_j \quad \forall j \in \mathcal{C} - \mathcal{N}_k, k \in \mathcal{K} \quad (5.17)$$

$$d_{jk} = y_j \vee z_{jk} \quad \forall j \in \mathcal{C}, k \in \mathcal{K} \quad (5.18)$$

$$f'_k = f_k w_k \quad \forall k \in \mathcal{K} \quad (5.19)$$

$$e_{jk} = (d_{jk} \wedge w_k) \vee \neg w_k \quad \forall j \in \mathcal{C}, k \in \mathcal{K} \quad (5.20)$$

$$w_k \leq M^w f_k \quad \forall k \in \mathcal{K} \quad (5.21)$$

$$v_{Pkm} \in \Psi_{km}(e_{jk}) \quad \forall k \in \mathcal{K}, m \in \mathcal{M} \} \quad (5.22)$$

Constraints (5.15)-(5.18) are formulated for practical limitations and features of the modular cell. Specifically, the two variables that represent design choices for genetic manipulations include: (i) y_j that takes a value of 0 if reaction j is deleted in the chassis (and consequently in all production networks) and 1 otherwise and (ii) z_{jk} that takes a value of 1 if reaction j is inserted in production network k . The maximum number of reaction deletions, is limited by α through constraint (5.15) while the maximum number of module reactions in each module β_k is imposed by (5.16). Constraint (5.16) excludes non-candidate reactions \mathcal{N}_k (since $j \in \mathcal{C} - \mathcal{N}_k$) so that endogenous module reactions can be fixed (i.e., $z_{jk} = 1$), according to problem-specific knowledge. Constraint (5.17) ensures that only reactions deleted in the chassis can be inserted back to the modules. Constraint (5.18) indicates that reaction j is deleted in production network k if the reaction is deleted in the chassis and not added as an endogenous module reaction. The designer can gradually increase α and β_k to obtain solutions with higher performance.

Constraints (5.19)-(5.21) are introduced for modeling purposes. The indicator variable, w_k , is introduced to allow for certain production networks to be ignored from the final

solution. Without w_k , the whole multi-objective problem becomes infeasible if a set of deletions renders one of the production networks infeasible (e.g., its minimum growth rate cannot be accomplished). However, in practice it is acceptable for some modules not to work with the chassis cell. If $w_k = 0$, the objective value $f'_k = 0$ (5.19) and reaction deletions do not apply to network k since $e_{jk} = 1$ (5.20); if $w_k = 1$, $f'_k = f_k$ and $e_{jk} = d_{jk}$, where f_k is any of the design objectives presented earlier (5.7)-(5.9). The use of w_k is likely to introduce symmetry (i.e., alternative integer solutions with no practical meaning) due to cases where $f_k = 0$ for a given k while the associated production network remains feasible, allowing w_k to take a value of 0 or 1. This symmetry is removed by enforcing w_k to be 0 if $f_k = 0$ (5.21).

Finally, constraint (5.22) indicates that the fluxes featured in the design objectives, v_{Pkm} , are contained in the polytope Ψ_{km} . The space of v_{Pkm} is originally defined as an optimization problem (5.10)-(5.13), thus representing a non-linear constraint and turning the ModCell design problem into a bilevel optimization problem. These inner optimization problems are linearized, leading to Ψ_{km} as described in the following sections.

Linearization of logical expressions

The logical expressions in Ω are replaced by the following linear constraints in the final problem formulation:

$d_{jk} = y_j \vee z_{jk}$ corresponds to:

$$d_{jk} \leq y_j + z_{jk} \quad (5.23)$$

$$d_{jk} \geq y_j \quad (5.24)$$

$$d_{jk} \geq z_{jk} \quad (5.25)$$

$$0 \leq d_{jk} \leq 1 \quad (5.26)$$

$f'_k = f_k w_k$ corresponds to:

$$f'_k \leq w_k M^{obj} \quad (5.27)$$

$$f'_k \leq f_k - (1 - w_k) M^{obj} \quad (5.28)$$

$$f'_k \leq f_k \quad (5.29)$$

$$0 \leq f'_k \leq M^{obj} \quad (5.30)$$

$e_{jk} = (d_{jk} \wedge w_k) \vee \neg w_k$, given $r_{jk} = d_{jk} \wedge w_k$, corresponds to:

$$e_{jk} = r_{jk} + 1 - w_k \quad (5.31)$$

$$r_{jk} \leq w_k \quad (5.32)$$

$$r_{jk} \leq d_{jk} \quad (5.33)$$

$$r_{jk} \geq w_k + d_{jk} - 1 \quad (5.34)$$

$$0 \leq r_{jk} \leq 1 \quad (5.35)$$

Linearization of inner optimization problems

Non-linear constraints expressed as linear programming problems can be linearized using basic mathematical programming theory. Consider the following canonical linear program, with primal variables $x \in \mathbb{R}^n$ and its dual variables $u \in \mathbb{R}^m$:

$$\max \quad \{c^\top x : Ax \leq b, x \geq 0\} \quad (5.36)$$

$$\min \quad \{b^\top u : A^\top u \geq c, u \geq 0\} \quad (5.37)$$

the strong duality theorem states that the objective functions of primal (5.36) and dual (5.37) are equal at their optima, $c^\top x^* = b^\top y^*$. Thus the optimal solution to the primal

problem is described by the following linear constraints:

$$x^* \in \{x \in \mathbb{R}^n : \quad (5.38)$$

$$Ax \leq b \quad (5.39)$$

$$A^\top u \geq c \quad (5.40)$$

$$c^\top x = b^\top u \quad (5.41)$$

$$x, u \geq 0 \} \quad (5.42)$$

Using the strong duality theorem as presented by Maranas and Zomorodi [154], the inner optimization problems (5.22) are linearized as follows:

$$\Psi_{km}(e_{jk}) := \{v_{jkm} \in \mathbb{R} : \quad (5.43)$$

$$\sum_{j \in \mathcal{J}_k} S_{ijk} v_{jkm} = 0 \quad \forall i \in \mathcal{I}_k \quad (5.44)$$

$$l_{jkm} e_{jk} \leq v_{jkm} \leq e_{jk} u_{jkm} \quad \forall j \in \mathcal{J}_k \quad (5.45)$$

$$\sum_{i \in \mathcal{I}_k} \lambda_{ikm} S_{ijk} - \mu_{jkm}^l + \mu_{jkm}^u = c_{jkm} \quad \forall j \in \mathcal{J}_k \quad (5.46)$$

$$\lambda_{ikm} \in \mathbb{R} \quad \forall i \in \mathcal{I}_k \quad (5.47)$$

$$0 \leq \mu_{jkm}^l \leq M \quad \forall j \in \mathcal{J}_k \quad (5.48)$$

$$0 \leq \mu_{jkm}^u \leq M \quad \forall j \in \mathcal{J}_k \quad (5.49)$$

$$\begin{aligned} \sum_{j \in \mathcal{J}_k} c_{jkm} v_{jkm} = & - \sum_{j \in \mathcal{J}_k - \mathcal{C}} (l_{jkm} \mu_{jkm}^l) + \sum_{j \in \mathcal{J}_k - \mathcal{C}} (u_{jkm} \mu_{jkm}^u) \\ & - \sum_{j \in \mathcal{C}} (l_{jkm} p_{jkm}^l) + \sum_{j \in \mathcal{C}} (u_{jkm} p_{jkm}^u) \end{aligned} \quad (5.50)$$

$$p_{jkm}^l \leq e_{jk} M \quad \forall j \in \mathcal{C} \quad (5.51)$$

$$\mu_{jkm}^l - (1 - e_{jk})M \leq p_{jkm}^l \leq \mu_{jkm}^l \quad \forall j \in \mathcal{C} \quad (5.52)$$

$$0 \leq p_{jkm}^l \leq M \quad \forall j \in \mathcal{C} \quad (5.53)$$

$$p_{jkm}^u \leq e_{jk} M \quad \forall j \in \mathcal{C} \quad (5.54)$$

$$\mu_{jkm}^u - (1 - e_{jk})M \leq p_{jkm}^u \leq \mu_{jkm}^u \quad \forall j \in \mathcal{C} \quad (5.55)$$

$$0 \leq p_{jkm}^u \leq M \quad \forall j \in \mathcal{C} \} \quad (5.56)$$

Constraints (5.44)-(5.45) correspond to the primal metabolic network problem and were introduced earlier in Π_{km} . Constraints (5.46)-(5.49) correspond to the dual problem. We use the dual variables, λ_{ikm} , for the primal mass balance constraints (5.44), together with μ_{jkm}^l and μ_{jkm}^u for the primal flux bound inequalities (5.45) involving lower and upper reaction bounds respectively. Constraints (5.47)-(5.49) emphasize the domain of the dual variables, with M being a large value above the expected value of any dual variable. Constraints (5.50)-(5.56) correspond to the strong duality equality. The left hand side of the strong duality equality (5.50) features the objectives presented in (5.10) for $m = \mu$ and (5.12) for $m = \bar{\mu}$. On the right hand side, products of binary and continuous variables appear, thus requiring linearization variables p_{jkm}^l and p_{jkm}^u . Constraints (5.51)-(5.56) ensure that $p_{jkm}^l = e_{jk}\mu_{jkm}^l$ and $p_{jkm}^u = e_{jk}\mu_{jkm}^u$.

Conversion of a multi-objective problem into a single-objective problem

The multi-objective optimization problem (5.1) is now described entirely in terms of linear constraints through Ω . However, to make the formulation compatible with MILP solver algorithms, the objective function vector, f' , must be expressed as a scalar. To accomplish this without loss of relevant information, we employed blended and goal attainment formulations [155].

Blended formulation In the blended formulation all objectives are summed as follows:

$$\max \quad \sum_{k \in \mathcal{K}} a_k f'_k \quad \text{s.t. } f' \in \Omega \quad (5.57)$$

where a_k is a scalar weighting factor associated with the design objective of product k . Different Pareto optimal solutions can be obtained by varying these weights. The blended formulation always provides Pareto optimal solutions as long as $a_k > 0$ ($\forall k \in K$). In practice, the product priority, a_k , can be determined by criteria such as product market value or “pathway readiness level” (i.e., certain pathways are easier to engineer than others).

Goal attainment formulation In the goal attainment problem a target value is defined for each objective:

$$\min \quad \sum_{k \in \mathcal{K}} (a_k^+ \delta_k^+ + a_k^- \delta_k^-) \quad (5.58)$$

s.t.

$$f'_k + \delta_k^+ - \delta_k^- = g_k \quad \forall k \in \mathcal{K} \quad (5.59)$$

$$\delta_k^+, \delta_k^- \geq 0 \quad \forall k \in \mathcal{K} \quad (5.60)$$

$$f' \in \Omega \quad (5.61)$$

The problem seeks to minimize the variables δ_k^+ and δ_k^- that represent the deficiency and excess of the objective f'_k from the target value g_k , respectively. Weighting parameters a_k^+ and a_k^- correspond to different types of discrepancy to be minimized. In general, when it is important to meet the target value without exceeding it, we set $a_k^+ = a_k^- = 1$; however, when the design objective is required to be greater or equal than the target value, we set $a_k^+ = 1$ and $a_k^- = 0$, effectively converting (5.59) into $f'_k + \delta_k^+ \geq g_k$. Solutions to the goal attainment problem are not guaranteed to be Pareto optimal, even if all demands g_k are met. To address this issue, the blended problem (5.57) can be solved where the objectives are constrained to be equal or greater than the values found by solving the goal attainment problem. In practice, the goal attainment formulation corresponds to the identification of the modular cell *compatible* with the largest number of modules. Here, a module k is said to be *compatible* if $f'_k \geq g_k$.

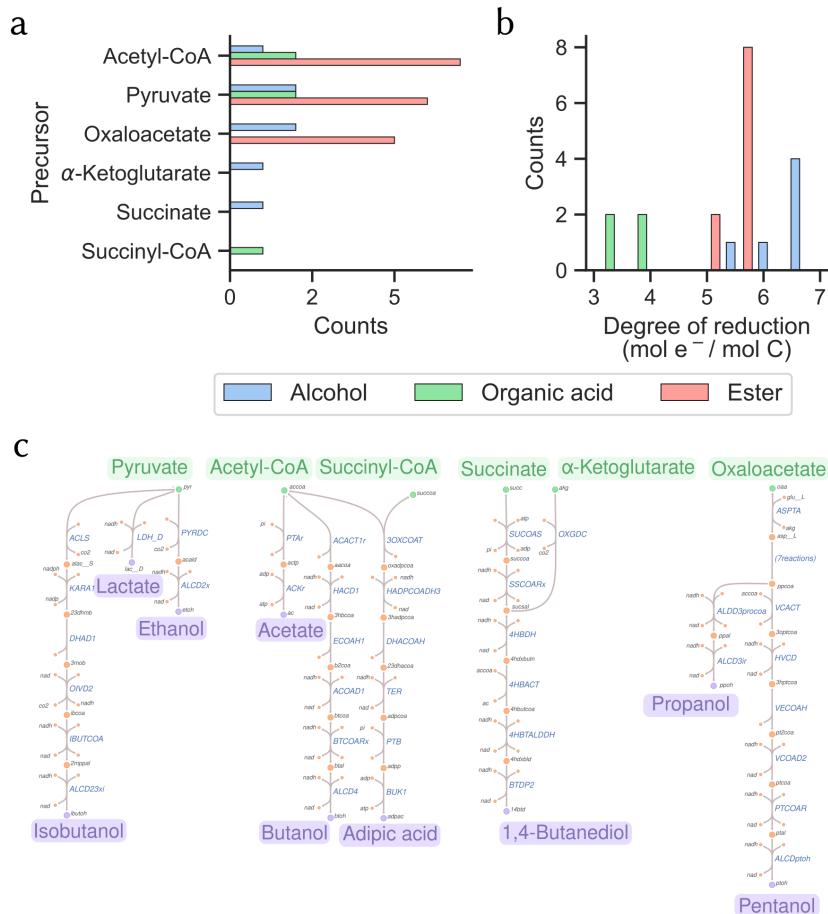
5.2.2 Implementation

Metabolic models

We used two parent models from which production networks were built, including: i) a core metabolic model of *E. coli* [241] to develop the ModCell2-MILP algorithm and compare with previous ModCell2 results [73], and ii) the iML1515 genome-scale metabolic model of *E. coli* [165] for biosynthesis of a library of endogenous and heterologous metabolites,

including 4 organic acids, 6 alcohols, and 10 esters (Figure 5.2) [4, 9, 127, 173, 198, 214, 243, 246, 269, 272]. These models were configured as in the previous ModCell2 study[73], briefly: Anaerobic conditions were imposed by setting oxygen exchange fluxes to be 0, and the glucose uptake rate was constrained to be at most 10 mmol/gCDW/h. When using the genome-scale model iML1515 to simulate *wGCP* designs, only the commonly observed fermentative products (acetate, CO₂, ethanol, formate, lactate, succinate) were allowed for secretion as described elsewhere [251].

Figure 5.2: Biochemical and metabolic diversity of the 20 production modules. (a) Precursor metabolite distribution, using the 12 essential biomass precursors as a reference. (b) Degrees of reduction of the produced metabolites. (c) Production pathway metabolic modules excluding esters.



ModCell2-MILP simulations

ModCell2-MILP was implemented using Pyomo [86], an algebraic modeling language embedded in the Python programming language. All simulations were performed on a computer with an Intel Core i7-3770 processor, 32 GB of random access memory, and the Arch Linux operative system. The implementation and scripts used to generate the results of this manuscript are available as part of the ModCell2 package via File S2 and <https://github.com/trinhlab/modcell2>.

Optimization solver configuration

The Pyomo [86] implementation of ModCell2-MILP was solved with IBM Ilog Cplex 12.8.0. To avoid incorrect solutions associated with numerical issues the following Cplex parameters were changed from their default values: (i) *numerical emphasis* was set to “true”, (ii) *integrality tolerance* was lowered to 10^{-7} , and (iii) the *MIP pool relative gap* was increased to 10^{-4} for enumerating alternative solutions. Alternative solutions were enumerated using the Cplex “populate” procedure.

5.2.3 Analysis methods

Reference flux distribution

The reference flux distribution, $\frac{v_{jk}^*}{|v_{Sk}^*|}$, is determined by solving the following quadratic program based on the parsimonious enzyme usage hypothesis [151, 132]:

$$\min_{v_{jk}} \quad \sum_{j \in \mathcal{J}_k} v_{jk}^2 \quad (5.62)$$

s.t.

$$\sum_{j \in \mathcal{J}_k} S_{ijk} v_{jkm} = 0 \quad \forall i \in \mathcal{I}_k \quad (5.63)$$

$$l_{jk} \leq v_{jk} \leq u_{jk} \quad \forall j \in \mathcal{J}_k \quad (5.64)$$

$$v_{Xk} = \text{MaxDesignBio} \quad (5.65)$$

Constraint (5.63) corresponds to mass balance for the metabolic network. Constraint (5.64) corresponds to reaction bounds, including reaction deletions found in the modular cell design problem. Constraint (5.65) fixes the biomass formation rate, v_{Xk} , to the maximum reachable by the design. This value (MaxDesignBio) is obtained by maximizing v_{Xk} subject to (5.63) and (5.64). The reference flux distribution $\frac{v_{jk}^*}{v_{Sk}^*}$ represents the desired metabolic state of a *wGCP* designed production network. This distribution, if feasible, is unique because the convex optimization problem is formulated with a positive definite quadratic objective function (see Theorem 16.4 in Nocedal and Wright[174]).

Flux variance clustering

Flux variance clustering (FVC) seeks to identify and group reactions that exhibit high flux changes under different conditions. Reactions with high flux variance can be considered as metabolic interfaces between core metabolic processes and pathway modules. In our study, each condition corresponds to a different product synthesis phenotype. FVC implementation entails three steps. First, flux distributions are simulated for each condition and standard deviations for each reaction are calculated. Then, a standard deviation threshold is set to select the reactions with highest flux changes across conditions. Finally, these selected reactions are clustered to identify patterns that repeat under specific conditions. The filtering threshold is set to capture the top reactions with most change while maintaining a sufficiently small list that is biologically meaningful. In our study, we chose an *ad-hoc* value that captures well-known reactions in *E. coli* central metabolism. To cluster the selected reactions, only flux magnitudes, not directionality, were considered in our study. Further, each reaction flux was normalized by the maximum value of that same reaction across all production networks. Clustering was performed using the method `clustermapper()` with default clustering-related parameters from the Python library Seaborn 0.9.

Flux sampling

To determine an ensemble of flux distributions for a production network, we used the ACHR algorithm [111] in the COBRA toolbox [90]. Constraints for flux sampling simulation include the reaction deletions and module reactions found in the ModCell design problem solution, a

fixed substrate uptake rate of -10 mmol glucose/gCDW/hr, and a minimum product synthesis flux of 50% of its maximum value.

Metabolic map drawing

Drawings of metabolic map were performed using the Escher [116] tool (<https://escher.github.io>) that produces *svg* files. Coloring, highlighting candidate reactions, and other systematic adjustments of metabolic maps were done with the Python-based *lxml* module. Additional editing for visual enhancement was done with the Inkscape software.

5.3 Results and discussion

5.3.1 Performance and solution time optimization of ModCell2-MILP

ModCell2-MILP can not only reproduce the results of the original ModCell2 formulation but also find more alternative solutions

To evaluate ModCell2-MILP, we compared its performance with the previously developed ModCell2 platform[73] that solves the optimization problem with multi-objective evolutionary algorithms (MOEAs). As a basis of comparison, we used the same *E. coli* core metabolic model, maximum number of deletion reactions α , and maximum number of module-specific reactions β_k for both ModCell2 and ModCell2-MILP. Due to fundamental differences in problem formulations for MOEA and MILP, we used the *lsGCP* design objective for ModCell2-MILP with multiple weighting factors, a_k , specifically selected to reproduce previous results, in the blended formulation and the *sGCP* design objective for ModCell2 (File S1). The results showed that ModCell2-MILP could generate the same Pareto optimal designs like ModCell2. In addition, ModCell2-MILP enumerated a larger number of alternative solutions than ModCell2. For example, the design named *sGCP-5-0-6* generated by ModCell2 had 3 alternative solutions while ModCell2-MILP found 8 alternative solutions. By increasing α to 8 and β to 2, we could identify a utopia design (i.e., one solution with the

maximum value for all objectives) with 192 alternative solutions, expanding the possibilities for experimental implementation.

Tuning MILP formulations significantly improves solution times

We considered three techniques that can improve solution times of ModCell2-MILP, including:

(i) *Fixing the network feasibility indicator w_k .* If all modules are expected to be compatible with a final ModCell design (i.e., $f_k > 0, \forall k \in \mathcal{K}$), w_k is set to be 1 for all $k \in \mathcal{K}$ to avoid computational efforts in finding non-optimal feasible solutions.

(ii) *Flux bound tightening.* Constraints of the form $e_{jkm}l_{jkm} \leq v_{jkm} \leq e_{jkm}u_{jkm}$ are known to result in weak linear relaxations, i.e., feasible values of v_{jkm} are far from their bounds l_{jkm} and u_{jkm} . To tighten the formulation by making continuous relaxations closer to the feasible integer solution, smaller values of u_{jkm} and l_{jkm} are determined by solving a series of linear programs that maximize and minimize each flux v_{jkm} in the parent production networks $\Pi_{km}(e_{jk} = 1, \forall j \in \mathcal{J}_k)$.

(iii) *Benders decomposition.* ModCell2-MILP has a separable structure compatible with Benders decomposition[75, 65] that creates a master problem, using binary variables and associated constraints (5.15)-(5.21), and sub-problems for each production network $\Psi_{km}(e_{jk})$ with fixed binary variables. This decomposition implementation is automatically done by Cplex 12.8.

We evaluated these three techniques for tuning MILP formulations and used the core *E. coli* model[73] for the benchmark study. The results showed that flux bound tightening, fixed w_k , and Benders decomposition could reduce the solution time to find solutions by 50%, 80%, and 95%, respectively (Table 5.1). By combining these techniques, the solution time was shortened by 96% from 63.3 s to 2.8 s. In subsequent studies, we used these three tuning techniques to solve the ModCell design problem unless otherwise noted.

Choice of design parameters affect solution time

In designing a modular cell with ModCell2-MILP, the designer needs to specify the formulation type (i.e., blended or goal attainment formulation), the target phenotype (e.g.,

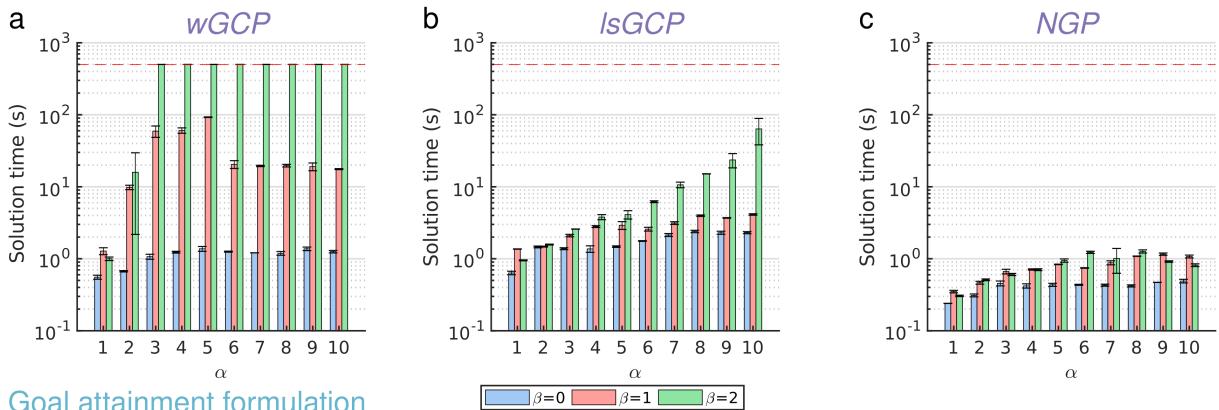
Table 5.1: Solution time reduction by tuning the ModCell2-MILP formulation. Fixed network indicator means $w_k = 1, \forall k \in \mathcal{K}$. The simulations were performed in triplicates.

Feasibility indicator w_k fixed	Benders decomposition	Bounds tightened	Solution time (s)
No	No	No	63.3 ± 16.9
No	No	Yes	32.5 ± 10.2
No	Yes	No	3.6 ± 0.1
No	Yes	Yes	3.4 ± 0.4
Yes	No	No	13.8 ± 2.7
Yes	No	Yes	11.9 ± 1.7
Yes	Yes	No	2.7 ± 0.3
Yes	Yes	Yes	2.8 ± 0.1

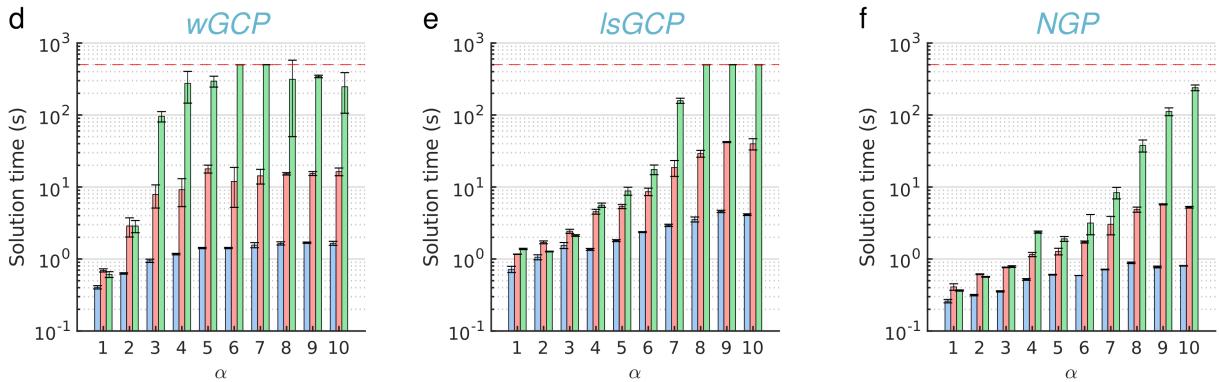
$wGCP$, $lsGCP$, and NGP), and the limits of deletion reactions (α) and endogenous module-specific reactions (β_k). We evaluated the impact of these parameters on solution time using the *E. coli* core model (Figure 5.3). Regardless of the formulation type, increasing α and β led to harder problems and hence required more solution time due to the exponentially increasing number of feasible solutions as expected. The goal attainment formulation took longer time to solve for the $lsGCP$ and NGP design objectives, but about the same time for the $wGCP$ design objective. Interestingly, the overall difficulty of $wGCP$ is higher than that of $lsGCP$ in both the blended and goal attainment formulations, despite $lsGCP$ having approximately twice the number of constraints. Furthermore, the NGP design objective could be solved most quickly, likely due to the narrower design space associated with the no-growth associated production of target metabolites.

Figure 5.3: Effect of design parameters on solution time. We examined the target design objective (i.e., *wGCP*, *lsGCP*, and *NGP*) and the limits of deletion reactions α and endogenous module-specific reactions β_k , on computation time for solving the ModCell2-MILP problem with the blended (a-c) and goal attainment (d-f) formulations. A time limit of 500 seconds indicated by a red dashed line was used in all cases, but only reached by certain *wGCP* and *lsGCP* cases with $\beta \geq 2$. The simulations were performed in duplicates.

Blended formulation



Goal attainment formulation



5.3.2 Design of a universal modular cell for a genome-scale metabolic model of *E. coli*

Reduction of the candidate reaction deletion set enables ModCell2-MILP to find modular cell designs for a large-scale metabolic network

Finding genetic modifications towards a desired phenotype using mathematical optimization for large-scale metabolic networks is a computationally expensive task, due to the combinatorial search space spanned by a large number of reaction deletion candidates in the network [63, 249]. Preprocessing of metabolic networks to reduce reaction candidates is not only critical but also practical for experimental implementation. The set of reaction candidates in the iML1515 *E. coli* model[165] was reduced from 2,712 to 276 by ModCell2 [73]. Using this model and the *wGCP* objective, an *E. coli* modular cell was then identified to be compatible with 17 out of 20 products with requirement of only 4 reaction deletions [73]. Since MOEA implemented in ModCell2 does not guarantee optimality, here we aimed to evaluate the capability of ModCell2-MILP for handling a large-scale metabolic network and identifying the Pareto optimality and potential alternative solutions.

We applied ModCell2-MILP to analyze the same iML1515 model with a set of 20 products using the same design parameters (i.e., α and β_k) and the blended formulation with all objective weights $a_k = 1$. The simulation shows that ModCell2-MILP could not solve the ModCell design problem to optimality over 2 days of run time, likely due to the large number of candidate deletion reactions still present in the genome-scale model. Currently the best MILP solution algorithms do not scale well with parallel computing. In order to obtain solutions within an acceptable time, the set of candidate reactions must be further reduced. Since only a small subset of all metabolic reactions in genome-scale models tend to be deleted by strain design algorithms [63, 118, 73], we used a pool of *wGCP* designs with $\alpha = 4, 5, 6$ and $\beta = 0, 1$ reported with ModCell2 [73] to identify relevant deletion candidates. From a set of 601 designs found by ModCell2, only 33 out of 276 reaction deletion candidates were used at least once. Hence, these 33 reactions were used to create a new, computationally-tractable set of reaction candidates. This new set contains reactions mostly from the well-characterized central metabolic pathways (Figure 5.4a) while the original set

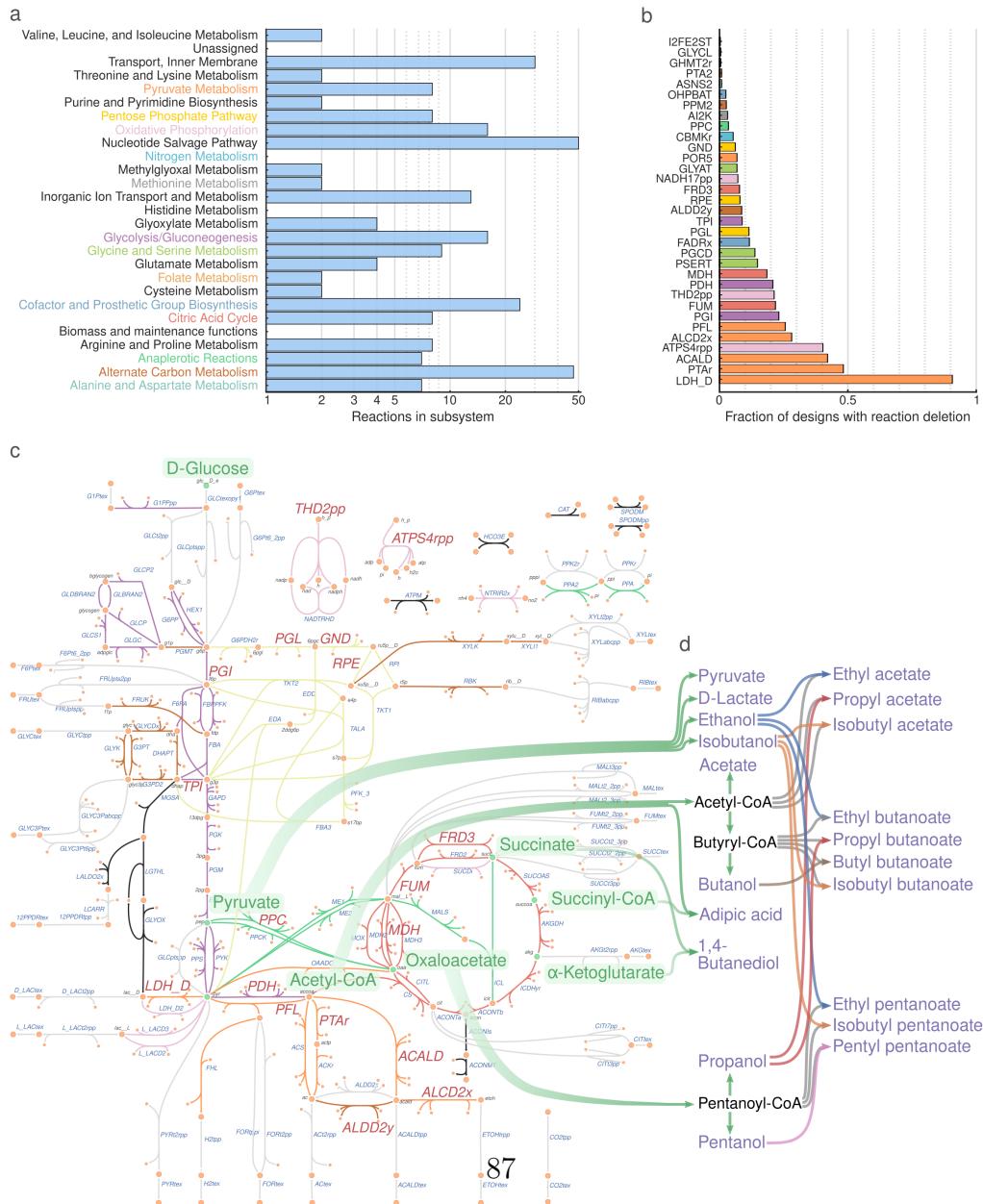
includes reactions in peripheral pathways that lead to biomass synthesis. Interestingly, within these 33 reaction candidates, only a few are used in most designs (Figure 5.4b), highlighting the importance of their removal in growth-coupled production phenotypes. Reactions with high deletion frequencies mainly occur in high-flux central metabolic pathways (Figure 5.4c), closely associated with cellular energetics and carbon precursors that interface with the production modules (Figure 5.4d).

Using the reduced reaction deletion candidate set, ModCell2-MILP could find an optimal solution in \sim 30 min and enumerated all optimal solutions in \sim 8 hours. All the optimal solutions found by ModCell2-MILP in this case were in agreement with those previously found by ModCell2 [73]. It should be noted that a reduced deletion candidate set can be identified for any metabolic model and target products by using previous designs identified with either ModCell2 or single-phenotype strain design algorithms [144]. This heuristic for reaction deletion candidate selection might affect design optimality to the extent that it omits relevant reactions. However, using a sufficiently informative pool of designs from other strain design algorithms helps minimize the chances of missing relevant candidates.

ModCell2-MILP can identify a universal modular cell compatible with all exchangeable production modules

Based on the computationally tractable reaction deletion candidate set, we next evaluated whether the goal programming formulation could help identify a universal ModCell design that is compatible with all modules. By screening for increasing α and β_k , we found that a design with $\alpha = 6$ and $\beta_k = 1$ could overcome the performance trade-offs between modules and hence constitute a universal modular cell that is compatible with all production networks considered (Figure 5.5a). Once coupled with a module, each resulting production strain displays the engineered phenotype with the defined minimum objective goal of 0.5 (i.e., 50% of the theoretical maximum product yield attained at the maximum growth rate). Remarkably, most products surpassed this minimum goal with yields above 90% of the theoretical maximum values (Figure 5.5b). All production networks displayed a feasible metabolic space where an increase in product synthesis rate is needed to attain faster growth

Figure 5.4: Metabolic functions of deletion candidate reactions. (a) Subsystem distribution for the original set of 276 candidate reactions in the iML1515 model. Those subsystems that contain a reaction used in at least one design are colored. (b) Deletion frequency for the reduced set of 33 candidate reactions. The analysis is based on a pool of 601 *wGCP* designs from different α and β parameters whose Pareto fronts were previously determined with ModCell2.[73] Bar colors indicate membership of these reactions to the subsystems. (c) Metabolic map of core metabolism. Key metabolites, including precursors for the 20 product modules (i.e., pyruvate, acetyl-CoA, succinyl-CoA, succinate, and α -ketoglutarate), are highlighted in green. Reactions are colored according to subsystem labels indicated in (a), reactions colored in light gray do not appear in any of the subsystems of (a), and reactions that are candidates for deletion, listed in (b), are labeled in red. (d) Link between major precursors and target products where colors are only used to facilitate visualization. Reaction and metabolite abbreviations correspond to BiGG[117] identifiers (<http://bigg.ucsd.edu/>).



rates (Figure 5.5c). This designed phenotype is useful for optimal pathway selection using adaptive laboratory evolution [66, 237] and/or pathway libraries [74].

5.3.3 Flexible metabolic flux capacity of *E. coli* core metabolism enables the design of a universal modular cell

Endogenous modules responsible for metabolic flexibility of a universal modular cell are identified by comparing flux distributions of production networks

The designed universal modular cell (Figure 5.5) can theoretically adapt to the conflicting metabolic requirements of all production modules (Table 5.2). To gain further insight into this unique metabolic capability of the modular cell, we analyzed the simulated *reference flux distributions* of each production network using the *flux variance clustering* (FVC) analysis (Materials and Methods). Reactions with the highest flux changes across the production networks are likely critical for the proper operation of the universal modular cell and might present potential bottlenecks. Such reactions were identified by filtering their reference flux standard deviation calculated across production networks with an *ad hoc* threshold of 0.2 (mol/substrate mol). Over 90% of the 535 active reactions, each of which carries a non-zero flux in at least one production network, had standard deviation values below the threshold, indicating highly conserved metabolic core pathways among production networks. Only 9.5% of the active reactions presented a standard deviation magnitude above the threshold (Figure 5.6a).

In our case study of designing a universal modular cell compatible with all 20 production modules, unbiased hierarchical clustering (Figure 5.6b) revealed the presence of four endogenous module types in the core metabolism of *E. coli* that are activated to fit specific production modules (Figure 5.6c). In the context of chassis metabolism, an endogenous module corresponds to a reaction or group of highly coupled reactions that become active to accomplish a certain metabolic function. The endogenous module classification can be understood in terms of location (i.e., proximity in the metabolic network) and three metabolic functions. The first function is the direction of carbon towards general precursor metabolites including (i) pyruvate and acetyl-CoA captured by acetyl-CoA-associated modules and (ii)

Figure 5.5: Identification of a universal modular cell compatible with all production modules under the *wGCP* design phenotype. (a) Goal programming solutions with increasing α and β values. The goal programming objective value (5.58) in the y-axis measures the difference between the performance of production strains and the target goal, i.e., $\sum_{k \in \{k \in \mathcal{K}: f'_k < g_k\}} (f'_k - g_k)$ where the target goal is set to be $g_k = 0.5$. The parameters $\alpha = 6$ and $\beta = 1$ are sufficient to identify a universal modular cell design meeting the required goal for all production networks. (b) Comparison between the yield performances of the designed modular production strains and maximum theoretical values. (c) The feasible flux spaces for the wild-type (gray) and designed modular production strains (crimson). Based on the *wGCP* design phenotype, to increase growth rate, each mutant must increase product synthesis rate. The genetic manipulations of this universal modular cell design are indicated in the metabolic map of Figure 5.6c.

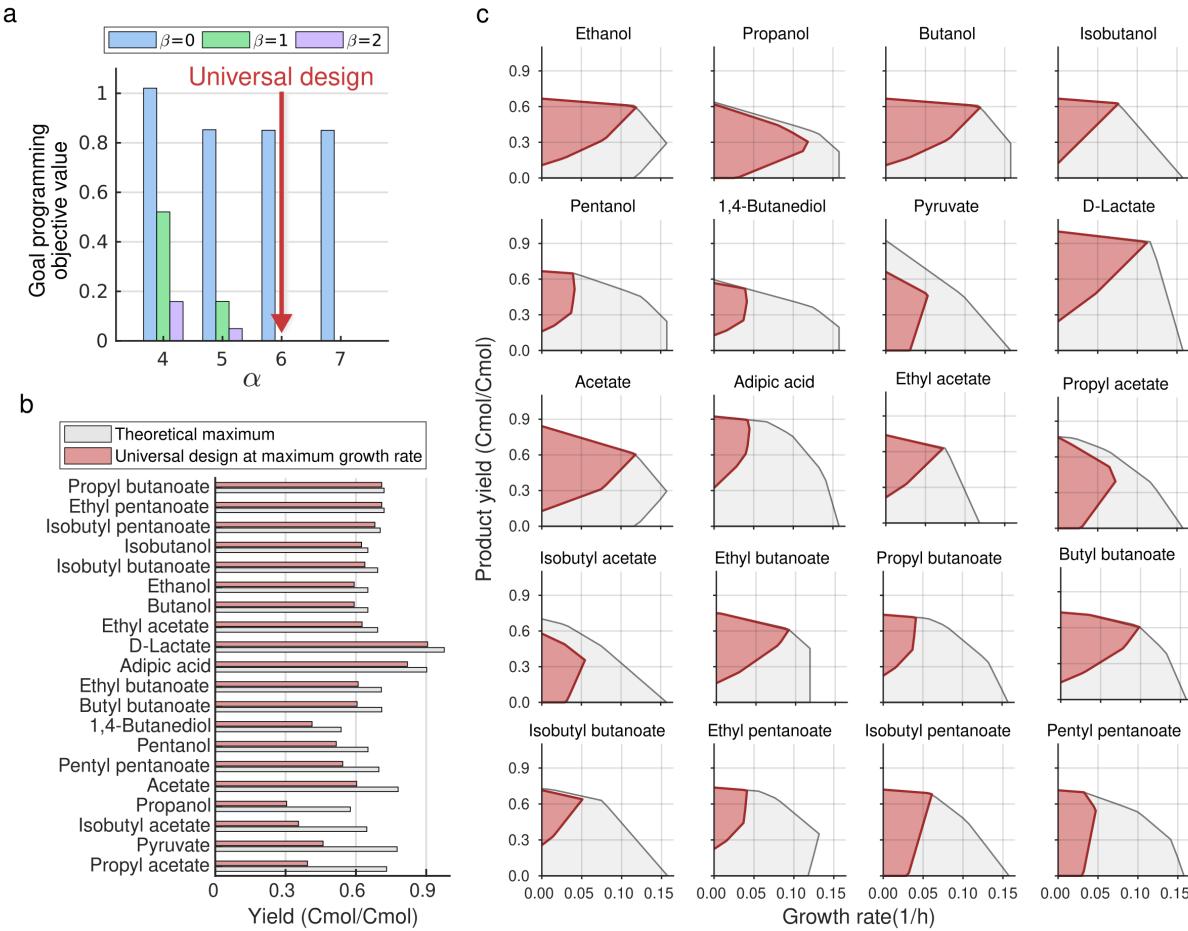


Table 5.2: Overall production module pathway stoichiometries and associated simulated secretion fluxes of the universal modular cell design. DoR is the degree of reduction of the final product (mol e^- / mol C). Metabolite secretion profiles are determined from the simulated reference flux distributions (mol C / mol C) of the universal modular cell design. Flux abbreviations: r_p , product; r_{ac} , acetate; r_{co_2} , CO₂; r_{for} , formate; r_{succ} , succinate. Note that the negative CO₂ fluxes in pyruvate and acetate production networks indicate overall CO₂ uptake enabled by phosphoenolpyruvate carboxylase (PPC).

Overall reaction	DoR	r_p	r_{ac}	r_{co_2}	r_{for}	r_{succ}
pyr + nadh → ethanol accoa + 2 nadh → ethanol (native)	7.0	0.58	0.01	0.27	0.04	-
oaa + glu + 2 atp + 2 nadph + nadh → akg + propanol	6.7	0.31	0.36	0.07	0.18	-
2 accoa + 4 nadh → butanol	6.5	0.59	0.01	0.28	0.04	-
2 pyr + nadph + nadh → isobutanol	6.5	0.62	-	0.31	-	-
oaa + glu + accoa + 3 nadh + 2 atp + 2 nadph → akg + pentanol	6.4	0.50	0.21	0.24	0.03	-
succ + akg + atp + 4 nadh + accoa → ac + 1,4-butanediol	5.5	0.46	0.33	0.17	-	-
→ pyruvate	3.0	0.46	-	-0.16	-	0.66
pyr + nadh → D-lactate	3.7	0.91	-	-	-	-
accoa → atp + acetate	3.5	0.60	0.60	-0.30	0.61	-
accoa + succoa + 2 nadh → atp + adipic acid	4.0	0.82	0.05	0.04	0.06	-
accoa + pyr + nadh → ethyl acetate	5.0	0.63	-	-	0.32	-
accoa + oaa + glu + 2 atp + 2 nadph + nadh → akg + propyl acetate	5.2	0.41	0.30	-	0.24	-
accoa + 2 pyr + nadph + nadh → isobutyl acetate	5.3	0.36	-	0.02	0.06	0.52
2 accoa + 3 nadh + pyr → ethyl butanoate	5.3	0.61	-	0.09	0.23	-
2 accoa + 3 nadh + oaa + glu + 2 atp + 2 nadph → akg + propyl butanoate	5.4	0.68	0.03	0.23	0.04	-
4 accoa + 6 nadh → butyl butanoate	5.5	0.61	-	0.14	0.18	-
2 accoa + 3 nadh + 2 pyr + nadph → isobutyl butanoate	5.5	0.64	-	0.16	0.16	-
oaa + glu + accoa + 2 nadh + 2 atp + 2 nadph + pyr → akg + ethyl pentanoate	5.4	0.68	0.03	0.23	0.04	-
oaa + glu + accoa + 2 nadh + 2 atp + 3 nadph + 2 pyr → akg + isobutyl pentanoate	5.6	0.67	0.01	0.25	0.03	-
2 oaa + 2 glu + 2 accoa + 4 nadh + 4 atp + 4 nadph → 2 akg + pentyl pentanoate	5.6	0.53	0.22	0.20	0.02	-

oxaloacetate, succinate, succinyl-CoA, and α -ketoglutarate captured by TCA-associated modules. The second function is the direction of carbon from the precursor metabolites towards secretable molecules, captured by the upstream and TCA-associated modules. The third function is the use of ATP- and NADP(H)-dependent pathways required to maintain homeostasis, captured by the acetyl-CoA-associated and energetic modules. While these functions are conceptually separable, their biochemical manifestation overlaps, i.e., specific metabolic reactions or pathways can simultaneously fulfill several functions.

Each endogenous module can be viewed as an interface of the universal modular cell with production modules that are exchangeable. The endogenous modules might become potential metabolic bottlenecks in practice if they cannot satisfy the predicted fluxes, and thus might be critical engineering targets when the associated production modules are used.

Acetyl-CoA-associated endogenous modules. This module type contains pyruvate formate lyase (PFL) and pyruvate dehydrogenase enzyme complex (PDH) reactions that

convert pyruvate to acetyl-CoA. Intuitively, products derived from pyruvate, such as isobutanol, require a low flux through PFL and PDH while those derived from acetyl-CoA require a high flux. Remarkably, the redox states of production strains determine the ratios of PFL to PDH fluxes. For example, the ethanol production network has a relatively high flux through PDH and a low flux through PFL; however, for ethyl acetate that has a lower degree of reduction than ethanol (Table 5.2), PFL with formate secretion is prioritized over PDH with NADH generation. Note that our model did not include the regulatory restriction that PDH is inhibited in *E. coli* anaerobically because the function of PDH is equivalent with the coupling of PFL and heterologous NADH-dependent formate dehydrogenase (FDH) demonstrated experimentally for increased butanol[214, 171] and pentanol[246] production.

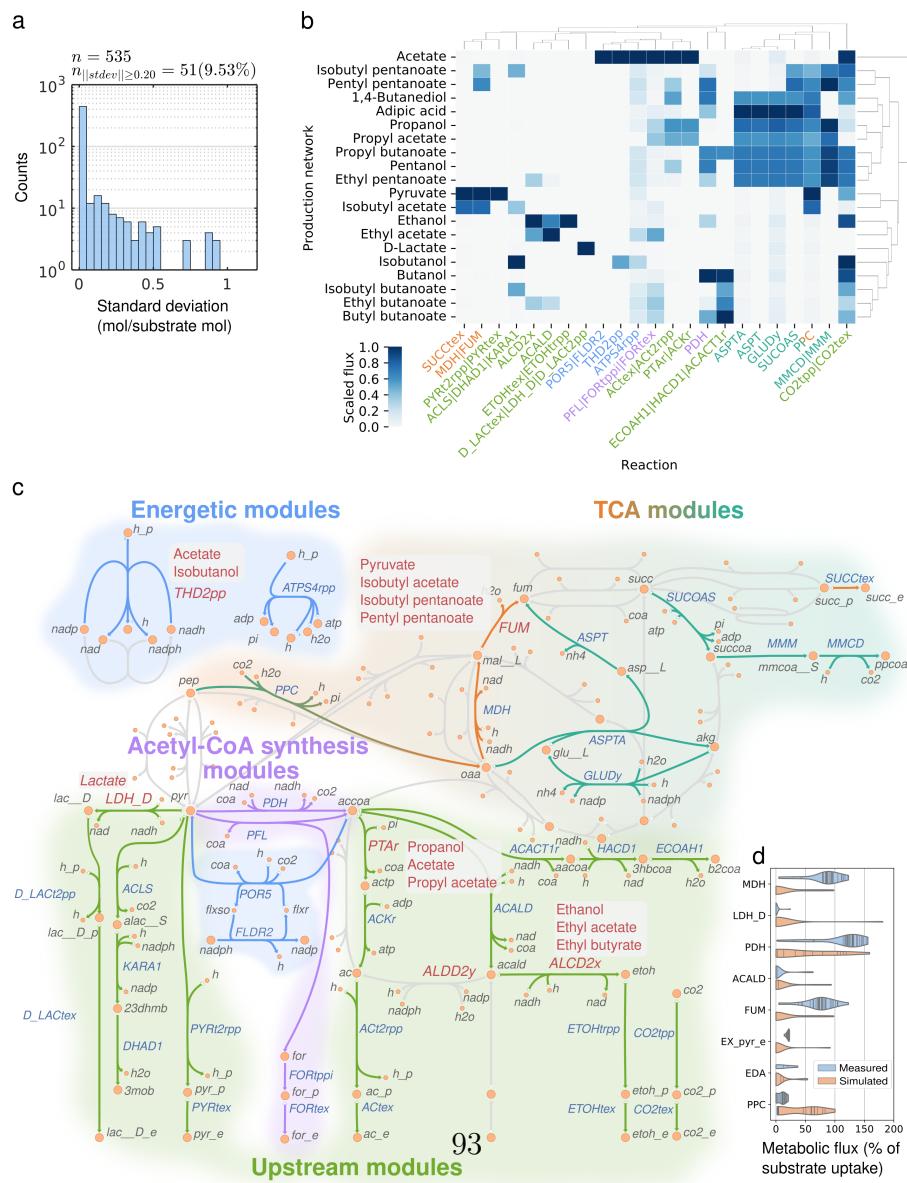
Upstream modules. This module type is formed by reactions located directly upstream of a secretable metabolite, often associated with the target production module, and thus provides the necessary precursor metabolite(s). Such reactions are commonly over-expressed in practice, e.g., the ECOAH1-HACD1-ACACT1r endogenous module (comprising of 3-hydroxyacyl-CoA dehydratase, 3-hydroxyacyl-CoA dehydrogenase, and acetyl-CoA acetyl transferase) responsible for generating butyryl-CoA and the ACLS-DHAD1-KARA1 endogenous module (comprising of acetolactate synthase, dihydroxy-acid dehydratase, and keto-acid reductoisomerase) responsible for generating isobutyryl-CoA. These endogenous modules can also become active to form byproducts in certain production networks, e.g., the PTAr-ACKr-ACT2rpp-ACtex endogenous module (comprising of phosphate acetyl transferase, acetate kinase, and cytosolic and periplasmic acetate transport) that not only carries the highest flux in the acetate production network but also becomes active in the propanol-associated modules.

TCA-associated endogenous modules This module type has the same function as the upstream endogenous modules but it is localized in the TCA (Krebs) cycle. Several products, including adipic acid, 1,4-butanediol, propanol, pentanol, and their associated esters, are derived from the TCA intermediates and interface with the universal modular cell via the TCA-derived endogenous modules. The SUCOAS-MMM-MMCD

endogenous module (comprising of succinyl-CoA synthetase, Methylmalonyl-CoA mutase, methylmalonyl-CoA decarboxylase) must be activated to convert succinate into succinyl-CoA and then propanoyl-CoA. Remarkably, two routes are present to synthesize fumarate from oxaloacetate, including the conventional MDH-FUM endogenous module (comprising of malate dehydrogenase and fumarase) that consumes NADH and the cyclic ASPTA-GLUDY-ASPT endogenous module (comprising of aspartate transaminase, glutamate dehydrogenase, and L-aspartase) that consumes NADPH. These NADH/NADPH cofactors are not interchangeable due to the deletion of the transhydrogenase THD2pp in the universal modular cell, so the isobutyl pentanoate and pentyl pentanoate modules, that are derived from the ASPTA-GLUDY-ASPT endogenous module, also have a high NADPH requirement. Some production networks, such as pyruvate and isobutyl acetate that are not based on the TCA-derived endogenous modules, secrete succinate instead of ethanol and/or lactate to balance redox by using the PPC-MDH-FUM-SUCCtex endogenous module (comprising of phosphoenolpyruvate carboxylase, malate dehydrogenase, fumarase, and succinate transport).

Energetic modules This module type primarily involves NAD(P)-dependent transhydrogenase (THD2pp) and ATP synthase (ATPS4rpp). Other reactions that allow coupling of phosphate- and electron-transfer cofactors are also included. The reactions in this module help buffer the diverse electron and ATP requirements of production networks. THD2pp is deleted in the chassis but used as a module reaction in the isobutanol and acetate production networks. In the case of isobutanol production, transhydrogenase expression has been demonstrated to increase the synthesis of NADPH and thus isobutanol [215]. Acetate has the smallest degree of reduction after pyruvate, which results in redox imbalance that is compensated via formate secretion. In conjunction with these mechanisms, ATPsynthase works in the reverse direction by hydrolyzing excess ATP. Other production networks also use ATPS4rpp to eliminate excess ATP as observed, for example, in the ethyl acetate production network. This strategy is consistent with ATP wasting approaches recently demonstrated [84].

Figure 5.6: Flexible metabolic flux capacity of *E. coli* metabolism enables the universal modular cell design. (a) Standard deviation of each reaction flux across production networks. (b) Scaled fluxes of the 51 reactions with standard deviation magnitude above 0.2, excluding proton, water transport, and exchange reactions. A scaled flux for a reaction is determined by the reference flux distribution value divided by the maximum value of that reaction across all production networks. Hence, a scaled flux of 0 indicates a given reaction does not carry any flux, and a scaled flux of 1 indicates that this reaction carries the highest flux across production networks. Several columns have multiple reactions, separated by |, since they carry exactly the same flux. (c) Endogenous modules of the universal modular cell. The reactions colored in red are deleted in the chassis, but are used as module reactions in the production networks shown in the adjacent gray boxes. Metabolites in periplasmic and extracellular compartments have “_p” and “_e” suffixed to their abbreviations, respectively. Metabolite and reaction abbreviations follow BiGG[117] notation. (d) Comparison between simulated and measured fluxes. The solid lines within the “violins” correspond to samples. The simulated fluxes for the reversible reactions, including FUM, LDH, MDH, and ACALD, were multiplied by -1 to reflect their most common direction.



Comparison between simulated and measured intracellular fluxes reveals flexible metabolic flux capacity of *E. coli* to accommodate the required wide flux ranges

Flux analysis of the production networks suggests that the core metabolic reactions (Figure 5.6b) require a wide range of fluxes when coupled with different production modules. To successfully implement this modular design in practice, we need to evaluate whether the metabolism of *E. coli* has the inherent metabolic flux capacity to accommodate these required fluxes. We compared the simulated reference flux distributions with a recent collection of 45 measured metabolic fluxes [112] that are collected from multiple studies across various conditions (e.g., growth under aerobic and anaerobic conditions, use of glucose or acetate or pyruvate as a carbon source) and genotypes (e.g., wild-type *E. coli* and mutants with single gene deletions) [99, 104, 278, 279]. Note that while the experimental data set provides a flux distribution baseline for wild-type and relatively small deviations for single gene deletion mutants, we anticipate that highly engineered strains with more gene deletions are likely to exhibit wider flux distributions.

Within the reactions present in the 23 groups that constitute endogenous modules (Figure 5.6b), 8 reactions also appeared in the experimental dataset (Figure 5.6d). Remarkably, a highly consistent overlap of flux ranges was observed between the simulated and measured fluxes for malate dehydrogenase (MDH), pyruvate dehydrogenase (PDH), acetaldehyde dehydrogenase (ACALD), fumarase (FUM), and 2-dehydro-3-deoxy-phosphogluconate aldolase (EDA). For the cases of D-lactate dehydrogenase (LDH_D), and pyruvate secretion (EX_pyr_e) that are directly coupled with the biosynthesis of lactate and pyruvate, respectively, we observed the maximum simulated fluxes surpass the measured values, suggesting that further engineering of wild-type and single-gene deletion *E. coli* is needed to attain the required fluxes. Indeed, previous studies[282, 31] have been able to redirect metabolic fluxes in *E. coli* for yields of lactate and pyruvate above 75% of the theoretical maximum values by simultaneous elimination of competing fermentative pathways for biosynthesis of acetate ($\Delta ackA$), formate ($\Delta pflB$), and ethanol ($\Delta adhE$). The only remaining discrepancy between the simulated and measured fluxes is PPC. Studies, not included in the comparison data set, have reported up to 50% more PPC flux observed

under aerobic conditions [185, 217], which is still considerably below several of the simulated fluxes. This result suggests that PPC can be a potential metabolic bottleneck in certain production modules. One possible solution is to include in the affected production modules the heterologous PPC from *Actinobacillus succinogenes* which has been successfully over-expressed in *E. coli* for increased succinate production [114]. Additionally, bacterial PPC activity can be increased by elevating the acetyl-CoA pool [140].

Random sampling of metabolic fluxes confirms the narrow operation range of endogenous modules

The reference flux distributions analyzed so far represent the ideal metabolic states for each production strain. However, other metabolic states might also exist. To address this uncertainty, we performed randomized flux sampling [111, 90] for each production network under the constraint that product synthesis rate must be above 50% of the maximum value. The results show that the metabolic flux distributions (Figure 5.7) for most reactions involved in the endogenous modules are very narrow, except for the two alternative pathways of ethanol biosynthesis, i.e., the endogenous PDH-ACALD-ALCD2x route comprising of pyruvate dehydrogenase, acetaldehyde dehydrogenase, and alcohol dehydrogenase (Figure 5.8a) and the heterologous PYRDC-ALCD2x route comprising of pyruvate decarboxylase and alcohol dehydrogenase. These two pathways can be used interchangeably in the ethanol production network, where there is a linear correlation between PYRDC and PDH fluxes (Figure 5.8b). Notably, the sampled fluxes cannot indicate preferential use of either the ethanol synthesis route because the model does not take into account of kinetic (k_{cat} , k_M) and regulatory constraints. In summary, even though reactions in the endogenous modules must have flexible metabolic flux capacities to enable a universal modular cell to be compatible with various exchangeable production modules, they must also operate within in a narrow flux range when interfacing with a specific production module.

Figure 5.7: Violin plot of sampled reaction flux distributions. Reaction colors are consistent with Figure 5.6. The flux of SUCOAS could not be sampled since this reaction is involved in a thermodynamically infeasible cycle.

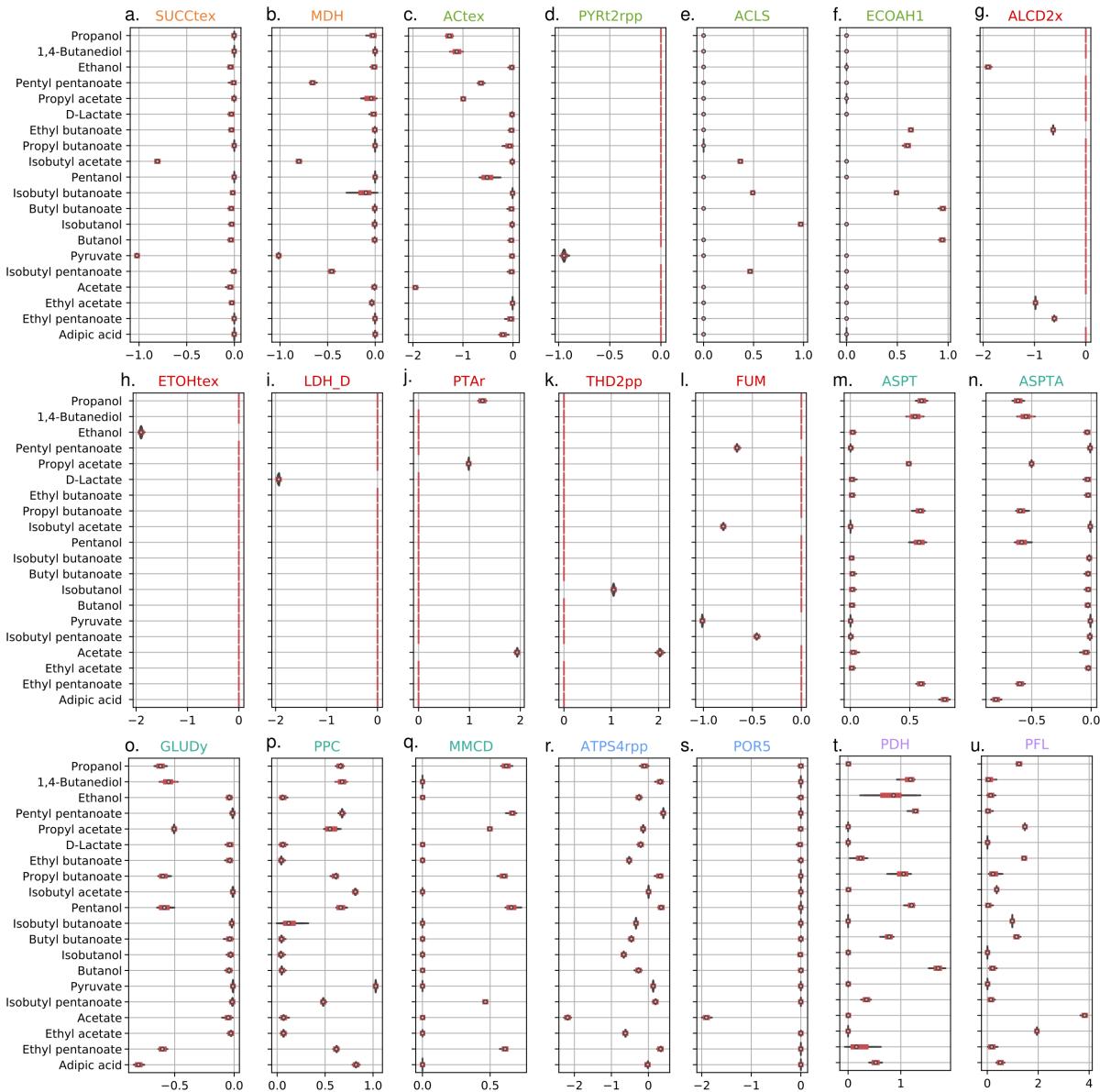
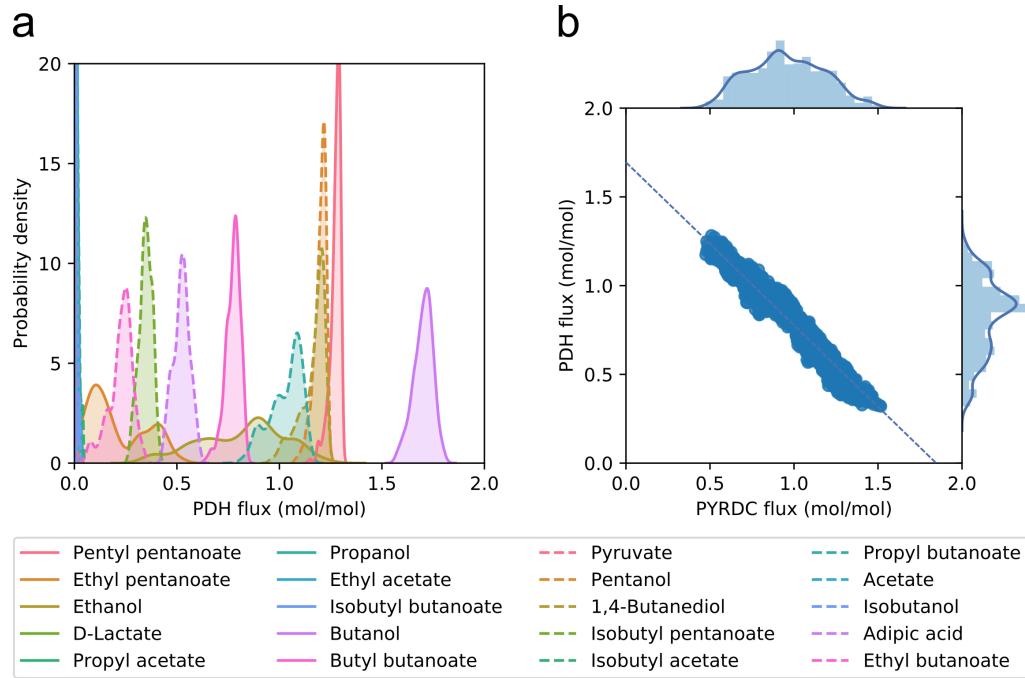


Figure 5.8: Sampled flux distributions of the ethanol biosynthesis pathways. (a) Probability density function of sampled fluxes for pyruvate dehydrogenase (PDH) across all production networks. Note that ethanol and ethyl pentanoate have the widest operation range. (b) Sampled metabolic fluxes of pyruvate decarboxylase (PYRDC) and PDH in the ethanol production network.



5.4 Conclusions

In this study, we formulated multi-objective modular strain design as blended and goal attainment optimization problems. These problems can be solved by MILP algorithms that guarantee Pareto optimal solutions, exhaustively search the space of alternative solutions, and specify design requirements such as module prioritization or universal compatibility. This multi-objective strain design approach can be extended with additional design variables (e.g., up- and down-regulation[186] or reaction insertion from database[187]) or alternative flux prediction models[37, 55] to expand its applications, including use of exchangeable metabolic modules for bioremediation and biosensing. In terms of biological significance, the ModCell2-MILP and FVC methods developed could identify a universal modular cell that harnesses the inherent modularity and flexibility of native *E. coli* metabolism to properly interface with a variety of biochemically diverse pathways. This universal design was

predicted to display a growth-coupled-to- product-formation phenotype for all pathways, enabling its use as a platform for pathway optimization through high-throughput library selection and/or adaptation. The feasibility of this universal design strategy is found to be consistent with experimental evidence of isolated metabolic engineering strategies towards target products and measured intracellular flux ranges. Furthermore, analysis of the metabolic fluxes in this universal design revealed clusters of reactions in central metabolism, named endogenous modules, that become activated to interface with specific pathways, providing a mechanistic view into the modularity of metabolic pathways. In this study, the universal design developed was limited to a library of 20 molecules in *E. coli* because one primary aim was to compare the MILP solution with the MOEA solution previously presented. Future studies will use the developed methods to design and understand modularity for different organisms and a larger library of product synthesis modules.

Supporting information

File S1 Spreadsheet with modular cell designs for *E. coli* core model.

File S2 Computer programs used to generate the results of this study.

5.5 Definitions

Sets

\mathcal{I}_k Metabolites in production network k .

\mathcal{J}_k Reactions in production network k .

\mathcal{K} Production networks that are derived from a combination of the parent metabolic network with the metabolic pathways associated with production modules. The parent metabolic network is the network of the host strain that is genetically manipulated to build a modular cell chassis.

- \mathcal{M} Metabolic states that correspond to the growth phase, denoted μ , and the non-growth or stationary phase, denoted $\bar{\mu}$.
- \mathcal{C} Candidate deletion reaction set. The removal of these reactions are applied to all production networks, $\mathcal{C} \subseteq \mathcal{J}^{\text{parent}} \subseteq \mathcal{J}_k, \forall k \in \mathcal{K}$.
- \mathcal{N}_k Non-targeted deletion reaction set in production network k . This set arises from the use of fixed endogenous module reactions z_{jk} in certain production networks.

Binary variables

- y_j Reaction deletion indicator that takes a value of 0 if reaction j is deleted in the chassis and 1 otherwise.
- z_{jk} Endogenous module reaction indicator that takes a value of 1 if reaction j is added back as module reaction in production network k and 0 otherwise.
- d_{jk} Reaction activity indicator that takes a value of 0 if reaction j in production network k might not carry a flux and 0 otherwise, thus $d_{jk} = y_j \vee z_{jk}$. This variable is declared as a continuous and linear constraints enforce the OR relation and thus makes the variable binary.
- w_k Production network feasibility indicator that takes a value of 0 if reaction deletions are ignored and the objective value is set to 0 for production network k , and a value of 1 otherwise.
- e_{jk} Reaction activity indicator adjusted to w_k that takes the value of d_{jk} if $w_k = 1$ and a value of 1 if $w_k = 0$, thus $e_{jk} = (d_{jk} \wedge w_k) \vee \neg w_k$.
- r_{jk} Linearization variable, $r_{jk} = d_{jk} \vee w_k$.

Continuous variables

- v_{jkm} Flux (mmol/gCDW/hr) of reaction j from network k at metabolic state m .
- v_{Pkm} Flux (mmol/gCDW/hr) of product synthesis reaction from network k at metabolic state m .
- v_{Xkm} Flux (mmol/gCDW/hr) of biomass synthesis reaction from network k at metabolic state m .

f_k	General objective function for production network k that can be represented by f_k^{wGCP} , f_k^{lsGCP} , or f_k^{NGP} .
f'_k	Objective function adjusted by w_k such that $f'_k = f_k$ if $w_k = 1$ and $f'_k = 0$ otherwise.
δ_k^+	Amount required by the objective value f'_k to attain the target goal g_k , i.e.. $\delta_k^+ = g_k - f_k$ if $f'_k < g_k$.
δ_k^-	Amount that the objective value f'_k surpasses the target goal g_k , i.e., $\delta_k^- = f'_k - g_k$ if $f'_k > g_k$.
λ_{ikm}	Dual variable associated with mass balance constraint of metabolite i from production network k at growth state m .
μ_{jkm}^l	Dual variable associated with the lower bound of reaction j from production network k at growth state m .
μ_{jkm}^u	Dual variable associated with the upper bound of reaction j from production network k at growth state m .
p_{jkm}^l	Linearization variable, $p_{jkm}^l = e_{jk}\mu_{jkm}^l$.
p_{jkm}^u	Linearization variable, $p_{jkm}^u = e_{jk}\mu_{jkm}^u$.

Parameters

S_{ijk}	Stoichiometric coefficient of metabolite i in reaction j of production network k .
l_{jkm}	Lower bound for reaction j of production network k at metabolic state m .
u_{jkm}	Upper bound for reaction j of production network k at metabolic state m .
γ	Minimum biomass synthesis rate required for growth states. Note that in this study a conservative value of 20% of the maximum predicted growth rate of the wild-type strain was used to generate all results.
α	Maximum number of deleted reactions in the modular cell chassis.
β_k	Maximum number of endogenous module reactions in production network k .
ϵ	Small scalar used for tilting the biomass objective function, leading to the minimum product rate available at the maximum growth rate. Note that in our study $\epsilon = 0.0001$ was used to generate all results.

$b_\mu, b_{\bar{\mu}}$ Weights on the growth and non-growth objectives of f_k^{lsGCP} , respectively. Note that in our study $b_\mu = 1$ and $b_{\bar{\mu}} = 10$ were used to generate all results.

- a_k Weighting factor applied to the objective function for production network k in the blended formulation. Note that in our study $a_k = 1, \forall k \in \mathcal{K}$ was used unless otherwise noted.
- g_k Target value for objective f'_k in the goal programming formulation.
- a_k^+ Weighting factor applied to δ_k^+ which emphasizes the importance of objective value f'_k to avoid falling below the target value g_k . Note that in our study $a_k^+ = 1, \forall k \in \mathcal{K}$ was used in all cases.
- a_k^- Weighting factor applied to δ_k^- which emphasizes the importance of the objective f'_k to avoid surpassing the target value g_k . Note that in our study $a_k^- = 1, \forall k \in \mathcal{K}$ was chosen everywhere except to determine the universal modular cell design, where $a_k^- = 0, \forall k \in \mathcal{K}$ was used.
- M^w Determines the minimum value of f_k that allows w_k to not be 0. A value of 10, corresponding to $f_k \geq 0.01$ for $w_k \neq 0$, was used in all cases.
- M^{obj} Upper bound for each objective value. Note that in our study a value of 20 was set for all cases.
- M Upper bound for dual variables. Note that in our study a value of 100 was set for all cases.

Chapter 6

Development of an updated genome-scale metabolic model of *Clostridium thermocellum* and its application for integration of multi-omics datasets

This chapter is based on the publication *Development of an updated genome-scale metabolic model of Clostridium thermocellum and its application for integration of multi-omics datasets*. Garcia, S., Thompson, R.A., Giannone, R. J., Dash, S., Maranas , C. D., and Trinh, C. T. *In preparation, 2019*. As first author I lead the development, implementation, and writing of this study. Supplementary Material 1 is provided in Appendix C, while Supplementary Files 2, 3, and 4 are provided as attachments.

Abstract

Solving environmental and social challenges such as climate change requires a shift from our current non-renewable manufacturing model to a sustainable bioeconomy. A promising technology to enable carbon neutral production of energy and materials from plant biomass

is consolidated bioprocessing (CBP). The most promising CBP organism identified thus far is *Clostridium thermocellum*, a thermophilic microbe capable of efficient degradation of untreated lignocellulosic biomass to produce biofuels and biomaterials. However, the complex metabolism of *C. thermocellum* is not fully understood, hindering metabolic engineering to achieve high rates, titers, and yields of valuable molecules. In this study, we developed an updated genome-scale model of *C. thermocellum* that accounts for recent metabolic findings, has improved prediction accuracy, and is standard-conformant to ensure easy reproducibility. To illustrate one of the many uses of genome-scale models, we applied the new model to study biotechnologically relevant mutants for ethanol production. This analysis was done with a novel quantitative multi-omics integration protocol that led to interesting findings in redox stress metabolism, providing new engineering targets for the production of reduced molecules. We anticipate the new model will become a useful tool for metabolic engineering and systems biology of *C. thermocellum*.

6.1 Introduction

Global oil reserves will be depleted soon,[212] and climate change could become a major driver of civil conflict.[94] These challenges to security and the environment need to be addressed by replacing our current non-renewable production of energy and materials for a renewable and carbon neutral approach.[191] The thermophilic bacterium *C. thermocellum* is capable of efficient degradation of lignocellulosic biomass to produce biofuels and biomaterial precursors, making this organism an exceptional candidate for biocatalysis.[178] However, its complex and poorly understood metabolism remains the main roadblock to achieve industrially competitive yields and titers of useful metabolites, including biofuels such as ethanol[233] and isobutanol.[141] To support metabolic engineering efforts of *C. thermocellum* in the last decade, several genome-scale models (GSMs) of metabolism have been developed.

The first GSM of *C. thermocellum*, named iSR432, was developed for strain ATCC27405 and applied to identify gene deletion strategies for high ethanol yield. [197] More recently, Thompson et al. developed the iAT601 genome-scale model [230] for strain DSM1313,

the current engineering platform strain due to better availability of genetic engineering tools.[7] The iAT601 model was used to identify genetic manipulations for high ethanol, isobutanol, and hydrogen production,[230] and to understand growth cessation prior to full substrate depletion observed under high-substrate loading fermentations that simulate industrial conditions.[232] In addition to these core and genome-scale steady-state metabolic models, a kinetic model of central metabolism, k-ctherm118, was recently developed and used to elucidate the mechanisms of nitrogen limitation and ethanol stress.[47] Due to the biotechnological relevance of the Clostridium genus, GSMS have also been developed for other species,[49] including *C. acetobutylicum*,[130, 210, 200, 158, 255, 48, 271] *C. beijerinckii*,[163] *C. butyricum*,[211] *C. cellulolyticum*,[200] and *C. ljungdahlii*.[167]

In this study, we developed an updated genome-scale model of *C. thermocellum*, named iCBI655, with more comprehensive and precise metabolic coverage, enhanced prediction accuracy, and extensive documentation. This model is a human curated database that coherently represents all the available genetic, genomic, and metabolic knowledge of *C. thermocellum* from both experimental literature and bioinformatic predictions. Consequently, the model not only enables metabolic flux simulation but also provides a framework to contextualize disparate datasets at the system level. To this end, we developed a quantitative multi-omics integration method and applied it to well-known biotechnological mutants for ethanol production, leading to new insights in redox stress mechanisms and potential engineering targets for enhanced production of reduced molecules.

6.2 Results

6.2.1 Development of an upgraded *C. thermocellum* genome-scale model named iCBI655

The iCBI655 model was developed using the published iAT601 model[230] as a starting point. The enhancements with respect to the previous model include updated metabolic pathways, new annotation, and new extensive documentation. A detailed account of these

changes can be found in the Supplementary Material 4. Here, we highlight the most relevant modifications.

Modeling updates

To facilitate model usage and reduce the chances of human error, the identifiers of reactions and metabolites were converted from KEGG into BiGG human-readable form.[117] Additionally, reaction and metabolite identifiers were also linked to the modelSEED database [92] that enables analysis through the KBase web interface. [8] The gene identifiers and functional descriptions were updated to the most current annotation (NCBI Reference Sequence: NC_017304.1). Metabolite formulas and charges from the modelSEED database[92] were included in the model and reactions were systematically corrected for charge and mass balance by the addition of protons and water.

Metabolic updates

The automated construction process used in the previous model introduced several inconsistencies that were corrected in the current model. We removed reactions that were blocked and non-gene-associated, apparently introduced during automated gap-filling. Two notable examples are i) the blocked selenate pathway which lacks experimental evidence (e.g., selenoproteins have not been found in *C. thermocellum*), and ii) blocked reactions involving molecular oxygen (e.g., oxidation of Fe^{2+} to Fe^{3+}) that are not possible in strict anaerobes. Furthermore, tRNA cycling reactions were unblocked by including tRNA into the biomass reactions.[195] Metabolite isomers were examined and consolidated under the same metabolite identifier when possible, leading to the removal of duplicated reactions and the elimination of gaps. Transport and exchange reactions were updated to reflect the export of amino acids and uptake of pyruvate as observed during fermentation experiments.[93]

In terms of specific reactions, oxaloacetate decarboxylase was eliminated from the model in accordance with recent findings.[177] The stoichiometries of pentose-phosphate reactions sedoheptulose 1,7-bisphosphate D-glyceraldehyde-3-phosphate-lyase (FBA3) and sedoheptulose 1,7-bisphosphate ppi-dependent phosphofructokinase (PFK3_ppi) were corrected (according to experimental evidence[199]) from the previous model by ensuring mass balance and

avoiding lumping multiple steps into one reaction. Transaldolase (TALA) was removed from the model due to lack of annotation for this gene in *C. thermocellum* and to also ensure PFK essentiality as observed experimentally (personal communication from Lynd Research Lab, Dartmouth College).

Several modifications were also performed in key bioenergetic reactions. The reactions catalyzed by membrane-bound enzymes inorganic diphosphatase (PPA) [281] and membrane-bound ferredoxin-dependent hydrogenase (ECH)[26] were corrected to capture proton translocation. Furthermore, hydrogenase reactions were updated to ensure ferredoxin association for all cases and remove those reactions which do not involve ferredoxin and only use NAD(P)H as cofactor based on our recent understanding of *C. thermocellum* metabolism.[15] Gene-protein-reaction associations logical relationships were updated to represent experimental knowledge, e.g., the hydrogenases BIF (CLO11313_RS09060-09070) and H2ASE (CLO1313_RS12830, CLO1313_RS02840) require of the maturase Hyd (CLO1313_RS07925, CLO1313_RS11095, CLO1313_RS12830) to be functional, and the maturase itself requires all of its subunits to operate. This enables accurate representations of *hydG* deletion genotypes.[16]

Two hypothetical reaction modifications were introduced to ensure consistency with reported phenotypes: i) To enable growth without the need for succinate secretion, as observed in experimental data (Supplementary Material 3), the reaction homoserine-O-trans-acetylase (HSERTA) was added to enable methionine biosynthesis (essential for growth) without succinate formation. Although this reaction is not currently known to be associated with any gene in *C. thermocellum*, it is known to be present in other clostridial GSMSs. [167] ii) The reaction deoxyribose-phosphate aldolase (DRPA) was removed to ensure correct lethality prediction of the $\Delta hydG\Delta ech\Delta pfl$ as well as the correct prediction of growth recovery in this mutant by addition of external electron sinks such as sulfate or ketoisovalerate (Table 6.1). DRPA was identified as the best target for removal from a systematic single-reaction deletion analysis (Section 6.4.4). Deletion of *hydG*, *ech*, and *pfl* are proven strategies for enhanced product synthesis while preserving cellular growth, [16, 231, 233] thus the correct prediction of $\Delta hydG\Delta ech\Delta pfl$ -associated phenotypes is critical to successfully use the model for computational strain design.[144, 170, 154, 257, 73, 72, 71]

Table 6.1: Comparison of mutant growth rate prediction between iAT601 and iCBI655. To simulate mutant genotypes for growth rate prediction, gene deletions were applied and growth rate was maximized without constraining secretion fluxes to known values, to recreate simulations for strain design were such additional constraints are not available. *In vivo* values are taken from Thompson et al.[231], where in some mutants growth rate was not reported, but growth recovery was reported, this is indicated with the “+” symbol.

Gene deletions	Medium	Fraction of W.T. growth rate (%)		
		<i>iAT601</i>	<i>iCBI655</i>	<i>In vivo</i>
<i>hydg</i>	MTC	100	100	73
<i>hydg-ech</i>	MTC	85	85	67
<i>hydg-pta-ack</i>	MTC	100	100	48
<i>hydG-ech-pfl</i>	MTC	58	0	0
<i>hydG-ech-pfl</i>	MTC + fumarate	377	726	0
<i>hydG-ech-pfl</i>	MTC + sulfate	58	65	+
<i>hydG-ech-pfl</i>	MTC + ketoisovalerate	97	101	+

6.2.2 Comparison of iCBI655 against other genome-scale models

We compared iCBI655 with the previous GSMS of *C. thermocellum* and the highly-curated GSM iML1515 of the extensively studied bacterium *Escherichia coli* (Table 6.2). The increased number of genes in iCBI655 with respect to iAT601 cover a variety of functions, including hydrogenase chaperons, cellulosome and cellulase, ATP synthase, and transporters. Remarkably, iCBI655 has a smaller percentage of blocked reactions than iAT601, indicating higher biochemical consistency. The number of metabolites in iCBI655 was smaller than those in iAT601 due mainly to the removal of metabolites that did not appear in any reaction, duplicated metabolites (e.g., certain isomers), and blocked pathways added automatically during gap-filling but that lack any gene association. *C. thermocellum* DSM1313 has 2911 protein coding genes, although not all are metabolic, of which iCBI655 covers 22%, while *E. coli* MG1655 has 4240 genes of which iML1515 covers 35%. Overall, iCBI655 increases the coverage of the metabolic functionality of *C. thermocellum* but remains far from the highly studied *E. coli*.

Table 6.2: Comparison of all genome-scale models of *C. thermocellum* and the latest *E. coli* genome-scale model.

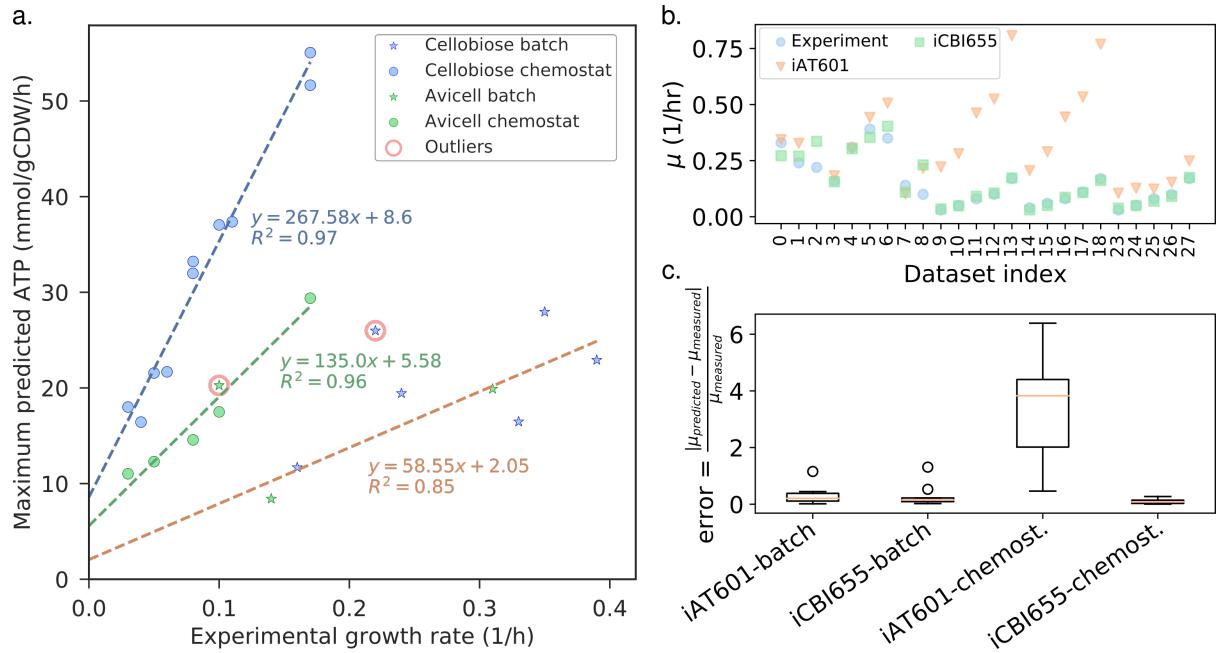
	iSR432	iCth446	iAT601	iCBI665	iML1515
Strain	ATCC27405	ATCC27405	DSM1313	DSM1313	MG1655
Genes	432	446	601	665	1515
Metabolites	583	599	903	795	1877
Reactions	632	660	872	854	2712
Blocked reactions	39.2%	32.1%	40.8%	35.1%	9.8%
Reference	[197]	[47]	[230]	This study	[165]

6.2.3 Training of model parameters under diverse conditions

Growth and non-growth associated maintenance (GAM and NGAM) are parameters that capture the consumption of ATP towards cell division and survival, respectively. These are known to be condition-specific, however, genome-scale models do not include a mechanistic description that allows to determine these ATP consumption rates as part of the simulation. Instead, GAM is incorporated into the biomass pseudo-reaction and NGAM has its own pseudo-reaction that hydrolyzes ATP at a rate tuned by constraints.

To increase model prediction accuracy for a wide number of conditions, we trained GAM and NGAM parameters of iCBI665 using an extensive dataset of 28 extracellular fluxes (Supplementary Material 3) measured during the growth phase under different reactor configurations, carbon sources, and gene deletion mutants. This approach is based on the method used to train the iML1655 *E. coli* model. [165] Remarkably, we observed highly linear trends under three different conditions, chemostat reactor with cellobiose as a carbon source, chemostat reactor with cellulose as a carbon source, and batch reactor with either cellobiose or cellulose as carbon sources (Figure 6.1a). This generalized training lead to increased growth rate prediction accuracy with respect to iAT601 which was trained with a smaller dataset (Figure 6.1b, c).

Figure 6.1: (a.) Training of GAM and NGAM parameters. Discrete points correspond to experimental data. The slope of the linear regression function corresponds to the GAM, while the intercept corresponds to the NGAM. The data points circled as outliers were not included in any of the linear regression calculations. (b.) Comparison of growth prediction error between iCBI655 and iAT601. The measured substrate uptake and product secretion fluxes from each dataset Supplementary Material 3 were used to constraint the model and maximum growth rate was calculated. (c.) Error in growth predictions under batch and chemostat conditions. Predicted and measured growth rates correspond to the values included in b.

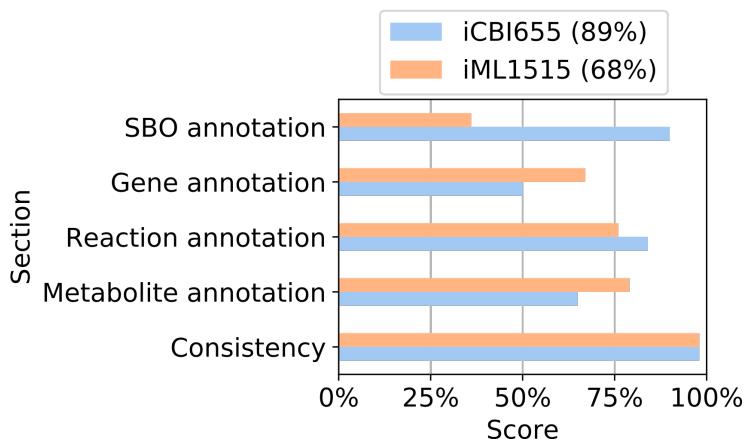


6.2.4 Assessment of model quality and standard compliance with Memote

The field of metabolic network modeling suffers from a lack of standard enforcement and quality control metrics that limits model reproducibility and applicability. To address this issue, Lieven et al. recently developed the Memote framework that systematically tests for standards and best practices in GSMS. [138] We applied Memote to the iCBI655 model and the *E. coli* iML1515 model for comparison (Figure 6.2). This analysis produces five independent scores that assess model quality. The *consistency score* measures basic biochemical requirements, such as mass and charge balance of metabolic reactions, and it was near 100% for both models. Additionally, the different annotation scores quantify how many elements in the

model contain relevant metadata. More specifically, the *systems biology ontology (SBO) annotation* indicates if an object in the model refers to a metabolite, reaction, or gene; while the respective *annotation scores* of these elements correspond to properties (e.g., name, chemical formula, etc.) and identifiers linking them to relevant databases, e.g., KEGG[109] or modelSEED.[92] The *overall score* is computed as a weighted average of all the individual scores with additional emphasis on the *consistency score*. In summary, the high scores obtained by iCBI655 reflect the quality of the model and ensures its applicability for future studies.

Figure 6.2: Scores provided by the quality control tool Memote[138] for iCBI655 and iML1515 (overall score indicated in the legend).



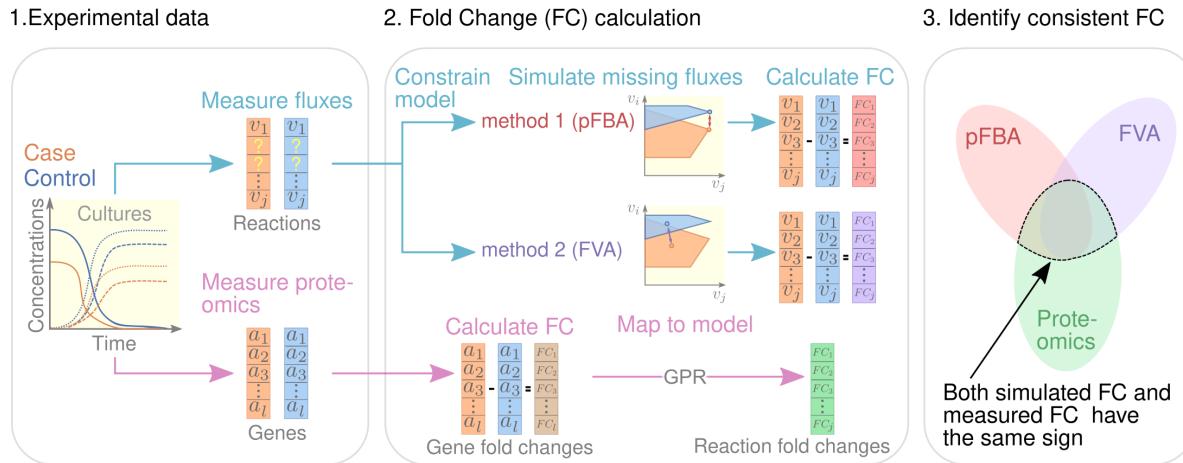
6.2.5 Model-guided systems analysis of proteomics and flux datasets reveals key pathways and cofactors during redox stress

Genome-scale models provide a framework to reconcile and analyze multiple datasets at the systems level. We developed an omics integration method anchored in the quantification of fold change (FC) between case and control samples. FC generalizes to different data types since it is often quantitatively reliable, while more precise metrics like intracellular protein or metabolite concentrations require more sophisticated targeted approaches for quantification. Furthermore, our method does not require one to mechanistically formulate or assume a quantitative relationship between omics measurements and simulated fluxes (Figure 6.3a). We first compare simulated flux changes, that are predicted from measured flux changes,

against measured omics fold changes. Then, we identify for further analysis *consistent reactions*, i.e., reactions with fold change of the same sign and different from zero in both measured and simulated fluxes (Section 6.4.6).

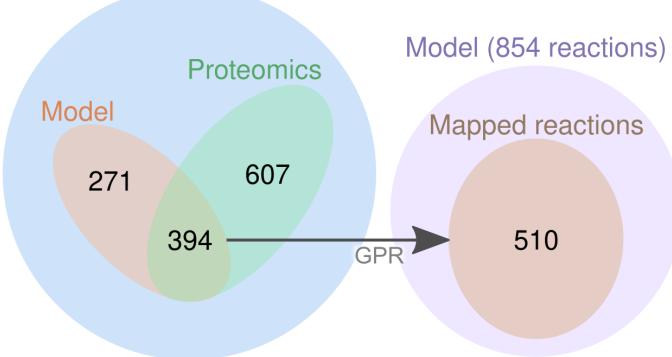
Figure 6.3: (a.) Multi-scale data integration and analysis procedure. (b.) Mapping of proteomics data for the $\Delta hydG$ - Δech case study to model reactions. (c.) Correlation between measured fold changes and simulated fold changes (pFBA in blue and FVA in orange) for all 70 consistent reactions of the $\Delta hydG$ - Δech case study.

a. Omics integration method

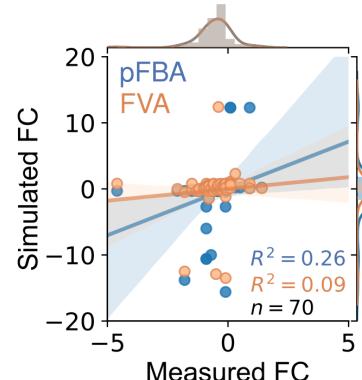


b. Mapping proteomics data to model

Genome (2911 protein coding genes)



c. Correlation of consistent cases



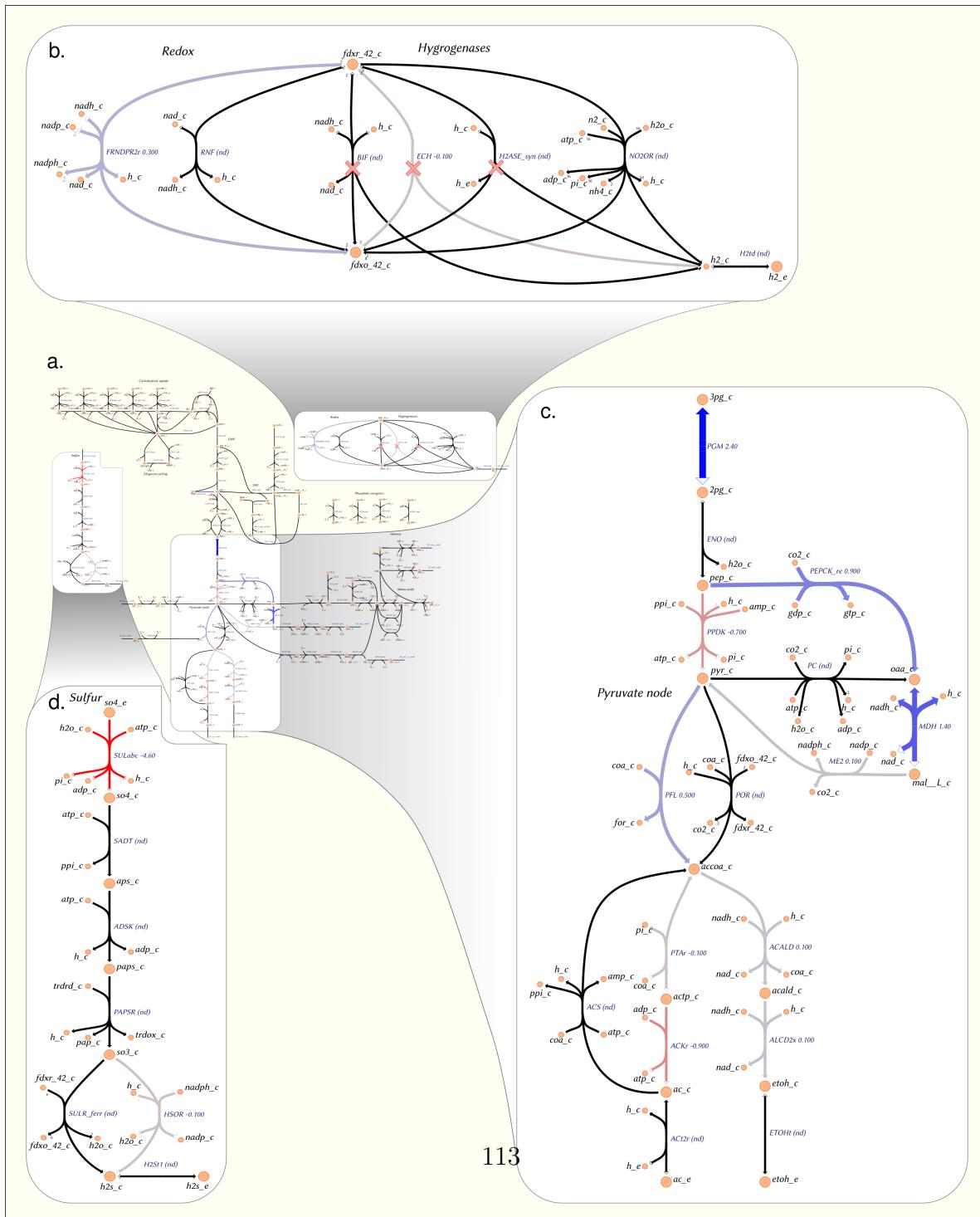
We applied this method to compare the *C. thermocellum* wild-type against the $\Delta hydG\Delta ech$ strain. This mutant was engineered to redirect electron flow from hydrogen to ethanol by removal of primary hydrogenases.[16, 231] First, we obtained measured FC by mapping the measured proteomics data to 510 out of the 856 reactions in the model

thorough the gene-protein-reaction (GPR) associations (Figure 6.3b). Then, we identified 70 consistent reactions by comparing measured FC with two types of simulated FC: i) parsimonious flux balance analysis (pFBA) that determines the flux distribution with the lowest total flux and ii) flux variability analysis (FVA), which identifies the feasible flux range of each reaction. The Pearson correlation coefficients between simulated and measured fluxes for the consistent reactions were 0.26 and 0.09 for pFBA and FVA respectively (Figure 6.3c). In general, the FVA reaction flux ranges remained mostly unchanged, suggesting that pFBA is a better representation of actual metabolic fluxes as previously observed.[151] Consistent reactions where flux and protein fold change have the same sign but different magnitude can be good indicators to identify regulatory effects at the metabolic level, e.g., substrate concentration affecting enzyme saturation (K_m), substrate and product concentrations affecting thermodynamic feasibility, and allosteric regulation. Alternatively, these discrepancies between measured and simulated FC magnitude could also be linked to enzyme efficiency (K_{cat}), e.g., highly efficient enzymes will have a small concentration increase but a high flux increase.

The top consistent reactions with the highest proteomics FC magnitude (Supplementary Material 1 - Table S1) belong primarily to the central metabolism of *C. thermocellum* (Figure 6.4a). Central metabolic pathways in this organism have been studied in depth with the aim of increasing ethanol production. We will provide a brief overview of the most recent findings and compare them with the results obtained from our analysis.

Redox metabolism *C. thermocellum* has various reactions to regulate the relative concentrations of NADH, NADPH, and Reduced ferredoxin (Figure 6.4b), since these cofactors are used as electron donors with high specificity throughout metabolism. Additionally, several hydrogenases oxidize these reduced cofactors to molecular hydrogen that is secreted by the cell to maintain redox balance. Removal of these hydrogenases through deletion of *ech* (corresponding to the ECH reaction) and *hydG* (corresponding to the BIF and H2ASE_{syn} reactions) was successfully applied to increase ethanol yield.[16] Thompson et al.[231] characterized the $\Delta hydG\Delta ech$ strain in depth by analysis of its extracellular fluxes with a core metabolic model, concluding that the major driver for ethanol production

Figure 6.4: Metabolic map visualization using the iCBI Escher map. Values next to reaction labels correspond to proteomics fold change between $\Delta hydG$ - Δech and wild-type strains only for the 70 consistent reactions identified by the omics analysis (Section 6.2.5). Reaction line thickness and color intensity are proportional to the fold change values, except for reactions drawn in black which do not belong to the 70 consistent reactions. A gradient from gray to blue is used to indicate a positive flux increase, while a gradient from gray to red is used to indicate a negative flux increase. Note that the positive or negative signs only indicate the directionality of reversible reactions. **(a.)** Overall map of central metabolism. **(b.)** Redox and hydrogenase metabolism, reactions marked with a red cross are deleted in $\Delta hydG$ - Δech . **(c.)** Pyruvate metabolism. **(d.)** Sulfur metabolism.



was redox balancing rather than carbon balancing. To overcome the predicted production bottlenecks in redox metabolism, *nfn* (corresponding to the FRNDPR2r reaction) and *rnf* (corresponding to RNF) over-expression were suggested. In a subsequent study, Lo et al.[143] successfully over-expressed *rnf* in $\Delta hydG\Delta ech$, but that did not lead to increase in ethanol yield. However, deletion of *rnf* and *nfn* led to lower ethanol and increase hydrogen production in $\Delta hydG$. This suggests that while the *rnf* and *nfn* enzymes are essential for ethanol production, they do not constitute the primary bottlenecks in this pathway.

Pyruvate node and the malate shunt Deng et al.[54] investigated the importance of the malate shunt in *C. thermocellum*, which converts phosphoenolpyruvate (*pep*) to oxaloacetate (*oaa*) and then to pyruvate (*pyr*), while transforming one mol of NADH generated during glycolysis to a mole of NADPH (Figure 6.4c). Interestingly, the authors noted that replacement of the malate shunt by alternative pathways not linked to NADPH increased ethanol production, carbon recovery, and reduced amino acid formation, suggesting that NADPH can be oxidized by secondary pathways.

Sulfur metabolism Sulfate serves as an electron acceptor to *C. thermocellum* which is capable of oxidizing it to sulfite and then sulfide (Figure 6.4d). Thompson et al.[231] demonstrated that the strain $\Delta hydG\Delta ech\Delta pfl$, which cannot grow in conventional medium due to its inability to secrete hydrogen or formate, recovered growth by sulfate supplementation to the culture medium. More recently, Biswas et al.[15] reported an increase in final sulfide concentration and over-expression of the associated sulfate uptake and reduction pathway in the $\Delta hydG$ strain, but did not observe a significant difference in final sulfide concentration in $\Delta hydG\Delta ech$. Remarkably, neither of the strains consumed cysteine from the medium, unlike the wild-type. Sulfide can be converted to cysteine by CYSS (Cysteine synthase) or homocysteine and then methionine by SHSL2 and METS (succinyl-homoserine succinate-lyase and methionine synthase), but the connection between the cessation of cysteine uptake and sulfate metabolism remains unclear.

Proteomics data reveals the importance of NADPH Our analysis reveals consistent indications of increased NADPH biosynthesis in the $\Delta hydG\Delta ech$ mutant across three major

metabolic areas: i) an increased translation of FRNDPR2r (also known as NFN) that converts one mol of reduced ferredoxin (*fdxr_42*) and one mole of NADH into two moles of NADPH. (Figure 6.4a); ii) increased translation of all three malate shunt enzymes and decreased translation of the alternative route PPDK; and iii) decreased translation of sulfur transporter and of HSOR that oxidizes sulfite into sulfide consuming NADPH. These observations are consistent with the failure of *rnf* over-expression to enhance ethanol production[143], since RNF produces NADH but the key cofactor bottleneck seems to be NADPH. Furthermore, a direct look at the proteomics data revealed that RNF subunits (Clo1313_0061-Clo1313_0066) had a statistically significant translation decrease in the mutant (Supplementary Material 3). The preference of $\Delta hydG\Delta ech$ towards NADPH could be due to the cofactor specificity of the remaining redox balancing pathways (e.g., isobutanol), thermodynamics and protein cost constraints, or a combination of both. A recent analysis of the thermodynamics of ethanol production in *C.thermocellum* that did not include peripheral pathways highlighted the importance of engineering strategies based on NADPH (e.g., introduction of NADPH-linked GAPDH (that converts glyceraldehyde-3-phosphate to 3-phospho-D-glyceroyl phosphate during glycolysis, and NADPH-FNOR that transfers electrons from reduced ferredoxin to NADPH.

Analysis of simulated fluxes to predict the function of NADPH The analysis based on consistent reactions strongly indicates that NADPH production is important in the mutant to achieve redox balance. However, since not all reactions in the model could be mapped to proteomics measurements and carbon recovery was lower in the mutant strain,[231] it remains to be fully clarified where NADPH is being oxidized. The flux simulations used to identify consistent reactions take into account all metabolic reactions. Thus, we examined the remaining reactions that had different fluxes between wild-type and mutant, and limited this search to exchange reactions and reactions that involve NADPH (Supplementary Material 1 - Table S2). These simulated fluxes predicted an increase in the isobutanol pathway, including keto-acid reductoisomerase (KARA1) that consumes NADPH and isobutanol secretion (EX_ibutoh_e). The isobutanol pathway can consume NADPH through several enzymes[141] and has increased flux during overflow

metabolism at high-substrate loading.[93, 232] The model also predicted a decrease in valine secretion (EX_val_L_e), since the isobutanol pathway competes with the valine pathway after KARA1. Remarkably, this prediction is consistent with the lower valine secretion measured in $\Delta hydg\Delta ech$.[15] Note that a certain amount of NADPH is likely oxidized by the mutated alcohol-dehydrogenase enzyme observed after short adaptation in $\Delta hydG$ that is compatible with both NADH and NADPH,[16] but this feature is not captured by the model since in general gene knockouts are simulated by blocking the associated reactions. Overall this analysis indicates that $\Delta hydg\Delta ech$ likely increases isobutanol secretion to alleviate redox imbalance.

Summary Previous studies of $\Delta hydg\Delta ech$ that used secretion fluxes[231] or omics[15] independently pointed at the general presence of redox imbalance in this mutant but were not able to resolve the specific importance of NADPH and associated pathways identified here through dataset integration with the genome-scale model. This illustrates the power of the model as contextualization tool, and provides new insights into the redox bottlenecks present in *C. thermocellum* that are critical in the production of reduced molecules. The reactions with major translational changes identified here can serve as the targets for further engineering.

6.3 Conclusions

In this study we developed a genome-scale metabolic model of the biotechnologically relevant organism *C. thermocellum*. Model development followed standards and best practices to ensure reproducibility and accessibility. We demonstrated the enhanced predictive capacity of the model for diverse fermentation conditions and for the lethality of important mutants. Genome-scale models have a broad range of applications in systems biology, including metabolic engineering, physiological discovery, phenotype interpretation, and studies of evolutionary processes. [62, 180] To illustrate the model applications, we chose to tackle the challenge of disparate data integration and interpretation at the systems level. We developed a novel method for this purpose, and used it to identify routes in central metabolism that were

selected to increase NADPH generation in the $\Delta hydg\Delta ech$ strain, revealing the importance of this cofactor over its alternatives and providing new engineering targets for enhanced biosynthesis of reduced products in *C. thermocellum*. The microorganisms *Escherichia coli* and *Saccharomyces cerevisiae* are two major workhorses of industrial biotechnology, and their respective genome-scale models [165, 146] are critical elements of strain engineering both in academia[19] and industry.[270] We anticipate the iCBI655 genome-scale model will also provide a versatile tool for systems metabolic engineering of *C. thermocellum*.

6.4 Methods

6.4.1 Standard model curation

The genome scale model iCBI655 was constructed from iAT601[230] by following the standard GSM development protocol.[229] Reaction and metabolite identifiers were mapped from KEGG to BiGG using the BiGG API.[117] Metabolite charges were obtained from modelSEED when available, and otherwise calculated using the Chemaxon pKa plugin[222] for a pH of 7.2.[229] The biomass objective function was consolidated into one pseudo-reaction avoiding the use of intermediate pseudo-metabolites present in iAT601. Reactions were assigned a confidence level based on a standard genome-scale model annotations.[229]

6.4.2 Metabolic flux simulations

Constraint-based modeling[180] is based on space feasible fluxes Ω_k defined by network stoichiometry and flux bounds that represent thermodynamic constraints and measured values:

$$\begin{aligned} \Omega_k := \{v_{jk} \in \mathbb{R} : \\ \sum_{j \in \mathcal{J}} S_{ij} v_{jk} = 0 \quad \forall i \in \mathcal{I} \end{aligned} \tag{6.1}$$

$$l_{jk} \leq v_{jk} \leq u_{jk} \quad \forall j \in \mathcal{J} \} \tag{6.2}$$

Here \mathcal{I} and \mathcal{J} are the sets of metabolites and reactions in the model, respectively, and v_j is the metabolic flux (mmol/hr/gCDW) through reaction j . Constraint (6.1) enforces mass balance for all metabolites in the network, where S_{ij} represents the stoichiometric coefficient of metabolite i in reaction j ; while constraint (6.2) enforces lower and upper bounds, l_j and u_j respectively, for each reaction j in the network.

In different simulation conditions, k , S_{ij} remains fixed given the structure of the network for all $i, j \in \mathcal{I}, \mathcal{J}$. However, certain bounds u_{jk} and l_{jk} are modified to represent specific metabolic constraints. For example, to apply measured reaction fluxes such as in the case of GAM and NGAM calculation or the omics integration protocol (Section 6.4.6), l_{jk} and u_{jk} are specified using the experimentally measured average (μ_{jk}) and standard deviation (σ_{jk}), which for normally distributed samples with 3 replicates produces an interval with a confidence level above 90% (6.3-6.4). Similarly, to represent a certain gene deletion mutant k , the bounds are set as $u_{jk} = l_{jk} = 0$ for the associated reaction j .

$$l_{jk} = \mu_{jk} - \sigma_{jk} \quad \forall j \in \text{Measured}_k \quad (6.3)$$

$$u_{jk} = \mu_{jk} + \sigma_{jk} \quad \forall j \in \text{Measured}_k \quad (6.4)$$

The feasible flux space Ω_k can be explored in different ways,[244, 180] often an optimization objective is defined to identify specific flux distributions $v_{jk}^{\text{sim}} \forall j \in \mathcal{J}$:

$$v_{jk}^{\text{sim}} \in \arg \max \left\{ \sum_{j \in \mathcal{J}} c_j v_{jk} : v_{jk} \in \Omega_k \right\} \quad \forall j \in \mathcal{J} \quad (6.5)$$

Here c_j is the coefficient of reaction j in the linear objective function, which is changed according to the simulation context. For example, to train GAM and NGAM (Figure 6.1a) the objective was set to maximize flux through the ATP hydrolysis reaction (i.e., $c_j = 1$ for j corresponding to ATP hydrolysis reaction and 0 otherwise); while to evaluate growth prediction accuracy (Figure 6.1b,c) the objective was set to maximize growth (i.e., $c_j = 1$ for j corresponding to growth pseudo-reaction and 0 otherwise).

6.4.3 Simulation of different environments

The model is configured to generally represent different medium and reactor conditions by modifying three aspects: 1) Model boundaries that indicate which metabolites may enter the extracellular environment (i.e., present in the growth medium) or may exit the extracellular environment (i.e., known to be secreted by *C. thermocellum*). This is can be adjusted through u_j and l_j for exchange reactions. In our simulations, only essential metabolites required for *in silico* growth may be consumed and only commonly observed metabolites may be produced, unless otherwise noted. 2) Biomass objective function, iCBI655 contains 3 possible biomass reactions: BIOMASS_CELLULOSE, used when cellobiose is the carbon source, thus 2% of cell dry weight (CDW) corresponds to cellulosome;[277] BIOMASS_CELLULOSE, used when cellulose is the carbon source, thus 20% of CDW corresponds to cellulosome; [277] BIOMASS_NO_CELLULOSOME, a biomass function where no amount of cellulosome is considered, used only as a reference since it does not correspond to any known experimental condition. The cellulosome fraction combined with the remaining protein fraction accounts for 52.85% of the CDW in all cases. [197, 231] Cellobiose conditions were used in all simulations unless otherwise noted. 3) GAM/NGAM, three sets of these parameters are available, batch, chemostat-cellulose, and chemostat-cellobiose, based on fitting the model to experimental data. Batch conditions were used in all simulations unless otherwise noted.

The simulation of cellulose growth was connected to glucose equivalent uptake (the value measured experimentally) through the following pseudo-reactions: $3 \text{ glceq_e} \rightarrow \text{cell3_e}$; $4 \text{ glceq_e} \rightarrow \text{cell4_e}$; $5 \text{ glceq_e} \rightarrow \text{cell5_e}$; $6 \text{ glceq_e} \rightarrow \text{cell6_e}$. Where $\text{cell}(x)\text{-e}$ corresponds to a celldextrin polymer with x glucose monomers, which can be imported inside the cell through the oligo-cellulose transport ABC system. The model is free to use any celldextrin length, although higher lengths have higher ATP yield. [277, 230]

6.4.4 Single-reaction deletion analysis for phenotype consistency

A core model of *C. thermocellum*[231] correctly predicted the lethality of $\Delta hydG\Delta ech\Delta pfl$, however the iAT601 genome-scale model built by extension of this core model failed to predict the absence of growth, suggesting that the genome-scale model has pathways inactive *in vivo*

but lead to the false growth prediction *in silico*. To solve this false positive prediction that was also originally present in iCBI655, we calculated maximum growth rate for all possible one additional reaction deletions in the $\Delta hydG\Delta ech\Delta pfl$ mutant. This analysis lead to three deletions that would cause a maximum growth rate prediction below 20% of the simulated wild-type value (considered to be lethal *in silico*[180]): (a) the removal of glycine secretion, but that would not be consistent with growth recovery by addition of external electron sinks; (b) the removal of 5,10-Methylenetetrahydrofolate oxidoreductase (MTHFC), however this leads PFL as the only source of essential biomass components, but PFL deletion is known to not be lethal on its own;[182] and (c) the elimination of Deoxyribose-phosphate aldolase (DRPA), which converts 2-Deoxy-D-ribose 5-phosphate into glyceraldehyde 3-phosphate and acetaldehyde, this acetaldehyde acts as an electron sink enabling growth. The last option was chosen since it does not lead to any known inconsistencies and also captures growth-recovery by external electron acceptor addition.[231]

6.4.5 Model comparison

The *C. thermocellum* and *E. coli* models were obtained from their respective publications in SBML format. Blocked reactions are calculated by allowing all exchange reactions to have an unconstrained flux (i.e., $lb_j = -1000$, $ub_j = 1000 \forall j \in Exchange$). This enables the most general scenario which produces the smallest number of blocked reactions in each model. Additional details can be found in Supplementary Material 4.

6.4.6 Omics integration protocol

The omics integration protocol consists of three steps: i) Simulation of fold changes; ii) mapping of measured gene fold changes to reactions; and iii) comparison of measured and simulated fold changes.

Calculation of simulated fold changes

To simulate metabolic fluxes, lower and upper bounds (6.2) are constrained according to experimental data as described in Section 6.4.2. Then, for the pFBA method, a quadratic

optimization problem (6.6) is solved leading to a unique flux distribution $v_{jk}^{\text{pFBA}} \forall j \in \mathcal{J}$.

$$v_{jk}^{\text{pFBA}} \in \arg \min \left\{ \sum_{j \in \mathcal{J}} v_{jk}^2 : v_{jk} \in \Omega_k \right\} \forall j \in \mathcal{J} \quad (6.6)$$

For the FVA method, a sequence of linear programming problems is solved where each flux is maximized (6.8) and minimized (6.7):

$$v_{jk}^{\min} \in \arg \min \{v_{jk} : v_{jk} \in \Omega_k\} \forall j \in \mathcal{J} \quad (6.7)$$

$$v_{jk}^{\max} \in \arg \max \{v_{jk} : v_{jk} \in \Omega_k\} \forall j \in \mathcal{J} \quad (6.8)$$

Note that for computation we applied the loop-less FVA method,[206, 32] as in implemented in cobrapy,[60] that introduces additional constraints in Ω_k to remove thermodynamically infeasible cycles from all feasible flux distributions.

FVA produces a flux range $[v_{jk}^{\min}, v_{jk}^{\max}]$ for each reaction $j \in \mathcal{J}$. To compare between states k (e.g., wild-type and mutant) we define the *FVA center*, a scalar variable that indicates a change in this range (6.9).

$$v_{jk}^{\text{FVA}} = \frac{v_{jk}^{\max} + v_{jk}^{\min}}{2} \quad (6.9)$$

Note that the FVA center, v_{jk}^{FVA} , does not attempt to quantify the fraction of overlap between ranges nor to identify what type of shift might have occurred from all possible permutations, but simply provide an indicator of whether there is an upward shift (center increase) or downward (center decrease) between two conditions k . Unlike v_{jk}^{pFBA} , v_{jk}^{FVA} does not necessarily represent a feasible flux distribution of Ω_k .

Finally, to determine the fold change for either pFBA or FVA simulated fluxes, the conventional procedure for fold change calculation in omics data is emulated. First, values are floored to avoid very large (or infinite) fold changes in cases with very small magnitude change. Given the minimum flux flooring value $\epsilon = 0.0001$ a flooring function (6.10) is

defined.

$$floor(v_j) = \begin{cases} v_j + \epsilon & \text{if } 0 < v_j < \epsilon \\ v_j - \epsilon & \text{if } 0 > v_j > -\epsilon \\ v_j & \text{otherwise} \end{cases} \quad (6.10)$$

Then, the fluxes are normalized to the substrate uptake rate $v_{\text{upt},k}$ and fold change is calculated in \log_2 space (6.11).

$$FC_j^{\text{sim}}(v_{j,\text{mut}}, v_{j,\text{wt}}) = \log_2 \left[floor \left(\frac{v_{j,\text{mut}}}{|v_{\text{upt},\text{mut}}|} \right) \right] - \log_2 \left[floor \left(\frac{v_{j,\text{wt}}}{|v_{\text{upt},\text{wt}}|} \right) \right] \quad (6.11)$$

Calculation of measured fold changes

Several omics data types are measured in terms of genes, then fold change between case and control samples, FC_l , is calculated in \log_2 space for each gene $l \in \mathcal{L}$, where \mathcal{L} is the set of genes in the model. These gene fold changes can be mapped to metabolic reaction fold changes using the gene-protein reaction associations (GPR), given \mathcal{G}_j as the set of genes with $FC_l \neq 0$ in the GPR of reaction j :

$$FC_j^{\text{meas}} = \frac{1}{|\mathcal{G}_j|} \sum_{l \in \mathcal{G}_j} FC_l \quad (6.12)$$

Identification of consistent fold changes

A reaction j is said to have a consistent fold change if the measured fold change has the same sign of at least one of the simulated fold changes, more formally:

$$\begin{aligned} \mathcal{M} := \{ j \in \mathcal{J} : & \left(\left[(FC_j^{\text{sim,pFBA}} < 0) \vee (FC_j^{\text{sim,FVA}} < 0) \right] \wedge (FC_j^{\text{meas}} < 0) \right) \\ & \vee \left(\left[(FC_j^{\text{sim,pFBA}} > 0) \vee (FC_j^{\text{sim,FVA}} > 0) \right] \wedge (FC_j^{\text{meas}} > 0) \right) \} \end{aligned} \quad (6.13)$$

Where $\mathcal{M} \subseteq \mathcal{J}$ is the set of consistent reactions which is considered for further analysis and the simulated fold changes are re-defined for brevity (6.14-6.15).

$$FC_j^{\text{sim,pFBA}} := FC_j^{\text{sim}}(v_{j,\text{mut}}^{\text{pFBA}}, v_{j,\text{wt}}^{\text{pFBA}}) \quad (6.14)$$

$$FC_j^{\text{sim,FVA}} := FC_j^{\text{sim}}(v_{j,\text{mut}}^{\text{FVA}}, v_{j,\text{wt}}^{\text{FVA}}) \quad (6.15)$$

6.4.7 Software implementation

Model development was performed using Python and Jupyter notebooks with open-source Python libraries including cobrapy.[60] The sequence of upgrades and improvements can be seen in the Git version control records, the repository is available online through Github (<https://github.com/trinhlab/ctherm-gem>) and in Supplementary Material 4.

6.4.8 Proteomics data collection

C. thermocellum wild-type and $\Delta hydG\Delta ech$ strains were cultured in batch reactors and metabolic fluxes were calculated as previously described. [231] For proteomics measurements, the wild-type and mutant strains were cultured in MNM and MTC media,[124] respectively (while both wild-type and mutant were originally cultured in MTC,[231] the wild-type had to be cultured separately in MNM medium due to insufficient volume for proteomics sampling in the MTC culture) MTC has higher nitrogen and trace mineral concentrations, but previous studies have shown no effect on growth rates. [124] Then, during the mid-exponential growth phase 10 mL samples were collected, centrifuged, and the resulting pellet was stored at -20°C . Cell pellets were then prepared for LC–MS/MS-based proteomic analysis. Briefly, proteins extracted via SDS, boiling, and sonic disruption were precipitated with trichloroacetic acid. [77] The precipitated protein was then resolubilized in urea and treated with dithiothreitol and iodoacetamide to reduce and block disulfide bonds prior to digestion with sequencing-grade trypsin (Sigma-Aldrich). Following two-rounds of proteolysis, tryptic peptides were salted, acidified, and filtered through a 10 kDa MWCO spin column (Vivaspin 2; GE Healthcare) and quantified by BCA assay (Pierce).

For each LC–MS/MS run, 25 µg of peptides were loaded via pressure cell onto a biphasic MudPIT column for online 2D HPLC separation and concurrent analysis via nanospray MS/MS using a LTQ-Orbitrap XL mass spectrometer (Thermo Scientific) operating in data-dependent acquisition (one full scan at 15 k resolution followed by 10 MS/MS scans in the LTQ, all one µscan; monoisotopic precursor selection; rejection of analytes with an undecipherable charge; dynamic exclusion = 30 s).[76]

Eleven salt cuts (25 mM, 30 mM, 35 mM, 40 mM, 45 mM, 50 mM, 65 mM, 80 mM, 100 mM, 175 mM and 500 mM ammonium acetate) were performed per sample run with each followed by 120 min organic gradient to separate peptides.

Resultant peptide fragmentation spectra (MS/MS) were searched against the *C. thermocellum* DSM1313 proteome database concatenated with common contaminants and reversed sequences to control false-discovery rates using MyriMatch v.2.1.[224] Peptide spectrum matches (PSM) were filtered by IDPicker v.3[150] to achieve a peptide-level FDR of <1 % per sample run and assigned matched-ion intensities (MIT) based on observed peptide fragment peaks. PSM MITs were summed on a per-peptide basis and those uniquely mapping to their respective proteins were imported into InfernoRDN.[226] Peptide intensities were log2-transformed, normalized across replicates by LOESS, standardized by median absolute deviation, and median centered across all samples. Peptide abundance data were then assembled to proteins via RRollup and further filtered to maintain at least two values in at least one replicate set. Protein abundances were then used for the modeling efforts describe herein.

All raw and database-searched LC-MS/MS data pertaining to this study have been deposited into the MassIVE proteomic data repository and have been assigned the following accession numbers: MSV000084488 (MassIVE) and PXD015973 (ProteomeXchange). Data files are available upon publication (<ftp://massive.ucsd.edu/MSV000084488/>).

Supplementary Materials

1. Supplementary figures and tables

2. iCBI655 model in various formats for cellobiose growth condition and map of central metabolic pathways in Escher format.
3. Flux dataset used to train the iCBI655 model and proteomics dataset for the wild-type and $\Delta hydG\Delta ech$ strains.
4. Software used to develop, configure, and analyze iCBI655.

Chapter 7

**Development of method to design
modular cells with many objectives
and its application to identify
generalized modular design principles**

Chapter 8

Conclusions

Despite the high interest in the application of modular design in synthetic biology and related fields, not many quantitative and systematic design frameworks exist. This thesis has developed such tools, notably using multi-objective optimization as basis to formulate modular design problems in synthetic biology. The driving application behind these developments is whole-cell biocatalysis, a technology that can lead to renewable and efficient manufacturing of chemicals, fuels, and materials. Primarily guided by their intuition, researchers at companies and universities have built platform strains that recycle the knowledge and labor applied towards a given product to expand towards other molecules that use similar metabolic pathways. Motivated by this principle, several iterations of the ModCell design method have been developed and applied to elucidate modular design principles for biocatalytic strains (Figure 8.1). Overall, this effort contributes to the current wave of converting molecular biology into a more quantitative science by developing and applying mechanistic models of metabolism, and provides new tools to develop modular biocatalytic strains. We envision these new design tools will lower the cost and time required to develop efficient and robust biocatalytic strains that harness the large space of molecules resulting from natural and synthetic metabolic pathways.

In computational biology, algorithmic and modeling challenges are critical aspects, however, as an applied field, simulation efforts need to be connected to experimental ones. Bridging the gap between simulations and experiments, can be addressed from two perspectives: i) Simulations are used *a priori* to generate a hypothesis, then experiments

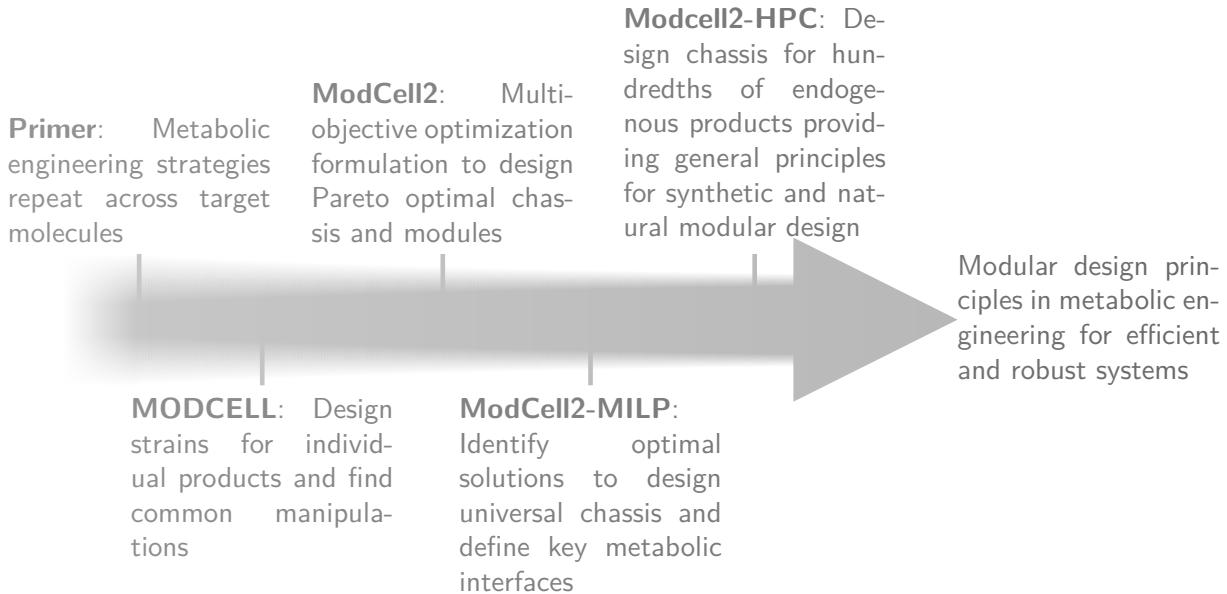


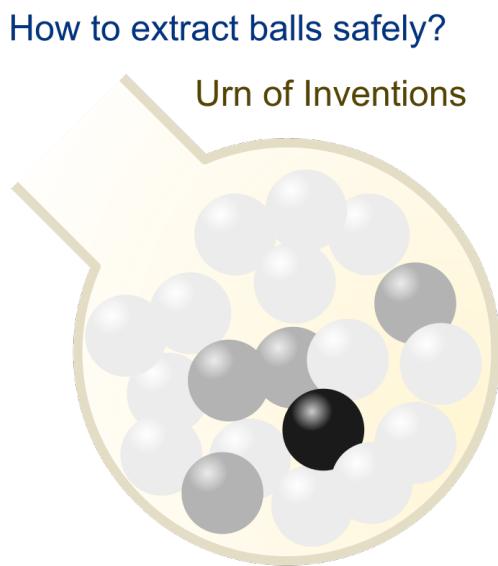
Figure 8.1: Advances of this thesis.

are conducted to test the hypothesis and also perhaps to validate the accuracy of the simulation; ii) Experimental observations are available, and simulations are used to explain them, i.e., to assist in developing a scientific theory. Chapter 6 falls under the second category, where the developed metabolic model is used to explain proteomics data at the system level to contribute towards a redox-imbalance theory of biocatalytic *C. thermocellum* strains. However, the majority of this work, formulated as a biocatalysis strain design problem, falls under the first category. Hence, the next wave of development of modular cell design principles should be focused on the implementation and characterization of the strains proposed here, closing the design-build-test cycle.

As with most contemporary scientific works, this thesis contributes a drop to the ocean of knowledge needed to address the scientific and social challenges of our time. There are multiple relevant facets to the problems tackled here. In particular, biological modeling remains limited by our ability to integrate disparate data types, and the technical challenges of measuring certain parameters such as the catalytic efficiency of each enzyme; while biocatalysis remains limited by poor enzyme expression and function in pathways of interest. Overall, our ability to build and manipulate living organisms for any feasible biological function, does not seem to be around the corner. However, the key challenges needed

for successful applied technologies are rapidly being overcome, as evidenced by the many biotechnology companies emerging over the last decade. As we develop novel technologies, we must also become aware of the ethical and existential risks associated with them. For example, genetic engineering for enhanced cognitive abilities could likely become an expensive medical treatment that increases the wealth gap in society. These concerns are specially relevant for the field of synthetic biology, as genetic engineering tools becomes more widely available enabling DIY biohacking [13]. These developments could pose an existential risk for our current civilization given that a highly destructive technology becomes sufficiently easy to use, and such technology cannot be “uninvented” or effectively policed. This challenge can be illustrated through The Urn of Inventions metaphore (Figure 8.2) [21]. Briefly, consider technologies to be balls in an urn, and our current strategy is to draw balls as fast as possible, perhaps to obtain wealth, prestige, and citations. However, if there was a “black ball” technology, which discovery would have highly damaging consequences, alternative strategies should be considered to prevent a global catastrophe. In summary, while issues like climate change already receive considerable attention, we should become more aware of other dangers of technological development and create policies accordingly.

Vulnerable World Hypothesis



Technology types	
	Beneficial (e.g., antibiotics)
	Mixed results (e.g., nuclear fission)
	Destroy civilisation (e.g., DIY pathogen)
Proposed solutions	
<ul style="list-style-type: none">• Restrict technological development• Ensure that there does not exist a large population of actors representing a wide distribution of motives• Establish extremely effective preventive policing• Establish effective global governance	

Figure 8.2: The Vulnerable World Hypothesis described through the Urn of Inventions metaphor. The hypothesis is that there exists a technology that once discovered would have devastating effects to civilisation. If the hypothesis is true, we should reconsider how scientific discovery is to be conducted to minimize such risk. See [21] for further explanation of the topic and proposed solutions.

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Appendices

A Supplementary Material 1 for Chapter 3

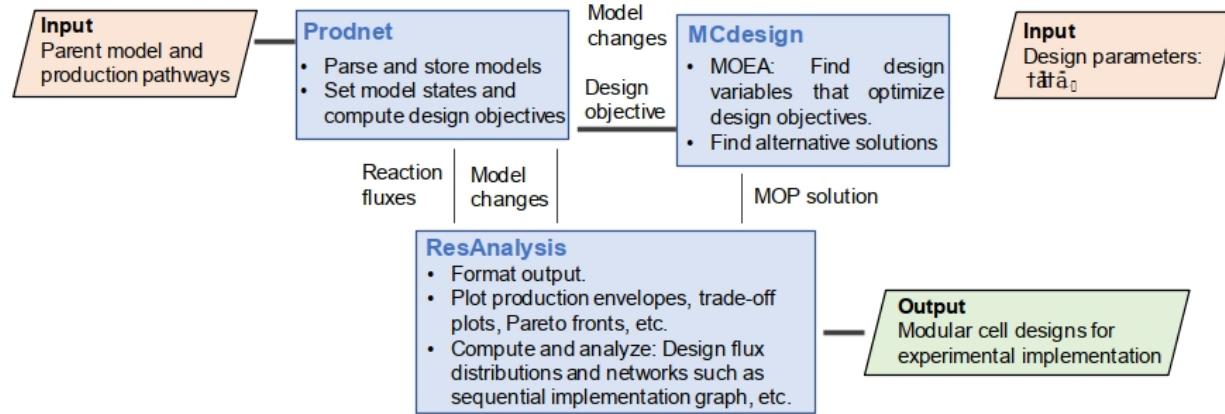


Figure A1: Software architecture of ModCell2. The Prodnet class preprocesses production network models and computes design objectives. The MCdesign class serves as an interface between the MOEA optimization method and metabolic models. The ResAnalysis class loads the Pareto set computed by MCdesign and performs analyses to identify the most promising designs.

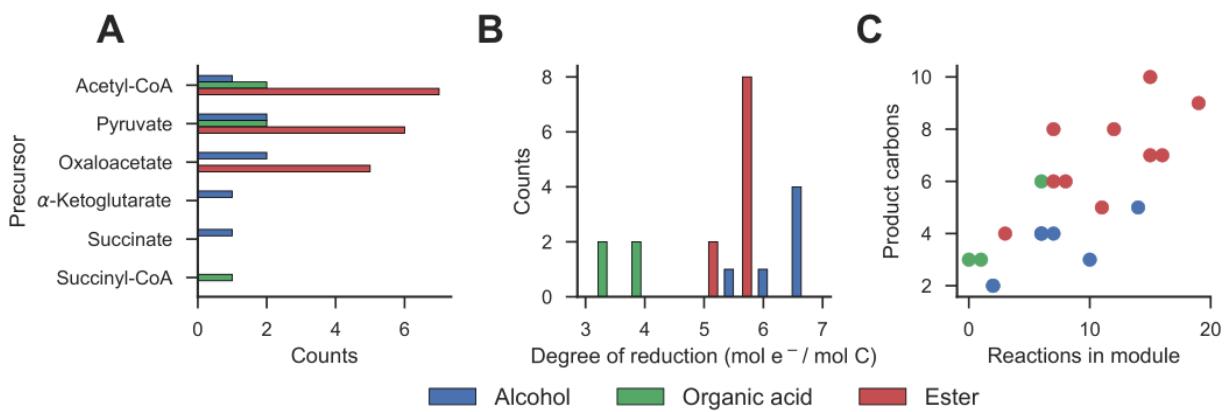


Figure A2: Properties of 20 production modules used in the *E. coli* genome-scale metabolic model for biosynthesis of 6 alcohols, 4 organic acids, and 10 esters. (A) Distribution of precursor metabolites. (B) Distribution of degrees of reduction of target products. (C) Correlation between the number of product carbons and the number of reactions in production modules. Alcohols include ethanol, propanol, butanol, isobutanol, pentanol, and 1,4-butandiol; acids include pyruvate, D-lactate, acetate, and adipic acid; and esters include ethyl acetate, propyl acetate, isobutyl acetate, ethyl butanoate, propyl butanoate, butyl butanoate, isobutyl butanoate, ethyl pentanoate, isobutyl pentanoate, and pentyl pentanoate.

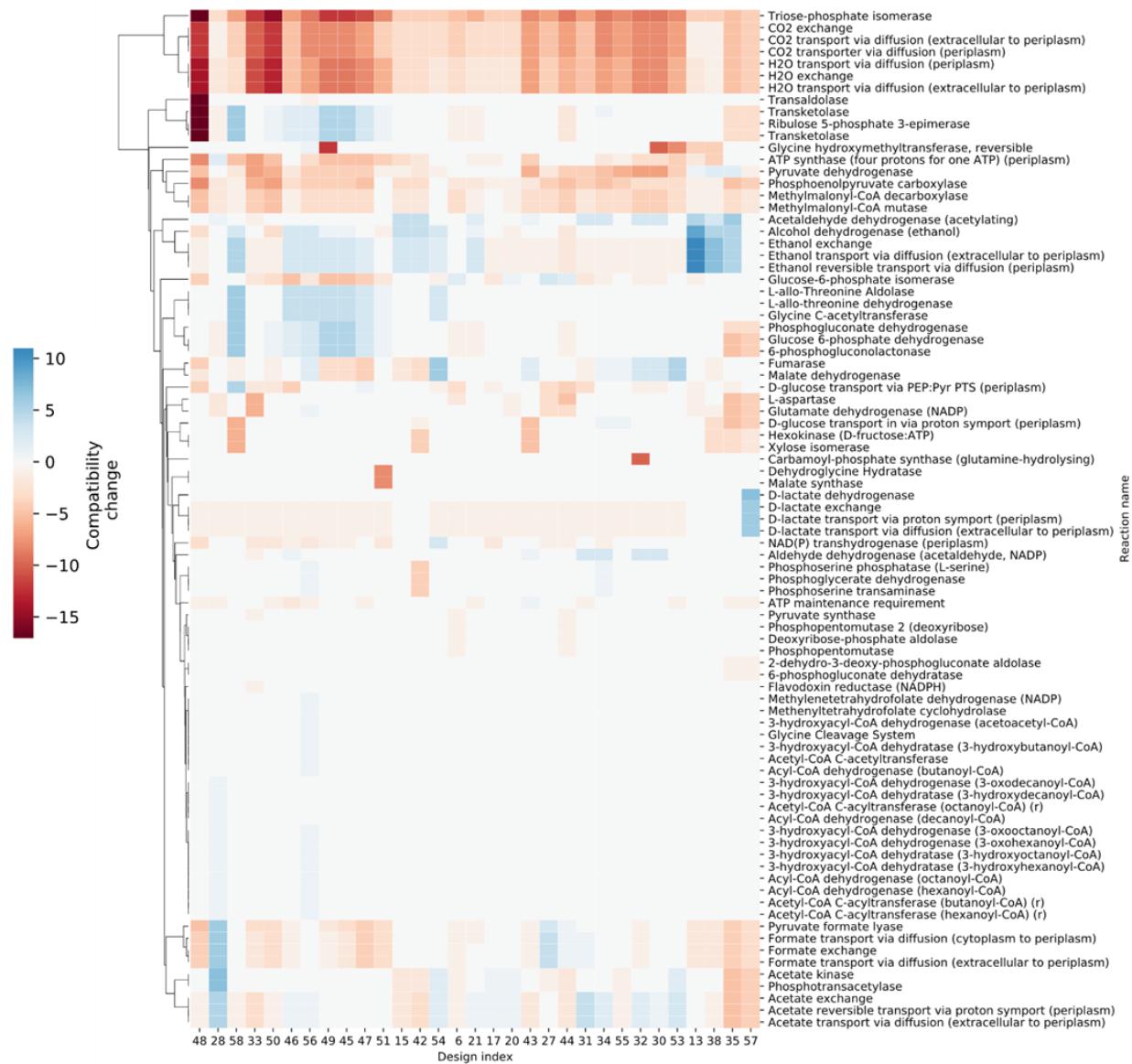


Figure A3: Robustness analysis for wGCP-4-0 designs for the *E. coli* genome scale model. Only the designs that are compatible with 4 or more products (compatibility 4) were considered. Each column corresponds to a design whereas each row corresponds to a single-reaction deletion. Included in the heat map are all reaction deletions with a compatibility change that is not 0 in at least one product.

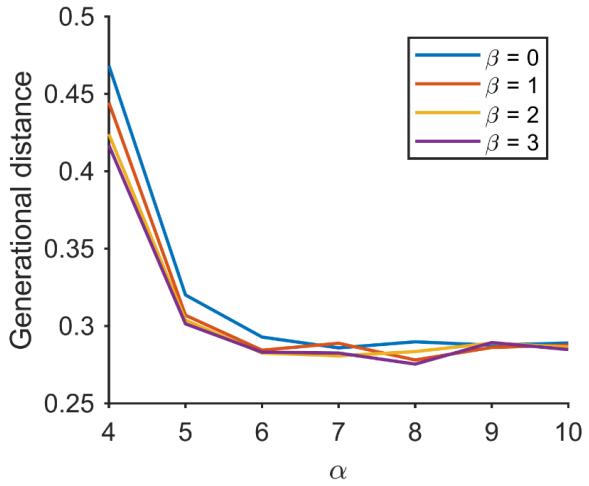


Figure A4: Generational distances between the calculated Pareto fronts and the reference utopia point. The generational distance is calculated as follows: $GD = \frac{|d|_2}{|d|_1}$ where $d_j = |\mathcal{PF}^j - \mathcal{PF}^*|_2$ where \mathcal{PF} is the calculated pareto front and $\mathcal{PF}^* = \vec{1}$ is the utopia point. A smaller value of GD indicates the overall objective values in the Pareto front are closer to the utopia point. The calculation was performed for the iML1515 model with 20 products using the wGCP objective, various α values, and a run time of 10 h for all cases.

B Supplementary Material 2 for Chapter 3

B.1 Solution method: Multiobjective Evolutionary Algorithm

Definitions

Terms

Parent network: A parent network is a metabolic model of a host organism that is used to construct a modular cell.

Production module: A production module is a metabolic pathway that is added to a modular cell to synthesize a target product.

Production network: A production network is a combination of a parent network and a production module.

MOEA: Multiobjective evolutionary algorithm.

Sets

\mathcal{I}_k : Set of metabolite indices in production network k .

\mathcal{J}_k : Set of reaction indices in production network k .

\mathcal{K} : Set of production network indices.

\mathcal{C} : Set of candidate reaction deletion indices, where $\mathcal{C} \subseteq \mathcal{J}^{parent} \subseteq \mathcal{J}_k, \forall k \in \mathcal{K}$.

Continuous variables

v_{jk} : Flux of reaction j in production network k .

v_{Pk} : Flux of target product (P) reaction in production network k .

v_{Xk} : Flux of biomass (X) synthesis reaction in production network k .

f_k : Objective function for production network k .

f_k^{wGCP} : $wGCP$ objective function for production network k .

f_k^{sGCP} : $sGCP$ objective function for production network k .

f_k^{NGP} : NGP objective function for production network k .

p_k : Penalty objective function for production network k .

q^{enum} : Objective function for enumerating alternative solutions.

Binary variables

y_j : Reaction deletion indicator that takes a value of 0 if reaction j is deleted in a modular cell, and 1 otherwise.

z_{jk} : Endogenous, module-specific reaction indicator that takes a value of 1 if reaction j is added back to the production module in network k , and 0 otherwise.

$d_{jk} = y_j \vee z_{jk}$: Modeling variable which takes a value of 1 if reaction j may carry flux in production network k , and 0 otherwise.

Parameters

S_{ijk} : Stoichiometric coefficient of metabolite i in reaction j of production network k .

l_{jk} : Lower bound flux for reaction j in production network k .

u_{jk} : Upper bound flux for reaction j in production network k .

α : Maximum number of deletion reactions in a modular cell.

β_k : Maximum number of endogenous module-specific reactions in the module of production network k .

ϵ : Small scalar used for tilting the biomass objective function to obtain the minimum product rate available at the maximum growth rate. In the simulation, we used $\epsilon = 0.0001$.

Solver

We used the *gamultiobj()* solver, an implementation of NSGA-II [51], from the MATLAB Optimization Toolbox to solve our combinatorial multiobjective optimization, formulated as an unconstrained multiobjective problem of the form:

$$\max(p_1, p_2, \dots, p_{|\mathcal{K}|})^T \quad (\text{B1})$$

with a *bitstring* population type where each individual is a binary vector corresponding to the design variables y_j (reaction deletions) and z_{jk} (endogenous module-specific reactions). To enforce the constraints on the number of deletion and endogenous module reactions, a penalty function p_k , instead of f_k , (Section B.1) and customized genetic operators (Section B.1) were used, respectively.

Penalty Objective function

To restrict the maximum number of reaction deletions, we optimized the following penalty function p_k instead of f_k :

$$p_k = \begin{cases} \frac{f_k}{\sum_{j \in C} (1 - y_j)} & \text{if } \sum_{j \in C} (1 - y_j) > \alpha \\ f_k & \text{otherwise} \end{cases} \quad (\text{B2})$$

The penalty function is designed to decrease f_k of an individual proportionally to the number of deletion reactions exceeding the set limit α . Implementation of this penalty function helps the optimization problem converge rapidly because favorable deletion reaction candidates are likely kept to obtain desirable solutions. After simulation, only solutions satisfying the maximum reaction deletion constraint are preserved to obtain the Pareto set of our original problem.

Design objective computation

Depending on desirable applications, the following design objectives are considered:

$$f_k^{wGCP} = \frac{v_{Pk}^\mu}{v_{P_{max}k}^\mu} \in [0, 1], \quad \forall k \in \mathcal{K} \quad (\text{B3})$$

$$f_k^{sGCP} = \frac{v_{Pk}^\mu}{v_{P_{max}k}^\mu} \frac{v_{Pk}^{\bar{\mu}}}{v_{P_{max}k}^{\bar{\mu}}} \in [0, 1], \quad \forall k \in \mathcal{K} \quad (\text{B4})$$

$$f_k^{NGP} = \frac{v_{Pk}^{\bar{\mu}}}{v_{P_{max}k}^{\bar{\mu}}} \in [0, 1], \quad \forall k \in \mathcal{K} \quad (\text{B5})$$

In (B3)-(B5), the terms v_{Pk}^μ , $v_{P_{max}k}^\mu$, $v_{Pk}^{\bar{\mu}}$, and $v_{P_{max}k}^{\bar{\mu}}$ are computed by solving the following linear programming problems:

$$v_{Pk}^\mu \in \arg \max \{v_{Xk} - \epsilon v_{Pk} : v_k \in \Pi_k^\mu(d_{jk})\} \quad (\text{B6})$$

$$v_{P_{max}k}^\mu \in \arg \max \{v_{Pk} : v_k \in \Pi_k^\mu(d_{jk} = 1, \forall j \in \mathcal{J}_k)\} \quad (\text{B7})$$

$$v_{Pk}^{\bar{\mu}} \in \arg \min \{v_{Pk} : v_k \in \Pi_k^{\bar{\mu}}(d_{jk})\} \quad (\text{B8})$$

$$v_{P_{max}k}^{\bar{\mu}} \in \arg \max \{v_{Pk} : v_k \in \Pi_k^{\bar{\mu}}(d_{jk} = 1, \forall j \in \mathcal{J}_k)\} \quad (\text{B9})$$

The maximum product synthesis fluxes in (B7) and (B9), used to normalize the design objectives in (B3)-(B5), only need to be computed once for each network prior to solving the multiobjective problem (MOP).

In (B6) – (B9), Π_k^μ is the space of steady-state reaction fluxes of production network k where a minimum cell growth is required, defined as follows:

$$\begin{aligned} \Pi_k^\mu(d_{jk}) := \{v_{jk} \in \mathbb{R} \forall j \in \mathcal{J}_k : \\ \sum_{j \in \mathcal{J}_k} S_{ijk} v_{jk} = 0, \quad \forall i \in \mathcal{I}_k \end{aligned} \quad (\text{B10})$$

$$l_{jk} \leq v_{jk} \leq u_{jk}, \quad \forall j \in \mathcal{J}_k \quad (\text{B11})$$

$$l_{jk} d_{jk} \leq v_{jk} \leq u_{jk} d_{jk}, \quad \forall j \in \mathcal{C} \quad (\text{B12})$$

$$v_{Xk} \geq \text{minimum growth rate}\} \quad (\text{B13})$$

Constraints (B10)-(B11) correspond to mass balance and flux bounds, as described in the main text. Constraint (B12) ensures that reaction j cannot carry any flux, if it is deleted in the modular cell and not present in module k . Constraint (B13) specifies any minimum growth rate requirement.

When the design goals involve the stationary phase (B8)-(B9), the space of steady-state reaction fluxes for production network k , $\Pi_k^{\bar{\mu}}$, is defined as follows:

$$\Pi_k^{\bar{\mu}}(d_{jk}) := \{v_{jk} \in \mathbb{R} \mid j \in \mathcal{J}_k : \sum_{j \in \mathcal{J}_k} S_{ijk} v_{jk} = 0, \quad \forall i \in \mathcal{I}_k\} \quad (\text{B14})$$

$$l_{jk} \leq v_{jk} \leq u_{jk}, \quad \forall j \in \mathcal{J}_k \quad (\text{B15})$$

$$l_{jk} d_{jk} \leq v_{jk} \leq u_{jk} d_{jk}, \quad \forall j \in \mathcal{C} \quad (\text{B16})$$

$$v_{Xk} = 0\} \quad (\text{B17})$$

If any of the linear programs associated with f_k becomes infeasible, i.e., $\Pi_k^\mu = \emptyset$ or $\Pi_k^{\bar{\mu}} = \emptyset$, then f_k is set to 0.

Termination criteria

We implemented a non-domination termination criterion to determine when simulation must stop to retrieve a solution, as described in Algorithm 1.

Algorithm 1: Non-domination termination criterion for MOEA. PF: Pareto front, PS: Pareto set.

```
[PF, PS] = solveMOP(initialPoint = ∅, stall_generations, ...)
total_generations = 0
do
    PF_old = PF
    PS_old = PS
    [PF, PS] = solveMOP(initialPoint = PS_old, stall_generations, ...)
    total_generations = total_generations + stall_generations
while any(PF dominates PF_old) and total_generations ≤ max_total_generations
    and run_time ≤ max_run_time
```

Based on this criterion, the solution is retrieved if new non-dominated solutions cannot be found for a predefined number of stall generations. For our study, we used highly conservative, empirical values of 500 and 1000 stall generations with runtime limits of 1-2h and 10-15h for core and genome scale models, respectively.

Customized genetic operators to handle endogenous module-specific reactions

We modified the default scattered crossover and uniform mutation operators of *gamultiobj()* to enforce the constraint on the number of endogenous module reactions and improve convergence. First, we ensured both crossover and mutation operators to produce only individuals that meet the maximum module reaction constraint, i.e., $\sum_{j \in \mathcal{J}_k} z_{jk} \leq \beta_k$, $\forall k \in \mathcal{K}$. Next, we required that only reactions deleted in the modular cell can be used as endogenous module-specific reactions, i.e., $z_{jk} \leq 1 - y_j$, $\forall j \in \mathcal{J}$, $k \in \mathcal{K}$. Finally, we specified the crossover operator to perform crossover on the variables associated with reaction deletions and endogenous module reactions separately, for each production network.

Parameters

All MOEA parameters, except the population size, were left as default. In our study, we set the empirically conservative values for population sizes of 200 and 400 for core and genome-scale models to converge in 2 h and 15 h of simulation time, respectively.

Enumeration of alternative solutions

If a solution w produces the same objective vector as a Pareto optimal solution x^* , i.e., $f(w) = f(x^*)$ and $w \neq x^*$, we say that w constitutes an alternative solution of x^* . To enumerate alternative solutions for a specific Pareto optimal design, we iteratively solve a minimization problem of the form:

$$\min q^{enum} \tag{B18}$$

using MATLAB's genetic algorithm *ga()*. Using the Jaccard similarity metric¹, we define q^{enum} , which takes a value of 0 if an alternative solution is found, as follows:

¹The Jaccard similarity between vectors r and s , $\text{jacc}(r, s)$, corresponds to the fraction of common elements between r and s . If r and s are the same, the Jaccard similarity is 1; if both vectors do not share any elements, then it takes a value of 0.

$$q^{enum} = \begin{cases} M & \text{if } \{y_j : j \in \mathcal{J}_k\} \in \text{ExcludedSol} \quad (\text{B19}) \\ 1 - \text{jacc}(f^*, f) + \sum_{j \in \mathcal{C}} (1 - y_j) & \text{if } \sum_{j \in \mathcal{C}} (1 - y_j) > \alpha \quad (\text{B20}) \\ 1 - \text{jacc}(f^*, f) & \text{otherwise} \quad (\text{B21}) \end{cases}$$

Initially, ExcludedSol will contain at least a target solution for which we are interested in finding alternative solutions. A large scalar M is returned if the current set of deletions $\{y_j\}$ has been found previously, and hence cannot be an alternative solution (B19). Likewise, a set of deletions $\{y_j\}$ may be a valid solution candidate but have more deletions than allowed (B20). In that case, the negated Jaccard similarity is penalized according to the number of reaction deletions.

Optimizing algorithm performance

Variable declaration. To minimize the number of free variables in the optimization problem, we created binary variables, y_j , only for the reaction candidate set C instead of all reactions in the parent model. Similarly, endogenous module reaction variables, z_{jk} , were only created for $j \in \mathcal{C}$ if $\beta_k > 0$.

Selection of starting population. To accelerate convergence in our simulation, we used a predetermined starting population of individuals, if possible. A starting population can be derived from a previously obtained result; for instance, the solutions from $\alpha = 6$ can be used as a starting population to find solutions for $\alpha = 7$. In some cases, we also used design strategies determined experimentally or originated from other strain design algorithms (e.g., Optknock).

Parallelization. To increase the simulation speed, we performed the objective function computations in parallel. This parallelization alleviated the bottlenecks of solving 1 linear programming problem (LP) in $wGCP$ (or NGP) and 2 LPs in $sGCP$.

Archive of solutions. Since computing objective functions is one critical bottleneck, we used a table (archive mapping design variables to design objectives) of previously evaluated individuals to avoid repeating this calculation. The size of the table is determined by the amount of memory available. For instance, we stored at most 50,000 solutions, which can be handled for 20 design objectives by a personal computer. When the table becomes full, it is erased to allow for higher quality individuals to be archived.

B.2 Specifying the Set of Deletion Reaction Candidates for Manipulation

The set of deletion reaction candidates, C , is a subset of all reactions in the parent network, excluding reactions infeasible to eliminate in practice and irrelevant to desirable phenotypes, as described below. Some criteria used in [63] were adapted and implemented in our study.

Macromolecule-associated reactions. These reactions involve macromolecules whose biologically relevant roles are not well represented in the model (e.g., glycogen) or do not impact the optimal design of target product biosynthesis pathways. We identified macromolecule-associated reactions by screening metabolite IDs and formulas, for instance, those with total carbon number above 10 except currency metabolites (e.g., ATP, acetyl-CoA, etc.)

Non-metabolic reactions. These reactions belong to the functional categories such as ion transport, tRNA charging, etc. We identified these non-metabolic reactions by screening the reaction-subsystem annotation in the parent network.

Modeling reactions. These reactions are sink reactions and/or reactions which are not well characterized. We identified the modeling reactions by screening reaction IDs and sbo terms in the parent network.

Transport reactions. These reactions involve metabolites transported across cellular compartments. Most of these reactions are not included in C due to their unspecific

annotation or non-enzymatic mechanisms except some well-annotated reactions such as ATP synthase or NAD(P) transhydrogenase. We identified these transport reactions by screening metabolites appearing in multiple compartments.

Exchange reactions. These reactions are pseudo-reactions used to simulate steady-state conditions. We identified these reactions based on the characteristics they only have either substrates or products.

Orphan reactions. These reactions do not have known encoding enzymes. We determined them by screening gene-protein-reaction associations in the parent model.

Essential reaction. The essential reactions are the reactions whose removal from the model makes the maximum growth rate fall below the minimum acceptable value (i.e, 10-20% of the predicted maximum growth rate). We identified these reactions by performing flux balance analysis combined with single reaction deletions.

Blocked reactions. These reactions carry a flux of 0 mmol/gCDW/hr across all production networks ([Figure B1.A](#)). We found these blocked reactions by performing flux variability analysis.

Reactions in fully correlated sets (co-sets). Sets of reactions that have linearly correlated fluxes are classified as co-sets. These reactions can belong to a linear pathway or more than one associated pathways. For each co-set, only one potential candidate reaction is needed to be considered in the reaction deletion candidate set. In our analysis, we considered all co-sets present in a master network, containing all production modules, to prevent potentially useful reaction deletions to be excluded from the candidate set ([Figure B1.B](#)). We found the co-sets by flux coupling analysis.

Special consideration for NGP designs. The NGP design objective does not involve the growth phase, unlike wGCP and sGCP. Thus, the set of reaction deletion candidates for NGP designs are determined as outlined above except: i) essential reactions that should

be considered in the candidate set and ii) blocked reactions that are determined under non-growth conditions (i.e. biomass flux is constrained to be 0).

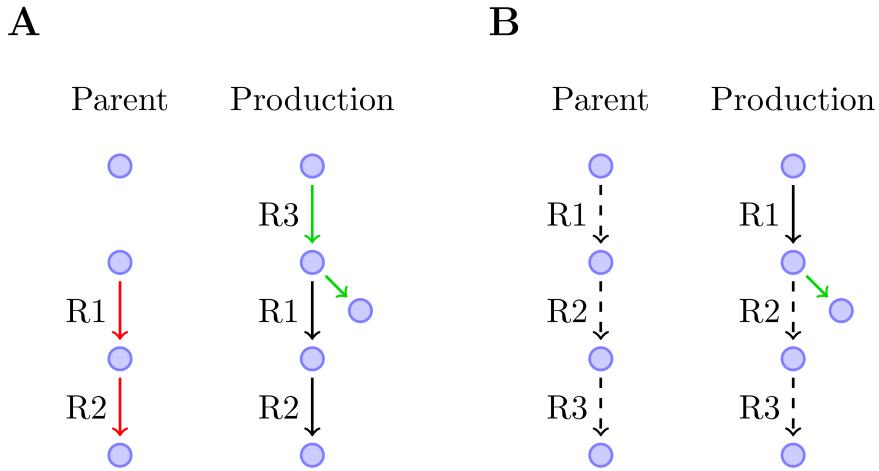


Figure B1: (A) Blocked reactions. The red arrows represent reactions originally blocked in the parent model, because the substrate of R1 cannot be produced. When heterologous reactions (green arrows) are added to produce a target chemical, the originally blocked reactions may become active and drain an intermediate of the production pathway. (B) Reaction co-sets. The dashed arrows are used to indicated a fully correlated set. The addition of heterologous reactions (green arrows), alters the co-set definition and has important effect in deletion candidates. If R1 is considered as a deletion candidate, instead of R2 or R3, that would prevent the elimination of a potentially undesired pathway.

C Supplementary Material 1 for Chapter 6

Table C1: The 70 consistent reactions in the $\Delta hydG$ - Δech case study and their associated fold changes. The biomass reaction is not included due to size. This table is continued in the following pages.

ID	Formula	Fold change		
		proteomics	pFBA	FVAcenter
MDH	mal_L_c + nad_c \leftrightarrow h_c + nadh_c + oaa_c	1.4	0.2	0.1
PEPCK_re	co2_c + gdp_c + pep_c \rightarrow gtp_c + oaa_c	0.9	0.1	0.1
VOR2b	3mob_c + coa_c + 2.0 fdxo_42_c \rightarrow co2_c + 2.0 fdxr_42_c + h_c + ibcoa_c	0.9	12.3	0.8
PFL	coa_c + pyr_c \rightarrow accoa_c + for_c	0.5	0.2	0.8
FRNDPR2r	2.0 fdxr_42_c + h_c + nadh_c + 2.0 nadp_c \leftrightarrow 2.0 fdxo_42_c + nad_c + 2.0 nadph_c	0.3	0.2	2.3
ALCD2x	acald_c + h_c + nadh_c \rightarrow etoh_c + nad_c	0.1	0.8	0.6
IBUTCOARx	h_c + ibcoa_c + nadh_c \rightarrow 2mppal_c + coa_c + nad_c	0.1	12.3	0.8
ACALD	accoa_c + h_c + nadh_c \rightarrow acald_c + coa_c + nad_c	0.1	0.8	1.1
ALCD23xi	2mppal_c + h_c + nadh_c \rightarrow ibutoh_c + nad_c	0.1	12.3	0.8
ME2	mal_L_c + nadp_c \rightarrow co2_c + nadph_c + pyr_c	0.1	0.3	0.1
PSCVT	pep_c + skm5p_c \rightarrow 3psme_c + pi_c	-0.1	-0.3	0.7
PTAr	accoa_c + pi_c \leftrightarrow actp_c + coa_c	-0.1	-2.7	-0.1
HSOR	3.0 h_c + 3.0 nadph_c + so3_c \rightarrow 3.0 h2o_c + h2s_c + 3.0 nadp_c	-0.1	-0.3	-1.2
TRDR	h_c + nadph_c + trdox_c \rightarrow nadp_c + trdrd_c	-0.1	-0.3	0.8
IGPS	2cpr5p_c + h_c \rightarrow 3ig3p_c + co2_c + h2o_c	-0.1	-0.3	0.2
GLUDy	glu_L_c + h2o_c + nadp_c \leftrightarrow akg_c + h_c + nadph_c + nh4_c	-0.1	-0.5	-0.2
ECH	2.0 fdxr_42_c + 3.0 h_c \leftrightarrow 2.0 fdxo_42_c + h2_c + h_e	-0.1	-15.6	-13.5

ALLAS	$24.0 \text{ ala_D_c} + 24.0 \text{ atp_c} + 24.0 \text{ cdpglyc_c} + \text{dg12dg_c} + 24.0 \text{ h2o_c} \rightarrow \text{ala_lta_c} + 24.0 \text{ amp_c} + 24.0 \text{ cmp_c} + 48.0 \text{ h_c} + 24.0 \text{ ppi_c}$	-0.1	-0.2	0.0
HSDxi	$\text{aspsa_c} + \text{h_c} + \text{nadh_c} \rightarrow \text{hom_L_c} + \text{nad_c}$	-0.1	-0.3	0.8
PRMICI	$\text{prfp_c} \rightarrow \text{prlp_c}$	-0.1	-0.3	-0.1
OCBT	$\text{cbp_c} + \text{orn_L_c} \leftrightarrow \text{citr_L_c} + \text{h_c} + \text{pi_c}$	-0.2	-0.3	-0.3
UAGCVT	$\text{pep_c} + \text{uacgam_c} \rightarrow \text{pi_c} + \text{uaccg_c}$	-0.2	-0.3	-0.1
ANS	$\text{chor_c} + \text{gln_L_c} \rightarrow \text{anth_c} + \text{glu_L_c} + \text{h_c} + \text{pyr_c}$	-0.2	-0.3	0.2
DHAD2	$23\text{dhmp_c} \rightarrow 3\text{mop_c} + \text{h2o_c}$	-0.2	-0.3	0.6
ASPO2y	$\text{asp_L_c} + \text{nadp_c} \rightarrow \text{h_c} + \text{iasp_c} + \text{nadph_c}$	-0.3	-0.3	-0.1
NADK	$\text{atp_c} + \text{nad_c} \rightarrow \text{adp_c} + \text{h_c} + \text{nadp_c}$	-0.3	-0.3	-0.1
METS	$5\text{mthf_c} + \text{hcys_L_c} \rightarrow \text{met_L_c} + \text{thf_c}$	-0.3	-0.3	0.8
IMPD	$\text{h2o_c} + \text{imp_c} + \text{nad_c} \leftrightarrow \text{h_c} + \text{nadh_c} + \text{xmp_c}$	-0.3	-0.3	-0.3
MG2abc	$\text{atp_c} + \text{h2o_c} + \text{mg2_e} \rightarrow \text{adp_c} + \text{h_c} + \text{mg2_c} + \text{pi_c}$	-0.3	-0.3	-0.1
PDHam1hi	$\text{h_c} + \text{pyr_c} + \text{thmpp_c} \rightarrow 2\text{ahethmpp_c} + \text{co2_c}$	-0.4	-0.3	12.4
ACAS_2ahbut	$2\text{ahethmpp_c} + 2\text{obut_c} \rightarrow 2\text{ahbut_c} + \text{thmpp_c}$	-0.4	-0.3	0.6
GF6PTA	$\text{f6p_B_c} + \text{gln_L_c} \rightarrow \text{gam6p_c} + \text{glu_L_c}$	-0.4	-0.3	0.0
CHRS	$3\text{psme_c} \rightarrow \text{chor_c} + \text{pi_c}$	-0.4	-0.3	0.7
SERH	$3\text{ig3p_c} + \text{ser_L_c} \rightarrow \text{g3p_c} + \text{h2o_c} + \text{trp_L_c}$	-0.4	-0.3	0.2
ALATA_L	$\text{akg_c} + \text{ala_L_c} \leftrightarrow \text{glu_L_c} + \text{pyr_c}$	-0.5	-0.3	-12.9
NNDPR	$\text{h_c} + \text{prpp_c} + \text{qln_c} \rightarrow \text{co2_c} + \text{nicrnt_c} + \text{ppi_c}$	-0.5	-0.3	-0.1
TMDS	$\text{dump_c} + \text{mlthf_c} \rightarrow \text{dhf_c} + \text{dtmp_c}$	-0.5	-0.3	-0.1
PHETA1	$\text{akg_c} + \text{phe_L_c} \leftrightarrow \text{glu_L_c} + \text{phpyr_c}$	-0.6	-0.3	0.8
TYRTA	$\text{akg_c} + \text{tyr_L_c} \leftrightarrow 34\text{hpp_c} + \text{glu_L_c}$	-0.6	-0.3	0.6
GMPS	$\text{atp_c} + \text{nh4_c} + \text{xmp_c} \rightarrow \text{amp_c} + \text{gmp_c} + 3.0 \text{ h_c} + \text{ppi_c}$	-0.6	-0.3	-0.3
SKK	$\text{atp_c} + \text{skm_c} \rightarrow \text{adp_c} + \text{h_c} + \text{skm5p_c}$	-0.6	-0.3	0.7
ACOTA	$\text{acorn_c} + \text{akg_c} \leftrightarrow \text{acg5sa_c} + \text{glu_L_c}$	-0.6	-0.3	-0.3
PPDK	$\text{amp_c} + 2.0 \text{ h_c} + \text{pep_c} + \text{ppi_c} \rightarrow \text{atp_c} + \text{pi_c} + \text{pyr_c}$	-0.7	-10.0	0.1

GLUPRT	$\text{gln_L_c} + \text{h2o_c} + \text{prpp_c} \rightarrow \text{glu_L_c} + \text{h_c} + \text{ppi_c} + \text{pram_c}$	-0.7	-0.3	-0.3
KARI	$2\text{ahbut_c} \leftrightarrow \text{cpd10162_c}$	-0.8	-0.3	0.6
KARI_23dhmp	$2\text{3dhmp_c} + \text{nadp_c} \leftrightarrow \text{cpd10162_c} + \text{h_c} + \text{nadph_c}$	-0.8	-0.3	0.6
ARGSL	$\text{argsuc_c} \leftrightarrow \text{arg_L_c} + \text{fum_c}$	-0.8	-0.3	-0.3
LEUTA	$4\text{mop_c} + \text{glu_L_c} \rightarrow \text{akg_c} + \text{leu_L_c}$	-0.8	-0.3	0.4
ILETA	$\text{akg_c} + \text{ile_L_c} \leftrightarrow 3\text{mop_c} + \text{glu_L_c}$	-0.8	-0.3	0.6
VALTA	$\text{akg_c} + \text{val_L_c} \leftrightarrow 3\text{mob_c} + \text{glu_L_c}$	-0.8	-1.4	-1.5
ARGSS	$\text{asp_L_c} + \text{atp_c} + \text{citr_L_c} \leftrightarrow \text{amp_c} + \text{argsuc_c} + 2.0 \text{ h_c} + \text{ppi_c}$	-0.8	-0.3	-0.3
SHSL2	$\text{h2s_c} + \text{suchms_c} \rightarrow \text{hcys_L_c} + \text{succ_c}$	-0.9	-6.0	0.8
AHSL	$\text{achms_c} + \text{cys_L_c} \leftrightarrow \text{ac_c} + \text{cyst_L_c} + \text{h_c}$	-0.9	-10.6	-0.3
SHSL1	$\text{cyst_L_c} + \text{h_c} + \text{succ_c} \leftrightarrow \text{cys_L_c} + \text{suchms_c}$	-0.9	-10.6	0.4
ACKr	$\text{actp_c} + \text{adp_c} \rightarrow \text{ac_c} + \text{atp_c}$	-0.9	-2.7	-0.1
QULNS	$\text{dhap_c} + \text{iasp_c} \rightarrow 2.0 \text{ h2o_c} + \text{h_c} + \text{pi_c} + \text{quln_c}$	-0.9	-0.3	-0.1
NADS2	$\text{atp_c} + \text{dnad_c} + \text{gln_L_c} + \text{h2o_c} \rightarrow \text{amp_c} + \text{glu_L_c} + 2.0 \text{ h_c} + \text{nad_c} + \text{ppi_c}$	-0.9	-0.3	-0.1
FE3abc	$\text{atp_c} + \text{fe3_e} + \text{h2o_c} \rightarrow \text{adp_c} + \text{fe3_c} + \text{h_c} + \text{pi_c}$	-1.0	-0.3	-0.1
ASPTA	$\text{akg_c} + \text{asp_L_c} \leftrightarrow \text{glu_L_c} + \text{oaa_c}$	-1.0	-0.3	0.2
CTPS1	$\text{atp_c} + \text{nh4_c} + \text{utp_c} \rightarrow \text{adp_c} + \text{ctp_c} + 2.0 \text{ h_c} + \text{pi_c}$	-1.2	-0.3	0.0
ACGK	$\text{acglu_c} + \text{atp_c} \rightarrow \text{acg5p_c} + \text{adp_c}$	-1.2	-0.3	-0.3
IGPDH	$\text{eig3p_c} \rightarrow \text{h2o_c} + \text{imacp_c}$	-1.2	-0.3	-0.1
AGPR	$\text{acg5sa_c} + \text{nadp_c} + \text{pi_c} \leftrightarrow \text{acg5p_c} + \text{h_c} + \text{nadph_c}$	-1.3	-0.3	-0.3
PHEt2r	$\text{h_e} + \text{phe_L_e} \leftrightarrow \text{h_c} + \text{phe_L_c}$	-1.5	-0.3	0.8
UAG4Ei	$\text{uacgam_c} \rightarrow \text{udpacgal_c}$	-1.5	-0.3	-0.1
CYSS	$\text{acser_c} + \text{h2s_c} \rightarrow \text{ac_c} + \text{cys_L_c}$	-1.8	-0.3	-0.5
BIF	$2.0 \text{ fdxr_42_c} + 3.0 \text{ h_c} + \text{nadph_c} \leftrightarrow 2.0 \text{ fdxo_42_c} + 2.0 \text{ h2_c} + \text{nad_c}$	-1.8	-13.8	-12.5

UMPK	$\text{atp_c} + \text{h_c} + \text{ump_c} \rightarrow \text{adp_c} + \text{udp_c}$	-2.1	-0.3	0.0
SULabc	$\text{atp_c} + \text{h}_2\text{o_c} + \text{so}_4\text{-e} \rightarrow \text{adp_c} + \text{h_c} + \text{pi_c} + \text{so}_4\text{-c}$	-4.6	-0.3	0.8

Table C2: pFBA simulated fluxes from $\Delta hydG$ - Δech case study. Only includes reactions involving NADPH or exchange reactions that have different flux between wild-type and mutant. The biomass reaction is not included due to size. Additionally, we also excluded reactions with the same fold change magnitude as the biomass reaction ($|FC| = 0.26$), likely because they are fully correlated.

ID	Formula	Fluxes (mmol/gCDW/hr)		
		W.T.	Mut.	FC
EX_ibutoh_e	$\text{ibutoh_e} \rightarrow$	0.0	0.49	12.26
KARA1	$\text{alac_S_c} + \text{h_c} + \text{nadph_c} \rightarrow 23\text{dhmb_c} + \text{nadp_c}$	0.22	0.59	1.42
EX_etoh_e	$\text{etoh_e} \rightarrow$	1.09	1.88	0.78
EX_h2o_e	$\text{h}_2\text{o_e} \leftrightarrow$	-0.38	0.5	0.42
EX_co2_e	$\text{co}_2\text{-e} \rightarrow$	2.07	2.77	0.42
ME2	$\text{mal_L_c} + \text{nadp_c} \rightarrow \text{co}_2\text{-c} + \text{nadph_c} + \text{pyr_c}$	2.9	3.51	0.28
EX_for_e	$\text{for_e} \rightarrow$	0.48	0.56	0.23
FRNDPR2r	$2.0 \text{ fdxr_42_c} + \text{h_c} + \text{nadh_c} + 2.0 \text{ nadp_c} \leftrightarrow 2.0 \text{ fdxo_42_c} + \text{nad_c} + 2.0 \text{ nadph_c}$	-1.02	-1.17	0.2
EX_nh4_e	$\text{nh}_4\text{-e} \leftrightarrow$	-0.73	-0.53	-0.48
GLUDy	$\text{glu_L_c} + \text{h}_2\text{o_c} + \text{nadp_c} \leftrightarrow \text{akg_c} + \text{h_c} + \text{nadph_c} + \text{nh}_4\text{-c}$	-0.61	-0.42	-0.53
EX_h_e	$\text{h_e} \leftrightarrow$	2.93	1.19	-1.3
EX_val_L_e	$\text{val_L_e} \rightarrow$	0.18	0.06	-1.54
ICDHyr	$\text{icit_c} + \text{nadp_c} \rightarrow \text{akg_c} + \text{co}_2\text{-c} + \text{nadph_c}$	0.21	0.04	-2.27
EX_ac_e	$\text{ac_e} \rightarrow$	0.93	0.17	-2.46
EX_lac_L_e	$\text{lac_L_e} \rightarrow$	0.05	0.01	-2.49
EX_succ_e	$\text{succ_e} \rightarrow$	0.41	0.0	-12.01
EX_h2_e	$\text{h}_2\text{-e} \rightarrow$	2.2	0.0	-14.43

Vita

Sergio Garcia is originally from Murcia, a southeastern region of Spain. After finishing highschool, he began his studies in Chemical Engineering at the university of Murcia, founded in 1272 among the first universities in the world. Although the Chemical Engineering program is only a few decades old. Sergio spent his junior year abroad at the University of Tennessee Knoxville (UTK) through the International Student Exchange Program scholarship, where he became involved in undergraduate research. He then returned to finish his degree in Murcia, where he also pursued undergraduate research at the Department of Biochemistry and Molecular Biology. After completion of his undergraduate degree, he returned to UTK to pursue a PhD in Chemical and Biomolecular Engineering. In his free time, Sergio enjoys playing music, meditation, and cycling.