

1. Consider an instance of the single-source shortest path problem with n vertices, m edges, a source vertex s , and no negative cycles. Which of the following is true?

1. For every vertex v reachable from source s , there is a shortest $s - v$ path with at most $n - 1$ edges.
2. For every vertex v reachable from the source s , there is a shortest $s - v$ path with at most n edges.
3. For every vertex v reachable from the source s , there is a shortest $s - v$ path with at most m edges.
4. There is no finite upper bound on the fewest number of edges in a shortest $s - v$ path.

(1) is the correct answer. If we had a shortest $s - v$ path with more than $n - 1$ edges then we have a non-negative cycle, removing this cycle would produce a $s - v$ path of at most $n - 1$ edges that is better than the previous solution.