

MALIS

Group Exercise

November 29 2022

Group Name:	
Group Members:	

1 Bias Variance Decomposition

[3 points] Suppose you collected a sufficiently large dataset generated by a polynomial of degree 4. Characterize the bias-variance of the estimates of the following models on the data with respect to the true model by choosing the appropriate entry.

Model	Bias	Variance
Linear regression	low/ high	low /high
Polynomial regression with degree 4	low /high	low /high
Polynomial regression with degree 10	low /high	low/ high

2 Support Vector Machines and Kernels

Consider a training set consisting of points in the 2D space $x = \{(1, 1), (1, -1), (-1, 1), (-1, -1)\}$ with labels $y = \{1, -1, -1, 1\}$.

- (a) [1/2 point] Is the dataset linearly separable in the original space? Justify your answer.

No. see plot 1

- (b) [1 1/2 points] Consider the following feature transformation: $\phi(\mathbf{x}) = [1, x_1, x_2, x_1 x_2]^T$, where x_1 and x_2 are the first and second coordinates of x . Your prediction function in this feature space is $\hat{y}(\mathbf{x}) = \mathbf{w}^T \phi(\mathbf{x})$. Give the coefficients, \mathbf{w} , of a maximum-margin decision surface separating the positive from the negative examples.

Hint: You should be able to do this by inspection, without the need of any significant computation.

$$\mathbf{w} = [0 \ 0 \ 0 \ 1]^T$$

- (c) [1 1/2 points] Plot the training set in the original space. Add one training sample to the plot so that the five samples can no longer be linearly separated in the feature space $\phi(\mathbf{x})$ using the coefficients \mathbf{w} you estimated in the previous question.

See plot 2

- (d) [1 1/2 points] What kernel $K(\mathbf{u}, \mathbf{v})$ does this feature transformation ϕ correspond to?

$$K(\mathbf{u}, \mathbf{v}) = 1 + u_1 v_1 + u_2 v_2 + u_1 u_2 v_1 v_2$$

Note: These 2 questions were part of the final exam in 2019.

