



Universitat de Lleida

Preferential attachment

Report

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1 Introduction

Using an anonymous and unlinkable ring signature-based forum, the way of choosing the K set of the signature ring can affect the privacy of users. In this report is demonstrated that preferential attachment way makes users more anonymous and invulnerable from knowing its messages than uniformly random manner.

1.1 Simulation program

The simulation forum program was made in `python3`. The code can be found [here](#). Its execution was made using 200 people and Zipf distribution to determine the number of messages of each member. Also, was parametrized the maximum number of messages from an author, in order to know which member can have the worst privacy. In all cases of s from 1.3 to 2.0, the number of messages determined from the distribution is 305.

The K , the size of the ring signature, ranges from 3 to 12. In order to compare the different ways of determining the signature, it is compared with authors of 1, 5 and 15 messages.

The number of each table is calculated as an average of 10 random seeds for sampling the distribution. So, the meaning of 1 message (msm) and $K = 4$ and $s = 1.3$ means that on an average of 10 times, has a privacy score of 13.4. The score of each element is calculated by:

$$privacyScore(X) = \frac{\#X \text{ has signed a message}}{\#X \text{ has really send a message}}$$

Given all the privacy scores of the different rings using an specific Zipf distribution, then is calculated the average of an specific member of them in order to compare, in general terms, the privacy between different Zipf distributions and different ring-signature methods.

2 $s: 1,3$

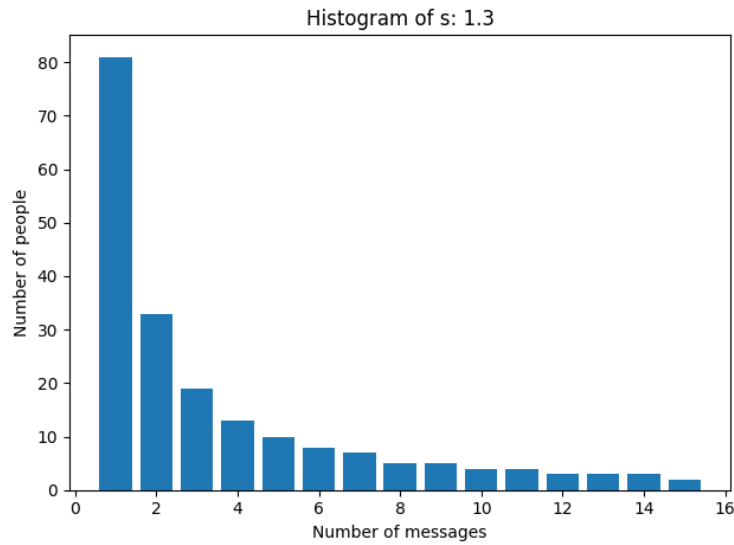


Figure 1: Histogram of Zipf Distribution using $s = 1.3$

| K | 1msm | 5msm | 15msm |
|----|-------|-------|--------|
| 3 | 10.4 | 2.34 | 1.4533 |
| 4 | 13.4 | 2.86 | 1.7533 |
| 5 | 17.7 | 3.76 | 1.9533 |
| 6 | 21.4 | 4.34 | 2.2133 |
| 7 | 24.8 | 4.82 | 2.4933 |
| 8 | 28.7 | 5.62 | 2.72 |
| 9 | 32.5 | 6.36 | 2.9267 |
| 10 | 36.7 | 7.16 | 3.2533 |
| 11 | 40.8 | 7.96 | 3.3867 |
| 12 | 44.9 | 8.84 | 3.5467 |
| | 27.13 | 5.406 | 2.57 |

Table 1: Uniformly random choice of Zipf distribution $s:1.3$

| K | 1msm | 5msm | 15msm |
|----|-------|-------|--------|
| 3 | 10.7 | 2.1 | 1.98 |
| 4 | 16.9 | 3.82 | 2.4 |
| 5 | 24.0 | 4.6 | 2.4867 |
| 6 | 28.1 | 5.22 | 2.4733 |
| 7 | 35.1 | 6.06 | 3.5 |
| 8 | 41.5 | 7.04 | 2.8733 |
| 9 | 43.4 | 6.24 | 4.5 |
| 10 | 53.4 | 7.42 | 3.66 |
| 11 | 58.2 | 8.64 | 3.64 |
| 12 | 63.6 | 8.54 | 4.0933 |
| | 37.49 | 5.968 | 3.1607 |

Table 2: Preferential attachment choice of Zipf distribution $s:1.3$

3 s: 1,4

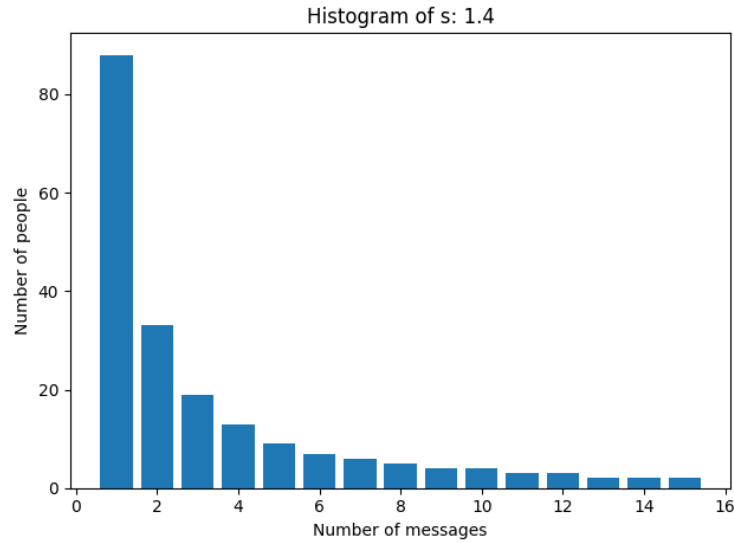


Figure 2: Histogram of Zipf Distribution using $s = 1.4$

| K | 1msm | 5msm | 15msm |
|----|-------|-------|--------|
| 3 | 10.0 | 2.24 | 1.4133 |
| 4 | 13.4 | 2.8 | 1.6333 |
| 5 | 17.5 | 3.72 | 1.8067 |
| 6 | 20.1 | 4.1 | 2.1467 |
| 7 | 24.4 | 4.74 | 2.2867 |
| 8 | 27.7 | 5.36 | 2.5467 |
| 9 | 31.2 | 6.04 | 2.7133 |
| 10 | 33.1 | 6.32 | 3.0933 |
| 11 | 38.0 | 7.12 | 3.1467 |
| 12 | 42.7 | 7.88 | 3.3867 |
| | 25.81 | 5.032 | 2.4173 |

Table 3: Uniformly random choice of Zipf distribution s :

| K | 1msm | 5msm | 15msm |
|----|-------|-------|--------|
| 3 | 10.6 | 2.12 | 2.24 |
| 4 | 17.7 | 3.48 | 2.4 |
| 5 | 25.6 | 3.66 | 2.8733 |
| 6 | 33.0 | 4.3 | 2.88 |
| 7 | 38.1 | 5.66 | 3.4667 |
| 8 | 45.1 | 6.1 | 3.28 |
| 9 | 46.5 | 7.18 | 4.1267 |
| 10 | 53.2 | 8.6 | 3.88 |
| 11 | 56.6 | 8.32 | 4.28 |
| 12 | 72.8 | 7.26 | 3.58 |
| | 39.92 | 5.668 | 3.3007 |

Table 4: Preferential attachment choice of Zipf distribution $s:1.4$

4 $s: 1,5$

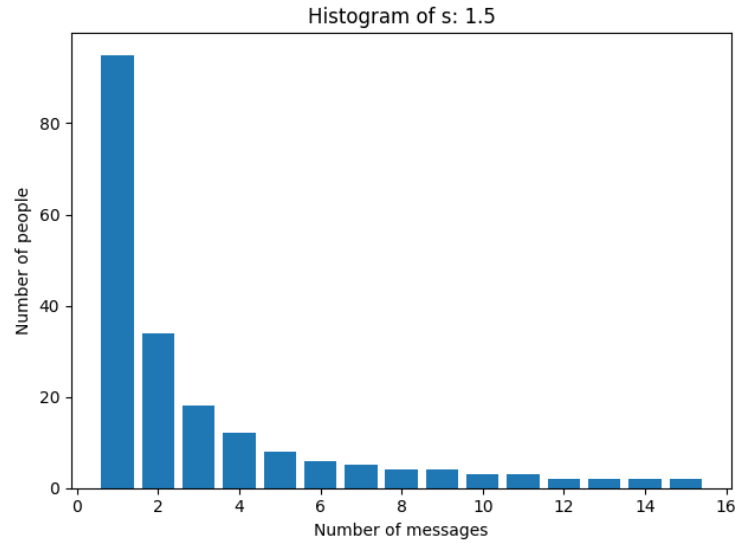


Figure 3: Histogram of Zipf Distribution using $s = 1.5$

| K | 1msm | 5msm | 15msm |
|----|-------|-------|--------|
| 3 | 8.9 | 2.12 | 1.3933 |
| 4 | 12.2 | 2.5 | 1.62 |
| 5 | 16.0 | 3.16 | 1.7733 |
| 6 | 18.6 | 3.9 | 2.0733 |
| 7 | 22.2 | 4.58 | 2.1867 |
| 8 | 25.3 | 4.98 | 2.38 |
| 9 | 30.0 | 5.66 | 2.5867 |
| 10 | 31.9 | 6.36 | 2.88 |
| 11 | 34.9 | 7.02 | 3.0333 |
| 12 | 39.4 | 7.14 | 3.2867 |
| | 23.94 | 4.742 | 2.3213 |

Table 5: Uniformly random choice of Zipf distribution $s: 1.5$

| K | 1msm | 5msm | 15msm |
|----|------|------|--------|
| 3 | 7.9 | 2.26 | 1.98 |
| 4 | 12.3 | 3.6 | 2.12 |
| 5 | 18.6 | 4.0 | 3.0867 |
| 6 | 22.0 | 4.96 | 2.7 |
| 7 | 30.0 | 5.9 | 3.6667 |
| 8 | 34.4 | 6.74 | 3.4333 |
| 9 | 40.2 | 6.06 | 3.7133 |
| 10 | 39.4 | 6.4 | 4.5467 |
| 11 | 49.2 | 7.2 | 4.0933 |
| 12 | 49.0 | 7.78 | 3.6867 |
| | 30.3 | 5.49 | 3.3027 |

Table 6: Preferential attachment choice of Zipf distribution $s:1.5$

5 $s: 1,6$

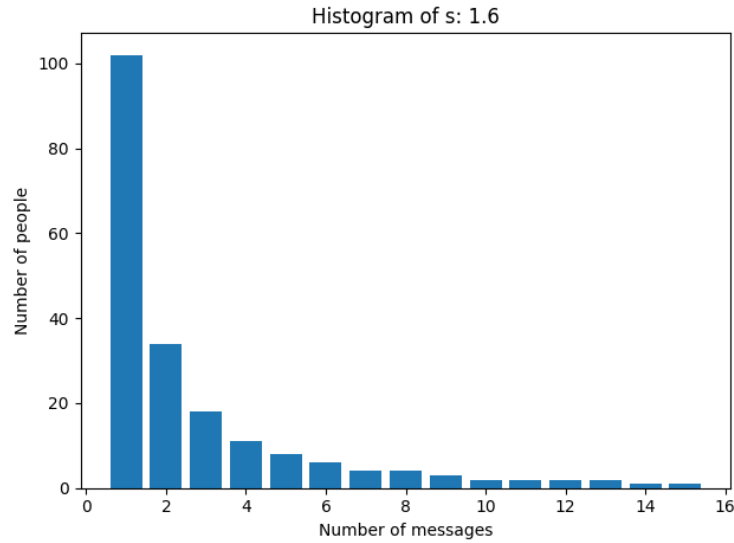


Figure 4: Histogram of Zipf Distribution using $s = 1.6$

| K | 1msm | 5msm | 15msm |
|----|-------|-------|--------|
| 3 | 8.3 | 2.22 | 1.3067 |
| 4 | 11.4 | 2.94 | 1.5667 |
| 5 | 15.3 | 3.28 | 1.7 |
| 6 | 17.8 | 3.92 | 1.9133 |
| 7 | 20.1 | 4.56 | 2.0333 |
| 8 | 23.0 | 5.1 | 2.24 |
| 9 | 27.3 | 5.44 | 2.4667 |
| 10 | 29.8 | 6.12 | 2.52 |
| 11 | 31.6 | 6.68 | 2.7133 |
| 12 | 35.0 | 7.18 | 2.9267 |
| | 21.96 | 4.744 | 2.1387 |

Table 7: Uniformly random choice of Zipf distribution $s:1.6$

| K | 1msm | 5msm | 15msm |
|----|-------|-------|--------|
| 3 | 7.1 | 2.2 | 1.8333 |
| 4 | 13.3 | 3.16 | 2.2 |
| 5 | 17.4 | 3.44 | 2.2867 |
| 6 | 19.6 | 4.84 | 2.7 |
| 7 | 25.6 | 5.32 | 2.9133 |
| 8 | 28.9 | 6.74 | 3.8 |
| 9 | 35.5 | 6.2 | 4.0933 |
| 10 | 37.5 | 6.26 | 4.1267 |
| 11 | 44.4 | 8.82 | 3.64 |
| 12 | 43.1 | 6.14 | 4.12 |
| | 27.24 | 5.312 | 3.1713 |

Table 8: Preferential attachment choice of Zipf distribution $s:1.6$

6 $s: 1,7$

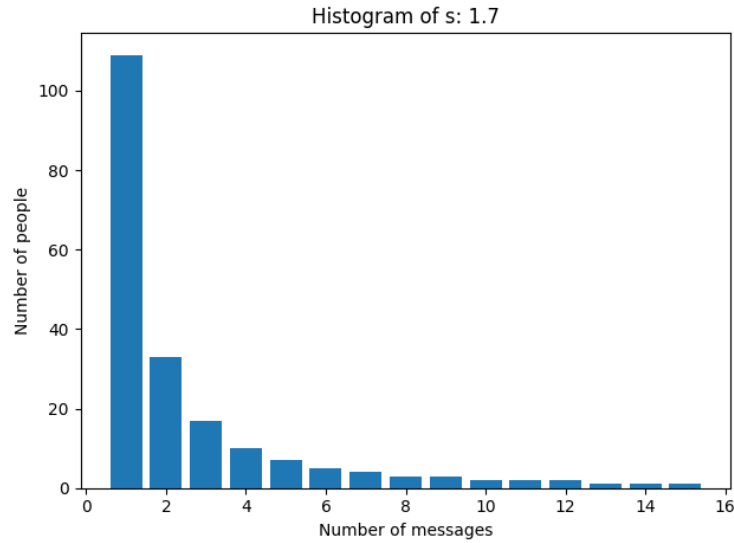


Figure 5: Histogram of Zipf Distribution using $s = 1.7$

| K | 1msm | 5msm | 15msm |
|----|-------|-------|--------|
| 3 | 7.4 | 1.98 | 1.2933 |
| 4 | 11.3 | 2.54 | 1.52 |
| 5 | 15.0 | 3.12 | 1.6533 |
| 6 | 17.4 | 3.52 | 1.86 |
| 7 | 19.4 | 4.04 | 2.0067 |
| 8 | 22.3 | 4.4 | 2.14 |
| 9 | 25.5 | 5.24 | 2.3133 |
| 10 | 27.8 | 5.9 | 2.4667 |
| 11 | 30.2 | 6.6 | 2.6333 |
| 12 | 34.0 | 6.94 | 2.8267 |
| | 21.03 | 4.428 | 2.0713 |

Table 9: Uniformly random choice of Zipf distribution $s:1.7$

| K | 1msm | 5msm | 15msm |
|----|-------|------|--------|
| 3 | 9.6 | 1.9 | 1.78 |
| 4 | 13.3 | 2.96 | 2.2733 |
| 5 | 18.1 | 3.58 | 2.52 |
| 6 | 22.3 | 3.62 | 2.7933 |
| 7 | 26.4 | 4.26 | 2.8867 |
| 8 | 32.7 | 4.76 | 3.2333 |
| 9 | 36.0 | 6.52 | 4.08 |
| 10 | 41.0 | 5.18 | 3.8133 |
| 11 | 43.6 | 7.5 | 4.02 |
| 12 | 47.6 | 6.32 | 3.34 |
| | 29.06 | 4.66 | 3.074 |

Table 10: Preferential attachment choice of Zipf distribution $s:1.7$

7 $s: 1,8$

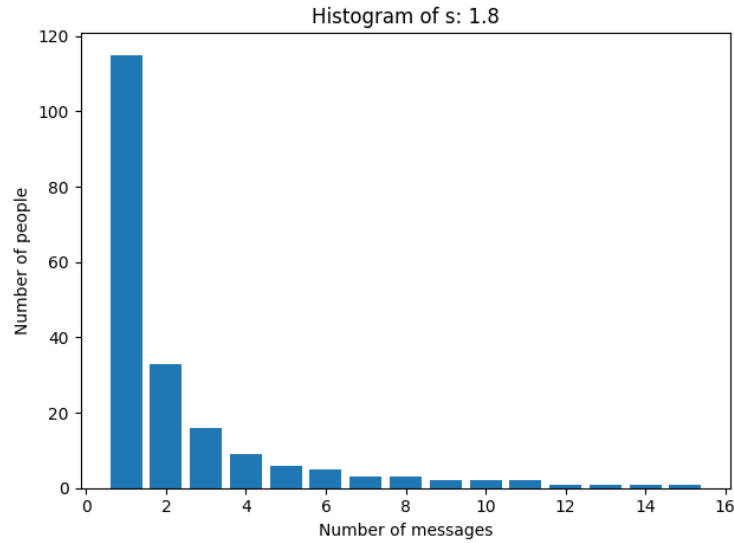


Figure 6: Histogram of Zipf Distribution using $s = 1.8$

| K | 1msm | 5msm | 15msm |
|----|-------|------|--------|
| 3 | 7.0 | 2.1 | 1.2267 |
| 4 | 10.1 | 2.42 | 1.4933 |
| 5 | 13.9 | 3.02 | 1.6133 |
| 6 | 15.5 | 3.42 | 1.8467 |
| 7 | 19.7 | 4.04 | 1.88 |
| 8 | 21.0 | 4.58 | 2.0 |
| 9 | 23.9 | 4.86 | 2.2733 |
| 10 | 26.2 | 5.42 | 2.44 |
| 11 | 28.4 | 5.96 | 2.5667 |
| 12 | 31.9 | 6.38 | 2.6933 |
| | 19.76 | 4.22 | 2.0033 |

Table 11: Uniformly random choice of Zipf distribution $s:1.8$

| K | 1msm | 5msm | 15msm |
|----|-------|------|--------|
| 3 | 7.3 | 2.68 | 1.8667 |
| 4 | 10.9 | 3.54 | 2.2933 |
| 5 | 15.1 | 2.9 | 2.2267 |
| 6 | 19.8 | 3.96 | 2.9067 |
| 7 | 23.9 | 3.04 | 2.96 |
| 8 | 27.8 | 4.16 | 3.6733 |
| 9 | 32.5 | 4.22 | 4.36 |
| 10 | 35.9 | 5.3 | 3.6267 |
| 11 | 35.3 | 4.56 | 3.8267 |
| 12 | 42.2 | 5.44 | 3.8733 |
| | 25.07 | 3.98 | 3.1613 |

Table 12: Preferential attachment choice of Zipf distribution $s:1.8$

8 s: 1,9

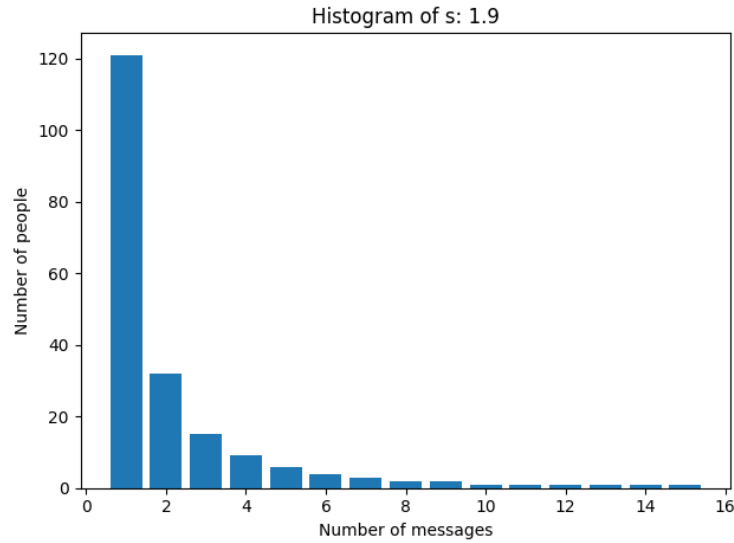


Figure 7: Histogram of Zipf Distribution using $s = 1.9$

| K | 1msm | 5msm | 15msm |
|----|-------|-------|--------|
| 3 | 6.0 | 1.72 | 1.2533 |
| 4 | 9.5 | 2.22 | 1.42 |
| 5 | 13.5 | 2.52 | 1.6 |
| 6 | 15.3 | 2.8 | 1.7933 |
| 7 | 17.9 | 3.28 | 1.8333 |
| 8 | 19.7 | 3.64 | 1.9933 |
| 9 | 22.1 | 3.82 | 2.1533 |
| 10 | 24.4 | 4.46 | 2.26 |
| 11 | 26.5 | 4.82 | 2.48 |
| 12 | 30.0 | 5.48 | 2.6 |
| | 18.49 | 3.476 | 1.9387 |

Table 13: Uniformly random choice of Zipf distribution $s:1.9$

| K | 1msm | 5msm | 15msm |
|----|-------|-------|--------|
| 3 | 6.9 | 3.04 | 1.9067 |
| 4 | 10.6 | 2.82 | 2.26 |
| 5 | 14.0 | 3.26 | 2.0533 |
| 6 | 18.1 | 5.44 | 2.3933 |
| 7 | 21.1 | 4.42 | 2.7533 |
| 8 | 24.4 | 6.64 | 3.1067 |
| 9 | 28.5 | 4.42 | 3.4 |
| 10 | 30.9 | 5.24 | 5.0533 |
| 11 | 39.2 | 6.96 | 4.2467 |
| 12 | 37.7 | 7.38 | 4.5933 |
| | 23.14 | 4.962 | 3.1767 |

Table 14: Preferential attachment choice of Zipf distribution $s:1.9$

9 s: 2,0

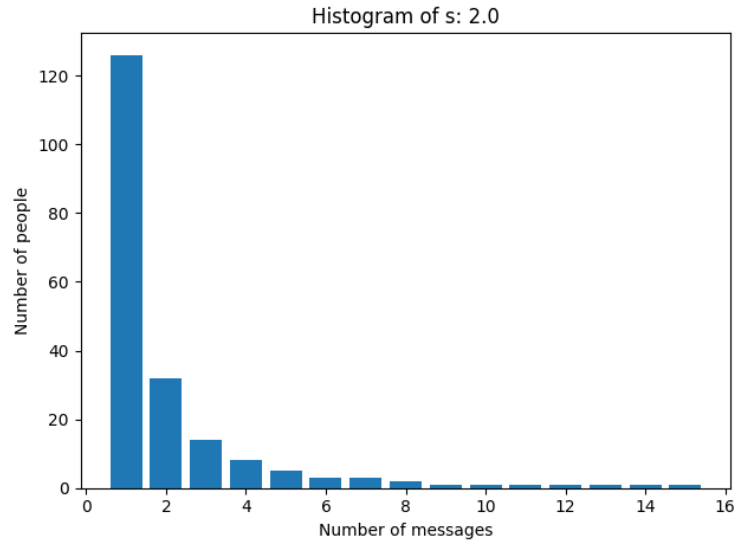


Figure 8: Histogram of Zipf Distribution using $s = 2.0$

| K | 1msm | 5msm | 15msm |
|----|-------|-------|--------|
| 3 | 6.4 | 2.0 | 1.2467 |
| 4 | 9.0 | 2.4 | 1.3933 |
| 5 | 12.9 | 2.8 | 1.6333 |
| 6 | 14.4 | 3.36 | 1.7133 |
| 7 | 17.5 | 3.84 | 1.8133 |
| 8 | 19.0 | 4.3 | 1.9933 |
| 9 | 21.6 | 4.8 | 2.04 |
| 10 | 23.2 | 5.24 | 2.2533 |
| 11 | 24.4 | 5.56 | 2.3533 |
| 12 | 28.4 | 5.88 | 2.5733 |
| | 17.68 | 4.018 | 1.9013 |

Table 15: Uniformly random choice of Zipf distribution $s:2.0$

| K | 1msm | 5msm | 15msm |
|----|------|-------|--------|
| 3 | 6.5 | 2.62 | 1.66 |
| 4 | 9.5 | 3.1 | 2.1533 |
| 5 | 14.2 | 3.84 | 2.3933 |
| 6 | 17.5 | 4.42 | 2.74 |
| 7 | 20.7 | 5.42 | 2.7733 |
| 8 | 23.6 | 3.58 | 3.14 |
| 9 | 26.8 | 6.34 | 3.7667 |
| 10 | 29.2 | 4.94 | 3.14 |
| 11 | 32.0 | 5.5 | 3.7133 |
| 12 | 36.0 | 7.9 | 4.4933 |
| | 21.6 | 4.766 | 2.9973 |

Table 16: Preferential attachment choice of Zipf distribution $s:2.0$