

### P3: Backtracking in Prolog

1. Given  $N$  2D coordinates, find all colinear subsets.
2. Given an integer  $N$ , find all ways to express the number as a sum of distinct primes.
3. Given a list  $a_1, \dots, a_n$ , find all strictly increasing sublists.
4. Given two natural numbers,  $n$  and  $m$ , find all possible ways of arranging the numbers between 1 and  $n$  such that the absolute difference between two adjacent numbers is  $m$ .
5. Find all size  $N$  sublists of a list. E.g.,  $[2,3,4]$   $N=2 \Rightarrow [[2,3],[2,4],[3,4]]$
6. Find all lists of  $N$  correctly closed pairs of parentheses. E.g.,  $n=4$   $((()))$  si  $((())())$
7. Find all arrangements of size  $K$  of a list. E.g.,  $[2,3,4]$   $K=2 \Rightarrow [[2,3], [3,2], [2,4], [4,2], [3,4], [4,3]]$ , not necessarily in this order
8. A sports bet player wants to bet on 4 soccer matches. The bets can be 1,X,2. Find all bets knowing that the last bet can't be 2 and there can be no more than two X bets.
9. Given a value  $N$ , find all permutations of  $N$  elements knowing that for any value  $i$ ,  $2 \leq i \leq n$ , there exists  $j$ ,  $1 \leq j \leq i$ , such that  $|p(i) - p(j)| = 1$ .
10. Given a list of distinct integers  $a_1, \dots, a_n$ , find all sublists whose sum is divisible by  $n$ .
11. Find all sublists of length  $2n + 1$  containing 0, -1, or 1, such that  $a_1 = 0$ ,  $a_{2n+1} = 0$  and  $|a_{i+1} - a_i| \in \{1, 2\}$
12. Given a list of distinct integers, find all sublists resembling a mountain, i.e., the sublists starts with an ascending sequence followed by a descending sequence. E.g., (10 16 27 18 14 7).
13. Given a graph of  $n$  countries on a map where the nodes are the countries and the edges represent that the two countries are neighbours. Find all ways to color  $n$  countries with  $m$  colors where no two neighbouring countries share a color.
14. Find all sublists that sum up to  $S$  of a list. E.g.,  $[1,2,3,4,5,6,10]$  si  $S=10 \Rightarrow [[1,2,3,4], [1,4,5], [2,3,5], [4,6], [10]]$  not necessarily in that order.
15. Given a positive number, find all ways of expressing that number as a sum of consecutive natural numbers.