

$$T_{rev} = \frac{C}{V}, \quad T_0 = \frac{C_0}{V_0}, \quad dT = \left. \frac{dT}{dp} \right|_0 dp + \frac{1}{2} \left. \frac{d^2T}{dp^2} \right|_0 dp^2 + \dots, \quad \frac{dT}{T} = \frac{T - T_0}{T_0}$$

$$\frac{C - C_0}{C_0} = a_0 \delta + a_1 \delta^2 \rightarrow C = C_0(a_0 \delta + a_1 \delta^2) + C_0 \Rightarrow \frac{dC}{d\delta} = C_0(a_0 + 2a_1 \delta)$$

$$\frac{\Delta V}{V} = \frac{\delta}{f^2} \rightarrow \frac{dV}{dp} = \frac{V}{pf^2}, \quad \frac{d^2V}{dp^2} = \left(\frac{V}{pf^2} \right) \frac{1}{pf^2} - \frac{1}{p^2} \left(\frac{V}{f^2} \right) - \frac{2}{f^3} \left(\frac{V}{p} \right) \left(\frac{df}{dp} \right) \ominus \frac{df}{f} = \beta^2 \frac{dp}{p} \rightarrow \frac{df}{f} = \beta^2 \frac{dp}{p} /$$

$$\ominus \frac{V}{p^2 f^4} - \frac{V}{p^2 f^2} - \frac{2V\beta^2}{f^2 p^2} = \frac{V}{p^2} \left(\frac{1}{f^4} - \frac{1}{f^2} - \frac{2\beta^2}{f^2} \right) = \cancel{\frac{V}{p^2} \left(\frac{1}{f^4} - \frac{1}{f^2} - \frac{2}{f^2} + \frac{2}{f^4} \right)}$$

$$\delta = \frac{p - p_0}{p_0} \rightarrow \frac{d\delta}{dp} = \frac{1}{p_0}$$

$$\left. \frac{dT}{dp} \right|_0 = \left(\frac{dC}{dp} \frac{1}{V} \right) \Big|_0 - \left(\frac{C}{V^2} \frac{dV}{dp} \right) \Big|_0 = C_0(a_0 + 2a_1 \delta) \Big|_0 \frac{1}{p_0} \frac{1}{V_0} - \frac{C_0}{V_0^2} \frac{V_0}{p_0 f_0^2} = C_0 \left(\frac{a_0}{p_0 V_0} - \frac{1}{V_0 p_0 f_0^2} \right)$$

$$\left. \frac{dT}{dp} \right|_0 dp / T_0 = \left(a_0 - \frac{1}{f_0^2} \right) \delta$$

$$\left. \frac{d^2T}{dp^2} \right|_0 = \frac{d}{dp} \left(\frac{d}{dp} \left(\frac{C}{V} \right) \right) \Big|_0 = \frac{d}{dp} \left(\frac{dC}{dp} \frac{1}{V} - \frac{C}{V^2} \frac{dV}{dp} \right) \Big|_0 =$$

$$= \left(\frac{d^2C}{dp^2} \frac{1}{V} \right) \Big|_0 - 2 \left(\frac{dC}{dp} \frac{1}{V^2} \frac{dV}{dp} \right) \Big|_0 + 2 \left(\frac{C}{V^3} \left(\frac{dV}{dp} \right)^2 \right) \Big|_0 - \left(\frac{C}{V^2} \frac{d^2V}{dp^2} \right) \Big|_0 =$$

$$= \left(\frac{2a_1 C_0}{p_0^2} \right) \frac{1}{V_0} - 2 \left(\left(\frac{C_0 a_0}{p_0} \right) \frac{1}{V_0^2} \frac{V_0}{p_0 f_0^2} \right) + 2 \left(\frac{C_0}{V_0^3} \frac{V_0^2}{p_0^2 f_0^4} \right) - \left(\frac{C_0}{V_0^2} \frac{V_0}{p_0^2} \left(\frac{1}{f_0^4} - \frac{1}{f_0^2} - \frac{2\beta_0^2}{f_0^2} \right) \right) =$$

$$= \frac{2C_0}{p_0^2 V_0} \left[a_1 - \frac{a_0}{f_0^2} + \frac{1}{f_0^4} - \frac{1}{2} \left(\frac{1}{f_0^4} - \frac{1}{f_0^2} - \frac{2}{f_0^2} + \frac{2}{f_0^4} \right) \right] =$$

$$= \frac{2C_0}{V_0 p_0^2} \left[a_1 - \frac{a_0}{f_0^2} + \frac{3}{2f_0^2} - \frac{1}{2f_0^4} \right]$$

$$\left. \frac{d^2T}{dp^2} \right|_0 \cdot \frac{1}{2} (dp)^2 \cdot \left(\frac{V_0}{C_0} \right) = \left[a_1 - \frac{a_0}{f_0^2} + \frac{3}{2} \frac{1}{f_0^2} - \frac{1}{2f_0^4} \right] \delta^2$$

$$\frac{dT}{T} = \left(a_0 - \frac{1}{f_0^2} \right) \delta + \left(a_1 - \frac{a_0}{f_0^2} + \frac{3}{2} \frac{1}{f_0^2} - \frac{1}{2f_0^4} \right) \delta^2$$