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in	18/10/24	Implementation of various optimization algorithms.		
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## Lab-1 : Genetic Algorithm for Optimization Problems

\* Genetic algorithm is a method for solving both constrained and unconstrained optimization problems that are based on natural selection, that process that drives biological evolution. The genetic algorithm repeatedly modifies a population of individual solutions.

The main algorithmic steps are:

[Population Initialization]

↓  
[Fitness Evaluation Test]

↓  
[Selection]

↓  
[Crossover (Recombination)]

↓  
[Mutation]

↓  
[Replacement]

↓  
[Termination]

- i) Population Initialization - Start with a randomly generated population of potential solutions, often represented as strings (like binary or real nos.)
- ii) Fitness Evaluation - Evaluate how well each solution performs relative

To the problem's objective.

- III) Selection - Select the best - performing solutions to be parents for next generation. Eg - Tournament Selection, roulette wheel selection
- IV) Crossover - Combine pairs of parents to produce offspring. This mimics biological reproduction where parts of each parent's genetic material are mixed. Eg:- Single point, Two point and uniform crossovers
- V) Mutation - Introduce random changes to some offspring to maintain genetic diversity and explore new areas of the solution space.
- VI) Replacement - Form a new generation by replacing some or all of the old population with the new offspring.
- VII) Iteration - Repeat the evaluation, selection, crossover, and mutation steps for several generations until a satisfactory solution is found or a predetermined condition is met.

### Applications:

- ① Optimization problems
  - Used for optimizing structures,

components and systems in field like aerospace and civil engineering.

- helps in optimizing the allocation of resources in industries like telecommunication and logistics.

## ② Machine learning

- Assists in selecting the most relevant features for improving model performance
- Optimizes the parameters of machine learning algorithms.

## ③ Robotics

- finds optimal paths for robots to navigate environments
- Optimizes control parameters for robotic movement.

## Lab 1:- Particle Swarm Optimization for Function Optimization

- Particle Swarm Optimization (PSO) is a popular optimization algorithm inspired by the social behaviour of birds and fish. It's particularly effective for function optimization, especially in complex, multidimensional spaces. It works mainly for function optimization.
- Algorithm :-

- Initialization - Set parameters such as the number of particles, maximum iterations, cognitive and social coefficients, and the search space boundaries.
- Initialize the positions and velocities of all particles randomly.
- Fitness Calculation - Evaluate the fitness of each particle using the objective function.
- Updating Best Positions - Each particle keeps track of:
  - personal best position (best) - the best position it has encountered so far.
  - global best position (gbest) - The

best position found by any particle in the swarm.

- Velocity update - Update the velocity of each particle based on its own best-known position and the best-known position of the swarm:

$$v_i^0 = w \cdot v_i^0 + c_1 \cdot r_1 \cdot (p_{\text{best}}^0 - x_i^0) + c_2 \cdot r_2 \cdot (g_{\text{best}}^0 - x_i^0)$$

- Position update - Update the position of each particle based on its new velocity

$$x_i^0 = x_i^0 + v_i^0$$

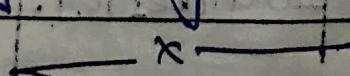
- Boundary conditions - If a particle moves out of the defined search space boundaries, it can be reset to the boundary, or reflected back into space

- Termination criteria - The process repeats until a stopping criterion is met like

maximum no. of iterations, etc.

## → Applications

- Mathematical function optimization
- Machine learning
- Signal Processing
- Engineering Design Problems



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## PSO - pseudocode

# initialise parameters

num\_particles = N

max\_iterations = MAX\_ITER

inertia\_weight = w

c1 = cognitive-parameter # personal best influence

c2 = social-parameter # global best influence

# initializing the swarm (particles)

for i in range(num\_particles):

    # particles[i].position = random position  
    # in search-space

    particles[i].velocity = random\_velocity()

    particles[i].pBest = particles[i].position

        # personal best initialized to the  
        # starting position

    particles[i].pBest\_value = bound

        fitness\_function(particles[i].  
        # position)

# initialize global best (gBest)

gBest = particles[0].pBest

gBest\_value = particles[0].pBest\_value

# main optimization loop

for Iteration in range(max\_iterations):

    for i in range(num\_particles):

        # evaluating fitness test of  
        # the current position

        fitness\_value = fitness\_function  
            (particles[i].position)

# update personal best (pBest)

if fitness\_value < particles[i].pBest\_value:  
    particles[i].pBest = particles[i].position  
    particles[i].pBest\_value = fitness\_value

# update global best (gBest)

if fitness\_value < gBest\_value:  
    gBest = particles[i].position  
    gBest\_value = fitness\_value

# update velocity and position of each particle

for i in range(num\_particles):  
    for d in range(num\_dimensions):  
        r1 = random(0,1)  
        r2 = random(0,1)

# update velocity

    particles[i].velocity[d] = (P inertia -  
        weight \* particles[p].velocity[d]  
        + v1 \* r1 \* (particles[p].pBest[d]  
            - particles[i].position[d]) +  
        c2 \* r2 \* (gBest[d] - particles[i].position[d]))

# update position

    particles[i].position[d] = particles[i].position[d] + particles[i].velocity[d]

# Ensure position is within bounds  
if particles[i].position[d] < lower\_bound[d]:

particles[i].position[d] = lower\_bound[d]

if particles[i].position[d] > upper\_bound[d]:

particles[i].position[d] =  
upper\_bound[d]

# Return the best seen found

return gBest, gBest-value

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## Ant Colony Optimization for TSP

Ant Colony Optimization is a metaheuristic algorithm inspired by the natural behaviour of ants searching for food. In ACO, artificial "ants" simulate the behaviour of real ants that deposit pheromones on the ground to communicate and mark their path, influencing the behaviour of other ants. This approach has been successfully applied to various combinatorial optimization problems, including TSP.

### Algorithm

#### ① Initialization

- Initialize the pheromone levels  $\rho_{ij}$  for all edges between cities (usually a small constant value).
- Set the parameters  $\alpha$ ,  $\beta$ , no. of ants, no. of iterations, pheromone evaporation rate etc.

#### ② Ant Tour Construction

- for each ant, start from a random city.
- At each step, the ant chooses the next day city based on the pheromone levels and distance.
- Repeat until all cities are visited and tour is completed.

### (3) pheromone update

- after all ants have completed their tours, update the pheromones on the edges according to the rule

$$\rho_{ij} = (\alpha - \beta) \rho_{ij} + \beta \Delta \rho_{ij}$$

•  $\beta$  is the pheromone evaporation rate

•  $\rho_{ij}$  is the amount of pheromone deposited by ants on the edge  $(i, j)$  which is inversely proportional to the length of the tour of the ant.

### (4) Termination

- if the stopping criteria (such as maximum no. of iterations or convergence to the optimal solution) are met, stop the algorithm.  
Otherwise, repeat from step 2.

### (5) Initialize pheromone matrix

$\rho_{ij} = 1$  for all pairs of cities  $(i, j)$

Initialize best tour = empty

Initialize best length = infinity

for Iteration = 1 to max\_iterations:

    Initialize all ants' tours

    for each ant  $k = 1$  to  $n$ :

        ant\_tour[k] = tour\_random()

        current\_city = randomCity()

        ant\_tour.append(current\_city)

while tour is not complete (all cities visited)  
 next-city = choose-next-city(current-city, ant-tour)  
 ant-tour.append(next-city)  
 current-city = next-city  
 tour-length = calculate-tour-length(ant-tour)  
 if tour-length < best-length:  
 best-tour = ant-tour  
 best-length = tour-length

apply pheromone vapourization ( $v_{ij}^{(t+1)} = (c_p)^{\alpha} v_{ij}^{(t)}$ )

for each ant  $K$ :  
 for each edge  $(i, j)$  in ant-tour:  
 update-pheromone( $c_p, P$ , ant-tour,  
 tour-length)

Return best-tour, best-length

~~function to choose the next city  
 using pheromone and distance~~

~~function choose-next-city(current-city,  
 visited-cities):~~

~~probabilities = [ ]~~

~~total-pheromone = 0~~

~~for each city  $j$  not in visited-cities:~~

~~pheromone =  $v[\text{current-city}]^j \times$~~

visibility =  $(1 / \text{distance}[\text{current\_city}, j])^{\alpha}$

total\_pheromone += pheromone<sup>~~old~~</sup>  
visibility

for each city  $j$  not in visitedCities:  
pheromode =  $\sqrt{\text{current\_city}^T P_j^{\alpha}}$

visibility =  $(1 / \text{distance}[\text{current\_city}, j])^{\alpha}$

probability =  $(\text{pheromone} * \text{visibility}) / \text{total\_pheromone}$

probabilities\_applied = probability

nextCity = selectCity based on  
probability (probabilities)  
return nextCity.

"func" to update pheromone on  
selected edge  $(i, j)$

func\_update\_pheromone ( $i, j$ , antCount,  
fourLength):

$$\Delta r = Q / \text{fourLength} \quad (Q \rightarrow \text{constant})$$

$$r[i][j] += \Delta r$$

## Applications:

Q. Feb 21/11/24

- ① Reservoir optimization
- ② Water distribution systems
- ③ Urban drainage system design
- ④ Finding best possible route
- ⑤ Job resource allocation

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## Cuckoo Search

### Summary:

The Cuckoo Search Algorithm is a nature inspired optimization algorithm based on the parasitic behaviour of cuckoo birds. This algorithm is designed to solve complex optimisation problems by mimicking the breeding behaviour of cuckoos and their interaction with host birds.

### Algorithm:

- ① Initialise population of  $n$  nests (solutions) randomly.
- ② Evaluate the fitness of all nests.
- ③ While stopping criterion is not met:
  - (a) For each nest:
    - i) Generate a new solution using Levy flight.
    - ii) Evaluate the fitness of new solution.
    - iii) If the new solution is better, replace the old nest with the new one.
  - B) Abandon some nests with probability  $p_a$  and replace them with new random solutions.
- ④ Return the best solution found.

## Pseudocode:

### ① Initialise parameters:

- $N$ : No. of nests (population size)
- MaxIter: Maximum number of iterations
- $Pa$ : Probability of discovering alien eggs
- Problem: specific bounds for the search space (lower and upper limits)

### ② Initialise nests (solutions)

- For each nest  $i = 1 \text{ to } N$ :
  - evaluate fitness ( $x_i$ ) using the objective function  $f(x_i)$
  - Randomly generate initial solution  $x_i$  within search space (lower bounds and upper bounds)

### ③ Evaluate fitness of each nest:

- For each nest  $i = 1 \text{ to } N$ :
  - evaluate fitness ( $x_i$ ) using the objective function  $f(x_i)$

### ④ Set best solution as the initial best solution:

- Set BestSolution =  $\arg\min(\text{fitness}(x_i))$  for  $i = 1 \text{ to } N$ .

### ⑤ For each iteration ( $t = 1 \text{ to } \text{MaxIter}$ ):

- ① Generate new solutions (nest) using Levy flights:

$$x_i^{(t+1)} = x_i^{(t)} + \alpha * \text{Lévy Flight}()$$

- ensure  $x_i^{(t)}$  stays within the search space bounds:
  - if  $x_i^{(t)}$  is out of bounds, adjust it to stay within the boundaries
- evaluate fitness ( $x_i^{(t)}$ )

(b) Evaluate and compare new solutions with the current nests.

- if  $\text{fitness}(x_i^{(t)}) < \text{fitness}(x_i^{(t)})\%$

- replace the old solution  $x_i^{(t)}$  with the new solution  $x_i^{(t)}$ .

(c) Randomly replace nests with a probability  $p_{a1}$  (discovery of alien eggs)  
for each nest  $i=1 \dots N$ %

- with probability  $p_{a2}\%$

- replace nest  $x_i^{(t)}$  with a randomly generated solution  
~~such that~~  $x_{\text{rand}}$  within the search space

- evaluate fitness( $x_{\text{rand}}$ )

(d) Update the best solution:

- if a better solution is found:  
~~Update Best Solution to the best solution among all nests~~

(e) Return the best solution found after MaxIterations:

- Return Best Solution.

Sohail  
(21/11/24)

# 9/11/24 Grey Wolf Optimization

Summary: is a nature-inspired optimization algorithm that simulates the social hierarchy and hunting behaviour of grey wolves in the wild.

## Algorithm / Pseudocode:

### ① Initialise population / parameters

- N: Number of wolves (population size)
- M: Maximum no. of iterations
- D: Dimensionality of the search space
- Search space bounds: lower and upper limits.

### ② Initialise population of wolves

- For each wolf  $i = 1 \dots N$ :
  - Randomly initialise position  $x_i$  in the search space (within bounds)
  - Evaluate fitness of  $x_i$ :  $f(x_i)$

### ③ Identify the top three wolves:

- Let  $x_{\alpha} =$  the wolf with the best fitness (alpha wolf)

→ Set  $\alpha = \beta^*$  the second best wolf  
(beta wolf)

→ Set  $\alpha = \delta^*$  the third best wolf (delta wolf)

④ For  $t=1$  to MaxIter<sup>o</sup>

For each wolf  $i=1$  to N<sup>o</sup>

→ Compute the distance to alpha, beta, and delta wolves.

$$D_{\alpha} = |C_1 * x - \alpha - x_i|$$

$$D_{\beta} = |C_2 * \alpha - \beta - x_i|$$

$$D_{\delta} = |C_3 * \alpha - \delta - x_i|$$

→ Update the position of wolf-i:

$$x_i(t+1) = (\alpha + \beta + \delta) / 3$$

where  $C_1, C_2, C_3$  are random coefficients used to balance exploration and exploitation.

$C_1, C_2, C_3$  are random vectors in the range  $[0, 1]$

→ Update the fitness of each wolf and identify the new alpha, beta and delta wolves based on fitness.

⑤ If stopping criteria met (e.g.: MaxIter or convergence), stop the loop.

⑥ Return the best solution found.

28/11/24 X-X. (position of the alpha wolf)

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## Summary

### PSO Algorithm

PSO is a methodology inspired by the choreography of a bird flock. It is a distributed behaviour algorithm that performs multidimensional search. PSO belongs to the class of metaheuristic methods as it makes few or no assumptions about the solutions. The algorithm works by moving particles (structures) in a search space based on efficient algorithms that use the position and velocity of the particles. Hence, all the individuals in the swarm can quickly converge to the global position and a near-optimal geographical position following the behaviour of flock and their flying histories.

### ACO Algorithm

The ACO is another swarm optimisation technique based on the behaviour of ants seeking a path between their colony and a source of food. The original idea has since diversified to solve a wider class of numerical problems. Usually, ACO is applied for problems that

exhibit frequent dynamic changes, the main advantage of ACO is the ability of the algorithm to run continuously while adapting to changes in real-time.

### CS Algorithm

The CSA algorithm is based on the cuckoo bird behaviour, which lays eggs in another host bird. The main goal of the cuckoo bird is to mimic the host bird's eggs and avoid being discovered by the host bird. Hence, the optimization goal is reached if the host bird cannot discover the cuckoo eggs.

### Grey Wolf Optimization

GWO is a metaheuristic algorithm that is inspired by the behaviour of grey wolves in leadership and hunting. The algorithm classifies a population of possible solutions into four types of wolves  $\alpha$ ,  $\beta$ ,  $\delta$  and  $\omega$ . The four types are based on the fitness selection, which means  $\alpha$  is considered the best and  $\omega$  is the worst. The new generation is created by updating the wolves in each one of these four groups. This update is

based on the first three best solutions obtained from  $\alpha$ ,  $\beta$ ,  $\delta$  in the previous generation.

### Parallel Cellular Algorithms

Parallel algorithms refer to a computational approach where multiple solution points or populations of solutions are utilized at each iteration of the algorithm. By employing parallel processors, they can significantly enhance the speed of convergence of the final solution. They divide a problem space into smaller, localized units, referred to as cells. Each cell operates independently yet interacts with its neighbors based on predefined rules.

### Optimization in gene expression

#### Genetic Algorithm

It often involves improving the computational efficiency and accuracy of methods used to model, predict, or analyze gene expression. These algorithms play a central role in bioinformatics for tasks like identifying gene regulatory networks, finding biomarkers or understanding the dynamics of gene activity in different conditions.

## Parallel cellular Algorithms

Parallel cell algorithms are a class of algorithms where computation is distributed over a grid of cells, and each cell performs operations in parallel based on simple local rules.

### Algorithm:

Step 1%: Define objective function  $f(x) = \sum x_i^2$

Step 2%: Initialize parameters

Grid size: n x n grid where each cell represents solution

Dimensionality: No. of variables in solution (eg 2D)

Bounds: Defines range of "sol" space

Mutation rate: probability of mutating a solution

Step 3%: Initialize grid

Randomly generate initial sol's of each cell within the defined bounds

Step 4%: Evaluate initial fitness

Calculate fitness for each cell using obj function

Step 5%: Main evolutionary loop  
for each iteration

- 1) Select parents : choose a cell & best soln from neighbourhood (up, down, left, right)
- 2) Apply crossover: Generate offspring
- 3)  $\textcircled{N}$ ) Apply mutation: Randomly modify offspring with small probability to indicate diversity
- 4) Replace soln: If offspring has better fitness than current soln, replace in grid.  
Update grid

Step 6: Track best soln after each iteration (42 iterations)

Step 7: Stop after a fixed no of iterations or if convergence is reached & return best solution and its fitness value.

Applications: ~~suboptimization~~  
~~optimal flow, route, job~~  
→ Image processing and computer vision

→ Simulating natural phenomena

→ Optimization problems

## Gene Expression Algorithm

problem: Symbolic regression

Given a set of input-output data points, derive a mathematical expression that best models the relationship between variables using gene expression Algorithm (GFA).

### Algorithm:

Step 1: Create a population of random genes where each is a sequence of terminals and functions.

Step 2: Decode each gene into an executable expression.

Step 3: Use tournament selection to pick the best gene parents

Step 4: Perform single point crossover to combine genes from 2 parents into offspring.

Step 5: Mutation: Randomly modify part of genes to introduce diversity

Step 6: Elitism carry forward the best genes from current generation to next.

Step 7: Iteration: Repeat the process

for "n" no. of generations.

Step 8: Results Output the best performing gene (expression) & fitness value.

Application area selection needed

- Control System Optimization
- Engineering Design Optimization
- Pattern Recognition and Classification

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