

Marginal Analysis

Answer Key — All Values

Q	Price (P)	Revenue (R)	Marginal Revenue	Total Cost	Marginal Cost	Profit ($\pi = R - TC$)
0	100	0	92	20	8	-20
1	92	92	76	28	4	64
2	84	168	60	32	4	136
3	76	228	44	36	8	192
4	68	272	28	44	14	228
5	60	300	12	58	22	242
6	52	312	-4	80	34	232
7	44	308	-20	114	50	194
8	36	288	-36	164	68	124
9	28	252	-52	232	88	20
10	20	200	—	320	—	-120

Formulas:

- Revenue: $R(Q) = P(Q) \times Q$ where $P(Q)$ is the price at quantity Q and $R(Q)$ is the revenue at quantity Q
- Marginal Revenue: $MR(Q) = R(Q+1) - R(Q)$
- Marginal Cost: $MC(Q) = TC(Q+1) - TC(Q)$
- Profit: $\pi = R - TC$

Underlying functions:

Demand: $P = 100 - 8Q$ | Cost: $TC = 0.5Q^3 - 3Q^2 + 10Q + 20$

Key observations:

- Maximum profit (\$242) occurs at $Q = 5$, highlighted in green
- At $Q = 4$: $MR (28) > MC (14)$ — still profitable to produce more
- At $Q = 5$: $MR (12) < MC (22)$ — producing more reduces profit
- Profit-maximizing output is between $Q = 4$ and $Q = 5$ (closest integer: $Q = 5$)