# FAQ: "Sessie" Introduction

SetDirectory[ParentDirectory[NotebookDirectory[]]]; Needs["SSSiCv100`"];

The toy "universe" is a string of characters, whose initial state can have any length and can contain any characters. (Two infinities here: length of string and size of the alphabet from which the characters are taken.) The "laws of nature" for the SSS are codified by a ruleset: a set of replacement instructions, each giving a string to search for and the string to replace it with. Ex: {"AB"->"BA"}. (More infinities: there is no limit on the number of rules in the ruleset, nor on the size of the strings, nor on the characters in the strings.)

In a sequential substitution system, rules must be applied sequentially in order (use the first rule if possible, the second only if the first fails, etc.) from left-to-right: if the first usable rule can be used at multiple locations in the state string, we apply it in the first possible (left-most) position.

Each application of any rule is an event, and each event destroys and/or creates cells (or letters) in the state string. Two events are considered to be causally connected if a cell created by one is destroyed by the other. (Later we'll explain more about how the causal network connections work, i.e. the lines that connect the nodes.)

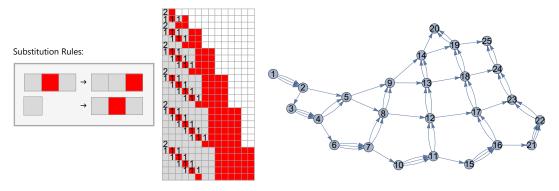
The causal network of an SSS can be visualized by treating all events as graph nodes and the causal connections between them as graph edges.

The basic command to display a Sessie is SSS. The template for usage is:

SSS[ruleset, initial state, number of steps, options]

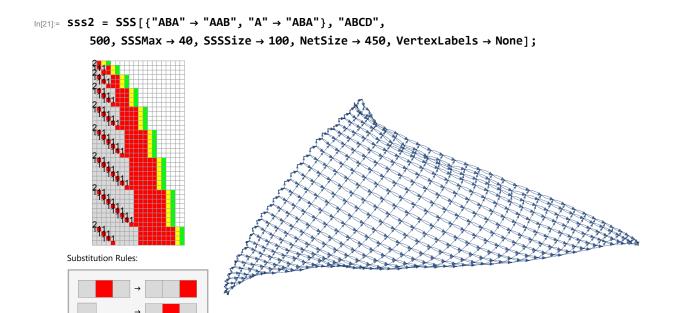
Ex:

ln[20]:= SSS1 = SSS[{"ABA"  $\rightarrow$  "AAB", "A"  $\rightarrow$  "ABA"}, "AB", 25, RulePlacement → Left, SSSSize → 100, NetSize → 300];



Try changing the rules in the ruleset, or the initial state string, or the number of steps. Or try it with some options:

In[18]:=



To find more information on any function use a question mark. For example:

#### In[ • ]:= ? SSS

Symbol

SSS[ruleset, init, n, opts] creates and displays a sequential substitution system (SSS) and its causal network, using ruleset (as a list of rules, or a RSS index), starting with the state init (using string notation), allowing the SSS to evolve for *n* steps. If the initial state string is omitted, SSSInitialState is called to provide a sufficiently complex string. Use the option EarlyReturn to give/deny permission to quit early if the SSS can be identified as dead or repeating.) Use option Mode  $\rightarrow$ Silent to suppress display of the sessie. Any other options given are passed on to SSSDisplay.

Out[ • ]=

(Returns a copy of the SSS that can then be displayed or manipulated without rebuilding, using SSSDisplay, SSSAnimate, or directly, looking at its keys, "Evolution" and "Net", etc.)

#### In[\*]:= ? SSSDisplay

Symbol SSSDisplay[sss, opts] displays the sequential substitution system sss and/or its causal network. Use SSS (or SSSInitialize and SSSEvolve) to construct it first. Options:  $Min \rightarrow n$  cuts off the display before the first n steps of the system. (Separate values can be specified for SSSMin and NetMin.)  $Max \rightarrow n$  cuts off the display after the first n steps of the system. (Separate values can be specified for SSSMax and NetMax.) VertexLabels → Automatic (or "Name") |

Out[ • ]=

HighlightMethod → Dot | Frame | Number (or

True) | None (or False) specifies how the matches in the SSS are highlighted.

"VertexWeight" | ... labels vertices by node number or distance from origin, etc.

ShowRule → Bottom | Top | Left | Right | None (or False)

specifies where to place the rulelist icon relative to the SSS visual display (if shown).

Sizes of display components are specified by the options NetSize, SSSSize,

IconSize and ImageSize (which refers to the pane containing the SSS display and icon).

NetMethod → GraphPlot | LayeredGraphPlot | TreePlot | GraphPlot3D | All | NoSSS | list of methods,

where NoSSS generates no SSS display (causal

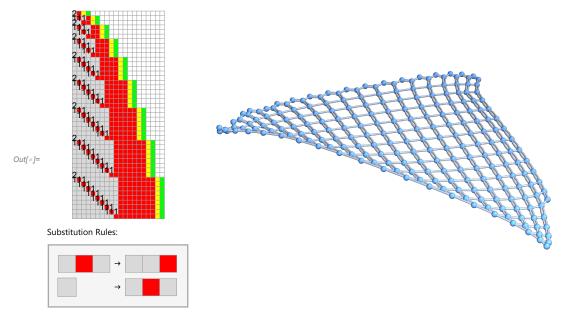
network only) and the other choices specify how the causal network is to be shown.

Once the sessie has been created you can display it (using SSSDisplay), change options, look at the network, etc. Choose options using SSSInteractiveDisplay, click one of the use buttons for one time or default use.

### In[\*]:= SSSInteractiveDisplay[sss2]

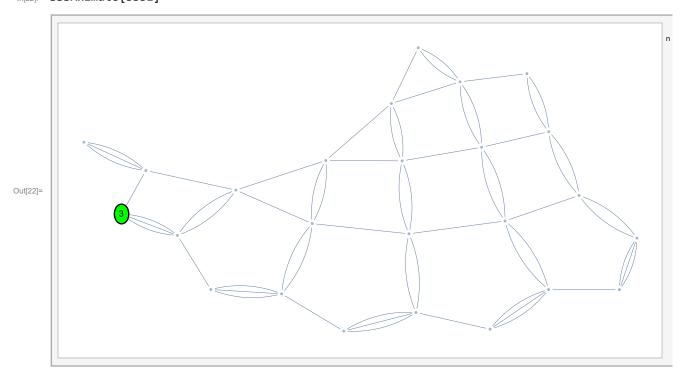
We might chose the GraphPlot3D display for the network. (Clicking and dragging with the mouse shows different view points.)

ImageSize → Automatic, VertexLabels → Placed [Automatic, Tooltip], DirectedEdges → False]
SSSDisplay[sss2, Min → 1, Max → 500, SSSMin → Automatic, SSSMax → 45, NetMin → Automatic,
NetMax → 224, HighlightMethod → Number, RulePlacement → Bottom, NetMethod → {GraphPlot3D},
ImageSize → 170.`, NetSize → 350, SSSSize → {Automatic, 220}, IconSize → {Automatic, 20},
VertexSize → Automatic, VertexLabels → Placed[Automatic, Tooltip], DirectedEdges → False]



SSSAnimate shows the order the network is created.

## In[22]:= SSSAnimate[sss1]



Other components of the Sessie object can also be studied individually.

```
// In[*]:= sss1["RuleSet"]
```

Out[\*]= {ABA  $\rightarrow$  AAB, A  $\rightarrow$  ABA}

In[@]:= sss1["Evolution"]

Out = AB, ABAB, AABB, ABAABB, AABABB, AAABBB, ABAAABBB, AABAABBB, AAAABBBB, AAAABBBB, AAAABBBB, AAAABBBB, ABAAAABBBB, AABAAABBBB, AAABAABBBB, AAAABBBBB, AAAAABBBBB, ABAAAAABBBBB, AABAAAABBBBB, AAABAABBBBB, AAAABABBBBB, AAAAABBBBBB, AAAAAABBBBBB, 

In[\*]:= sss1["RulesUsed"]

The RuleSet contains the "laws of nature" for this toy universe which are always invoked sequentially. The first rule is always used before the second, if possible, and the rule is always used in the left most position in the state string. The Evolution gives the list of all state strings from the initial state on. For instance, sss1 only contains the first 25 time steps. The colored box picture is a visual representation of these state strings. The component RulesUsed gives the list of which rules were used at each time step.

FAQ Sessie Intro, 2024.11.12, Kenneth Caviness and Colton Edelbach