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## Homework 12

ENGR 133-003 Created by Sean DeBarr 4/19/2019

```
clear
close all
clc
```

### Problem T11.2-1

```
clear

disp("*****" + newline + "Problem T11.2-1" + newline);

% declare symbolic variable
syms x

% declare equation symbolically
eqn = sqrt(1 - x^2) == x;

% solve equation symbolically
solution = solve(eqn);

% display results
fprintf("The solution is: %s\n\n", solution);

*****
Problem T11.2-1

The solution is: 2^(1/2)/2
```

### Problem T11.2-2

```
clear

disp("*****" + newline + "Problem T11.2-2" + newline);

% declare symbolic variables
syms x y a
```

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```

% declare equations symbolically
eqn1 = x + 6*y == a;
eqn2 = 2*x - 3*y == 9;

% solve equations symbolically for 'x' and 'y'
solution = solve(eqn1, eqn2, x , y);

% display results
fprintf("The solution for 'x' in terms of 'a' is: %s\n", solution.x);
fprintf("The solution for 'y' in terms of 'a' is: %s\n\n",
    solution.y);

*****
Problem T11.2-2

The solution for 'x' in terms of 'a' is: a/5 + 18/5
The solution for 'y' in terms of 'a' is: (2*a)/15 - 3/5

```

## Problem 11.7

```

clear

disp("*****" + newline + "Problem 11.7" + newline);

%
*****
% Part a
disp("Part a" + newline);

% declare symbolic variables
syms x a

% declare equation symbolically
eqn = x^3 + 8*x^2 + a*x + 10 == 0;

% solve equation symbolically for 'x'
solution = solve(eqn);

% display results
fprintf("The solution for 'x' in terms of 'a' is: \n");
disp(solution);

%
*****
% Part b
disp("Part b" + newline);

% evaluate solution for 'a = 17'
roots = subs(solution, a, 17);

```

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```

% convert to numerical answer
roots = double(roots);

% display results
fprintf("The roots of the equation for 'a = 17 are: %g, %g, %g\n\n",
    roots(1), roots(2), roots(3));

% verify with matlab poly function
fprintf("This solution is verified using poly:");
disp(poly(roots));

*****
Problem 11.7

Part a

The solution for 'x' in terms of 'a' is:
    root(z^3 + 8*z^2 + a*z + 10, z, 1)
    root(z^3 + 8*z^2 + a*z + 10, z, 2)
    root(z^3 + 8*z^2 + a*z + 10, z, 3)

Part b

The roots of the equation for 'a = 17 are: -5, -2, -1

This solution is verified using poly:      1      8      17      10

```

## Problem 11.9

```

clear

disp("*****" + newline + "Problem 11.9" + newline);

%
*****
% Part a
disp("Part a" + newline);

% declare symbolic variable
syms th

% declare equations symbolically
rA = 1 / (1 - 0.01 * cos(th));
rB = 0.1 / (1 - 0.9 * cos(th));

% find intersection points
solution = solve(rA - rB);

% convert to numerical answer
solution = double(solution);

% display results

```

---

```

fprintf("The intersection points are:\n");
disp(solution(1));
disp(solution(2));
fprintf("Since the intersections are imaginary, the orbits do not
    intersect.\n\n");

%
*****
% Part b
disp("Part b" + newline);
clear

% declare symbolic variable
syms th

% declare equations symbolically
rA = 1 / (1 - 0.01 * cos(th));
rB = 1.5 / (1 - 0.5 * cos(th));

% find intersection points
solution = solve(rA - rB);

% convert to numerical answer
solution = double(solution);

% find r coordinates
r1 = double(subs(rA, th, solution(1)));
r2 = double(subs(rB, th, solution(2)));

% display results
fprintf("The orbits intersect at (%g, %g)", r1, solution(1));
fprintf(" and (%g, %g).\n\n", r2, solution(2));

*****
Problem 11.9

Part a

The intersection points are:
    0.0000 - 0.0472i

    0.0000 + 0.0472i

Since the intersections are imaginary, the orbits do not intersect.

Part b

The orbits intersect at (0.989796, 3.14159) and (0.989796, 3.14159).

```

## Problem 11.10

```
clear
```

---

```

disp("*****" + newline + "Problem 11.10" + newline);

%
*****
% Part a
disp("Part a" + newline);

% declare symbolic variable
syms th1 th2

% declare equations symbolically
eqn1 = 3*cos(th1) + 2*cos(th1 + th2) == 3;
eqn2 = 3*sin(th1) + 2*sin(th1 + th2) == 1;

% evaluate solutions
S = solve(eqn1, eqn2);

% convert to degrees
S1 = double(S.th1) * (180 / pi);
S2 = double(S.th2) * (180 / pi);

% display results
fprintf("The elbow up solution is (%g, %g)\n", S1(1), S2(1));
fprintf("and the elbow down solution is (%g, %g).\n\n", S1(2), S2(2));

%
*****
% Part b
disp("Part b" + newline);

% declare symbolic variable
syms th1 th2 x

% declare equations symbolically
eqn1 = 3*cos(th1) + 2*cos(th1 + th2) == x;
eqn2 = 3*sin(th1) + 2*sin(th1 + th2) == 1;

% evaluate solutions
S = solve(eqn1, eqn2, th1, th2);

% declare x interval
xr = 2:0.01:4;

% create data points for each x in interval
th1r = subs(S.th1, x, xr);
th2r = subs(S.th2, x, xr);

% convert to degrees
th1r = double(th1r) * (180 / pi);
th2r = double(th2r) * (180 / pi);

% plot solutions
subplot(2, 1, 1);

```

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```

p1 = plot(xr, th1r);
hold on;
grid on;
p2 = plot(3, S1(1), 'ko');
p3 = plot(3, S1(2), 'rx');
xlabel("x (feet)");
ylabel("Theta1 (degrees)");
title("Motor angles vs x");
legend([p2, p3], "elbow up", "elbow
    down", "Location", "northeastoutside");

subplot(2, 1, 2);
p4 = plot(xr, th2r);
hold on;
grid on;
p5 = plot(3, S2(1), 'ko');
p6 = plot(3, S2(2), 'rx');
xlabel("x (feet)");
ylabel("Theta2 (degrees)");
legend([p5, p6], "elbow up", "elbow
    down", "Location", "northeastoutside");

clear

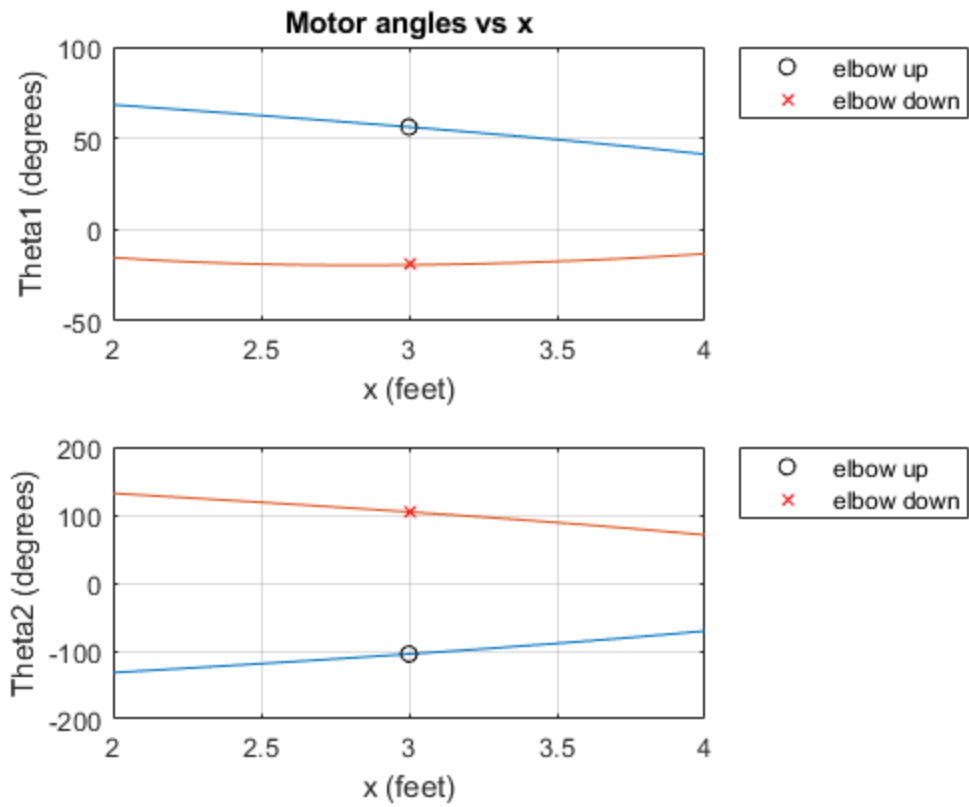
*****
Problem 11.10

Part a

The elbow up solution is (56.1962, -104.478)
and the elbow down solution is (-19.3263, 104.478).

Part b

```



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