### **TimeSeries**

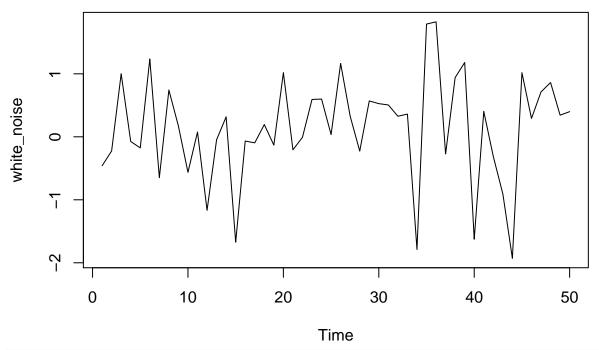
#### Sergio Solano

9 de marzo de 2017

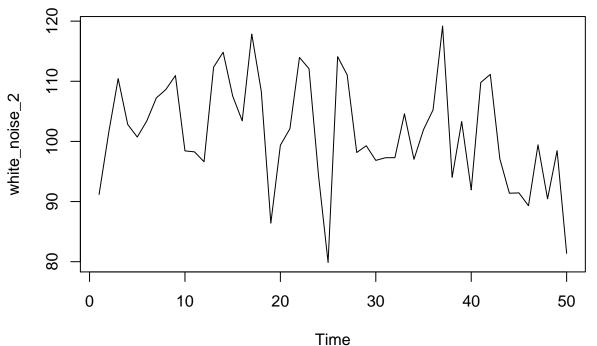
#### Pruebas series de tiempo de Time Series Analysis and its applications

```
# Plot AirPassengers
plot(AirPassengers)
     900
     500
AirPassengers
     400
     300
     200
                 1950
                            1952
                                        1954
                                                    1956
                                                               1958
                                                                           1960
                                             Time
# View the start and end dates of AirPassengers
start(AirPassengers)
## [1] 1949
               1
end(AirPassengers)
## [1] 1960
              12
# Use time(), deltat(), frequency(), and cycle() with AirPassengers
time(AirPassengers)
##
             Jan
                      Feb
                                Mar
                                         Apr
                                                  May
## 1949 1949.000 1949.083 1949.167 1949.250 1949.333 1949.417 1949.500
## 1950 1950.000 1950.083 1950.167 1950.250 1950.333 1950.417 1950.500
## 1951 1951.000 1951.083 1951.167 1951.250 1951.333 1951.417 1951.500
## 1952 1952.000 1952.083 1952.167 1952.250 1952.333 1952.417 1952.500
## 1953 1953.000 1953.083 1953.167 1953.250 1953.333 1953.417 1953.500
## 1954 1954.000 1954.083 1954.167 1954.250 1954.333 1954.417 1954.500
## 1955 1955.000 1955.083 1955.167 1955.250 1955.333 1955.417 1955.500
## 1956 1956.000 1956.083 1956.167 1956.250 1956.333 1956.417 1956.500
## 1957 1957.000 1957.083 1957.167 1957.250 1957.333 1957.417 1957.500
```

```
## 1958 1958.000 1958.083 1958.167 1958.250 1958.333 1958.417 1958.500
## 1959 1959.000 1959.083 1959.167 1959.250 1959.333 1959.417 1959.500
## 1960 1960.000 1960.083 1960.167 1960.250 1960.333 1960.417 1960.500
##
                     Sep
                               Oct
                                        Nov
             Aug
                                                 Dec
## 1949 1949.583 1949.667 1949.750 1949.833 1949.917
## 1950 1950.583 1950.667 1950.750 1950.833 1950.917
## 1951 1951.583 1951.667 1951.750 1951.833 1951.917
## 1952 1952.583 1952.667 1952.750 1952.833 1952.917
## 1953 1953.583 1953.667 1953.750 1953.833 1953.917
## 1954 1954.583 1954.667 1954.750 1954.833 1954.917
## 1955 1955.583 1955.667 1955.750 1955.833 1955.917
## 1956 1956.583 1956.667 1956.750 1956.833 1956.917
## 1957 1957.583 1957.667 1957.750 1957.833 1957.917
## 1958 1958.583 1958.667 1958.750 1958.833 1958.917
## 1959 1959.583 1959.667 1959.750 1959.833 1959.917
## 1960 1960.583 1960.667 1960.750 1960.833 1960.917
deltat(AirPassengers)
## [1] 0.08333333
frequency(AirPassengers)
## [1] 12
cycle(AirPassengers)
        Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec
## 1949
              2
                  3
                                  7
                                          9 10
                                                 11
                                                     12
          1
                      4
                          5
                              6
                                      8
## 1950
              2
                  3
                      4
                          5
                              6
                                  7
                                      8
                                          9
                                            10
                                                11
                                                    12
         1
## 1951
              2
                 3
                     4
                          5
                                  7
                                          9
                                                     12
         1
                              6
                                      8
                                            10
                                                 11
## 1952
              2
                 3
                     4
                          5
                                 7
         1
                              6
                                      8
                                          9
                                             10
                                                 11
                                                     12
## 1953
              2
                 3
                     4
                          5
                              6
                                 7
                                      8
                                          9 10
                                                11 12
        1
## 1954
              2
                 3
                     4
                          5
                              6
                                 7
                                      8
                                          9 10 11 12
         1
## 1955
              2
                 3
                                 7
                                                     12
         1
                     4
                          5
                              6
                                     8
                                          9 10
                                                11
## 1956
              2
                 3 4
                         5
                              6
                                7
                                     8
                                         9 10 11
                                                     12
         1
## 1957
              2
                 3 4
                          5
                                7
                                     8
                                         9 10 11 12
## 1958
              2
                 3
                     4
                          5
                              6
                                 7
                                     8
                                         9 10 11 12
         1
## 1959
              2
                  3
                      4
                          5
                              6
                                  7
                                      8
                                          9
                                             10
                                                 11
                                                     12
                          5
## 1960
              2
                  3
                      4
                              6
                                 7
                                      8
                                          9 10
                                                11
                                                    12
# Simulate a WN model with list(order = c(0, 0, 0))
white_noise <- arima.sim(model = list(order = c(0,0,0)), n = 50)
# Plot your white_noise data
ts.plot(white_noise)
```



```
# Simulate from the WN model with: mean = 100, sd = 10
white_noise_2 <- arima.sim(model = list(order = c(0,0,0)), n = 50, mean = 100, sd = 10)
# Plot your white_noise_2 data
ts.plot(white_noise_2)</pre>
```

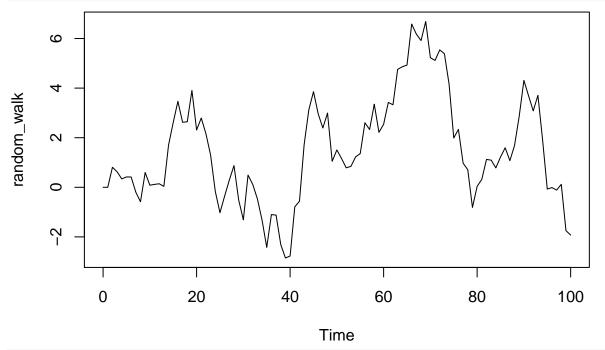


cambios en una serie de tiempo de Random Walk siguen un comportamiento de White noise.

```
# Generate a RW model using arima.sim
random_walk <- arima.sim(model = list(order = c(0, 1, 0)) , n = 100)
# Plot random_walk</pre>
```

 $\operatorname{Los}$ 

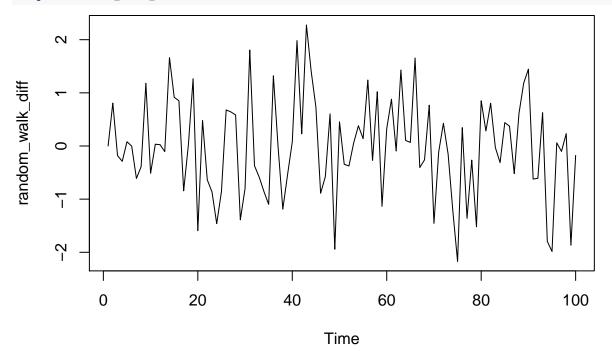
#### ts.plot (random\_walk)



# Calculate the first difference series
random\_walk\_diff <- diff(random\_walk)
# Plot random\_walk\_diff</pre>

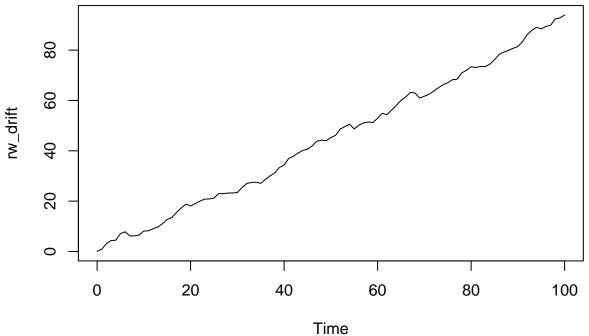
\_ \_ \_ \*\*

ts.plot(random\_walk\_diff)



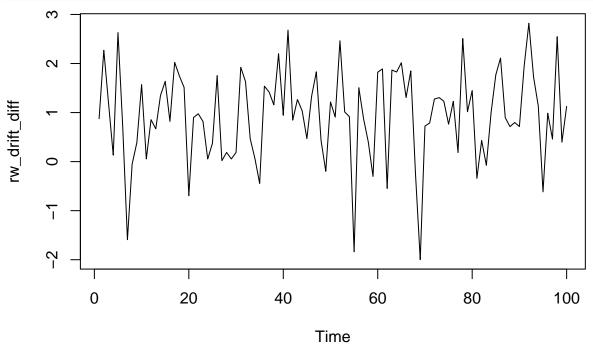
# RANDOM WALK WITH DRIFT

```
# Generate a RW model with a drift uing arima.sim
rw_drift <- arima.sim(model = list(order = c(0, 1, 0)), n = 100, mean = 1)
# Plot rw_drift
ts.plot(rw_drift)</pre>
```



```
# Calculate the first difference series
rw_drift_diff <- diff(rw_drift)

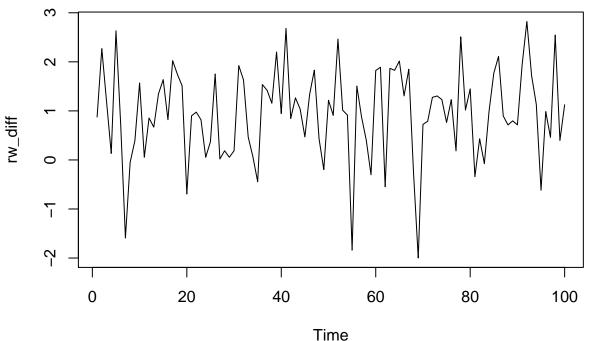
# Plot rw_drift_diff
ts.plot(rw_drift_diff)</pre>
```



```
random_walk <- rw_drift

# Difference your random_walk data
rw_diff <- diff(random_walk)

# Plot rw_diff
plot.ts(rw_diff)</pre>
```

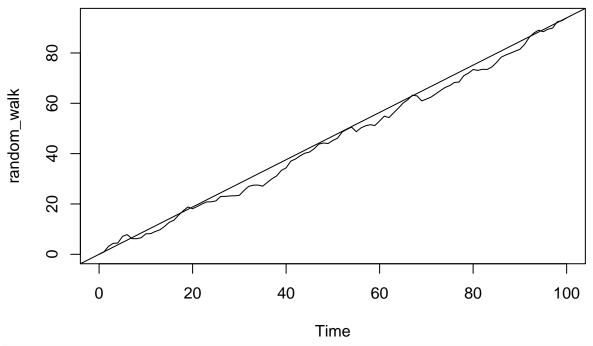


```
# Now fit the WN model to the differenced data
model_wn <- arima(rw_diff,order = c(0, 0, 0))

# Store the value of the estimated time trend (intercept)
int_wn <- model_wn$coef

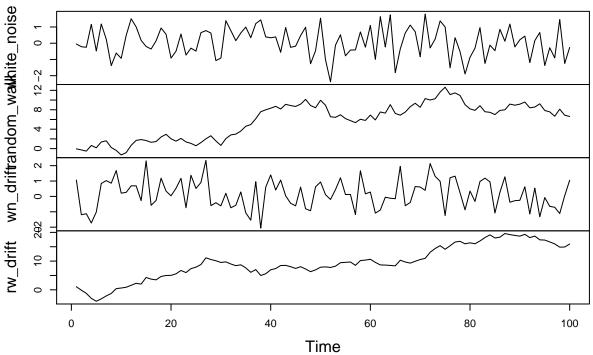
# Plot the original random_walk data
ts.plot(random_walk)

# Use abline(0, ...) to add time trend to the figure
abline(0,int_wn)</pre>
```



```
# RANDOM WALK CON Y SIN DRIFT (Estationarity)
#
# The white noise (WN) and random walk (RW) models are very closely related. However, only the RW is al
#
# Recall that if we start with a mean zero WN process and compute its running or cumulative sum, the re
# Use arima.sim() to generate WN data
white_noise <- arima.sim(model = list(order = c(0, 0, 0)), n = 100)
# Use cumsum() to convert your WN data to RW
random_walk <- cumsum(white_noise)
# Use arima.sim() to generate WN drift data
wn_drift <- arima.sim(model = list(order = c(0, 0, 0)), mean=0.4, n = 100)
# Use cumsum() to convert your WN drift data to RW
rw_drift <- cumsum(wn_drift)
# Plot all four data objects
plot.ts(cbind(white_noise, random_walk, wn_drift, rw_drift))</pre>
```

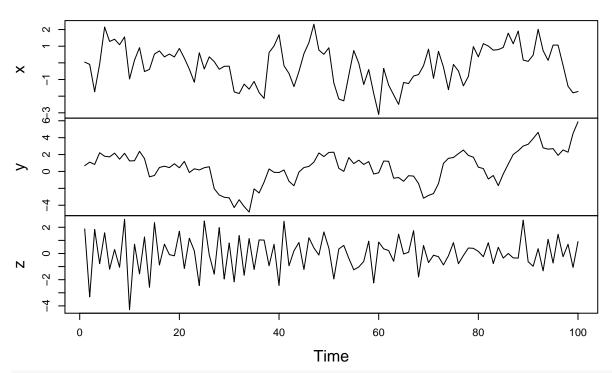
### cbind(white\_noise, random\_walk, wn\_drift, rw\_drift)



```
# # Generate means from eu_percentreturns
# colMeans(eu_percentreturns)
# # Use apply to calculate sample variance from eu_percentreturns
# apply(eu_percentreturns, MARGIN = 2, FUN = var)
# # Use apply to calculate standard deviation from eu_percentreturns
# apply(eu_percentreturns, MARGIN = 2, FUN = sd)
# # Display a histogram of percent returns for each index
\# par(mfrow = c(2,2))
# apply(eu_percentreturns, MARGIN = 2, FUN = hist, main = "", xlab = "Percentage Return")
# # Display normal quantile plots of percent returns for each index
\# par(mfrow = c(2,2))
# apply(eu_percentreturns, MARGIN = 2, FUN = qqnorm, main = "")
# qqline(eu_percentreturns)
# pairs(eu_stocks)
# MODELOS AUTOREGRESIVOS:
# Simulate an AR model with 0.5 slope
x \leftarrow arima.sim(model = list(ar = 0.5), n = 100)
# Simulate an AR model with 0.9 slope
y \leftarrow arima.sim(model = list(ar = 0.9), n = 100)
```

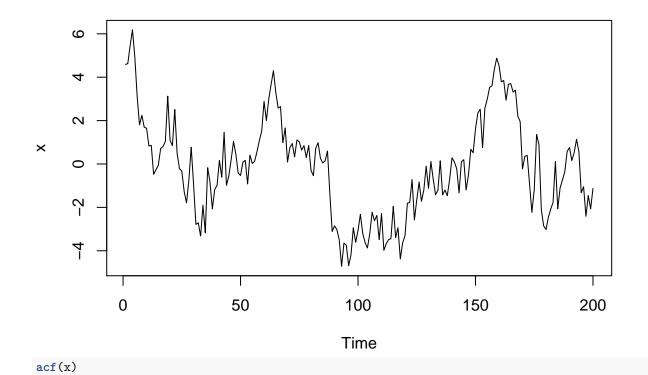
```
# Simulate an AR model with -0.75 slope
z <- arima.sim(model = list(ar = -0.75), n = 100)
# Plot your simulated data
plot.ts(cbind(x, y, z))</pre>
```

## cbind(x, y, z)

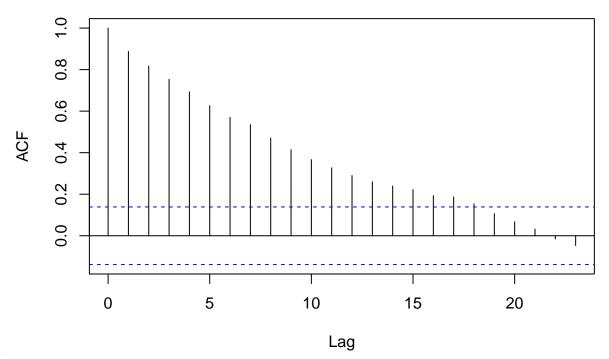


###### COMPARAR MODELOS AR con RandomWalks

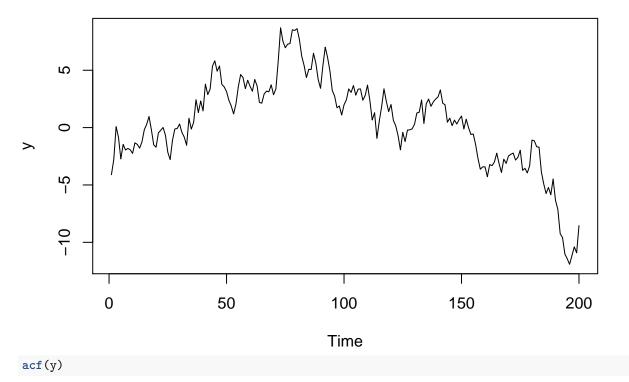
```
# Simulate and plot AR model with slope 0.9
x <- arima.sim(model = list(ar = 0.9), n = 200)
ts.plot(x)</pre>
```



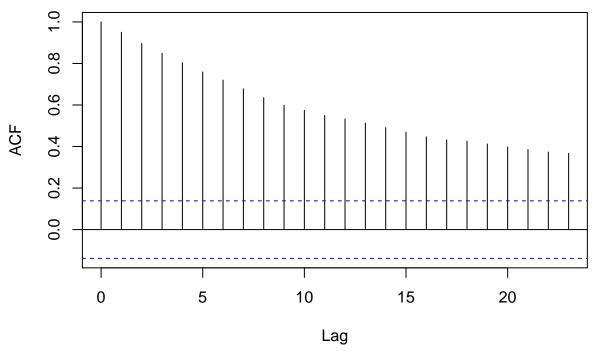
## Series x



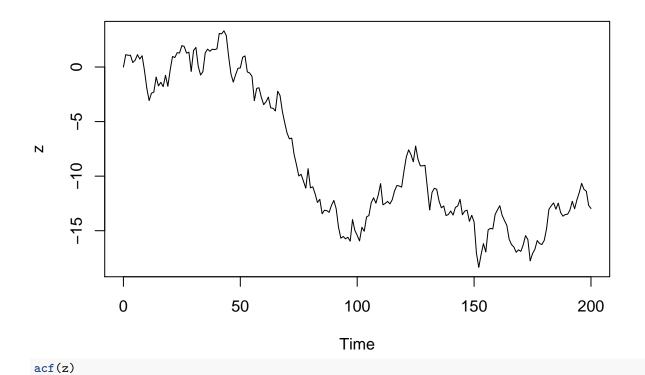
# Simulate and plot AR model with slope 0.98
y <- arima.sim(model = list(ar = 0.98), n = 200)
ts.plot(y)</pre>



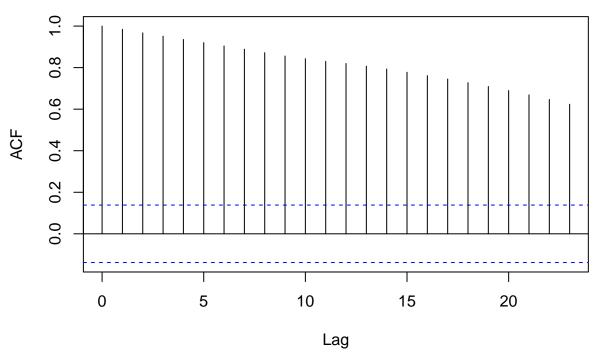
## Series y



```
# Simulate and plot RW model
z <- arima.sim(model = list(order = c(0, 1, 0)), n = 200)
ts.plot(z)</pre>
```



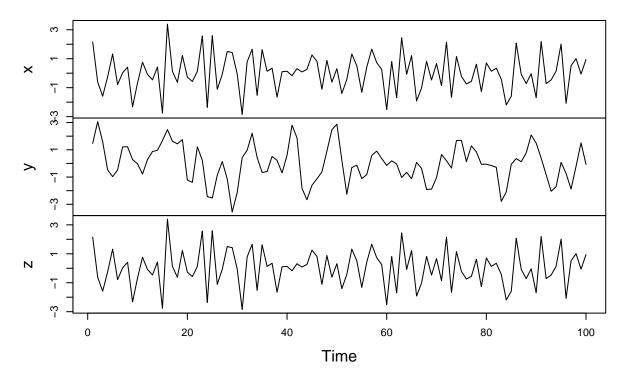
## Series z



```
# # AJUSTAR UN AR
# # Fit an AR model to Nile
# AR_fit <-arima(Nile, order = c(1,0,0))
# print(AR_fit)
#
# # Use predict() to make a 1-step forecast</pre>
```

```
# predict_AR <- predict(AR_fit)</pre>
# # Obtain the 1-step forecast using $pred[1]
# predict_AR$pred[1]
# # Use predict to make 1-step through 10-step forecasts
# predict(AR_fit, n.ahead = 10)
# # Run to plot the Nile series plus the forecast and 95% prediction intervals
\# ts.plot(Nile, xlim = c(1871, 1980))
# AR_forecast <- predict(AR_fit, n.ahead = 10)$pred
\# AR\_forecast\_se \leftarrow predict(AR\_fit, n.ahead = 10)$se
# points(AR_forecast, type = "l", col = 2)
# points(AR_forecast - 2*AR_forecast_se, type = "l", col = 2, lty = 2)
\# points(AR_forecast + 2*AR_forecast_se, type = "l", col = 2, lty = 2)
# # AJUSTAR UN MA
# Generate MA model with slope 0.5
x \leftarrow arima.sim(model = list(ma = 0.5), n = 100)
# Generate MA model with slope 0.9
y \leftarrow x \leftarrow arima.sim(model = list(ma = 0.9), n = 100)
# Generate MA model with slope -0.5
z \leftarrow x \leftarrow arima.sim(model = list(ma = -0.5), n = 100)
# Plot all three models together
plot.ts(cbind(x, y, z))
```

## cbind(x, y, z)



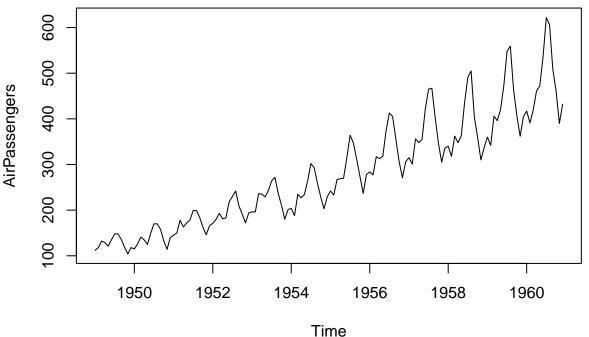
```
# # # Ajustando un MA
#
# # Make a 1-step forecast based on MA
# predict_MA <- predict(MA, n.ahead = 1)
#
# # Obtain the 1-step forecast using $pred[1]
# predict_MA$pred[1]
#
# # Make a 1-step through 10-step forecast based on MA
# predict(MA, n.ahead = 10)
#
# # Plot the Nile series plus the forecast and 95% prediction intervals
# ts.plot(Nile, xlim = c(1871, 1980))
# MA_forecasts <- predict(MA, n.ahead = 10)$pred
# MA_forecast_se <- predict(MA, n.ahead = 10)$se
# points(MA_forecasts, type = "l", col = 2)
# points(MA_forecasts - 2*MA_forecast_se, type = "l", col = 2, lty = 2)
# points(MA_forecasts + 2*MA_forecast_se, type = "l", col = 2, lty = 2)
# points(MA_forecasts + 2*MA_forecast_se, type = "l", col = 2, lty = 2)</pre>
```

#### Pruebas series de tiempo de Time Series Analysis and its applications course

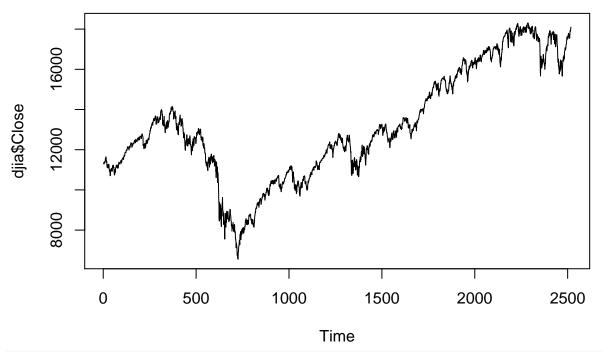
```
# # R Arima base

# View a detailed description of AirPassengers
help(AirPassengers)

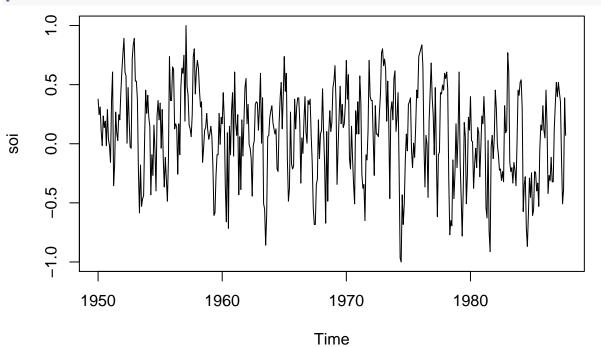
# Plot AirPassengers
ts.plot(AirPassengers)
```



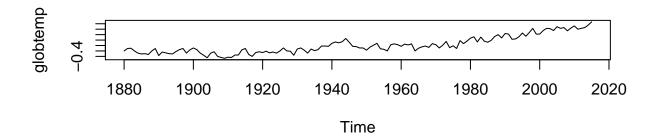
```
# Plot the DJIA daily closings
ts.plot(djia$Close)
```

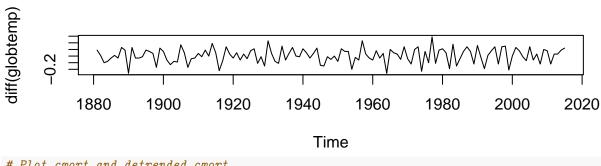


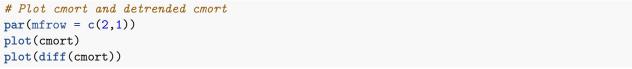
# Plot the Southern Oscillation Index
plot(soi)

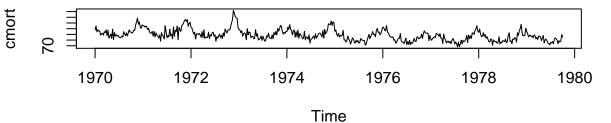


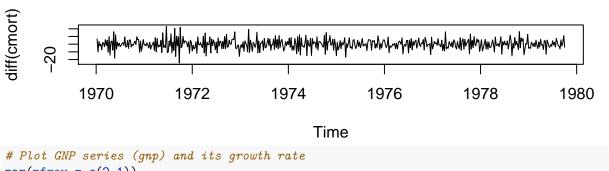
```
# Plot globtemp and detrended globtemp
par(mfrow = c(2,1))
plot(globtemp)
plot(diff(globtemp))
```



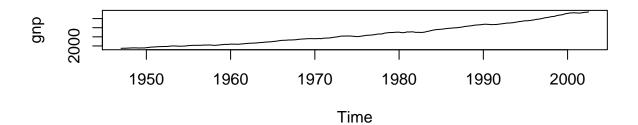


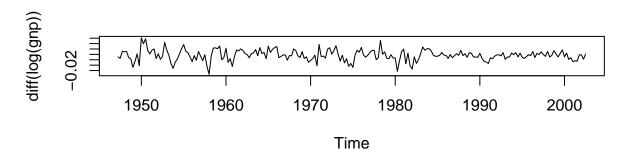






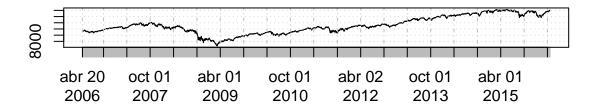
```
# Plot GNP series (gnp) and its growth rate
par(mfrow = c(2,1))
plot(gnp)
plot(diff(log(gnp)))
```



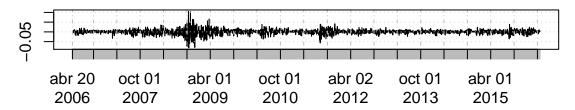


# Plot DJIA closings (djia\$Close) and its returns
par(mfrow = c(2,1))
plot(djia\$Close)
plot(diff(log(djia\$Close)))

## djia\$Close



## diff(log(djia\$Close))



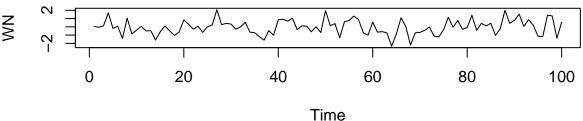
##SIMULAR MA & AR

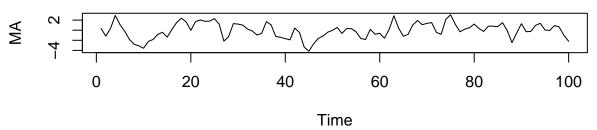
# Generate and plot white noise
WN <- arima.sim(model=list(order=c(0,0,0)),n=100)
plot(WN)</pre>

```
# Generate and plot an MA(1) with parameter .9

MA <- arima.sim(model=list(order=c(0,0,1), ma = 0.9),n=100)

plot(MA)
```



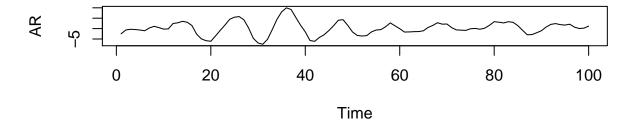


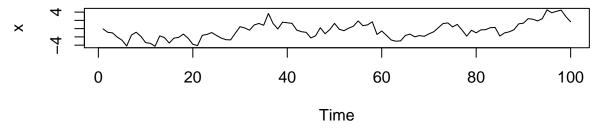
```
# Generate and plot an AR(2) with parameters 1.5 and -.75
AR <- arima.sim(model=list(order=c(2,0,0), ar =c(1.5,-0.75)),n=100)
plot(AR)

# # SIMULAR Y AJUSTAR AR

# Generate 100 observations from the AR(1) model
x <- arima.sim(model = list(order = c(1, 0, 0), ar = .9), n = 100)

# Plot the generated data
plot(x)</pre>
```

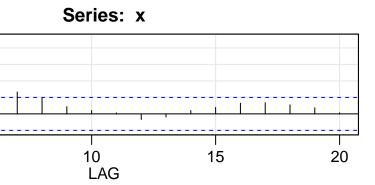




# Plot the sample P/ACF pair acf2(x)

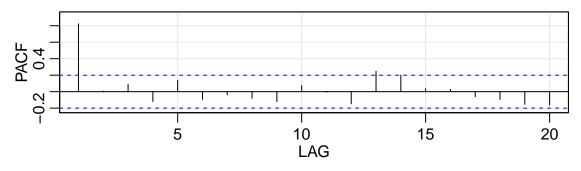
5

ACF 0.4



15

20

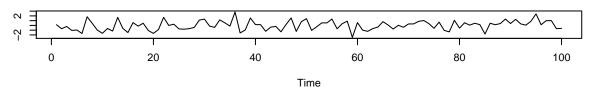


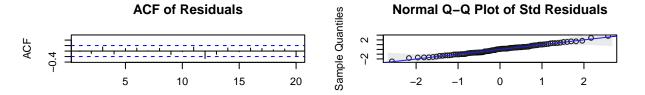
## ACF PACF [1,] 0.82 0.82 [2,] 0.68 0.01 0.59 0.09 [3,] ## [4,] 0.47 -0.12 [5,] 0.42 0.14

```
## [6,] 0.35 -0.09
## [7,] 0.27 -0.04
## [8,] 0.19 -0.08
## [9,] 0.09 -0.12
## [10,] 0.04 0.07
## [11,] 0.01 -0.01
## [12,] -0.07 -0.15
## [13,] -0.04 0.25
## [14,] 0.04 0.20
## [15,] 0.08 0.04
## [16,] 0.13 0.03
## [17,] 0.14 -0.06
## [18,] 0.11 -0.09
## [19,] 0.07 -0.15
## [20,] 0.01 -0.16
\# Fit an AR(1) to the data and examine the -table
sarima(x, 1, 0, 0)
## initial value 0.661628
        2 value 0.084199
## iter
## iter
       3 value 0.084066
        4 value 0.084032
## iter
## iter
       5 value 0.084014
## iter
       6 value 0.083974
        7 value 0.083969
## iter
## iter
        8 value 0.083967
## iter
        9 value 0.083965
## iter 10 value 0.083962
## iter 11 value 0.083962
## iter 12 value 0.083961
## iter 13 value 0.083961
## iter 14 value 0.083961
## iter 15 value 0.083961
## iter 15 value 0.083961
## iter 15 value 0.083961
## final value 0.083961
## converged
## initial value 0.084956
       2 value 0.084898
## iter
## iter
       3 value 0.084845
## iter
        4 value 0.084844
       5 value 0.084843
## iter
## iter
       6 value 0.084842
        7 value 0.084842
## iter
## iter
         8 value 0.084842
## iter
        9 value 0.084842
## iter 10 value 0.084842
## iter 10 value 0.084842
## iter 10 value 0.084842
## final value 0.084842
## converged
```

#### Model: (1,0,0) Standardized Residuals

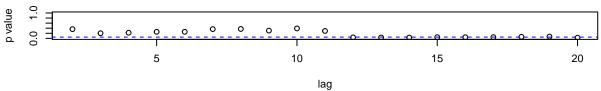
LAG





#### p values for Ljung-Box statistic

Theoretical Quantiles



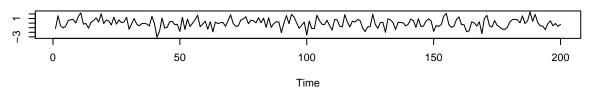
```
## $fit
##
## Call:
   stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D, d, q))
##
       Q), period = S), xreg = xmean, include.mean = FALSE, optim.control = list(trace = trc,
##
##
       REPORT = 1, reltol = tol))
##
## Coefficients:
##
            ar1
                   xmean
##
         0.8247
                 -0.3500
## s.e. 0.0550
                  0.5914
##
## sigma^2 estimated as 1.172: log likelihood = -150.38, aic = 306.76
##
## $degrees_of_freedom
## [1] 98
##
##
  $ttable
##
         Estimate
                      SE t.value p.value
           0.8247 0.0550 14.9926 0.0000
   xmean -0.3500 0.5914 -0.5918 0.5554
##
## $AIC
## [1] 1.198286
##
## $AICc
## [1] 1.220786
##
```

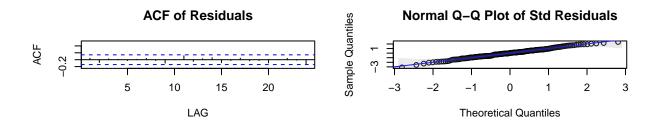
```
## $BIC
 ## [1] 0.2503895
  # # aJUSTAR MA(2)
  # astsa is preloaded
 x \leftarrow arima.sim(model = list(order = c(2, 0, 0), ar = c(1.5, -.75)), n = 200)
  \# Plot x
 plot(x)
 # Plot the sample P/ACF of x
 acf2(x)
                                                               150
              0
                              50
                                              100
                                                                                 200
                                              Time
                                       Series: x
ACF
0.5
    -0.5
                     5
                                                 15
                                                               20
                                   10
                                                                              25
                                           LAG
 PACF
5 0.5
    3
    9
                                   10
                                                 15
                      5
                                                                20
                                                                              25
                                           LAG
             ACF PACF
 ##
 ##
      [1,] 0.83 0.83
 ##
      [2,] 0.45 -0.72
     [3,] 0.05 0.01
     [4,] -0.27 -0.07
 ##
  ##
     [5,] -0.43 -0.01
     [6,] -0.43 0.00
 ##
 ##
     [7,] -0.32 -0.04
     [8,] -0.15 0.00
 ##
 ## [9,] 0.02 0.05
 ## [10,] 0.15 0.05
```

```
## [11,] 0.22 -0.03
## [12,] 0.22 -0.03
## [13,] 0.16 0.08
## [14,] 0.08 -0.06
## [15,] -0.01 0.02
## [16,] -0.07 0.04
## [17,] -0.10 -0.07
## [18,] -0.11 -0.06
## [19,] -0.11 0.02
## [20,] -0.10 -0.07
## [21,] -0.08 0.00
## [22,] -0.06 -0.09
## [23,] -0.05 -0.02
## [24,] -0.03 0.08
## [25,] 0.02 0.07
# Fit an AR(2) to the data and examine the t-table
sarima(x,2,0,0)
## initial value 0.941414
## iter
        2 value 0.785436
## iter 3 value 0.410362
## iter 4 value 0.254312
## iter 5 value -0.018321
## iter 6 value -0.033822
        7 value -0.060554
## iter
## iter
        8 value -0.062409
## iter
        9 value -0.063509
## iter 10 value -0.064166
## iter 11 value -0.064209
## iter 12 value -0.064209
## iter 13 value -0.064210
## iter 14 value -0.064210
## iter 14 value -0.064210
## iter 14 value -0.064210
## final value -0.064210
## converged
## initial value -0.052052
## iter 2 value -0.052099
## iter 3 value -0.052124
## iter
       4 value -0.052126
## iter
        5 value -0.052126
        6 value -0.052126
## iter
## iter
         6 value -0.052126
## iter
         6 value -0.052126
## final value -0.052126
```

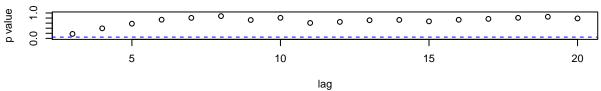
## converged

#### Model: (2,0,0) Standardized Residuals





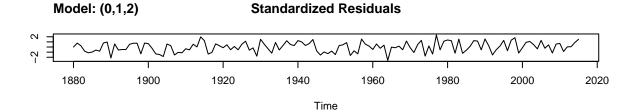
#### p values for Ljung-Box statistic

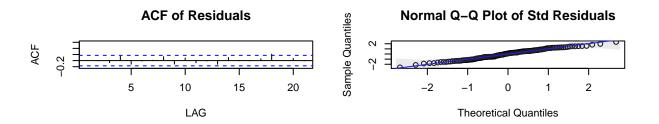


```
## $fit
##
## Call:
   stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D, q))
##
       Q), period = S), xreg = xmean, include.mean = FALSE, optim.control = list(trace = trc,
##
##
       REPORT = 1, reltol = tol))
##
   Coefficients:
##
##
            ar1
                     ar2
                            xmean
##
         1.4562
                 -0.7540
                          -0.0229
## s.e. 0.0463
                  0.0461
                           0.2240
##
## sigma^2 estimated as 0.8883: log likelihood = -273.36, aic = 554.73
##
## $degrees_of_freedom
##
  [1] 197
##
##
   $ttable
##
                      SE t.value p.value
         Estimate
## ar1
           1.4562 0.0463 31.4225 0.0000
          -0.7540 0.0461 -16.3540 0.0000
## xmean -0.0229 0.2240 -0.1022 0.9187
##
## $AIC
## [1] 0.911498
##
## $AICc
## [1] 0.9225237
```

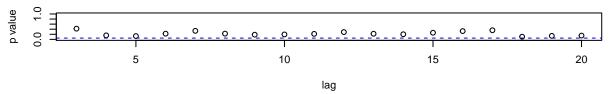
```
##
## $BIC
## [1] -0.03902719
# # # SIMULANDO ARIMAS
# Fit an ARIMA(0,1,2) to globtemp and check the fit
sarima(globtemp, 0, 1, 2)
## initial value -2.220513
## iter 2 value -2.294887
## iter 3 value -2.307682
## iter 4 value -2.309170
## iter 5 value -2.310360
## iter 6 value -2.311251
## iter 7 value -2.311636
## iter 8 value -2.311648
## iter 9 value -2.311649
## iter 9 value -2.311649
## iter 9 value -2.311649
## final value -2.311649
## converged
## initial value -2.310187
## iter 2 value -2.310197
## iter 3 value -2.310199
## iter 4 value -2.310201
## iter 5 value -2.310202
## iter 5 value -2.310202
## iter 5 value -2.310202
## final value -2.310202
```

## converged



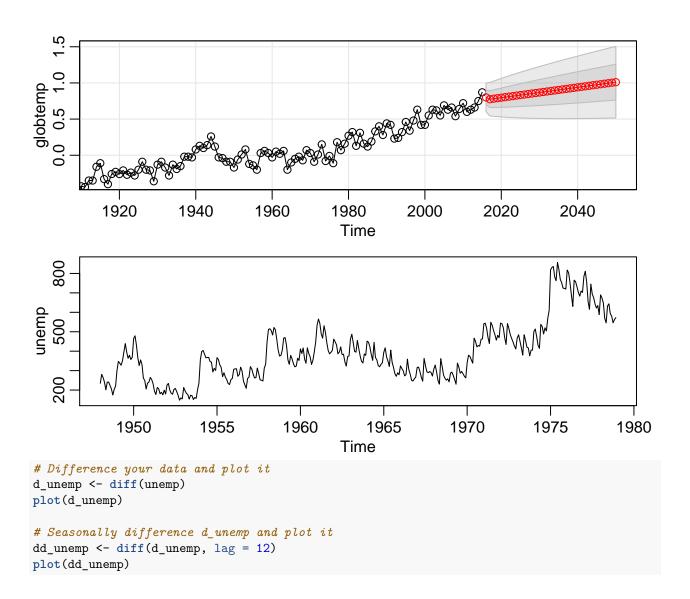


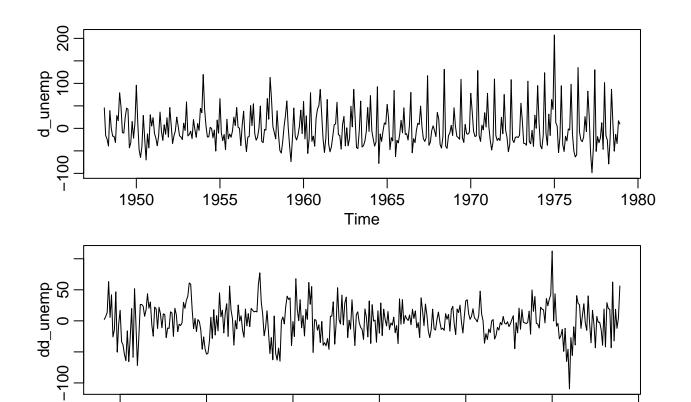
#### p values for Ljung-Box statistic



```
## $fit
##
## Call:
   stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D, q))
##
       Q), period = S), xreg = constant, optim.control = list(trace = trc, REPORT = 1,
##
       reltol = tol))
##
   Coefficients:
##
##
             ma1
                           constant
                      ma2
##
         -0.3984
                  -0.2173
                              0.0072
         0.0808
                   0.0768
                              0.0033
##
  s.e.
##
## sigma^2 estimated as 0.00982: log likelihood = 120.32, aic = -232.64
##
## $degrees_of_freedom
##
  [1] 133
##
##
  $ttable
##
                         SE t.value p.value
            Estimate
## ma1
             -0.3984 0.0808 -4.9313 0.0000
##
             -0.2173 0.0768 -2.8303 0.0054
              0.0072 0.0033 2.1463 0.0337
  constant
##
## $AIC
## [1] -3.579224
##
## $AICc
## [1] -3.562273
```

```
##
## $BIC
## [1] -4.514974
# Forecast data 35 years into the future
sarima.for (globtemp, n.ahead = 35, p = 0, d = 1, q = 2)
## $pred
## Time Series:
## Start = 2016
## End = 2050
## Frequency = 1
## [1] 0.7995567 0.7745381 0.7816919 0.7888457 0.7959996 0.8031534 0.8103072
## [8] 0.8174611 0.8246149 0.8317688 0.8389226 0.8460764 0.8532303 0.8603841
## [15] 0.8675379 0.8746918 0.8818456 0.8889995 0.8961533 0.9033071 0.9104610
## [22] 0.9176148 0.9247687 0.9319225 0.9390763 0.9462302 0.9533840 0.9605378
## [29] 0.9676917 0.9748455 0.9819994 0.9891532 0.9963070 1.0034609 1.0106147
##
## $se
## Time Series:
## Start = 2016
## End = 2050
## Frequency = 1
## [1] 0.09909556 0.11564576 0.12175580 0.12757353 0.13313729 0.13847769
## [7] 0.14361964 0.14858376 0.15338730 0.15804492 0.16256915 0.16697084
## [13] 0.17125943 0.17544322 0.17952954 0.18352490 0.18743511 0.19126540
## [19] 0.19502047 0.19870459 0.20232164 0.20587515 0.20936836 0.21280424
## [25] 0.21618551 0.21951471 0.22279416 0.22602604 0.22921235 0.23235497
## [31] 0.23545565 0.23851603 0.24153763 0.24452190 0.24747019
### SERIES DE TIEMPO ESTACIONALES
# Plot unemp
plot(unemp)
```

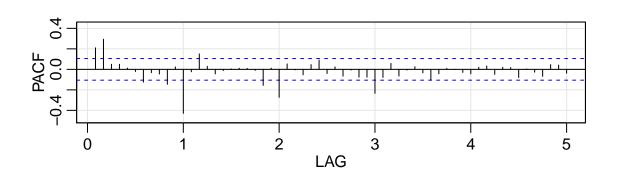




Time

# Plot P/ACF pair of fully differenced data to lag 60
dd\_unemp <- diff(diff(unemp), lag = 12)
acf2(dd\_unemp, max.lag = 60)</pre>





```
ACF PACF
    [1,] 0.21 0.21
##
    [2,] 0.33 0.29
    [3,] 0.15 0.05
##
##
    [4,] 0.17 0.05
##
   [5,] 0.10 0.01
##
   [6,] 0.06 -0.02
   [7,] -0.06 -0.12
##
##
   [8,] -0.02 -0.03
##
   [9,] -0.09 -0.05
## [10,] -0.17 -0.15
## [11,] -0.08 0.02
## [12,] -0.48 -0.43
## [13,] -0.18 -0.02
## [14,] -0.16 0.15
## [15,] -0.11 0.03
## [16,] -0.15 -0.04
## [17,] -0.09 -0.01
## [18,] -0.09 0.00
## [19,] 0.03 0.01
## [20,] -0.01 0.01
## [21,] 0.02 -0.01
## [22,] -0.02 -0.16
## [23,] 0.01 0.01
## [24,] -0.02 -0.27
## [25,] 0.09 0.05
## [26,] -0.05 -0.01
## [27,] -0.01 -0.05
## [28,] 0.03 0.05
## [29,] 0.08 0.09
## [30,] 0.01 -0.04
## [31,] 0.03 0.02
## [32,] -0.05 -0.07
## [33,] 0.01 -0.01
## [34,] 0.02 -0.08
## [35,] -0.06 -0.08
## [36,] -0.02 -0.23
## [37,] -0.12 -0.08
## [38,] 0.01 0.06
## [39,] -0.03 -0.07
## [40,] -0.03 -0.01
## [41,] -0.10 0.03
## [42,] -0.02 -0.03
## [43,] -0.13 -0.11
## [44,] 0.00 -0.04
## [45,] -0.06 0.01
## [46,] 0.01 0.00
## [47,]
         0.02 -0.03
## [48,]
         0.11 - 0.04
## [49,]
         0.13 0.02
## [50,]
         0.10 0.03
## [51,]
         0.07 - 0.05
## [52,] 0.10 0.02
## [53,] 0.12 0.02
```

```
## [54,] 0.06 -0.08
## [55,] 0.14 0.00
## [56,] 0.05 -0.03
## [57,] 0.04 -0.07
## [58,] 0.04 0.05
## [59,] 0.07 0.04
## [60,] -0.03 -0.04
# Fit an appropriate model
sarima(unemp,2,1,0,0,1,1, S=12)
## initial value 3.340809
## iter 2 value 3.105512
## iter 3 value 3.086631
## iter 4 value 3.079778
## iter 5 value 3.069447
## iter 6 value 3.067659
## iter 7 value 3.067426
## iter 8 value 3.067418
## iter 8 value 3.067418
## final value 3.067418
## converged
## initial value 3.065481
## iter 2 value 3.065478
## iter 3 value 3.065477
## iter 3 value 3.065477
## iter 3 value 3.065477
## final value 3.065477
## converged
```

```
Model: (2,1,0) (0,1,1) [12]
                                          Standardized Residuals
   4
   ^{\circ}
   0
   7
             1950
                            1955
                                          1960
                                                         1965
                                                                        1970
                                                                                      1975
                                                                                                     1980
                                                    Time
                   ACF of Residuals
                                                               Normal Q-Q Plot of Std Residuals
   0.4
                                                     Sample Quantiles -2 0 2 4
ACF
0.2
   0.0
                                  2.0
                                                                                              2
     0.0
            0.5
                   1.0
                          1.5
                                         2.5
                                                3.0
                                                           -3
                                                                         -1
                                                                                0
                                                                                                     3
                                                                        Theoretical Quantiles
                          LAG
                                     p values for Ljung-Box statistic
  0.8
p value
0.4
   0.0
                                                                    25
            5
                         10
                                       15
                                                     20
                                                                                  30
                                                                                                35
                                                     lag
## $fit
##
## Call:
    stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D,
         Q), period = S), include.mean = !no.constant, optim.control = list(trace = trc,
##
##
        REPORT = 1, reltol = tol))
##
##
    Coefficients:
##
               ar1
                        ar2
                                 sma1
##
           0.1351
                    0.2464
                              -0.6953
    s.e. 0.0513
                    0.0515
                               0.0381
##
## sigma^2 estimated as 449.6: log likelihood = -1609.91, log likelihood = -1609.91, aic = 3227.81
##
## $degrees_of_freedom
    [1] 369
##
##
## $ttable
##
          Estimate
                         SE t.value p.value
            0.1351 0.0513
                               2.6326 0.0088
## ar1
            0.2464 0.0515
                               4.7795
                                       0.0000
##
    ar2
          -0.6953 0.0381 -18.2362 0.0000
##
    sma1
##
## $AIC
##
    [1] 7.12457
##
```

```
## $AICc
## [1] 7.130239
##
## $BIC
## [1] 6.156174
# Plot differenced chicken
plot(diff(chicken))
# Plot P/ACF pair of differenced data to lag 60
acf2(diff(chicken), max.lag = 60)
diff(chicken)
   7
                         2005
                                                    2010
                                                                               2015
                               Time
Series: diff(chicken)
   0.8
ACF
0.2
   -0.4
                                     2
                                                    3
                       1
                                                                   4
        0
                                                                                 5
                                           LAG
   0.8
PACF
0.2
   ġ.
                                     2
        0
                       1
                                                    3
                                                                   4
                                                                                 5
                                           LAG
            ACF PACF
##
##
     [1,] 0.72 0.72
##
     [2,]
          0.39 -0.29
     [3,] 0.09 -0.14
##
##
    [4,] -0.07 0.03
    [5,] -0.16 -0.10
##
##
    [6,] -0.20 -0.06
```

```
[7,] -0.27 -0.19
##
   [8,] -0.23 0.12
  [9,] -0.11 0.10
## [10,] 0.09 0.16
## [11,] 0.26 0.09
## [12,] 0.33 0.00
## [13,] 0.20 -0.22
## [14,] 0.07 0.03
## [15,] -0.03 0.03
## [16,] -0.10 -0.11
## [17,] -0.19 -0.09
## [18,] -0.25 0.01
## [19,] -0.29 -0.03
## [20,] -0.20 0.07
## [21,] -0.08 -0.04
## [22,] 0.08 0.06
## [23,] 0.16 -0.05
## [24,] 0.18 0.02
## [25,] 0.08 -0.14
## [26,] -0.06 -0.19
## [27,] -0.21 -0.13
## [28,] -0.31 -0.06
## [29,] -0.40 -0.08
## [30,] -0.40 -0.05
## [31,] -0.33 0.01
## [32,] -0.18 0.03
## [33,] 0.02 0.10
## [34,] 0.20 0.02
## [35,] 0.30 -0.01
## [36,]
         0.35 0.09
## [37,] 0.26 -0.12
## [38,] 0.13 0.01
## [39,] -0.02 -0.01
## [40,] -0.14 -0.05
## [41,] -0.23 0.02
## [42,] -0.21 0.12
## [43,] -0.18 -0.05
## [44,] -0.11 -0.13
## [45,] -0.03 -0.07
## [46,] 0.08 0.01
## [47,] 0.21 0.14
## [48,] 0.33 0.05
## [49,] 0.26 -0.20
## [50,] 0.12 -0.01
## [51,] -0.01 0.07
## [52,] -0.11 -0.04
## [53,] -0.13 0.02
## [54,] -0.09 0.00
## [55,] -0.09 -0.08
## [56,] -0.06 0.03
## [57,] 0.03 0.04
## [58,] 0.17 0.00
## [59,] 0.29 0.01
## [60,] 0.32 0.03
```

# # Fit ARIMA(2,1,0) to chicken - not so good sarima(chicken, 2,1,0)

```
## initial value 0.001863
## iter 2 value -0.156034
## iter 3 value -0.359181
## iter 4 value -0.424164
## iter 5 value -0.430212
## iter 6 value -0.432744
## iter 7 value -0.432747
## iter 8 value -0.432749
## iter 9 value -0.432749
## iter 10 value -0.432751
## iter 11 value -0.432752
## iter 12 value -0.432752
## iter 13 value -0.432752
## iter 13 value -0.432752
## iter 13 value -0.432752
## final value -0.432752
## converged
## initial value -0.420883
## iter 2 value -0.420934
## iter 3 value -0.420936
## iter 4 value -0.420937
## iter 5 value -0.420937
## iter 6 value -0.420937
## iter 6 value -0.420937
## iter 6 value -0.420937
## final value -0.420937
## converged
```

```
Model: (2,1,0)
                                      Standardized Residuals
                                                     2010
                          2005
                                                                                  2015
                                                Time
                 ACF of Residuals
                                                          Normal Q-Q Plot of Std Residuals
                                               Sample Quantiles
  9.0
ACF
0.2
                                                         0000
              0.5
                        1.0
                                   1.5
                                                            -2
                                                                   -1
                                                                          0
                                                                                        2
                                                                   Theoretical Quantiles
                        LAG
                                  p values for Ljung-Box statistic
  0.8
p value
0.4
                                                                  15
                                          10
                                                                                           20
                                                 lag
## $fit
##
## Call:
## stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D,
       Q), period = S), xreg = constant, optim.control = list(trace = trc, REPORT = 1,
##
##
       reltol = tol))
##
##
   Coefficients:
##
             ar1
                       ar2 constant
##
         0.9494
                 -0.3069
                              0.2632
## s.e. 0.0717
                   0.0718
                              0.1362
##
## sigma^2 estimated as 0.4286: log likelihood = -178.64, aic = 365.28
##
## $degrees_of_freedom
   [1] 177
##
##
## $ttable
##
             Estimate
                           SE t.value p.value
               0.9494 0.0717 13.2339 0.0000
## ar1
              -0.3069 0.0718 -4.2723 0.0000
## ar2
   constant 0.2632 0.1362 1.9328 0.0549
##
## $AIC
## [1] 0.1861622
##
```

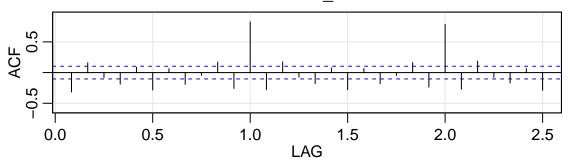
```
## $AICc
## [1] 0.1985432
##
## $BIC
## [1] -0.7606218
# Fit SARIMA(2,1,0,1,0,0,12) to chicken - that works
sarima(chicken,2,1,0,1,0,0,12)
## initial value 0.015039
## iter 2 value -0.226398
        3 value -0.412955
## iter
## iter
       4 value -0.460882
## iter
       5 value -0.470787
## iter
       6 value -0.471082
## iter
        7 value -0.471088
## iter
       8 value -0.471090
        9 value -0.471092
## iter
## iter 10 value -0.471095
## iter 11 value -0.471095
## iter 12 value -0.471096
## iter 13 value -0.471096
## iter 14 value -0.471096
## iter 15 value -0.471097
## iter 16 value -0.471097
## iter 16 value -0.471097
## iter 16 value -0.471097
## final value -0.471097
## converged
## initial value -0.473585
## iter 2 value -0.473664
## iter
        3 value -0.473721
## iter
        4 value -0.473823
        5 value -0.473871
## iter
## iter
        6 value -0.473885
## iter
        7 value -0.473886
        8 value -0.473886
## iter
        8 value -0.473886
## iter
         8 value -0.473886
## iter
## final value -0.473886
## converged
```

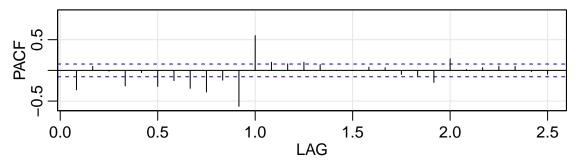
```
Model: (2,1,0) (1,0,0) [12]
                                       Standardized Residuals
  7
                                                       2010
                          2005
                                                                                    2015
                                                 Time
                  ACF of Residuals
                                                           Normal Q-Q Plot of Std Residuals
                                                  Quantiles 0 1 2
ACF
0.2
                                                  Sample (
-2
    0.0
           0.5
                  1.0
                        1.5
                               2.0
                                      2.5
                                             3.0
                                                             -2
                                                                    -1
                                                                            0
                                                                                          2
                                                                    Theoretical Quantiles
                        LAG
                                   p values for Ljung-Box statistic
  0.8
p value
0.4
                        10
                                     15
                                                   20
                                                                25
                                                                              30
                                                                                           35
                                                  lag
## $fit
##
## Call:
## stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D,
        Q), period = S), xreg = constant, optim.control = list(trace = trc, REPORT = 1,
##
##
       reltol = tol))
##
##
   Coefficients:
##
             ar1
                       ar2
                               sar1
                                      constant
          0.9154
##
                  -0.2494
                            0.3237
                                        0.2353
   s.e. 0.0733
                    0.0739
                            0.0715
                                        0.1973
##
## sigma^2 estimated as 0.3828: log likelihood = -169.16, aic = 348.33
##
## $degrees_of_freedom
   [1] 176
##
##
## $ttable
##
             Estimate
                            SE t.value p.value
               0.9154 0.0733 12.4955 0.0000
## ar1
              -0.2494 0.0739 -3.3728
                                         0.0009
## ar2
               0.3237 0.0715 4.5238 0.0000
## sar1
   {\tt constant}
               0.2353 0.1973 1.1923 0.2347
##
## $AIC
## [1] 0.0842377
```

```
##
## $AICc
## [1] 0.09726452
##
## $BIC
## [1] -0.8448077
###### Natalidad US

# Plot P/ACF to lag 60 of differenced data
d_birth <- diff(birth)
acf2(d_birth)</pre>
```

# Series: d\_birth

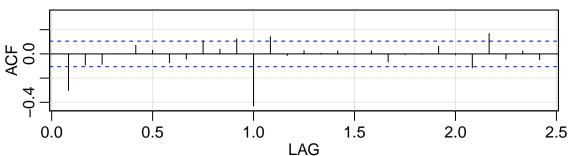


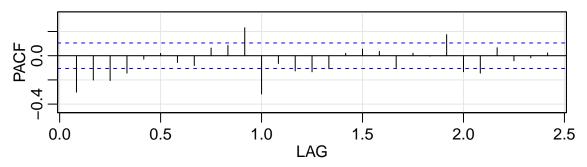


```
##
          ACF PACF
##
    [1,] -0.32 -0.32
##
    [2,] 0.16 0.06
##
    [3,] -0.08 -0.01
##
   [4,] -0.19 -0.25
   [5,] 0.09 -0.03
   [6,] -0.28 -0.26
##
##
   [7,] 0.06 -0.17
##
   [8,] -0.19 -0.29
  [9,] -0.05 -0.35
## [10,] 0.17 -0.16
## [11,] -0.26 -0.59
## [12,] 0.82 0.57
## [13,] -0.28 0.13
## [14,] 0.17
               0.11
## [15,] -0.07
              0.13
## [16,] -0.18 0.09
## [17,] 0.08 0.00
```

```
## [18,] -0.28 0.00
## [19,] 0.07 0.05
## [20,] -0.18 0.04
## [21,] -0.05 -0.07
## [22,] 0.16 -0.10
## [23,] -0.24 -0.20
## [24,] 0.78 0.19
## [25,] -0.27 0.01
## [26,] 0.19
               0.05
## [27,] -0.08 0.07
## [28,] -0.17 0.07
## [29,] 0.07 -0.02
## [30,] -0.29 -0.06
\# Plot P/ACF to lag 60 of seasonal differenced data
dd_birth <- diff(d_birth, lag = 12)</pre>
acf2(dd_birth)
```

# Series: dd\_birth





```
ACF PACF
##
##
   [1,] -0.30 -0.30
##
   [2,] -0.09 -0.20
   [3,] -0.09 -0.21
   [4,] 0.00 -0.14
##
##
   [5,] 0.07 -0.03
   [6,] 0.03 0.02
##
   [7,] -0.07 -0.06
##
   [8,] -0.04 -0.08
   [9,] 0.11 0.06
##
## [10,] 0.04 0.08
## [11,] 0.13 0.23
## [12,] -0.43 -0.32
```

```
## [13,] 0.14 -0.06
## [14,] -0.01 -0.13
## [15,] 0.03 -0.13
## [16,] 0.01 -0.11
## [17,] 0.02 0.02
## [18,] 0.00 0.06
## [19,] 0.03 0.04
## [20,] -0.07 -0.10
## [21,] -0.01 0.02
## [22,] 0.00 0.00
## [23,] 0.06 0.17
## [24,] -0.01 -0.13
## [25,] -0.12 -0.14
## [26,] 0.17 0.07
## [27,] -0.04 -0.04
## [28,] 0.03 -0.02
## [29,] -0.05 0.02
# Fit SARIMA(0,1,1)x(0,1,1)_12. What happens?
sarima(birth,0,1,1,0,1,1,12)
## initial value 2.219164
## iter
        2 value 2.013310
## iter 3 value 1.988107
## iter 4 value 1.980026
       5 value 1.967594
## iter
## iter
        6 value 1.965384
## iter
        7 value 1.965049
## iter
        8 value 1.964993
## iter
        9 value 1.964992
## iter
         9 value 1.964992
## iter
         9 value 1.964992
## final value 1.964992
## converged
## initial value 1.951264
## iter
        2 value 1.945867
## iter
        3 value 1.945729
        4 value 1.945723
## iter
## iter
       5 value 1.945723
## iter
       5 value 1.945723
## iter
       5 value 1.945723
## final value 1.945723
## converged
```

```
Model: (0,1,1) (0,1,1) [12]
                                       Standardized Residuals
            1950
                          1955
                                        1960
                                                      1965
                                                                    1970
                                                                                  1975
                                                                                                1980
                                                 Time
                  ACF of Residuals
                                                           Normal Q-Q Plot of Std Residuals
                                                Sample Quantiles
  9.7
ACF
0.2
    0.0
           0.5
                  1.0
                        1.5
                               2.0
                                      2.5
                                             3.0
                                                                     -1
                                                                            0
                                                                                         2
                                                                                                3
                                                                    Theoretical Quantiles
                        LAG
                                   p values for Ljung-Box statistic
  0.8
p value
0.4
                                       15
                                                    20
                                                                 25
                                                                              30
                          10
                                                                                           35
                                                  lag
## $fit
##
## Call:
## stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D,
        Q), period = S), include.mean = !no.constant, optim.control = list(trace = trc,
##
##
       REPORT = 1, reltol = tol))
##
##
   Coefficients:
##
              ma1
                       sma1
##
          -0.4734
                    -0.7861
          0.0598
                     0.0451
## s.e.
##
## sigma^2 estimated as 47.4: log likelihood = -1211.28, aic = 2428.56
##
## $degrees_of_freedom
   [1] 371
##
##
## $ttable
##
         Estimate
                       SE t.value p.value
          -0.4734 0.0598 -7.9097
                                           0
## ma1
## sma1 -0.7861 0.0451 -17.4227
##
## $AIC
## [1] 4.869388
##
## $AICc
```

```
## [1] 4.874924
##
## $BIC
## [1] 3.890415
# Add AR term and conclude
sarima(birth,1,1,1,0,1,1,12)
## initial value 2.218186
        2 value 2.032584
## iter
## iter
       3 value 1.982464
       4 value 1.975643
## iter
## iter
       5 value 1.971721
## iter
       6 value 1.967284
       7 value 1.963840
## iter
## iter 8 value 1.961106
## iter 9 value 1.960849
## iter 10 value 1.960692
## iter 11 value 1.960683
## iter 12 value 1.960675
## iter 13 value 1.960672
## iter 13 value 1.960672
## iter 13 value 1.960672
## final value 1.960672
## converged
## initial value 1.940459
## iter 2 value 1.934425
       3 value 1.932752
## iter
## iter
       4 value 1.931750
## iter
       5 value 1.931074
## iter
       6 value 1.930882
## iter
       7 value 1.930860
## iter
       8 value 1.930859
       8 value 1.930859
## iter
```

## final value 1.930859

## converged

```
Model: (1,1,1) (0,1,1) [12]
                                       Standardized Residuals
            1950
                          1955
                                        1960
                                                     1965
                                                                   1970
                                                                                 1975
                                                                                               1980
                                                 Time
                                                           Normal Q-Q Plot of Std Residuals
                 ACF of Residuals
  0.5
                                                Sample Quantiles
    0.0
           0.5
                  1.0
                        1.5
                               2.0
                                      2.5
                                             3.0
                                                                    -1
                                                                            0
                                                                                         2
                                                                                               3
                        LAG
                                                                    Theoretical Quantiles
                                   p values for Ljung-Box statistic
  0.8
p value
0.4
          -a -a -a
                        10
                                     15
                                                  20
                                                                25
                                                                             30
                                                                                           35
                                                  lag
## $fit
##
## Call:
## stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D,
        Q), period = S), include.mean = !no.constant, optim.control = list(trace = trc,
##
##
       REPORT = 1, reltol = tol))
##
##
   Coefficients:
##
             ar1
                       ma1
                                sma1
##
          0.3038
                  -0.7006
                            -0.8000
## s.e. 0.0865
                    0.0604
                              0.0441
##
## sigma^2 estimated as 45.91: log likelihood = -1205.93, log aic = 2419.85
##
## $degrees_of_freedom
   [1] 370
##
##
## $ttable
##
        Estimate
                       SE t.value p.value
           0.3038 0.0865
                            3.5104
                                       5e-04
## ar1
          -0.7006 0.0604 -11.5984
                                       0e+00
## ma1
         -0.8000 0.0441 -18.1302
                                       0e+00
   sma1
##
## $AIC
## [1] 4.842869
##
```

```
## $AICc
## [1] 4.848523
##
## $BIC
## [1] 3.87441
## FORECASTING SEASONAL DATA
# Fit your previous model to unemp and check the diagnostics
sarima(unemp, 2,1,0,0,1,1,12)
## initial value 3.340809
## iter 2 value 3.105512
## iter 3 value 3.086631
## iter 4 value 3.079778
## iter 5 value 3.069447
## iter 6 value 3.067659
## iter 7 value 3.067426
## iter 8 value 3.067418
## iter 8 value 3.067418
## final value 3.067418
## converged
## initial value 3.065481
## iter 2 value 3.065478
## iter 3 value 3.065477
## iter 3 value 3.065477
## iter 3 value 3.065477
## final value 3.065477
## converged
```

```
Model: (2,1,0) (0,1,1) [12]
                                          Standardized Residuals
   4
   ^{\circ}
   0
   7
             1950
                            1955
                                           1960
                                                          1965
                                                                         1970
                                                                                        1975
                                                                                                      1980
                                                     Time
                   ACF of Residuals
                                                               Normal Q-Q Plot of Std Residuals
   0.4
                                                     Sample Quantiles -2 0 2 4
ACF
0.2
   0.0
                                  2.0
                                                                                               2
     0.0
            0.5
                   1.0
                           1.5
                                         2.5
                                                3.0
                                                            -3
                                                                          -1
                                                                                 0
                                                                                                      3
                                                                         Theoretical Quantiles
                           LAG
                                      p values for Ljung-Box statistic
  0.8
p value
0.4
   0.0
                                                                    25
            5
                          10
                                        15
                                                      20
                                                                                   30
                                                                                                 35
                                                      lag
## $fit
##
## Call:
    stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D,
         Q), period = S), include.mean = !no.constant, optim.control = list(trace = trc,
##
##
         REPORT = 1, reltol = tol))
##
##
    Coefficients:
##
               ar1
                        ar2
                                  sma1
##
           0.1351
                    0.2464
                              -0.6953
    s.e. 0.0513
                    0.0515
                               0.0381
##
## sigma^2 estimated as 449.6: log likelihood = -1609.91, log likelihood = -1609.91, log likelihood = -1609.91
##
## $degrees_of_freedom
    [1] 369
##
##
## $ttable
##
          Estimate
                         SE t.value p.value
            0.1351 0.0513
                               2.6326 0.0088
## ar1
            0.2464 0.0515
                               4.7795
                                        0.0000
##
    ar2
          -0.6953 0.0381 -18.2362 0.0000
##
    sma1
##
## $AIC
##
    [1] 7.12457
##
```

```
## $AICc
## [1] 7.130239
##
## $BIC
## [1] 6.156174
# Forecast the data 3 years into the future
sarima.for(unemp,n.ahead = 36,2,1,0,0,1,1,12)
## $pred
##
                      Feb
             Jan
                               Mar
                                        Apr
                                                 May
                                                           Jun
## 1979 676.4664 685.1172 653.2388 585.6939 553.8813 664.4072 647.0657
## 1980 683.3045 687.7649 654.8658 586.1507 553.9285 664.1108 646.6220
## 1981 682.6406 687.0977 654.1968 585.4806 553.2579 663.4398 645.9508
##
                      Sep
                               Oct
                                        Nov
                                                  Dec
             Aug
## 1979 611.0828 594.6414 569.3997 587.5801 581.1833
## 1980 610.5345 594.0427 568.7684 586.9320 580.5249
  1981 609.8632 593.3713 568.0970 586.2606 579.8535
##
## $se
##
              Jan
                        Feb
                                  Mar
                                            Apr
                                                                           Jul
## 1979 21.20465 32.07710 43.70167 53.66329 62.85364 71.12881 78.73590
## 1980 116.99599 124.17344 131.51281 138.60466 145.49706 152.12863 158.52302
## 1981 194.25167 201.10648 208.17066 215.11503 221.96039 228.64285 235.16874
                        Sep
                                  Oct
                                            Nov
              Aug
## 1979 85.75096
                  92.28663 98.41329 104.19488 109.67935
## 1980 164.68623 170.63839 176.39520 181.97333 187.38718
## 1981 241.53258 247.74268 253.80549 259.72970 265.52323
# Fit the chicken model again and check diagnostics
sarima(chicken,2,1,0,1,0,0,12)
  1000
                1972
                                                                     1980
                             1974
                                           1976
                                                        1978
                                                                                   1982
                                            Time
## initial value 0.015039
## iter
          2 value -0.226398
## iter
          3 value -0.412955
## iter
          4 value -0.460882
          5 value -0.470787
## iter
          6 value -0.471082
## iter
## iter
          7 value -0.471088
```

8 value -0.471090

9 value -0.471092

## iter 10 value -0.471095 ## iter 11 value -0.471095

## iter ## iter

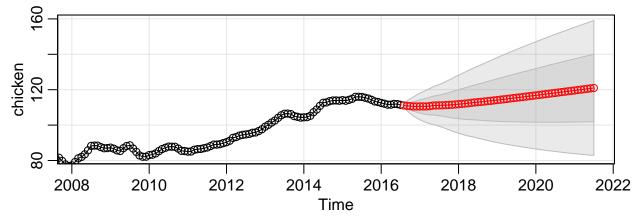
```
## iter 12 value -0.471096
## iter
         13 value -0.471096
          14 value -0.471096
          15 value -0.471097
   iter
## iter
          16 value -0.471097
         16 value -0.471097
## iter
## iter 16 value -0.471097
## final value -0.471097
## converged
## initial value -0.473585
## iter
           2 value -0.473664
           3 value -0.473721
## iter
           4 value -0.473823
## iter
## iter
           5 value -0.473871
## iter
           6 value -0.473885
## iter
           7 value -0.473886
## iter
           8 value -0.473886
           8 value -0.473886
## iter
## iter
           8 value -0.473886
## final value -0.473886
## converged
                                        Standardized Residuals
                                                                                     .
2015
                           2005
                                                        2010
                                                  Time
                  ACF of Residuals
                                                  Sample Quantiles –2 0 1 2
ACF
0.2
                                                                                           2
    0.0
                  1.0
                         1.5
                                2.0
                                       2.5
                                              3.0
                                                                     -1
                                                                             0
           0.5
                                                              -2
                         LAG
                                                                     Theoretical Quantiles
                                    p values for Ljung-Box statistic
  0.8
p value
0.4
          5
                        10
                                      15
                                                                 25
                                                                              30
                                                                                            35
                                                   20
                                                   lag
## $fit
##
```

## stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D,

## Call:

```
Q), period = S), xreg = constant, optim.control = list(trace = trc, REPORT = 1,
##
##
       reltol = tol))
##
## Coefficients:
##
            ar1
                     ar2
                            sar1
                                 constant
                -0.2494
##
         0.9154
                          0.3237
                                    0.2353
## s.e. 0.0733
                  0.0739 0.0715
                                    0.1973
##
## sigma^2 estimated as 0.3828: log likelihood = -169.16, aic = 348.33
##
## $degrees_of_freedom
## [1] 176
##
## $ttable
##
            Estimate
                         SE t.value p.value
              0.9154 0.0733 12.4955
                                     0.0000
## ar1
             -0.2494 0.0739 -3.3728
## ar2
                                     0.0009
              0.3237 0.0715 4.5238
                                     0.0000
## sar1
## constant
              0.2353 0.1973 1.1923 0.2347
##
## $AIC
## [1] 0.0842377
##
## $AICc
## [1] 0.09726452
## $BIC
## [1] -0.8448077
# Forecast the chicken data 5 years into the future
sarima.for(chicken,n.ahead = 60,2,1,0,1,0,0,12)
## $pred
##
                      Feb
                               Mar
                                         Apr
                                                  May
                                                           Jun
                                                                    J<sub>11</sub>]
             .Jan
## 2016
## 2017 110.5358 110.5612 110.5480 110.7055 111.0047 111.1189 111.1552
## 2018 111.8108 111.9782 112.1330 112.3431 112.5991 112.7952 112.9661
## 2019 114.1331 114.3464 114.5556 114.7827 115.0247 115.2473 115.4617
## 2020 116.7942 117.0224 117.2492 117.4819 117.7193 117.9505 118.1790
## 2021 119.5651 119.7980 120.0306 120.2650 120.5010 120.7350 120.9681
             Aug
                      Sep
                               Oct
                                        Nov
## 2016 111.0907 110.8740 110.6853 110.5045 110.5527
## 2017 111.1948 111.2838 111.3819 111.4825 111.6572
## 2018 113.1380 113.3260 113.5168 113.7085 113.9242
## 2019 115.6765 115.8965 116.1174 116.3386 116.5675
## 2020 118.4077 118.6380 118.8686 119.0993 119.3326
## 2021
##
## $se
##
               Jan
                          Feb
                                     Mar
                                                 Apr
                                                            May
                                                                        Jun
## 2016
## 2017
        3.7414959 4.1793190 4.5747009 4.9373266 5.2742129 5.5903499
## 2018 8.2010253 8.5605811 8.9054714 9.2372195 9.5572539 9.8667955
## 2019 12.0038164 12.2921541 12.5738417 12.8492868 13.1188976 13.3830477
## 2020 15.1557253 15.3959082 15.6323906 15.8653300 16.0948844 16.3212022
```

```
## 2021 17.8397890 18.0473081 18.2524651 18.4553364 18.6559977 18.8545213
                         Aug
##
              Jul
                                    Sep
                                               Oct
                                                          Nov
                                                                     Dec
                   0.6187194
                             1.3368594 2.0462419 2.6867986 3.2486625
## 2016
## 2017 5.8893133 6.2367345 6.6253573 7.0309771 7.4344077 7.8255932
## 2018 10.1668604 10.4736807 10.7857727 11.0980056 11.4063211 11.7085266
## 2019 13.6420693 13.9002670 14.1573839 14.4122197 14.6638269 14.9117124
## 2020 16.5444204 16.7657634 16.9852163 17.2025022 17.4174076 17.6298379
## 2021 19.0509752
```

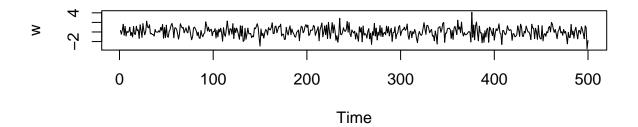


### Pruebas series de tiempo de Time Series Analysis and its applications text

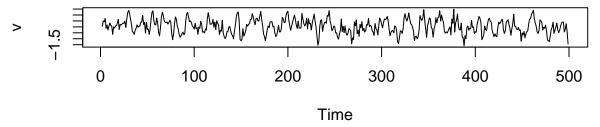
Página 13 Moving Average

```
w = rnorm (500,0,1)
v = filter(w, sides = 2, rep(1/3,3))
par(mfrow=c(2,1))
plot.ts(w,main = "white noise")
plot.ts(v, main = "moving average")
```

## white noise



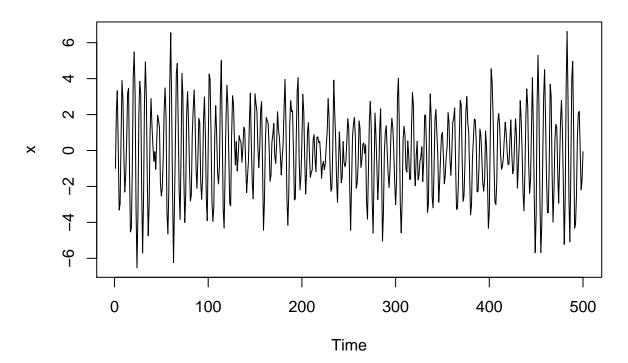
# moving average



### Autoregesivo

```
w = rnorm(550,0,1)
x = filter (w, filter = c(1,-0.9), method = "recursive")[-(1:50)]
plot.ts(x, main = "autoregression")
```

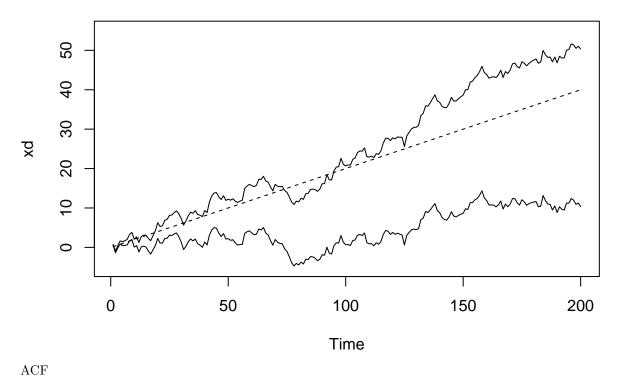
# autoregression



Autoregesivo con drift

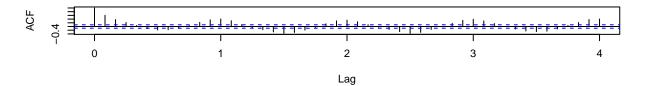
```
set.seed(154)
w = rnorm(200,0,1); x = cumsum (w)
wd = w + .2; xd = cumsum(wd)
plot.ts(xd, ylim = c(-5,55), main = "random walk")
lines(x); lines(0.2*(1:200), lty = "dashed")
```

# random walk

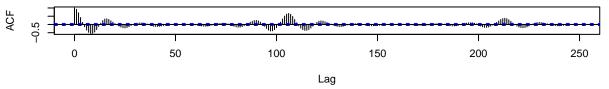


```
par(mfrow = c(3,1))
acf(soi, 48, main = "Southern Oscilation Index")
acf(speech, 250)
par(mfrow=c(3,1))
```

#### **Southern Oscilation Index**

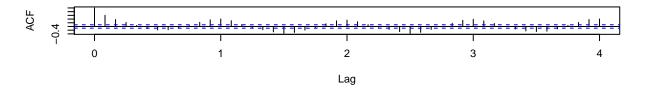


#### Series speech

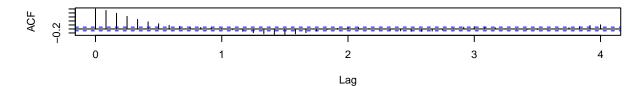


```
acf(soi, 48, main="Southern Oscillation Index")
acf(rec, 48, main="Recruitment")
ccf(soi, rec, 48, main="SOI vs Recruitment", ylab="CCF")
```

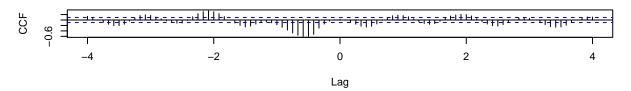
#### **Southern Oscillation Index**



#### Recruitment

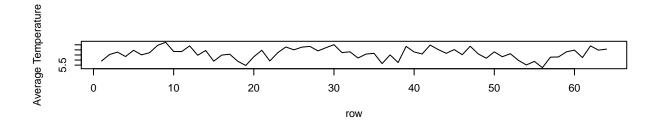


### **SOI vs Recruitment**



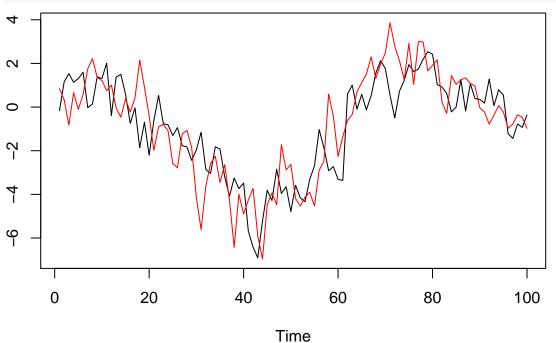
```
# Varios vectores
persp(1:64, 1:36, soiltemp, phi=30, theta=30, scale=FALSE, expand=4, ticktype="detailed", xlab="rows",
plot.ts(rowMeans(soiltemp), xlab="row", ylab="Average Temperature")
```





# **VECTORES AUTOREGRESIVOS**

```
B1<-matrix(c(0.7, 0.2, 0.2, 0.7), 2)
var1<-VAR.sim(B=B1,n=100,include="none")
ts.plot(var1, type="l", col=c(1,2))
```



```
VARselect(var1, lag.max=9, type="const")
```

```
## $selection
## AIC(n) HQ(n) SC(n) FPE(n)
## 1 1 1 1
##
## $criteria
## 1 2 3 4 5 6
## AIC(n) -0.004781104 0.05373217 0.05239784 0.05727888 0.1294645 0.1453231
```

```
0.062008485 0.16504815 0.20824021 0.25764765 0.3743596 0.4347447
## SC(n) 0.160770072 0.32965079 0.43868392 0.55393241 0.7364854 0.8627116
## FPE(n) 0.995277884 1.05543577 1.05443691 1.06032595 1.1409261 1.1609733
##
                7
                          8
## AIC(n) 0.1819582 0.2581421 0.3365710
## HQ(n) 0.5159061 0.6366164 0.7595717
## SC(n) 1.0097141 1.1962654 1.3850617
## FPE(n) 1.2068686 1.3060686 1.4176983
var1_est <- VAR(var1,p = 1)</pre>
## Warning in VAR(var1, p = 1): No column names supplied in y, using: y1, y2 , instead.
var1 est
##
## VAR Estimation Results:
## ==========
## Estimated coefficients for equation y1:
## ===============
## Call:
## y1 = y1.11 + y2.11 + const
##
##
        y1.l1
                   y2.11
                               const
  0.67774002 0.23472999 -0.09862114
##
##
##
## Estimated coefficients for equation y2:
## ==============
## Call:
## y2 = y1.11 + y2.11 + const
##
                            const
       y1.11
                y2.11
## 0.41445790 0.58815891 0.01955353
```

### MODELOS ESTADO ESPACIO

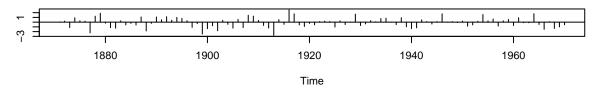
El paquete base de R permite evaluar modelos estado espacio con la función

Más información sobre modelos estado espacio se puede encontrar aquí: link StructTS

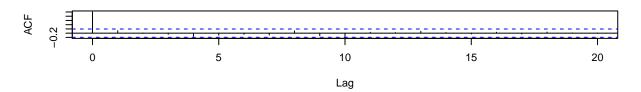
```
# rm(list = ls())
fitNile <- StructTS(Nile, "level")
fitNile

##
## Call:
## StructTS(x = Nile, type = "level")
##
## Variances:
## level epsilon
## 1469 15099
tsdiag(fitNile)</pre>
```

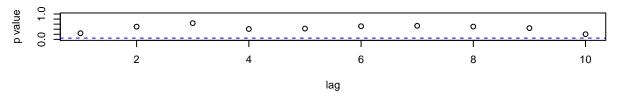
#### Standardized Residuals



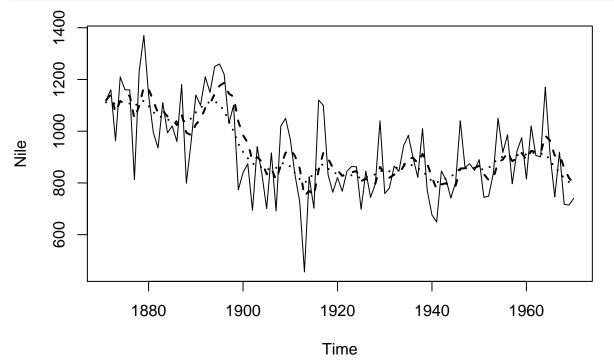
### **ACF of Residuals**



## p values for Ljung-Box statistic

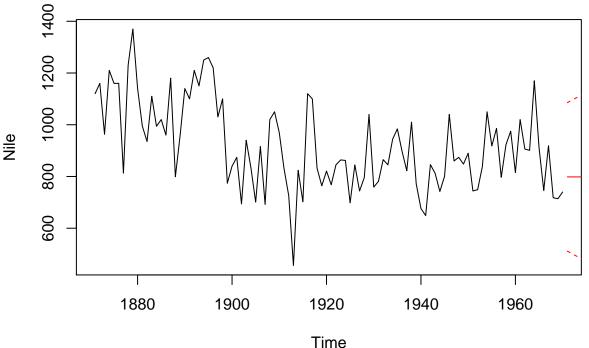


```
plot(Nile, type = "1")
lines(fitted(fitNile), lty = "dashed", lwd = 2)
lines(tsSmooth(fitNile), lty = "dotted", lwd = 2)
```



```
SP_fit <- StructTS(Nile, "level")
SP_forecast <- predict(SP_fit, n.ahead = 100)$pred</pre>
```

```
SP_forecast_se <- predict(SP_fit, n.ahead = 100)$se
plot(Nile, type = "l")
points(SP_forecast, type = "l", col = 2)
points(SP_forecast - 2*SP_forecast_se, type = "l", col = 2, lty = 2)
points(SP_forecast + 2*SP_forecast_se, type = "l", col = 2, lty = 2)</pre>
```



```
# Del link anterior
## Structural time series models
par(mfrow = c(3, 1))
plot(Nile)
## local level model
(fit <- StructTS(Nile, type = "level"))</pre>
##
## Call:
## StructTS(x = Nile, type = "level")
##
## Variances:
##
     level epsilon
      1469
              15099
lines(fitted(fit), lty = 2)
                                       # contemporaneous smoothing
lines(tsSmooth(fit), lty = 2, col = 4) # fixed-interval smoothing
plot(residuals(fit)); abline(h = 0, lty = 3)
## local trend model
(fit2 <- StructTS(Nile, type = "trend")) ## constant trend fitted
##
## Call:
## StructTS(x = Nile, type = "trend")
```

##

```
## Variances:
##
     level
               slope epsilon
                        15047
      1427
##
                   0
pred <- predict(fit, n.ahead = 30)</pre>
## with 50% confidence interval
ts.plot(Nile, pred$pred,
        pred$pred + 0.67*pred$se, pred$pred -0.67*pred$se)
                                                                              1960
                1880
                               1900
                                               1920
                                                               1940
                                               Time
```

