1. Introduction

ML process of training a piece of software, called model, to make useful predictions or to generate content from data.

Types:

- Supervised learning(two most common use cases regression and classification) • Unsupervised learning(clusterization common)
- Reinforcement learning(penalties and rewards->generated policy)
- Generative AI(generate something from input)
- \boldsymbol{Y} the variable that we predict.
- **Feature**(x) the variable in the data vector. Types:
- 1. Numerical
- 2. Categorical Ordinal
- 1.1. Supervised

Nominal

Hyperparam meta parameter for model. Model do not learn it.

Solves regression and classification tasks. $X \longrightarrow F \longrightarrow y$

Regression model predicts continuous values.

Classification model predicts categorical values.

 $X \longrightarrow F \longrightarrow X'$

1.3. Reinforement learning

TODO

1.2. Unsupervised

Gradient(∇f) defines direction and rate of fastest increase of scalar-valued differentiable function f.

Stop criteria for the gradient descent can be a threshold for the gradient value.

Gradient descent iterative optimization algorithm of the first order to find the local minimum of the function.

2.2. Optimization Optimisation target minimize loss function.

 $MSE = \frac{1}{N} \sum_{(x,y) \in D} (y - prediction(x))^{2}$

 $\Theta^{i+1} = \Theta^i - h \frac{\partial f}{\partial \Theta^i}$

mini-batch - batch of random examples (e.g. 10-1000). This approach can support struggling with local min-

Iteration step for model paraneter:

How much *i*'s would be in a N dataset? Depends, upon model converges. Possible data slices for 1 ephoch:

iterations number of batches in epoch. each iteration adjusts model's parameters.

batch size the number of training examples in one pass. The higher the batch size, the more memory space

you'll need.

TODO

 $\frac{\partial f}{\partial \Theta_i} = \frac{1}{2N} \sum_{i=1}^n \left(\left(\sum_{j=1}^m (\Theta_j x_j) - y_i \right)^2 \right)$

note: N is the iteration dataset(or batch) size, x_j is a point in vector, Θj is the parameter value that is const if not

$$\left(\sum_{j=1}^2 (\Theta_j x_j) - y_i\right)^2 = (\Theta_0 x_0 + \Theta_1 x_1 - y_i)^2$$

$$\Theta_1 x_1 \text{ and } y_i \text{ is a constants if we differentiate by } \Theta_0, \text{ so we have: } \left((\Theta_0 x_0 + C_i)^2\right)', \text{ also: } (\Theta_0 x_0 + C_i) \text{ is an inside f } v.$$

 $((\Theta_0 x_0 + C_i)^2)' = 2(\Theta_0 x_0 + C_i)(x_0)$

 $\frac{\partial f}{\partial \Theta_i} = x_i \frac{1}{N} \sum_{i=1}^n \left(\sum_{j=1}^m \Theta_j x_j - y_i \right)$

Final differential formula:

2.3. Linear regression

inside f v.

TODO

2.3. Linear regression
When we have not linear plot, to solve this linear regression problem we can add additional polynomial(
$$x^2$$
) or functional($\sin(x)$, \sqrt{x}) features

functional($\sin(x), \sqrt{x}$) features. y = 00 + 0121 + 02212 + 0321 + 04X1 + 04X1 + 0521 X1

Figure 1: Synthetic features for regression with linear Θ params

How to choose function to create additional features? Intuitively as a hyperparams. There are automatic methods

Problem is: Bias vs variance tradeoff.

overfitting.

4. Classification

 $y \in \{1, 2, 3, .., k\}$

bias

variance

3. Data

to make models - feature selection approach.

Dataset should be divided minimum for train(60), validation(20) and final test(20). This divided datasets must not have semantic intersections(same people, same cars, same buildings etc.). Cross validation - method, which on small dataset find conceptual ML model that possibly solves task. TODO

Regularization formula L2(makes features balance): $L = \frac{1}{2N} \sum_{i=1}^n \left(y(x_i) - y_i\right)^2 + \Lambda \sum_{i=1}^m (\Theta_i^2) \longrightarrow \min_{\Theta}$

Regulaization technique of discouraging learning a more complex or flexible model, so as to avoid the risk of

4.1. Logistic regression

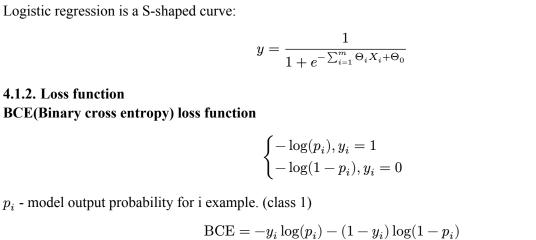
3.1. Underfitting and overfitting **Underfitting** model performs poorly Causes: Model is too weak How to beat: Make model more complex Overfitting model performs well on training data, but not in evaluation

Causes: To complex model, too few data How to beat: Simplify model, add data

Regularization formula L1(makes feature selection): $L = \frac{1}{2N} \sum_{i=1}^{n} (y(x_i) - y_i)^2 + \Lambda \sum_{i=1}^{m} (|\Theta|) \longrightarrow \min_{\Theta}$

Figure 2: Classification visualization Accordingly to image, linear regression is not suitable for this type of task(especially right) Firstly, we will solve binary classification task $\{0, 1\}$. Model will have 1 output - probability of x is from class 1.

variables. With a threshold returned probability can be mapped to a discrete value.



 $\begin{cases} \text{TP } y_i, p_i = \{1,1\} \text{ BSE} = 0 \\ \text{TN } y_i, p_i = \{0,0\} \text{ BSE} = 0 \\ \text{FN } y_i, p_i = \{1,0\} \text{ BSE} \rightarrow \inf \\ \text{FP } y_i, p_i = \{0,1\} \text{ BSE} \rightarrow \inf \end{cases}$

 $L = -\frac{1}{N} \sum_{i=1}^n (y_i \log(p_i) + (1-y_i) \log(1-p_i)) \longrightarrow \min$

 $\frac{\partial f}{\partial \Theta_i} = -\frac{1}{N} \sum_{i=1}^n \left(y_i \log(p_i) + (1 - y_i) \log(1 - p_i) \right)'$

Linear regression Logistic

2.1. Gradient descent

 $\nabla f = \frac{\partial f}{\partial x}i + \frac{\partial f}{\partial y}i + \frac{\partial f}{\partial z}k$

Example for gradient in cartesian coordinate system f:

Where
$$h$$
 is a *learning step*.

differentiated, y_i is a constant for each i.

Let's simplify function for two parameters and 3 data slices:

 $\frac{1}{2N} \sum_{i=1}^{3} \left(\left(\sum_{i=1}^{2} (\Theta_{j} x_{j}) - y_{i} \right)^{2} \right)$ Simplify each *i* argument:

Process is simple, count *gradient* for each *parameter* and change parameters by gradient descent.
$$\Theta_i \longrightarrow \text{gradient} \longrightarrow \Theta_i^T$$

With formula of compound derivative (u(v))' = u'(v) * v'

Task make a function, that separates known classes.

Logistic regression type of regression that predicts a probability of an outcome given one or more independent

4.2. Metrics

Criteria

Target

Usecase

Loss for gradient:

4.1.1. Formula

Straight line S-shaped curve Probability (0,1) of the value

Distribution type

Linear examples:

 Predicting pumpkin sales volume based on the price, time of year, and store location Logistic examples: • Predicting if a person will get a disease based on status, salary, genetics • Prediction if a person will quit a job based on meetings, pull requests, office time. Predicting the marriage of a person based by car, salary, outlook, office time, education, country.

Regression plot dependency Output type

Precision TP/(TP+FP) Recall TF/(TF+FN)

5. Regressions comparison

Give a most precise number Give a probability of belonging to category Predict house prise Define type of a tumor, is price > 500k\$ Normal **Binomial**

6. Lib https://www.statlect.com/

• file:

299 page

To define success of model **metrics** are used. $A = \left(\frac{N_{\mathrm{correct}}}{N}\right) 100\%$

Continuous

• Predicting the height of an adult based on the mother's and father's height

• https://towardsdatascience.com/logistic-regression-detailed-overview-46c4da4303bc

from the finite category

• https://en.wikipedia.org/wiki/Logistic regression