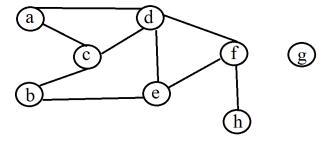
Due date: Monday, November 30, 2020 at 11:59pm

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Note: you can have different names for vertices: $\{a \ b \ c \ d \ e ..\} = \{v1 \ v2 \ v3 \ v4 ..\} = \{1 \ 2 \ 3 \ 4 ..\}$

In this program you are required to implement BFS.

First, you can create the below graph and print the resulting adjacency matrix/list. Or create a random graph.

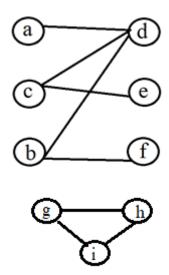


Part A.

- 1. Request the user to determine the starting vertex (a) for BFS algorithm
- 2. Call *BFS* function to find the vertices reachable from vertex *u* and print the *shortest paths* and their *lengths/distances*.

Part B.

In this part you are required to determine if a random undirected graph is <u>bipartite</u> or not. You can use the below graph to test.



Here, we work with three colors for the vertices: gray (not visited), [blue, red] (opposite colors)

- 1. Print the resulting adjacency matrix/list.
- 2. Implement 2 functions: *Explore* and *Is_bipartite*
- 3. In *Explore* function,
 - a. For each vertex (v) initialize v.color = "gray".
 - b. Start from the first vertex, color it "blue" and call Is_bipartite on that.
 - c. Next, go to the next unexplored vertex (having *gray* color), color it "blue" and call *Is_bipartite* again.
 - d. Repeat step c. until every vertex is explored/colored or a not bipartite graph is detected.
- 4. Now to implement our second function (*Is_bipartite*), you need to change your BFS function in part A.
 - a. Keep popping each vertex from Q. (call it u)
 - b. Go to the adjacency list of \mathbf{u} , (adj(\mathbf{u})), and for each neighbor (\mathbf{v}):
 - c. If $v.\ color == "gray"$, assign an opposite color to v and push it into the $Q.\ (Example: u.color is blue, and <math>v.color$ is $gray \rightarrow we$ set v.color = "red")
 - d. Else if v.color == u.color: Stop the entire code and print "NOT bipartite".
- 5. Print the color of all the vertices.