Тесты

Тест 1(n = 15)

```
format long;
n = 15;
H = hilb(n);
e = ones(n,1);
b = H*e;
x_lu = LU_solve(H,b);
x_qr = QR_solve(H,b);
```

Норма погрешностей:

```
norm(x_lu - e)
ans =
   14.477418322101377

norm(x_qr - e)
ans =
   1.515345701284949e+02
```

Исследование влияния параметра регуляризации:

```
alpha = 1e-12;
E = eye(n);
d = zeros(1e4,1);
for i = 1:1e4
    A = H + alpha*i*E;
    x = QR_solve(A,b);
    d(i) = norm(x - e);
end
semilogx(alpha*(1:1e4),d);
title('QR');
xlabel('$\alpha$','Interpreter',"latex");
ylabel('d');
```

```
7 × 10<sup>-4</sup>
                                                                                    QR
      6
      5
      4
b
      3
      2
      1
      0
                                                                                  10<sup>-10</sup>
     10<sup>-12</sup>
                                                                                                                          10<sup>-9</sup>
                                            10<sup>-11</sup>
                                                                                                                                                                10<sup>-8</sup>
                                                                                      \alpha
```

```
[m,i] = min(d);
disp('Минимум при альфа:');
```

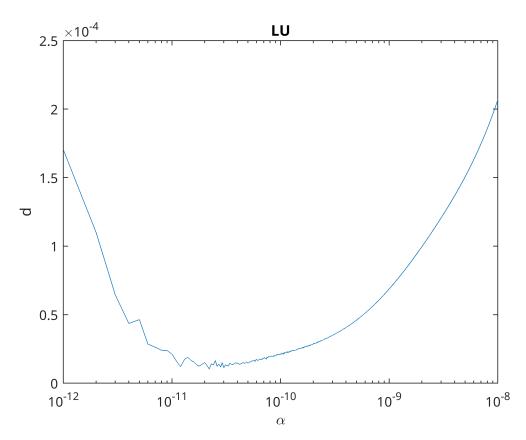
Который равен:

```
m
```

1.557714868056843e-05

```
alpha = 1e-12;
E = eye(n);
d = zeros(1e4,1);
for i = 1:1e4
    A = H + alpha*i*E;
    x = LU_solve(A,b);
    d(i) = norm(x - e);
end
semilogx(alpha*(1:1e4),d);
title('LU');
```

```
xlabel('$\alpha$','Interpreter',"latex");
ylabel('d');
```



```
[m,i] = min(d);
disp('Минимум при альфа:');
```

Который равен:

```
m = 1.033167731781375e-05
```

Тест 2(n = 20)

```
n = 20;
H = hilb(n);
e = ones(n,1);
b = H*e;
x_lu = LU_solve(H,b);
```

```
x_qr = QR_solve(H,b);
```

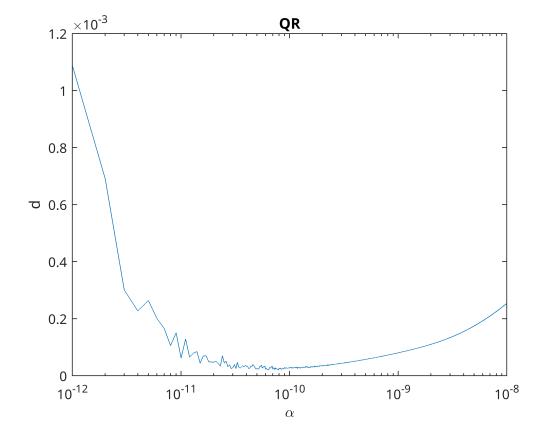
Норма погрешностей:

```
norm(x_lu - e)
ans =
    1.276901113376399e+02

norm(x_qr - e)
ans =
    4.329126736148064e+02
```

Исследование влияния параметра регуляризации:

```
alpha = 1e-12;
E = eye(n);
d = zeros(1e4,1);
for i = 1:1e4
    A = H + alpha*i*E;
    x = QR_solve(A,b);
    d(i) = norm(x - e);
end
semilogx(alpha*(1:1e4),d);
title('QR');
xlabel('$\alpha$','Interpreter',"latex");
ylabel('d');
```



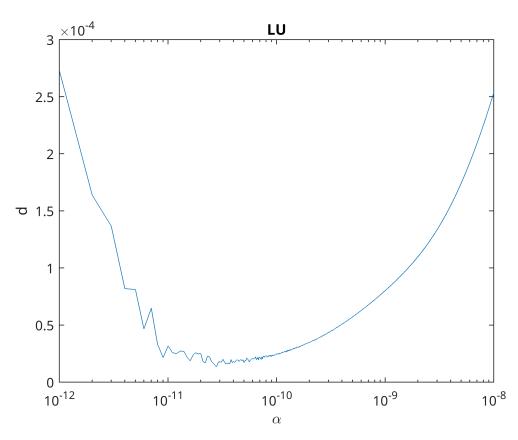
```
[m,i] = min(d);
disp('Минимум при альфа:');
```

Который равен:

```
m
```

m = 2.022569013333741e-05

```
alpha = 1e-12;
E = eye(n);
d = zeros(1e4,1);
for i = 1:1e4
    A = H + alpha*i*E;
    x = LU_solve(A,b);
    d(i) = norm(x - e);
end
semilogx(alpha*(1:1e4),d);
title('LU');
xlabel('$\alpha$','Interpreter',"latex");
ylabel('d');
```



```
[m,i] = min(d);
disp('Минимум при альфа:');
```

Который равен:

```
m = 1.363301345515417e-05
```

Тест 3(n = 25)

```
n = 25;
H = hilb(n);
e = ones(n,1);
b = H*e;
x_lu = LU_solve(H,b);
x_qr = QR_solve(H,b);
```

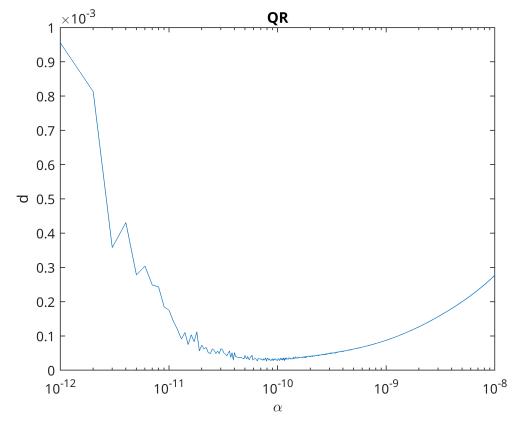
Норма погрешностей:

```
norm(x_lu - e)
ans =
    6.454667338562547e+02

norm(x_qr - e)
ans =
    4.567302536131110e+02
```

Исследование влияния параметра регуляризации:

```
alpha = 1e-12;
E = eye(n);
d = zeros(1e4,1);
for i = 1:1e4
    A = H + alpha*i*E;
    x = QR_solve(A,b);
    d(i) = norm(x - e);
end
semilogx(alpha*(1:1e4),d);
title('QR');
xlabel('$\alpha$','Interpreter',"latex");
ylabel('d');
```



```
[m,i] = min(d);
```

```
disp('Минимум при альфа:');
```

```
i*alpha

ans = 7.900000000000000000e-11

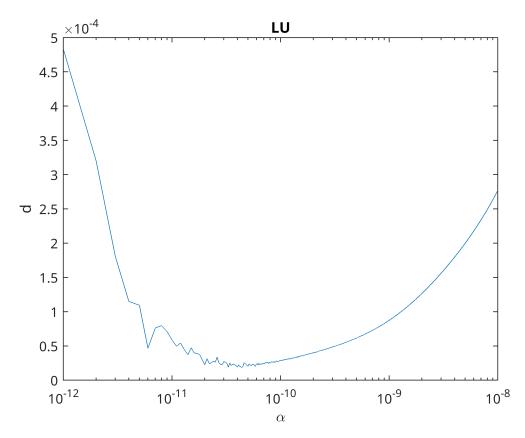
disp('Который равен:');
```

Который равен:

```
m =
```

2.630347261279233e-05

```
alpha = 1e-12;
E = eye(n);
d = zeros(1e4,1);
for i = 1:1e4
    A = H + alpha*i*E;
    x = LU_solve(A,b);
    d(i) = norm(x - e);
end
semilogx(alpha*(1:1e4),d);
title('LU');
xlabel('$\alpha$','Interpreter',"latex");
ylabel('d');
```



```
[m,i] = min(d);
disp('Минимум при альфа:');
```

```
i*alpha
```

ans =

4.400000000000000e-11

```
disp('Который равен:');
```

Который равен:

m

m =

1.856914958199387e-05

$$[1_1,u_1] = LU(H);$$