ML process of training a piece of software, called model, to make useful predictions or to generate content from data.

Types:

- Supervised learning(two most common use cases regression and classification) • Unsupervised learning(clusterization common)

Feature(x) the variable in the data vector. Types:

1. Numerical

2. Categorical

- Ordinal
- Nominal

 $X \longrightarrow F \longrightarrow y$

Regression model predicts continuous values.

1.4. Reinforement learning

Gradient(∇f) defines direction and rate of fastest increase of scalar-valued differentiable function f. Example for gradient in cartesian coordinate system f:

2.2. Optimization

2.1. Gradient descent

Stop criteria for the gradient descent can be a threshold for the gradient value.

Optimisation target minimize loss function. Simple example of the loss function is a MSE.

Mean squared error(MSE) measures the average of squeared errors.
$$\mathrm{MSE} = \frac{1}{N} \sum_{(x,y) \in D} \left(y - \mathrm{prediction}(x) \right)^2$$

Iteration step for model paraneter:

• simple - 1 full dataset • stochastic - 1 record

TODO

epoch one pass of all the training examples

[Comparison of batch sizes link]

batch size the number of training examples in one pass. The higher the batch size, the more memory space you'll need. iterations number of batches in epoch. each iteration adjusts model's parameters.

Simplify each *i* argument:

Final differential formula:

Let's simplify function for two parameters and 3 data slices: $\frac{1}{2N} \sum_{i=1}^{3} \left(\left(\sum_{i=1}^{2} (\Theta_{j} x_{j}) - y_{i} \right)^{2} \right)$

$$((\Theta_0 x_0 + C_i)^2)' = 2(\Theta_0 x_0 + C_i)(x_0)$$

$$\Theta_i \longrightarrow \operatorname{gradient} \longrightarrow \Theta_i^T$$
 solve this linear regression problem we denote the solution of th

Process is simple, count gradient for each parameter and change parameters by gradient descent.

 $\frac{\partial f}{\partial \Theta_i} = x_i \frac{1}{N} \sum_{i=1}^n \left(\sum_{j=1}^m \Theta_j x_j - y_i \right)$

3. Data

overfitting.

4. Classification

 $y \in \{1, 2, 3, .., k\}$

Regularization formula L1(makes feature selection):

Task make a function, that separates known classes.

bias

variance

TODO

Figure 1: Synthetic features for regression with linear Θ params How to choose function to create additional features? Intuitively as a hyperparams. There are automatic methods

TODO https://www.statlect.com/fundamentals-of-statistics/normal-linear-regression-model

not have semantic intersections(same people, same cars, same buildings etc.).

to make models - feature selection approach.

2.3.1. Normal Linear Regression Model

Solves regression and classification tasks.

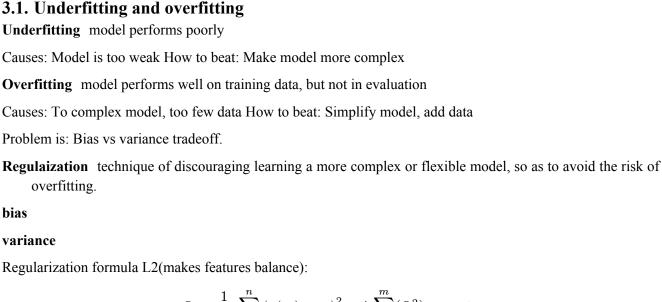
Where h is a learning step. How much *i*'s would be in a N dataset?

$$\overline{\partial\Theta_i} = \overline{2N} \sum_{i=1}^{\infty} \left(\left(\sum_{j=1}^{\infty} (\Theta_j x_j) - y_i \right) \right)$$
 note: N is the iteration dataset(or batch) size, x_j is a point in vector, Θj is the parameter value that is const if not differentiated, y_i is a constant for each i.

$$\Theta_1 x_1$$
 and y_i is a constants if we differentiate by Θ_0 , so we have: $\left(\left(\Theta_0 x_0 + C_i\right)^2\right)'$, also: $\left(\Theta_0 x_0 + C_i\right)$ is an inside f v .

 $\left(\sum_{i=1}^{2} (\Theta_{j} x_{j}) - y_{i}\right)^{2} = (\Theta_{0} x_{0} + \Theta_{1} x_{1} - y_{i})^{2}$

2.3. Linear regression When we have not linear plot, to solve this linear regression problem we can add additional polynomial(
$$x^2$$
) or functional($\sin(x)$, \sqrt{x}) features.



Dataset should be divided minimum for train(60), validation(20) and final test(20). This divided datasets must

Cross validation - method, which on small dataset find conceptual ML model that possibly solves task. TODO

Figure 2: Classification visualization

Firstly, we will solve binary classification task {0, 1}. Model will have 1 output - probability of x is from class 1.

Accordingly to image, linear regression is not suitable for this type of task(especially right)

 $L = \frac{1}{2N} \sum_{i=1}^{n} (y(x_i) - y_i)^2 + \Lambda \sum_{i=1}^{m} (|\Theta|) \longrightarrow \min_{\Theta}$

Figure 3: Logistic regression 4.1.1. Formula

Precision TP/(TP+FP). How model is confident for class a. Recall TF/(TF+FN). Which coverage for class a.

 $\frac{\partial f}{\partial \Theta_i} = -\frac{1}{N} \sum_{i=1}^n \left(y_i \log(p_i) + (1-y_i) \log(1-p_i) \right)'$

Linear examples: • Predicting the height of an adult based on the mother's and father's height • Predicting pumpkin sales volume based on the price, time of year, and store location

- 6. Removing correlated features Before train model it may be worth to perform "dimensionality reduction" to save space, without loosing too
- https://en.wikipedia.org/wiki/Logistic regression • file:

Logistic examples:

- **7.** Lib • https://www.statlect.com/

Loss for gradient:

4.2. Metrics

Criteria

Target

Usecase

Distribution type

Regression plot dependency

- file:

- https://towardsdatascience.com/logistic-regression-detailed-overview-46c4da4303bc

- Reinforcement learning(penalties and rewards->generated policy) • Generative AI(generate something from input)
- Online and batch learning. Y - the variable that we predict.
- 1.1. Data mining Data mining applying ML techniques to dig into large amounts of data can help discover factors, that are not immediately apparent.

Hyperparam meta parameter for model. Model do not learn it.

- 1.2. Supervised
- Classification model predicts categorical values. 1.3. Unsupervised $X \longrightarrow F \longrightarrow X'$
- The learning system, called agent can observe the environment, select and perform actions, and get rewards or
- penalties. It must learn then by itself what is the best strategy, called a policy to get the most reward over the time.
- 2. Optimisation and loss function
- $\nabla f = \frac{\partial f}{\partial x}i + \frac{\partial f}{\partial y}i + \frac{\partial f}{\partial z}k$ **Gradient descent** iterative optimization algorithm of the first order to find the local minimum of the function.
 - $\Theta^{i+1} = \Theta^i h \frac{\partial f}{\partial \Theta^i}$
- Depends, upon model converges. Possible data slices for 1 ephoch: • mini-batch - batch of random examples(e.g. 10-1000). This approach can support struggling with local min-
 - $\frac{\partial f}{\partial \Theta_i} = \frac{1}{2N} \sum_{i=1}^n \left(\left(\sum_{j=1}^m (\Theta_j x_j) y_i \right)^2 \right)$

inside f
$$v$$
.

With formula of compound derivative $(u(v))' = u'(v) * v'$

$$y = \frac{\theta_0}{\theta_1} + \frac{\theta_1 \chi_1 + \theta_2 \chi_2}{\theta_2 \chi_1 + \theta_3 \chi_1^2 + \theta_4 \chi_1^2 + \theta_5 \chi_1 \chi_2}$$

oo weak How to beat: Make model more complex el performs well on training data, but not in evaluation ex model, too few data How to beat: Simplify model, add data is variance tradeoff. Ethnique of discouraging learning a more complex or flexible model, so a mula L2(makes features balance):
$$L = \frac{1}{2N} \sum_{i=1}^{n} \left(y(x_i) - y_i \right)^2 + \Lambda \sum_{i=1}^{m} (\Theta_i^2) \longrightarrow \min_{\Theta}$$

4.1. Logistic regression **Logistic regression** type of regression that predicts a probability of an outcome given one or more independent variables. With a threshold returned probability can be mapped to a discrete value.

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p_i - model output probability for i example. (class 1) $BCE = -y_i \log(p_i) - (1 - y_i) \log(1 - p_i)$ $\begin{cases} \text{TP } y_i, p_i = \{1,1\} \text{ BSE} = 0 \\ \text{TN } y_i, p_i = \{0,0\} \text{ BSE} = 0 \\ \text{FN } y_i, p_i = \{1,0\} \text{ BSE} \rightarrow \inf \\ \text{FP } y_i, p_i = \{0,1\} \text{ BSE} \rightarrow \inf \end{cases}$ $L = -\frac{1}{N} \sum_{i=1}^n (y_i \log(p_i) + (1-y_i) \log(1-p_i)) \longrightarrow \min$

 $\begin{cases} -\log(p_i), y_i = 1 \\ -\log(1-p_i), y_i = 0 \end{cases}$

Output type Continuous

To define success of model **metrics** are used. $A = \left(\frac{N_{\text{correct}}}{N}\right) 100\%$

 Predicting if a person will get a disease based on status, salary, genetics • Prediction if a person will quit a job based on meetings, pull requests, office time. • Predicting the marriage of a person based by car, salary, outlook, office time, education, country.

- https://towardsdatascience.com/
- 299 page

- Logistic regression is a S-shaped curve: $y = \frac{1}{1 + e^{-\sum_{i=1}^{m} \Theta_i X_i + \Theta_0}}$ 4.1.2. Loss function BCE(Binary cross entropy) loss function
 - 5. Regressions comparison Linear regression Logistic
 - Define type of a tumor, is price > 500k\$ Predict house prise **Binomial** Normal
 - much information