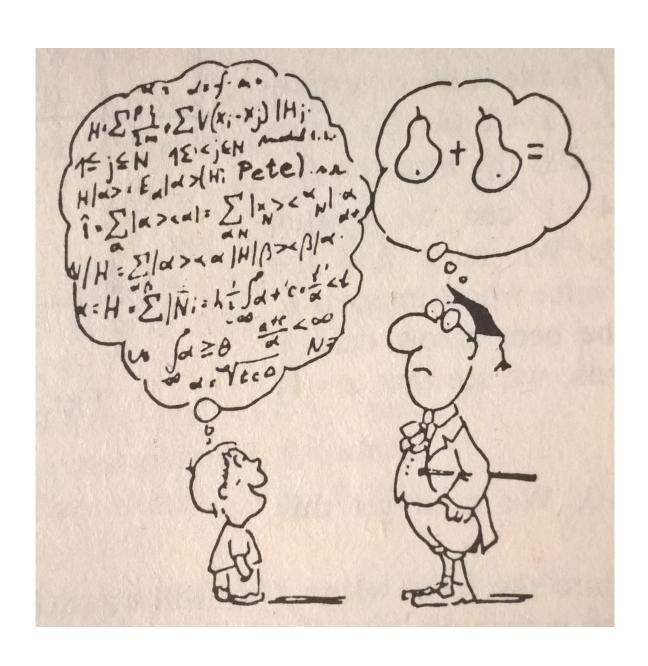
MATH BASICS



1 Definition

1.1 Exponents

1.

$$a^n = a \times a \times a \times a \dots n \quad factors \quad (n \in \mathbb{N}, \ a \in \mathbb{R})$$

2.

$$a^{-m} = \frac{1}{a^m} \qquad (m \in \mathbb{Z}^+, \ a \in \mathbb{R}, \ a \neq 0)$$

and

$$\frac{1}{a^{-m}} = a^m$$

3.

$$a^0 = 1 \qquad (a \in \mathbb{R}, \ a \neq 0)$$

1.2 Rational Exponents:

1.

$$\sqrt[n]{a} \ = \ r \qquad (a \ > \ 0, \ n \in \mathbb{N}, \ n \geqslant 2, \ r \ > \ 0), \iff r^n \ = \ a$$

2.

$$a^{\frac{1}{n}} = \sqrt[n]{a}; \qquad (a > 0, n \geqslant 2, n \in \mathbb{N})$$

3.

$$a^{\frac{-1}{n}} = \sqrt[n]{a^{-1}}; \qquad (a > 0, n > 0, n \in \mathbb{N})$$

4.

$$a^{\frac{m}{n}} = \sqrt[n]{a^m}; \qquad (a > 0; m, n \in \mathbb{Z}, n \geqslant 2)$$

2 Law

2.1 Exponents

1.

$$a^m \times a^n = a^{m+n}$$
 $(m, n \in \mathbb{N})$
 $a^m \times a^n = a^{m+n}$ $(m, n \in \mathbb{Z}; a \neq 0, if m \text{ or } n < 0)$

2.

$$\frac{a^m}{a^n} = a^{m-n} \qquad (m, \ n \in \mathbb{Z}; \ a \in \mathbb{R}; \ a \neq 0)$$

3.

$$(ab)^m = a^m b^m \qquad (m \in \mathbb{Z})$$

4.

$$(a^m)^n = a^{mn} \qquad (m, n \in \mathbb{Z})$$

2.2 Rational Exponents

1.

$$a^r \times a^t = a^{r+t} \qquad (a > 0; \quad r, \ t \in \mathbb{Q})$$

2.

$$\frac{a^r}{a^t} = a^{r-t} \qquad (a > 0; \quad r, \ t \in \mathbb{Q})$$

3.

$$(a^t)^r = a^{tr} \qquad (a > 0, \quad t, \ r \in \mathbb{Q})$$

4.

$$(ab)^t = a^t b^t; \quad \left(\frac{a}{b}\right)^t = \frac{a^t}{b^t}; \quad (a, b > 0, t \in \mathbb{Q})$$

and

$$a^t b^t = (ab)^t$$
 and $\frac{a^t}{b^t} = \left(\frac{a}{b}\right)^t$

2.3 Distributive law

$$a(b + c) = ab + ac$$

 $(a + b)(c + d) = (a + b)c + (a + b)d$
 $= ac + bc + ad + bd$
 $A^{2} - B^{2} = (A - B)(A + B)$

2.4 Commutative law

$$ab = ba$$

3 Properties

3.1 Addition

$$0 + a = a$$

$$\frac{a}{b} + \frac{c}{b} = \frac{a + c}{b} \qquad (b \neq 0)$$

$$\frac{a}{b} - \frac{c}{b} = \frac{a - c}{b} \qquad (b \neq 0)$$

3.2 Multiplication

$$0 \times a = 0$$

$$\frac{0}{a} = 0 \times \frac{1}{a} = 0$$

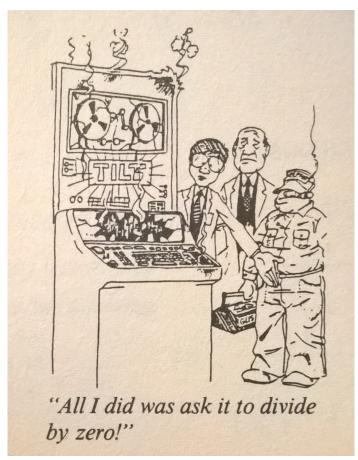
$$1 \times a = a$$

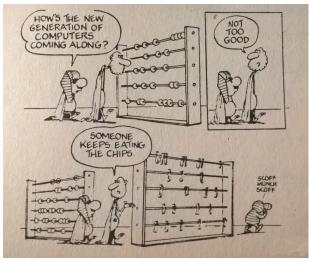
$$\frac{a}{b} \times \frac{c}{d} = \frac{ac}{bd} \quad (b \neq 0; d \neq 0)$$

3.3 Division

$$\frac{a}{0} = undefined$$

$$\frac{p}{q} \div \frac{r}{s} = \frac{p}{q} \times \frac{s}{r} = \frac{ps}{qr} \qquad (q \neq 0; r \neq 0; s \neq 0)$$





4 Examples



$$\sqrt{a^2} = a \qquad (a > 0) \qquad \qquad \sqrt{a^n} = a^{\frac{n}{2}}$$

$$\sqrt{\frac{1}{a}} = \frac{1}{\sqrt{a}}$$

$$a^{\frac{m}{1}} = a^m \qquad \frac{a^m}{a^n} = a^{m-n}$$

$$\frac{a \angle \alpha^{\circ} \ b \angle \beta^{\circ}}{c \angle \gamma^{\circ}} \ = \ \frac{a \times b}{c} \quad \angle \left(\alpha^{\circ} + \beta^{\circ} - \gamma^{\circ}\right)$$

If
$$a \cdot b = 0$$
, then $a = 0$ or $b = 0$

Square Property

$$Z = \sqrt{a^2 + a^2}$$

$$Z = \sqrt{2} a^2$$

$$Z = \sqrt{2} \sqrt{a^2}$$

$$Z = \sqrt{2} a$$

$$a \angle \alpha + b \angle \beta = \sqrt{(a \sin \alpha + b \sin \beta)^2 + (a \cos \alpha + b \cos \beta)^2}$$

and

$$\angle \arctan(\frac{(a \sin \alpha + b \sin \beta)}{(a \cos \alpha + b \cos \beta)})$$

 $y'(x) = e^{4x+5}$ = $4 e^{4x+5}$

$$\lim_{s\to 0} GH(s) = \lim_{s\to 0} 7 \frac{4+3s}{5+2s+6s^2}$$

$$= \lim_{s\to 0} 7 \frac{4(1+\frac{3}{4}s)}{5(1+\frac{2}{5}s+\frac{6}{5}s^2)}$$

$$= 7 \frac{4}{5}$$

Deniratives made casej.

$$y = \cos^3(\operatorname{sen}(x^2 + x))$$

$$y' = z^3$$

$$x = \cos(\operatorname{sen}(x^2 + x))$$

$$x = \operatorname{sen}(x^2 + x)$$

$$x$$

5 Methods

HCF - highest common factor (pôr variável em evidência)

CF - Common factors

Factorisation

LCD or LCM - Lowest common denominator or lowest common multiple