

```
In[4]:= SetDirectory[ParentDirectory[NotebookDirectory[]]];
Needs["SSSiCv100`"];
IC = IndexedConcatenate; Cat = Concatenate;
```

Write a decimal in IC from, then do an operation on it

Simple multiplication 1

$$\frac{1}{3} = 0.333 \dots = 0.\overline{3} = 0.\overset{\infty}{\text{€}3}$$

$$3 \left(\frac{1}{3}\right) = 0.999 \dots = 0.\overline{9} = 0.\overset{\infty}{\text{€}9}$$

$$2 \left(\frac{1}{3}\right) = 0.666 \dots = 0.\overline{6} = 0.\overset{\infty}{\text{€}6}$$

Simple multiplication 2

$$\frac{1}{7} = 0.\overline{142857} = 0.\overset{\infty}{\text{€}(142857)}$$

$$2 \left(\frac{1}{7}\right) = 0.\overline{285714} = 0.\overset{\infty}{\text{€}(285714)}$$

Simple multiplication 3

$$0.010010001 \dots = 0.\overset{\infty}{\text{€}} \left(\left(\overset{i}{\underset{j=1}{\text{€}0}} \right) 1 \right)$$

$$5 (0.010010001 \dots) = 0.\overset{\infty}{\text{€}} \left(\left(\overset{i}{\underset{j=1}{\text{€}0}} \right) 5 \right)$$

Division 1: method = partially unpack

$$\frac{1}{7} = 0.\overset{\infty}{\text{€}(142857)} = 0.142857\overset{\infty}{\text{€}(142857)}$$

$$\begin{aligned} \frac{1}{2} \left(\frac{1}{7}\right) &= \frac{0.142857142857\overset{\infty}{\text{€}(142857)}}{2} = 0.\frac{142857142857}{2} \frac{\overset{\infty}{\text{€}(142857)}}{2} \\ &= 0.071428571428 \frac{1\overset{\infty}{\text{€}(142857)}}{2} = 0.071428571428571428 \frac{1\overset{\infty}{\text{€}(142857)}}{2} \end{aligned}$$

$$= 0.071428 \overset{\infty}{\text{€}(571428)} = 0.0 \overset{\infty}{\text{€}(714285)}$$

Not simple! Relies on our recognizing that a pattern has been established.

Division 2:

$$\frac{1}{3} \left(\frac{1}{7}\right) = \frac{0.142857142857\overset{\infty}{\text{€}(142857)}}{3} = 0.\frac{142857142857}{3} \frac{\overset{\infty}{\text{€}(142857)}}{3} = 0.047619047619 \frac{\overset{\infty}{\text{€}(142857)}}{2} = 0.\overset{\infty}{\text{€}(047619)}$$

Easier! But still requires human recognition.