

$$\text{div } \vec{E} = \vec{\nabla} \cdot \vec{E} = \frac{\partial E_x}{\partial x} + \frac{\partial E_y}{\partial y} + \frac{\partial E_z}{\partial z}$$

$$E_x = E_{x_m} e^{i(\omega t - k_x x - k_y y - k_z z)}, E_y = \dots, E_z = \dots$$

$$\frac{\partial E_x}{\partial x} = E_x (-i k_x) \quad \frac{\partial E_y}{\partial y} = E_y (-i k_y) \quad \frac{\partial E_z}{\partial z} = E_z (-i k_z)$$

$$\text{div } \vec{E} = -i E_x k_x - i E_y k_y - i E_z k_z = -i \vec{k} \cdot \vec{E}$$

$$\begin{aligned} \frac{\partial \vec{E}}{\partial t} &= \frac{\partial}{\partial t} \left[E_{x_m} e^{i(\omega t - \vec{k} \cdot \vec{r})} \right] \vec{e}_x + \frac{\partial}{\partial t} \left[E_{y_m} e^{i(\omega t - \vec{k} \cdot \vec{r})} \right] \vec{e}_y + \frac{\partial}{\partial t} \left[E_{z_m} e^{i(\omega t - \vec{k} \cdot \vec{r})} \right] \vec{e}_z \\ &= i \omega E_x \vec{e}_x + i \omega E_y \vec{e}_y + i \omega E_z \vec{e}_z = i \omega \vec{E} \end{aligned}$$

$$\text{rot } \vec{E} = \left(\frac{\partial E_z}{\partial y} - \frac{\partial E_y}{\partial z} \right) \vec{e}_x + \left(\frac{\partial E_x}{\partial z} - \frac{\partial E_z}{\partial x} \right) \vec{e}_y + \left(\frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} \right) \vec{e}_z$$

$$\frac{\partial E_z}{\partial y} = \frac{\partial}{\partial y} \left[E_{z_m} e^{i(\omega t - k_x x - k_y y - k_z z)} \right] = E_z (-i k_y)$$

$$= -i \vec{k} \times \vec{E}$$