1. Compute $\sum_{j=5}^{200} 6$

$$\sum_{j=5}^{200} 6 = 6 \cdot (200 - 5 + 1)$$
$$= 6 \cdot (196)$$

2. Compute $\sum_{p=-20}^{100} k$

$$\sum_{p=-20}^{100} k = k \cdot (100 + 20 + 1)$$
$$= k \cdot (121)$$

3. Compute $\sum_{k=-5}^{100} 8^k$

$$\sum_{k=-5}^{100} 8^k = \sum_{k=-5}^{-1} 8^k + \sum_{k=0}^{100} 8^k$$

$$= \sum_{k=1}^{5} (\frac{1}{8})^k + \frac{8^{101} - 1}{8 - 1}$$

$$= \frac{(\frac{1}{8})^k - 1}{(\frac{1}{8}) - 1} - 1 + \frac{8^{101} - 1}{8 - 1}$$

4. Compute $\sum_{j=1}^{n} \sum_{i=1}^{j} (2 \cdot i + 3)$

$$\sum_{j=1}^{n} \sum_{i=1}^{j} (2 \cdot i + 3) = \sum_{j=1}^{n} \sum_{i=1}^{j} 2 \cdot i + \sum_{j=1}^{n} \sum_{i=1}^{j} 3$$

$$= \sum_{j=1}^{n} j^{2} + \sum_{j=1}^{n} j + \sum_{j=1}^{n} 3 \cdot j$$

$$= \frac{(n)(n+1)(2n+1)}{6} + \frac{n(n+1)}{2} + 3 \cdot \frac{n(n+1)}{2}$$

5. Show $log_b(x^a) = alog_b(x)$

$$log_b x = c$$

$$b^c = x$$

$$b^{c \cdot a} = x^a$$

$$c \cdot a = log_b(x^a)$$

$$c \cdot log_b(x) = log_b(x^a)$$

6. Show
$$log_b(x \cdot y) = log_b(x) + log_b(y)$$

$$log_b(x) = p$$

$$log_b(y) = s$$

$$x = b^p$$

$$y = b^s$$

$$x \cdot y = b^{p \cdot s}$$

$$x \cdot y = b^{p+s}$$

$$log_b(x \cdot y) = p + s$$

$$log_b(x \cdot y) = log_b(x) + log_b(y)$$

7. Show $log_b(\frac{x}{y}) = log_b(x) - log_b(y)$

$$log_b(x) = c$$

$$log_b(y) = k$$

$$x = b^c$$

$$y = b^k$$

$$\frac{x}{y} = \frac{b^c}{b^k}$$

$$\frac{x}{y} = b^{c-k}$$

$$log_b(\frac{x}{y}) = c - k$$

$$log_b(\frac{x}{y}) = log_b(x) - log_b(y)$$

8. Show $b^{log_b x} = x$

$$log_b x = c$$

$$x = b^c$$

$$x = b^{log_b x}$$

9. Show $y^{log_b x} = x^{log_b y}$

$$log_b(x) = k \iff x = b^k$$

$$log_b(y) = c \iff y = b^c$$

$$x^{log_b(y)} = b^{k \cdot log_b(y)}$$

$$x^{log_b(y)} = b^{log_b(y^k)}$$

$$x^{log_b(y)} = y^k$$

$$x^{log_b(y)} = y^{log_b(x)}$$

10. Show $log_b(x) = \frac{1}{log_x(b)}$

$$log_b(x) = c$$

$$log_x(b) = k$$

$$x = b^c$$

$$b = x^k$$

$$x \cdot b = b^c \cdot x^k$$

$$log_b(x) + 1 = c + k \cdot log_b(x)$$

$$log_b(x) + 1 = log_b(x) + log_x(b) \cdot log_b(x)$$

$$1 = log_x(b) \cdot log_b(x)$$

$$\frac{1}{log_x(b)} = log_b(x)$$

11. Show $log_b(x) = \frac{log_a(x)}{log_a(b)}$

$$y = log_b(x)$$

$$z = log_a(x)$$

$$z = log_a(b^y)$$

$$z = y \cdot log_a(b)$$

$$z = log_b(x) \cdot log_a(b)$$

$$log_a(x) = log_b(x) \cdot log_a(b)$$

$$\frac{log_a(x)}{log_a(b)} = log_a(x)$$

12. Compute $log_2(2^2 \times 3^4)$

$$log_2(2^2) + log_2(3^4) = 2 \cdot log_2(2) + 4 \cdot log_2(3)$$
$$= 2 + 4 \cdot (1.5)$$

13. Compute $log_2(\frac{64 \times 128 \times 3}{1024 \times 2^{15}})$

$$log_{2}(\frac{64 \times 128 \times 3}{1024 \times 2^{15}}) = log_{2}(64 \times 128 \times 3) - log_{2}(1024 \times 2^{15})$$

$$= log_{2}(64) + log_{2}(128) + log_{2}(3) - log_{2}(1024) - 15 \cdot log_{2}(2)$$

$$= 6 + 7 + (1.5) - 10 - 15$$

14. Compute $log_2(log_2(16))$

$$log_2(log_2(16)) = log_2(4)$$
$$= 2$$

15. Compute $(log_2(8))^4$

$$(log_2(8))^4 = (3)^4$$

16. Compute $(log_2^4 128^2)$

$$(log_2(128^2))^4 = (2 \cdot log_2(128))^4$$
$$= 2^4 \cdot 7^4$$
$$= (2 \cdot 7)^4$$
$$= 14^4$$

17. Compute $5^{\log_5(15)} + 3^{\log_3(8)}$

$$5^{\log_5(5)} + 3^{\log_3(8)} = 5 + 8$$

18. Compute $8^{log_2(6)}$

$$8^{log_2(6)} = 2^{log_2(6^3)}
= 6^3$$

19. Compute $4^{\log_2(\log_2(5))} + 6^{\log_6(2)}$

$$2^{\log_2(\log_2(5)^2)} + 2 = \log_2(5)^2 + 2$$

20. Compute $log_2((\frac{log_4(8)}{log_3(27)})^2)$

$$log_{2}((\frac{log_{4}(8)}{log_{3}(27})^{2}) = log_{2}((\frac{\frac{3}{2}}{3})^{2})$$

$$= log_{2}((\frac{1}{2})^{2})$$

$$= log_{2}(\frac{1}{4})$$

$$= -2$$

21. Compute the deriative of $(2x^5 + 3x^9 + lnx)$

$$\frac{d}{dx}(2x^5 + 3x^9 + lnx) = 10x^4 + 27x^8 + \frac{1}{x}$$

22. Compute the deriative of $(ln^2(x) + x \cdot (x+1)^2)$

$$\frac{d}{dx}(\ln^2(x) + x \cdot (x+1)^2) = 2 \cdot \ln(x) \cdot \frac{1}{x} + (x+1)^2 + 2 \cdot x \cdot (x+1)$$

23. Compute the derivative of $\frac{\sqrt{5x+2}}{x \cdot \sin(x)}$

$$\frac{d}{dx}(\frac{\sqrt{5\cdot x + 2}}{x \cdot sin(x)}) = \frac{\frac{5}{2} \cdot (5 \cdot x + 2)^{-\frac{1}{2}}(x \cdot sin(x)) - (5 \cdot x + 2)^{\frac{1}{2}}(sin(x) + x \cdot cos(x))}{x^2 \cdot sin^2(x)}$$

24.