## **GLM**

### Advanced regression

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### Outline

- Assumptions
- ► Normal distribution
- types
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- estimators
- probit (normal distribution)
- interpretation

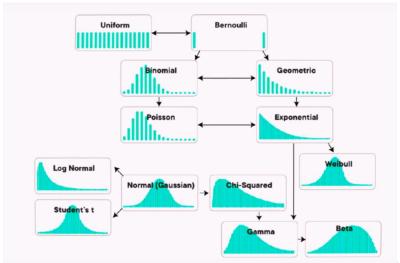
# Assumptions

- Linearity of data
- Sample should be randomly selected for population
- X matrix should not be correlated within
- X marrix should not be correlated with error
- Variance of error should be constant
- Normality of Y

## Normall Distribution



# **Types**



#### Idea



## Link functions

- Identity
- ▶ log (logit)
- probit
- poisson
- negative binomial
- ▶ etc

## Logit

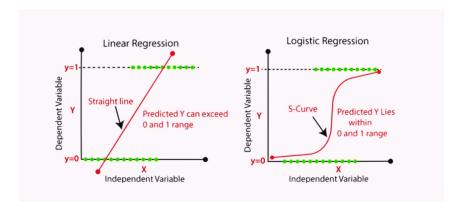
This type of regression suits for binary varaible.

$$Y = log(\frac{p}{1 - p}) \tag{1}$$

Coef output not an absolute straightforward number to interpret it's a chance.

Chance is a probability relation. 1 means that there is equal probability for success and for fail.

# Logit



#### Estimator

MLE - Maximul likelihood Estimator more suits to logit and other GLM

likelihood = 
$$\hat{y} * y + (1-\hat{y}) * (1-y)$$
 (2)

$$log-likelihood = log(\hat{y}) * y + log(1-\hat{y}) * (1-y)$$
(3)

maximize: 
$$\sum_{i}^{n} log(\hat{y}_i) * y_i + log(1-\hat{y}_i) * (1-y_i)$$
 (4)

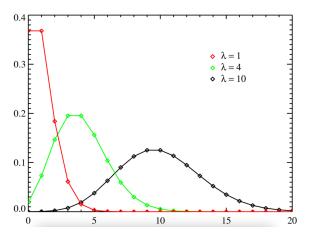
minimize: 
$$\sum_{i}^{n} - (log(\hat{y}_{i}) * y_{i} + log(1 - \hat{y}_{i}) * (1 - y_{i}))$$
 (5)

#### **Probit**

Probit - absolutely the same as logit, but instread of sigmoid generates normal distribution. It hardly could be interpreted as easily as logit, so it's the reason why it so unpopular.

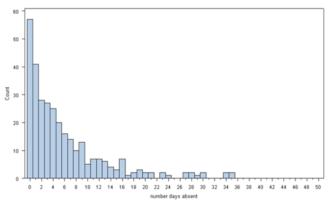
#### Poisson

Usually used for count data. But it's not dealing with zeros.



# Negative Binomial

Negative binomial is a mix of poisson and Gamma distribution.



## Output

```
Call:
alm(formula = Survived ~ Sex + Pclass, family = "binomial", data = df)
Deviance Residuals:
           10 Median 30
   Min
                                  Max
-2.2030 -0.7036 -0.4519 0.6719 2.1599
Coefficients:
          Estimate Std. Error z value Pr(>|z|)
(Intercept) 3.2946 0.2974 11.077 <2e-16 ***
Sexmale
         Pclass
      -0.9606 0.1061 -9.057 <2e-16 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' '1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 1186.7 on 890 degrees of freedom
Residual deviance: 827.2 on 888 degrees of freedom
AIC: 833.2
Number of Fisher Scoring iterations: 4
```

# Output

```
\``\{r\}
\logit \%-\% \coef \%-\% \exp
\``\|
\(\text{(Intercept)} \text{Sexmale Pclass} \\ 26.9677456 \text{ 0.0711192 } \text{ 0.3826812}
```