

1 Compute the values for

1.  $\sum_{i=-1}^4 3$
2.  $\sum_{i=1}^5 (\frac{1}{3})^i$
3.  $\sum_{i=1}^n 3$
4.  $\sum_{i=-3}^n 3$
5.  $\sum_{k=0}^n 2^k + \sum_{k=5}^n 2^k$
6.  $\sum_{i=0}^n (\frac{2}{3})^i + \sum_{i=-4}^n (\frac{2}{3})^i$
7.  $\sum_{i=1}^n (i^3 + 2 \cdot i^2 - i + 1)$
8.  $\sum_{i=5}^n (-4 \cdot i + \frac{i}{5})$
9.  $\sum_{j=0}^k \sum_{i=1}^j (i - j^2 - 2)$
10.  $\sum_{j=1}^m \sum_{k=1}^j (3 \cdot k - 3 \cdot j + i)$
11.  $\sum_{l=-4}^n \sum_{j=1}^k \sum_{i=1}^j (i - 4)$

2. Calculate the answer

1.  $\log_4 x = 5 \rightarrow x = ?$
2.  $\log_3 y = 4 \rightarrow y = ?$
3.  $x = 7^2 \rightarrow \log_7 x = ?$
4.  $x = 32 \rightarrow \log_2 x = ?$
5.  $2^{\log 5} + 4^{\log 6} - 27^{\log 3 5}$
6.  $9^{\log 3 2} - 25^{\log 5 4} - 36^{\log 6 7} + 8^{\log 8 6}$
7.  $\log(4^5 \times 8^3) - \log(16 - 8) + \log(\frac{2^{10}}{4 \times 3^2})$
8.  $\log(3^2 \times 64^3) - \log(\frac{2^{10} \times 128^3}{9 \times 8^2})$
9.  $\log \log 16$
10.  $\log 16 \times \log 16$
11.  $\log^2 16$
12.  $\log_2 \log_5 625 - \log_3 \log_4 2^{3^9} + \log^4 2^5 - \frac{\log^2(4^3 \times 3^5)}{\log_5 125}$
13.  $\log \log_8 \log 256 + \log^5(3^2) \times 4^{\log 7}$
14.  $\log_6 x = 5 \rightarrow \log_x 6 = ?$

15.  $\log_y x = 10 \rightarrow \log_x y = ?$
16.  $\log_4 32 - \log_8^2 4$
17.  $\log_4 8 + \log_9 27 - \log_{25}^2 125 - \log_8^3 16 + \log_4 \log 256$

**3.** Compute the derivative of

1.  $-5 \cdot x^3 + 2 \cdot x - 1$
2.  $3 \cdot x^4 - 2\sqrt{x} + x^{\frac{1}{2}} - 6x^{-\frac{2}{3}} - 5$
3.  $x \cdot \sqrt{x} + \sqrt{\sqrt{x}}$
4.  $\log x - x^2 \ln x + \ln x^4$
5.  $\ln^3(x\sqrt{2x-3}) + \sqrt{\ln x^2}$
6.  $\frac{\sqrt[4]{x+5} - \ln x}{(x-1)^3}$

**4.** Determine the limit of

1.  $\lim_{x \rightarrow \infty} \frac{3x+2}{-5x-6}$
2.  $\lim_{x \rightarrow \infty} (\frac{1}{x} + 3)$
3.  $\lim_{x \rightarrow \infty} \frac{x^3+x-\sqrt{3x}}{\sqrt{x}}$
4.  $\lim_{x \rightarrow \infty} \frac{x^3+x-\sqrt{3x}}{5 \cdot x^{2.25} \cdot \sqrt{\sqrt{x}}}$
5.  $\lim_{x \rightarrow \infty} \frac{x^{0.1} - \sqrt{3}}{\sqrt{\sqrt{x}}}$
6.  $\lim_{x \rightarrow \infty} \frac{x^x}{2^x}$
7.  $\lim_{x \rightarrow \infty} \frac{x^x}{x(2^x)}$
8.  $\lim_{x \rightarrow \infty} \frac{\sqrt{2}^{\log^4 x^3}}{\log(2 \cdot x + 7)}$
9.  $\lim_{x \rightarrow \infty} \frac{x+1}{\frac{3 \cdot x \ln x}{2x^2}}$
10.  $\lim_{x \rightarrow \infty} \frac{\sqrt{2}^{\log x^3}}{\log^{\ln x}(2x)}$

**5.** Compute the exact values for

1.  $\int_1^n (2 \cdot x^4 + 5\sqrt{x})$
2.  $\int_1^n (x^4 - 3 \cdot x^2 + \frac{1}{x} - \frac{1}{x^2}) dx$
3.  $\int_1^n (\frac{3}{\sqrt{x}} + \ln x + e^x) dx$
4.  $\int_1^n x \cdot \sin x dx$

**6.** Use mathematical induction to prove that

$$1 + 2 + \dots + n = \frac{n(n+1)}{2}$$

**7.** Use mathematical induction to prove that

$$1 + 2^2 + \dots + n^2 = \frac{n(n+1)(2n+1)}{6}$$