```
#include <iostream>
#include <vector>
#include <random>
#include <chrono>
using std::getline;
using std::string;
using std::cout;
using std::endl;
using std::vector;
using std::cin;
using std::swap;
using std::default random engine;
using std::uniform_int_distribution;
bool get_line(const string& user_prompt, string& line){
  cout << user_prompt;</pre>
  getline(cin, line);
  return !line.empty();
void insertion_sort(vector<int>& arr){
  for(int i = 1;i < arr.size();i++){
    for(int j = i; j > 0 && arr[j] < arr[j - 1]; j--){
       swap(arr[j], arr[j - 1]);
    }
  }
}
void partial sort(vector<int>& arr, int lower bound, int upper bound){
  for(int i = lower bound;i <= upper bound;i++){
    for(int j = i; j > 0 && arr[j] < arr[j - 1]; j--){
       swap(arr[j], arr[j - 1]);
  }
}
int median_of_three(vector<int>& arr, int lo, int hi){
  int mid = (lo + hi) / 2;
  if(arr[lo] > arr[hi])
    swap(arr[lo], arr[hi]);
  if(arr[lo] > arr[mid])
    swap(arr[lo], arr[mid]);
  if(arr[mid] > arr[hi])
    swap(arr[mid], arr[hi]);
  return mid;
}
int partition(vector<int> &arr, int lo, int hi){
  int i = lo - 1, j = hi;
  int pivot_value = arr[hi];
  while(true){
    while(arr[++i] < pivot_value) if(i == hi) break;
    while(arr[--j] > pivot_value) if(j == lo) break;
    if(i \ge j) break;
    swap(arr[i], arr[j]);
  swap(arr[i], arr[hi]);
  return i;
```

```
void guick sort(vector<int>& arr, int lo, int hi){
  const int CUTOFF_TO_INSERTION_SORT = 3;
  if(hi <= lo + CUTOFF_TO_INSERTION_SORT){</pre>
    partial_sort(arr, lo, hi);
    return;
  int pivot idx = median of three(arr, lo, hi);
  swap(arr[pivot idx], arr[hi]);
  int new pivot idx = partition(arr, lo, hi);
  quick sort(arr, lo, new pivot idx - 1);
  quick_sort(arr, new_pivot_idx + 1, hi);
}
void quick_sort(vector<int>& arr){
  quick_sort(arr, 0, arr.size() - 1);
int main() {
  string line;
  while(get_line("enters a positive integer: ", line)){
    int n = stoi(line);
    unsigned seed = std::chrono::system_clock::now().time_since_epoch().count();
    default_random_engine gen(seed);
    const int LOWER_BOUND = -5000;
    const int UPPER_BOUND = 5000;
    uniform int distribution<int> uniform int distribution(LOWER BOUND, UPPER BOUND);
    vector<int> a:
    for(int i = 0; i < n; i++)
      a.push_back(uniform_int_distribution(gen));
    const int TRIALS = 100;
    vector<double> insertion_sort_times;
    vector<double> quick_sort_times;
    for(int i = 0;i < TRIALS;i++){
      vector<int> insertion_sort_copy = a;
      auto start = std::chrono::steady_clock::now();
      insertion_sort(insertion_sort_copy);
      auto end = std::chrono::steady_clock::now();
      std::chrono::duration<double> elapsed seconds = end - start;
      insertion_sort_times.emplace_back(elapsed_seconds.count());
      vector<int> quick_sort_copy = a;
      start = std::chrono::steady_clock::now();
      quick_sort(quick_sort_copy);
      end = std::chrono::steady_clock::now();
      elapsed_seconds = end - start;
      quick_sort_times.emplace_back(elapsed_seconds.count());
    double in_sort_avg_runtime = accumulate(insertion_sort_times.begin(), insertion_sort_times.end(), 0.0) / TRIALS;
    double quick_sort_avg_runtime = accumulate(quick_sort_times.begin(), quick_sort_times.end(), 0.0) / TRIALS;
    cout << "The average runtime for insertion sort is: " << in_sort_avg_runtime << endl;
    cout << "The average runtime for quick sort is: " << quick_sort_avg_runtime << endl;
  }
}
```