

Cascading several elements

A receiver is made up of three main elements: a preamplifier, a mixer, and an IF amplifier with noise figures of 3, 6, and 10 dB.

- If the overall gain of the receiver is 30 dB, and the IF amplifier gain is 10 dB,

What is the minimum gain of the preamplifier to achieve an overall noise figure of no more that 5 dB?

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In [1]:
         using Optim
         # Given parameters in dB
         NF_1_dB = 3
         NF 2 dB = 6
         NF_3_dB = 10
         NF total max dB = 5
         G IF dB = 10
         G_{overall_dB} = 30
         # Convert dB to linear scale for noise figures and gains
         NF_1 = 10^{(NF_1_dB / 10)}
         NF_2 = 10^(NF_2_dB / 10)
         NF_3 = 10^{(NF_3_dB / 10)}
         NF_total_max = 10^(NF_total_max_dB / 10)
         G_{IF} = 10^{(G_{IF}dB / 10)}
         G_{overall} = 10^{(G_{overall_dB} / 10)}
         # Function to calculate total noise figure for given G1 in linear scale
         function calculate NF total(G1 linear)
             G 1 G 2 = G overall / G IF # Total gain divided by IF amplifier gain gives product d
             # Assuming G2 is fixed and we adjust G1, calculate total noise figure (linear scale)
             NF total = NF 1 + (NF 2 - \frac{1}{1})/G1 linear + (NF 3 - \frac{1}{1})/(G1 linear * G 1 G 2)
             return NF total
         end
         # Objective function to minimize: difference between calculated NF total and target NF \operatorname{\sf td}
         function objective_function(G1_linear)
             NF_total = calculate_NF_total(G1_linear)
             return (NF_total - NF_total_max)^2 # Squared difference for minimization
         end
         # Initial guess for G1_linear (since we don't have specific info, start with a reasonable
         initial guess = 10 # Linear scale
         # Use an optimization library to minimize the objective function and find optimal G1
         result = optimize(objective function, 1, 1000) # Adjust bounds (1, 1000) as needed based
         # Extract the optimized G1 value
         G1 optimized linear = Optim.minimizer(result)
         G1_optimized_dB = 10 * log10(G1_optimized_linear)
         println("Optimized G1 in linear scale: ", G1_optimized_linear)
         println("Optimized G1 in dB: ", G1_optimized_dB)
```

```
Optimized G1 in linear scale: 2.6315606874740136
Optimized G1 in dB: 4.202133899076101
```

⁻ If its gain is set to this minimum,

What would the system noise figure become if the noise figure of the IF amplifier is increased to 20 dB?

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In [2]:
         # Define given parameters
         NF_1_dB = 3 # Preamplifier noise figure in dB
         NF_2_dB = 6 # Mixer noise figure in dB
         NF_3_new_dB = 20 # Updated IF amplifier noise figure in dB
         G_overall_dB = 30 # Overall system gain in dB
         G_IF_dB = 10 # IF amplifier gain in dB
         # Convert dB to linear scale for noise figures and gains
         NF_1 = 10^{(NF_1_dB / 10)}
         NF_2 = 10^{(NF_2_dB / 10)}
         NF_3_{new} = 10^{(NF_3_{new}_{dB} / 10)}
         G 	ext{ overall } = 10^{(G 	ext{ overall } dB / 10)}
         G_{IF} = 10^{(G_{IF}dB / 10)}
         # Placeholder for the optimized G1 value in linear scale from previous optimization
         # Replace this with the actual value you found
         G1_optimized_linear = 10  # This is a placeholder, replace with actual optimized G1 value
         # Calculate G1 st G2 based on the overall gain and IF amplifier gain
         G_1_G_2 = G_overall / G_IF
         # Function to calculate the total noise figure with the updated NF_3
         function calculate_total_noise_figure(NF_1, NF_2, NF_3_new, G1, G_1_G_2)
             # Total noise figure calculation using Friis formula
             NF_{total} = NF_1 + (NF_2 - 1) / G1 + (NF_3_new - 1) / (G1 * G_1_G_2)
             return 10 * log10(NF total) # Convert the total noise figure back to dB
         end
         # Calculate the new system noise figure with the updated IF amplifier noise figure
         NF_total_new_dB = calculate_total_noise_figure(NF_1, NF_2, NF_3_new, G1_optimized_linear,
         println("New system noise figure with updated IF amplifier noise figure: ", NF_total_new_
```

New system noise figure with updated IF amplifier noise figure: 3.7882825438470857 dB

In []: