LECTURE 1.

Communication (Simplistic view).

Transmit $x(t) = \cos(\pi t)$ f is greenency, $x \mapsto y \in H_{\overline{x}}$. f is string. f is string. f is f then f is f is f then f is f is f is f then f is f.

d: antenna losses

Idelas due to signal

- Tx in 3-0 space.

- Power preserved in surface of sphere: (ruising the r, center is anten)

7 Fixed Repulsower 7 Rx power & 1/2.

Area 7 Rx power & 1/2.

like before : + > r(+).

Consider movement.

$$t \times (x) = \cos x \pi y + x$$
 $r(x) = r_0 + v \cdot t$

 $\stackrel{?}{=} E\left(S,t,\Gamma(t)\right) = \frac{ds}{\Gamma(t)} \cdot \cos 2\pi S \left(t - \frac{\Gamma(t)}{E}\right)$

DOPPLER shift: D=-FV.

 $= \frac{1}{E\left(S,+,\Gamma(4)\right)} = \frac{L_5}{\Gamma_0 + \nu, 4} \cdot \cos 2\pi S\left(+\left(1-\frac{\nu}{c}\right) - \frac{c}{c}\right)$

= 25 . cos zas (+ - 10 - V+)

 \Rightarrow essective frequency change $ft \rightarrow f(1-\frac{v}{c}).t : f \rightarrow f(1-\frac{v}{c})$

> Frequency reduction 5 -> F(1-1/2) 3. D=-FV

Inote: not LTI now.

= ds . cos 211 f + (1-4) - 5

Fixed Tx, Fixed Rx, possedly replecting wall.

Use method of ray tracing" : consider dominant (main) paths.

$$Er(s,t) = \frac{\alpha}{r} \cdot \cos z\pi s \left(t - \frac{r}{c}\right) - \frac{\alpha}{zd - r} \cos z\pi s \left(t - \frac{zd - r}{c}\right)$$

$$r is \qquad distance 1. \quad 2d - r = distance 2.$$

Duper position (addition of two sinusoids, with disperent phases).

Possible effect of cancella out.

Phase the dd PLT(π)-41 (π phase ships in electric siells of Em wave when replected from optically desser medicina).

Ad = 2πς id-r + π - 2πς t. (Essentially canceling each other out close to the wall

Coherence boundwidth: Change is prequency f, so that channel (i.e magnitude of rx signal) remains relatively the same. so that phase shift changes 2 # BU = 411 f (d-r) +TT & change f 7 477 f (d-r) 2 I $\frac{1}{2}$ $\frac{1}$ node: rd-r-raid is called delay spread (dissource in delay). 3 211 F. [= = 1] = Wc = 1] Wc = 1] Wc = 1] (note: is set 2Ts (rd-r-r) 2TT > We = 2Td

Substantial phase shipt
the constant sactor does not really watter) (TT or IT). in fact with We = T.

Ad # 175 (2d-r - +) = 275 (2d-2r) = 475 (d-r)

7 x= = = = = = = Atc

changing r while roult in phase shift of I

3 coherence distance Stend

411 F. X 7 7 7 X 7 7 7 7 8 2 4 7 5 . 8 2 4 8 .

(is I set "substantial phase shipt" xd x 4TF(d-r) x T

7 ste nd = d (depending on convention).

(cherense distance: same scenario.

- Channel strength changes as you move through constructive of destr intog.

("multipath gading").

Let $(s,t) = \frac{d}{2\pi i} \cos 2\pi s \left[t - \frac{r(t)}{r(t)} \right] + \frac{d}{r(t)} \cos 2\pi s \left[t - \frac{1}{r(t)} \right]$



= $\frac{2}{r_0 \tau v t}$ cosins $\left\{ \frac{v t}{c} - \frac{10}{c} \right\} + \frac{2}{id - r_0 - v t}$ cosins $\left\{ \frac{v t}{c} - \frac{1}{v t} \right\} + \frac{2}{id - r_0 - v t}$ cosins $\left\{ \frac{v t}{c} - \frac{v t}{c} \right\} + \frac{2}{id - r_0 - v t}$ cosins $\left\{ \frac{v t}{c} - \frac{v t}{c} \right\} + \frac{2}{id - r_0 - v t}$ cosins $\left\{ \frac{v t}{c} - \frac{v t}{c} \right\} + \frac{2}{id - r_0 - v t}$

Now assume (Jux for simplicity) that we are close to the wall

$$\frac{1}{2} = \frac{1}{4} \left[\frac{1}{4} + \frac{1}{4} \left(\frac{1}{4} + \frac{1}{4} \right) - \frac{1}{4} \right] - \frac{1}{4} \left[\frac{1}{4} + \frac{1}{4} + \frac{1}{4} \right] - \frac{1}{4} \left[\frac{1}{4} + \frac{1}{4} + \frac{1}{4} + \frac{1}{4} \right] - \frac{1}{4} + \frac{1$$

 $F_{r}(s,r) = 2d \cdot sin \left[\frac{1}{10} s \left(\frac{1}{2} - \frac{1-r_{0}}{c} \right) \cdot \frac{1}{10} s \left(\frac{1}{10} + \frac{1}{2} \right) \right]$ Very slow Sreq F = Very Sest (Sree F)

s'= s.v = 1 7'= 1

I Coherence period: T' = 1/45' = 1/45' = 1/45' = (recall (=5.1). benerally note of LLT. (in process, it will change many times).

Anoster way to see har period of slow rmusoid.

Also write
$$\Delta t_c$$
 & T_c in terms of Poppler Spread.

Per Doppler Spread here P_s : P_z - P_z -

Example:
$$V = 60 \, \text{Fm/h}$$
 $S = 16 \, \text{Hz}$ (typical grea).
 $V = \frac{60.13 \, \text{M}}{36005} = \frac{50}{3} \, \text{m/s}^2$ $\Rightarrow D_S \approx 2.5 \cdot \frac{V}{c} = \frac{2.18 \cdot 50}{3.3.10^8} \approx 2.5.100 \, \text{m} \text{ Hz}$.

7 Te = 1 = 10 5 25 mS; AXe = V. Te = 50.5.10 = 75 = 75 = 75 pew a

Input - output Model. Consider many paths (many restectors). pen=cosingle) i= , i= n / x diggerent paths i (many...). Input x(+)= cos275+ lecall our attenuation examples before: y(+) = { ai(s,+). *(+-5i(s,+)). how long is taken for each Probagation delays si (5, +): travel growthart. puth to

attenuations ai (Et). that Ji (s,+) & di (s,+) are sunctions of both S, t. recall Bandwidth is small compared to Sc=16Hz (central greanency) So all prequencipes that we use are (in relative terms) very close to Se=16Ha. (&W typically 1 MHz orso) [0.9996Hz -> 1.0016Hz]. ~ 16Hz Ji & ai are indep of f = Agsume > 5i(+), ai(+) be careful: channel $y(t) = \underbrace{\leq a_i(t) \cdot x(t - T_i(t))}_{i}$ response still a

Sunction of F

Just like in previous examples.

Recall: we have accepted linearity.

y (4) = h (3,7) * X(+): For h (1,5) & T.V. channel impulse response.

 $y(t) = \int h(t, \tau) \cdot \mathbf{y}(t-\tau) d\tau$ $\int but also (snow begone).$

 $y(t) = \sum_{i} a_{i}(t) \cdot \chi(t-J_{i}(t))$

Put two to pethes.

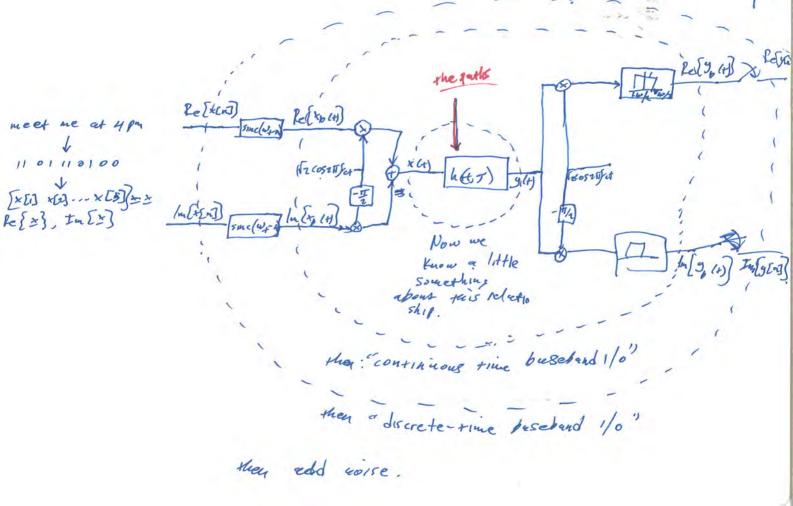
7 (h (+, +)= { Ea; (+). 8 (7-7; (4)).

 $Verign: y(4) = \begin{cases} k(4,7) \times (4-7) dJ = \begin{cases} \xi a_i(4) \cdot \delta(q-7;(4)) \cdot x (4-7) dJ \\ -\infty \end{cases}$ $= \begin{cases} \xi a_i(4) \cdot \int \delta(\tau-\tau;(4)) \times (4-\tau) d\tau = \xi a_i(4) \cdot x (4-\tau;(4)) \\ i \end{cases}$

\$ LTV impulse response of channel. [y(t) = h(t, r) * x(t).

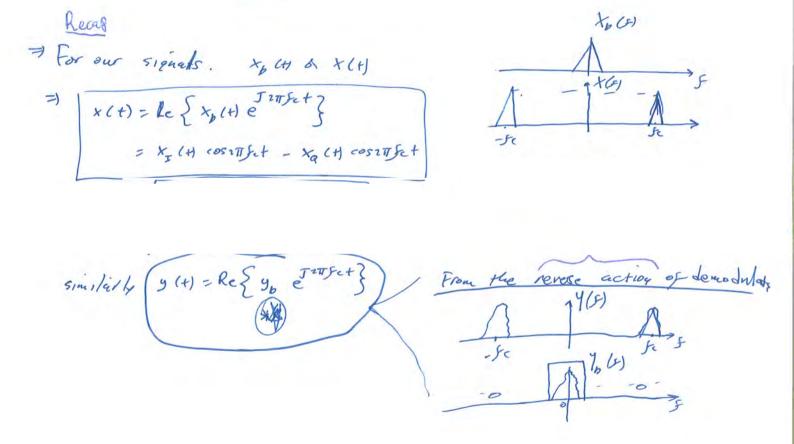
x(4) (1(1)) -y(0) c (we have seen) Our task now will be to extend the concept of this "channel" to molude important processes of communication. Let us skletch theys. process

Communication process in a slimpte: from #'s to " meet me at upm" = m1 messege mi -> 11011 0100 \$ -> (-i - nti)-c - nti) = [x[] x(2] -- x[5] => Re{=}=[1-11-1], In[=]=[-11-1] This region ly inite dandwidth Rex[0]:1 Re[x[1]=-1 I need to smoother signals. of modulate with sequence of smooth. syac functions \$ = * { smc[w+-n]} to prec + (4) that has Finite BW 1/4 (4) S. Wow S. - High Freezeway modulation Low prequency signals suffer From Vapid attenuation (casily assorted by walls, esc) a CoszAfet Seal-26Hz Sew Se Selw - then demodulaxe table by " costofet) of their sample - then sample



Establish relationship between Baseband h (+, J) Sin (ETTECT) X(+) = Re{ = X_b(+), e JzTfc.t} Similarly y(+)= Re{ yo (+) . e = } From reverse ection of demodulations

In practice: how is this achieved? X(+) = Re { X(+) . e } I write & (+) = & (+) + I & (+) & recell e = costrifet + I smithet L) > X(+) = Re { XI (+) (cossufet + J sin 27/2+) + J X(+) (cossufet + J sin 27/2+ +) }. = X (4). cosz Tifet - X (4) sig z Tife. +



Now ready to establish relationship x (+) → h (+, 7) - 3 4 (+) feeall:
9(+) = \(\frac{1}{2} = \frac{1}{2} ailth gath affecuetion = Re{y, in estat} , +(+) = Re{x_in estat} (from begoe). > Re{ y, 14 = Justic+} = { a; (4) Re{ x 6 (4-5; (4)). e Truste(4-7; (4))} = Re{ { a; (4) x 6 (4-7; (4)) } = Re{ } } $9 \operatorname{Re} \left\{ y_{b}(t) \right\} = \operatorname{Re} \left\{ \underbrace{z}_{a: (t)} \times_{b} (t - T_{i}(t)) \right\} = \underbrace{\operatorname{Trans.} T_{i}(t)}_{e}$ $\left\{ \underbrace{z}_{a: (t)} \times_{b} (t - T_{i}(t)) \right\} = \underbrace{\operatorname{Trans.} T_{i}(t)}_{e}$ $\left\{ \underbrace{east}_{a: (t)} \times_{b} (t - T_{i}(t)) \right\} = \underbrace{\operatorname{Trans.} T_{i}(t)}_{e}$ $\left\{ \underbrace{east}_{a: (t)} \times_{b} (t - T_{i}(t)) \right\} = \underbrace{\operatorname{Trans.} T_{i}(t)}_{e}$ $\left\{ \underbrace{east}_{a: (t)} \times_{b} (t - T_{i}(t)) \right\} = \underbrace{\operatorname{Trans.} T_{i}(t)}_{e}$ $\left\{ \underbrace{east}_{a: (t)} \times_{b} (t - T_{i}(t)) \right\} = \underbrace{\operatorname{Trans.} T_{i}(t)}_{e}$ Im (4, (4) = In { E a: (4) +, (+5-7; (+1). 2 . e $\exists \int_{b}^{\infty} (t) = \underbrace{\sum_{a_{i}(t)}^{a_{i}(t)} e^{-\int u \int_{b}^{a_{i}} J_{i}(t)}}_{i} (t)$ $= \underbrace{\sum_{a_{i}(t)}^{a_{i}(t)} \int_{e}^{u} J_{i}(t)}_{i} (t)$ $= \underbrace{\sum_{a_{i}(t)}^{a_{i}(t)} \int_{e}^{u} J_{i}(t)}_{i} (t)$ $= \underbrace{\sum_{a_{i}(t)}^{a_{i}(t)} \int_{e}^{u} J_{i}(t)}_{i} (t)$ where $a_i^b(t) = a_i(t)$. e Fest.

7 h_b (t, 5) changes &t = = \frac{1}{4} \left(\frac{1}{4} = \frac{1}{4} \frac{1}{4} = \frac{1}{4} \frac{1}{4} = \frac{1}{4} \frac{1}{109 \frac{1}{4}} \right) 8 at 7 speeds (sqr 2 60 km/s). 27 cm (sew).

- 3.18

4.5e.V 24.18.60.10

107 g

2 4 cm (sew)

2 49.66.10 = 9

2 4 5 ms

49.66.10 = 1000

(Sew ms). - Interesting observation on sceneucy response of helt. T).

To memory of channel of Td

(a bit tricky). by desimition S(t) - holt, T) - y, (t) = h, (t) - send an impalse though channel - All signals will be collected (from all goeths) in the orater of what we will call "Lely spread" = T = max | Ji - Is | Ji = di , 7 = dI

- In colleret nets (mainly urban), typical distance - dissocincop di- of sew hundred westers 3 5i-75=di-ds = sew huded up ≈ sew us (\$1=10.1065). > "memory of channel" ho (+,) = few us. = To But To K To 2 sew as. Impalse response (since it is only ofter many impulses that the channel will change)