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## Continuous Top-k Dominating Queries

Maria Kontaki, Apostolos N. Papadopoulos, Yannis Manolopoulos

**Abstract**—Top-k dominating queries use an intuitive scoring function which ranks multidimensional points with respect to their dominance power, i.e., the number of points that a point dominates. The k points with the best (e.g., highest) scores are returned to the user. Both top-k and skyline queries have been studied in a streaming environment, where changes to the data set are very frequent. In such an environment, continuous query processing techniques are required towards efficient monitoring of query results, since periodic query re-execution is computationally intensive, and therefore, prohibitive. This work contains the first study of continuous top-k dominating queries over data streams. In comparison to continuous top-k and skyline queries, continuous top-k dominating queries pose additional challenges. Three exact algorithms (BFA, EVA, ADA) are studied, and among them ADA, which is enhanced with additional optimization techniques, shows the best overall performance. In some cases, we are willing to trade accuracy for speed. Towards this direction, two approximate algorithms are proposed (AHBA and AMSA). AHBA offers probabilistic guarantees regarding the accuracy of the result based on the Hoeffding bound, whereas AMSA performs a more aggressive computation resulting in more efficient processing. Evaluation results, based on real-life and synthetic data sets, show the efficiency and scalability of our techniques.

 $\textbf{Index Terms} \\ \textbf{-} \textbf{Top-} \\ k \text{ dominating queries, data streams, continuous queries, algorithms, analysis, approximation.}$ 

#### 1 Introduction

During the last decade we are witnessing a significant interest of the data management community in preference-based query processing [12], [14] where in addition to hard constraints (e.g., price < 100 €) the results must satisfy some additional specific properties (known as preferences) related to the attribute values associated to each tuple. Tuples are typically represented as points in  $\mathbb{R}^d$  space, where d is the number of attributes. For the rest of the discussion we use the term point to denote a tuple and the term dimension to denote an attribute.

Two of the most widely used preference-based queries are: (i) the *top-k* query and (ii) the *skyline* query. In a top-kquery, a ranking function  $f: \mathbb{R}^d \to \mathbb{R}$  is required, which assigns a value to each point p. The result of a top-kquery comprises the k points with the highest values with respect to f(). A nice feature of top-k queries is that the number of answers is controlled by the parameter k, although in some cases the cardinality of the result set may exceed k due to ties (i.e., two or more points may have the same value.) In such a case, either all ties will be part of the answer or a tie breaking criterion is applied to select exactly k answers. The most important limitation of top-k queries is that a ranking function is required. This function is usually user-defined, whereas different functions generally result in different results. Moreover, in several cases the selection of an appropriate ranking function is not intuitive. For example, in an e-commerce application, there is no straightforward way to combine the attributes CPU speed and battery autonomy to select the most interesting laptop computers.

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Skyline queries, on the other hand, do not require a ranking function and they have the scaling invariance property, meaning that if scaling is applied to dimension values the result remains unchanged. The result of a skyline query is composed of the points that are not *dominated* by any other point. The dominance relationship depends on the semantics of each attribute; in some cases small values are preferable (e.g., price) whereas in other cases large values are desirable (e.g., quality). Without loss of generality, we focus on minimizing dimension values (the smaller the better). Therefore, a point p dominates another point p (p < p), if and only if p is no worse than p in all dimensions and strictly better than p in at least one dimension.

Recently, an interesting alternative has been proposed which combines the concept of dominance with the notion of ranking functions. This new query is termed top-k dominating query [25], [36], [37] and in a sense it is a combination of top-k and skyline queries: it uses a ranking function to rank points (as in top-k queries) and it uses the dominance relationship (as in skyline queries). The score associated to a point  $p_i$ , denoted as  $score(p_i)$ , equals the number of points that  $p_i$  dominates. The motivation behind this idea is to define a preference query that maintains the advantages and eliminates the limitations of both top-k and skyline queries. Therefore, top-k dominating queries have the following desirable properties: (i) the number of results is controllable, (ii) the result is scaling invariant, (iii) no user-defined ranking function is required, and (iv) each point is assigned an intuitive score which determines its rank.

To illustrate the differences among the aforementioned query types we give a simple example. Let  $\mathcal{P}$  be a set of 2-dimensional points corresponding to records with two attributes as shown in Figure 1. The coordinates of each point are given in parentheses. According to the

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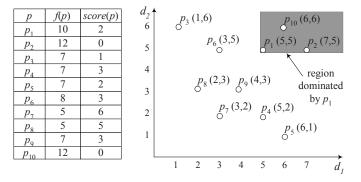


Fig. 1. Points and scores.

previous discussion, the skyline set comprises all points that are not dominated. These points are  $p_3$ ,  $p_8$ ,  $p_7$  and  $p_5$ . Let f(p) = p.x + p.y be a monotonically increasing ranking function. An example top-k query could ask for the k=2 points with the best (lowest) rank. In this case, the preferred points are  $p_7$  and  $p_8$ . Finally, a top-3 dominating query would return  $p_7$ ,  $p_8$  and  $p_6^1$ , since these points provide the highest domination score (the number of points they dominate is the largest).

Assume that the network operation center of a University campus is interested in continuously detecting computers that may establish possible attacks. Unfortunately, there are a lot of criteria that should be balanced before a wise choice is made. Assume further, that three characteristics of each computer are used, i) the consumed bandwidth, ii) the number of connections and iii) the number of destinations of its connections. A skyline query will return computers that tend to maximize one of the above attributes. Additionally the size of the result is not bounded. Moreover, the design of the appropriate ranking function for a top-k query can be turned out very difficult, even for a network analyst. On the other hand, a continuous top-k dominating query on the 3dimensional space is a more intuitive way to detect computers with suspicious behavior.

Efficient algorithms have been proposed to answer top-k queries, skyline queries, and, more recently, top-k dominating queries. The fundamental property of these algorithms is that they operate in an ad-hoc fashion, meaning that they initiate a query processing task only if a query is issued. This is sufficient for applications operating on static or almost static data sets, where updates are rare. However, many modern applications adopt the streaming model of computation, and therefore, *continuous* query processing algorithms are required to refresh the query result. Examples of such emerging applications are computer network monitoring, scientific data analysis, data management in sensor networks, document filtering in information retrieval, web-based alerts, publish/subscribe services, just to name a few.

The common property of these applications is that updates are very frequent, rendering query re-execution a non viable solution.

This paper contains the first study of continuous top-k dominating queries over multidimensional data streams. We adopt the *sliding window* approach [1], where only the n most recent points, called *active points*, are taken into account. We associate to each point  $p_i$  two time instances:  $p_i.arr$  is the arrival time of  $p_i$ , whereas  $p_i.exp$  is the corresponding expiration time. When a point expires, it is removed from the set of active points.

Continuous query evaluation poses significant challenges in comparison to ad-hoc processing. In continuous skyline queries, if  $p_i$  is dominated by  $p_j$  and  $p_i$  expires later than  $p_i$  (i.e.,  $p_i.exp > p_i.exp$ ), then it is safe to prune  $p_i$  since it will never be part of the skyline because of  $p_j$ . Moreover, in skyline queries, the transitivity property holds, i.e., if  $p_i$  dominates  $p_i$  and  $p_i$  dominates  $p_h$  then  $p_j$  dominates  $p_h$ . Thus, if  $p_i$  is discarded, one can still discard  $p_h$  due to the existence of  $p_j$ , as long as  $p_j$  expires later than both  $p_i$  and  $p_h$ . In a continuous top-k query, if there are k points with a better rank than  $p_i$ , and  $p_i$  expires earlier, it is safe to discard  $p_i$ . Moreover, the rank of a point does not vary as time progresses and it is not affected by other points, since the function f() is based on the attribute values of each point. Therefore, one can discard points if the above condition holds without affecting the query result.

On the other hand, continuous top-k dominating queries are much more complicated regarding pruning and processing. First, it is not possible to eliminate a point, even if it will never be part of the top-k result. This is because the existence of a point affects the domination score of others and thus, the arrival/expiration of a point may change the score of a significant number of other points. Second, the computation of the domination score of a point is a costly operation and it must be avoided whenever possible. However, incoming points must be assigned a score in order to decide if they are part of the answer. Existing algorithms are not equipped with the necessary tools to handle these challenges. On the contrary, our algorithms are able to continuously monitor the result of top-k dominating queries efficiently. The key contributions of this work have as follows:

- We study three exact algorithms for continuous topk dominating query processing, one of which is the clear winner due to its excellent performance. The proposed algorithm is based on a carefully designed event scheduling technique, towards avoiding costly computations.
- A performance analysis is offered studying the expected number of the most expensive computations incurred.
- Two approximate algorithms are proposed. These algorithms introduce a very useful efficiency/accuracy trade-off, and on average they achieve more than 95% accuracy, being between one and three orders of magnitude faster

<sup>1.</sup> Note that  $p_4$  and  $p_9$  have the same score as  $p_6$ . Optionally, the system could return these points also. If we allow this, then we should expect that the number of answers may be larger than k. Alternatively, a tie-breaking criterion may be used to discard points.

than the best exact algorithm.

- A thorough experimental evaluation is carried out based on real-life and synthetic data sets, providing evidence regarding the applicability, scalability and efficiency of the proposed algorithms.
- A discussion is carried out regarding the support of alternative sliding window models.

The rest of the article is organized as follows. Section 2 discusses related work in the area. Section 3 offers background information and defines the problem. Section 4 studies the properties of continuous top-*k* dominating queries and proposes a sliding window algorithm to solve the problem. Section 5 introduces some optimizations for performance improvement. Section 6 performs a theoretical analysis of the proposed algorithm. Approximate algorithms are studied in Section 7, offering faster execution times by slightly penalizing accuracy. In Section 8, we discuss the support of other sliding window models. Performance evaluation results, based on real-life as well as synthetic data sets, are given in Section 9, whereas Section 10 concludes the work.

#### 2 RELATED WORK

Preferences have been used in disciplines such as Game Theory (e.g., Pareto optimality [24]), Computational Geometry (e.g., maximal vectors [16]), Multicriteria Optimization [28], just to name a few. Recently they have been applied to databases as well [12], [14]. Preference-based queries received considerable attention, due to their usefulness in selecting the most "desirable" objects, especially when the selection criteria are contradictory. In databases, preference-based selections usually take the form of either top-k [8] or skyline queries [4].

Fagin's pioneering work [7], [8] inspired many of the subsequent research efforts [20] to design algorithms that operate under the assumption that the values in each dimension can be provided in sorted order. An extensive survey of top-k query processing techniques in relational databases can be found in [13]. Recently, the reverse top-k query [33] has been proposed and studied in relational databases. The literature is also rich in algorithms to support skyline query processing [4], [6], [25]. In [25] an efficient branch-and-bound skyline query processing scheme has been proposed, which utilizes the R-tree index [10] and shows significant performance improvements over previously proposed methods.

The main drawback of skylines is that the number of points comprising the result is not bounded. This means that a skyline query may return an excessive number of points, generating a cumbersome result. Towards alleviating this problem, several techniques have been designed. For example, *k*-dominant skylines, proposed in [5], relax the definition of dominance, to allow some points to be dominated, thus, reducing the cardinality of the skyline set. In [29], a variation of skyline queries, the *representative skyline*, has been studied. Another technique has been proposed in [18] for selecting skyline

points according to their domination capabilities. More specifically, the algorithm selects a subset of the skyline points aiming at maximizing the total number of dominated tuples. However, this method is NP-hard for high-dimensional spaces, and therefore, approximation algorithms are required towards fast computation.

Ranking of objects according to their domination power has been addressed in [17], [26], [36], [37]. In [36], [37] the authors propose efficient algorithms to determine the top-k dominating points by using an aggregate R-tree index. In [26], a method is studied to rank and cluster multidimensional points according to their domination power. In [17] the authors study efficient algorithms for top-k dominating query processing in uncertain databases. A pruning approach has been proposed to reduce the space of a probabilistic top-k dominating query and in addition, approximate queries are examined. Incremental evaluation of top-k dominating queries is examined in [15]. However, the proposed method does not take into account stream characteristics such as the expiration time of points, and therefore, is inappropriate to handle high speed streams. The concept of dominance score has been also used in [27] to rank web services based on multiple criteria.

The common characteristic of all the aforementioned approaches is that they offer solutions to process adhoc queries, whereas they do not provide mechanisms for continuous query processing over multidimensional data streams. Therefore, for each insertion/deletion of a point, the ranks of active points are computed from scratch. Towards continuous query evaluation, streaming algorithms for skyline [30] and top-k [23] query processing have been proposed. In these works, data form a streaming sequence of points, where each point is characterized by its arrival and expiration time instances, and a sliding window is used to define the set of active points (i.e., the most recently arrived points). More specifically, in [30], an incremental algorithm for continuous skyline queries has been proposed, based on the expiration time of points and the R-tree index. Additionally, continuous evaluation of top-k queries has been proposed in [23]. The proposed algorithm transforms a continuous topk to a k-skyband query [25], based on the observation that the records that appear in some result of top-kare the ones that belong to the k-skyband in the scoretime space. These algorithms are inspired by previously proposed techniques for continuous multidimensional query processing, such as the ones studied in [22].

The efficiency of the majority of the aforementioned techniques relies heavily on the use of pruning, i.e., the elimination of points towards faster processing. Unfortunately, the pruning techniques applied in those algorithms cannot be applied in the case of continuous top-k dominating queries. Due to the challenging nature of the problem, fast pruning-free solutions are required to guarantee accuracy, bookkeeping structures should be efficient to support high update rates and the proposed algorithms should be easily adapted to different sliding

window schemes, to cover a broad range of applications. In the sequel, we develop our proposal towards efficient processing of continuous top-k dominating queries over multidimensional data streams, by studying both exact and approximate solutions.

#### 3 BACKGROUND

Let  $\mathcal{P}=\{p_1,p_2,...,p_n\}$  be a set of *d*-dimensional points. We use the symbol  $p_{i,j}$  to denote the value of the j-th dimension of the *i*-th point. A point  $p_x$  dominates  $p_y$  $(p_x \prec p_y)$ , if  $\forall j \in \{1, ...d\}$ ,  $p_{x,j} \leq p_{y,j}$  and  $\exists m \in \{1, ...d\}$  such that  $p_{x,m} < p_{y,m}$ . The number of points dominated by  $p_i$ is denoted as  $score(p_i)$ :  $score(p_i) = |\{p_i \in \mathcal{P}, p_i \prec p_i\}|$ . The result of a top-k dominating query is denoted by TOPK and contains the k = |TOPK| points with the best (highest) scores. The arrival and expiration time of a point  $p_i$  is denoted as  $p_i.arr$  and  $p_i.exp$ , respectively. For convenience, the j-th best score is written as  $score_j$ , whereas by  $exp_j$  we denote the j-th smallest expiration time for points contained in TOPK. The current time instance is monitored by the variable now. Table 1 summarizes the basic symbols used. In this work, we focus on the following problem:

**Problem Definition:** Given a dynamic data stream containing n active points  $p_1, ..., p_n$ , where  $p_i \in \mathbb{R}^d$  and n is the sliding window size, monitor the k points with the highest domination score continuously.

There exist two basic sliding window types. In a *count-based* sliding window, the number of active points remains constant, and if r new points arrive the r oldest expire. In a *time-based* sliding window, the number of active points may not be constant. The expiration time of a point does not depend on the arrival or expiration of other points. The set of active points is composed of all points arrived the last T time instances. For presentation simplicity we adopt the count-based sliding window,

TABLE 1 Frequently used symbols.

Symbol	Interpretation					
$\mathcal{P}$	set of active points					
n	number of active points $(n =  \mathcal{P} )$					
d	number of dimensions					
$d_j$	the <i>j</i> -th dimension, $j = 1,, d$					
$p_i$	the $i$ -th point, $i = 1,, n$					
$p_{i,j}$	the value of the $i$ -th point in the $j$ -th dimension					
$p_i.arr$	the arrival time of point $p_i$					
$p_i.exp$	the expiration time of point $p_i$					
$score(p_i)$	the number of points dominated by $p_i$					
TOPK	the set of k points with the best scores					
k	number of points in the result $(k =  TOPK )$					
now	the current time instance					
$score_j$	the <i>j</i> -th best <i>score</i> value of the top- <i>k</i> points					
$exp_j$	the $j$ -th min expiration time of points in $TOPK$					
g	number of cells per dimension (total #cells = $g^d$ )					
$c_i$	the i-th grid cell					
$\Phi(p_i)$	points dominating $p_i$ and expiring later than $p_i$					

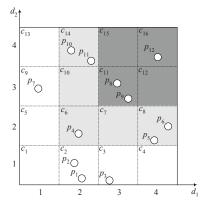


Fig. 2. Fully and partially dominated cells.

where the arrival of a new point triggers the expiration of the oldest one. In this scheme, time progresses in every update, whereas the arrival and expiration time instances of a point  $p_i$  satisfy the formula:  $p_i.exp = p_i.arr + n$ . Later, we discuss how our algorithms can handle other sliding window schemes.

A grid-based indexing scheme is used for bookkeeping purposes and for maintaining simplicity in the presentation of the algorithms. We note, however, that our algorithms do not strictly depend on the indexing structure, and therefore, other access methods could be used by performing the necessary modifications. It has been observed that this simple index structure has excellent performance in highly dynamic environments [23], [32], [35]. Each grid cell contains the IDs of the points contained in this cell. Cell  $c_i$  dominates completely all cells residing in the upper-right region with respect to the upper-right corner of  $c_i$ . For example, cell  $c_6$  in Figure 2 dominates cells  $c_{11}$ ,  $c_{12}$ ,  $c_{15}$  and  $c_{16}$ . These cells are called fully dominated cells or simply dominated cells. On the other hand, cells  $c_6$ ,  $c_7$ ,  $c_8$ ,  $c_{10}$  and  $c_{14}$  may contain points that are dominated by a point in  $c_6$ . These cells are called partially dominated cells. In Figure 2, the cells that are fully dominated by  $c_6$  are dark-shaded, whereas these that are partially dominated by  $c_6$  are light-shaded.

In addition to fast bookkeeping, the grid is used to compute the domination score  $score(p_i)$  of a point  $p_i$ . First, we determine the cell  $c_j$  containing  $p_i$ . Note that this operation is very fast and it only takes constant time. To compute  $score(p_i)$  it is necessary to count the number of points dominated by  $p_i$ . These points are contained in the cells that are fully or partially dominated by the cell hosting  $p_i$ . For instance, in Figure 2,  $p_4$  dominates  $p_6$  and  $p_{11}$  which reside in partially dominated cells. Moreover, there are 3 points  $(p_8, p_9 \text{ and } p_{12})$  in the fully dominated cells. Therefore, the total score of  $p_4$  is  $score(p_4) = 2 + 3 = 5$ . This process is called  $exact\ score\ computation\$ and it is the most time consuming task.

The naïve approach to evaluate a top-k dominating query continuously, is to perform all domination checks among points. More specifically, for a new point  $p_x$ , its score  $score(p_x)$  is computed by counting the number of

points dominated by  $p_x$ . Moreover, the score of a point  $p_y$ ,  $y \neq x$  should be increased if  $p_y$  dominates  $p_x$ . When a point expires, the scores of other points need to be updated. We call this simple algorithm BFA (<u>Brute-Force Algorithm</u>). It is expected that BFA will invoke a large number (O(n)) of domination checks between points.

#### 4 EVENT-BASED PROCESSING

In this section we propose an *event-based* algorithm (EVA) which uses event scheduling and rescheduling towards avoiding the examination of points for inclusion in TOPK. Let  $p_i$  be a point that is not part of TOPK and therefore,  $score(p_i) < score_k$  (recall that  $score_k$  is the k-th best score). In each update, the value of  $score_k$  can be reduced at most by one and the value of  $score(p_i)$  can be increased at most by one. Therefore,  $p_i$  cannot be in TOPK in less than  $\lceil (score_k - score(p_i))/2 \rceil$  time instances, unless a top-k dominating point expires during this period. Thus, we can determine a safe interval of time as suggested in the following lemma.

**Lemma 1**. Given the minimum expiration time  $exp_1$  of the top-k dominating points and the current time instance now, a point  $p_i$  cannot be part of TOPK in less than  $SI_1(p_i)$  time instances, where:

$$SI_1(p_i) = \min\{\lceil (score_k - score(p_i)/2 \rceil, exp_1 - now \}$$
 (1)

**Proof**. There are two possible cases in which  $p_i$  can be part of TOPK in each update: (i) if a point in TOPKexpires or (ii) if the score of  $p_i$  becomes larger than or equal to  $score_k$ . The first case is covered by the second part of Equation 1, since  $exp_1$  is the minimum time in which a top-k point expires. For the second case, we assume the worst case scenario, in which  $score_k$ decreases by one and  $score(p_i)$  increases by one in each update (the k-th best point dominates the expired point and does not dominate the new point whereas for  $p_i$  the opposite is true). Therefore, the difference between their scores is reduced at most by 2 in each update. Thus, at least for the next  $\lceil (score_k - score(p_i))/2 \rceil - 1$  time instances,  $score(p_i)$  is less than  $score_k$ . In summary, there are only two cases in which a point can be part of TOPK and both of them are covered by Equation 1.  $\square$ 

The safe interval  $SI_1(p_i)$  serves as a lower bound, indicating that during this interval,  $p_i$  is impossible to enter TOPK and thus, it is ignored. If now is the current time,  $p_i$  will be examined again as a possible candidate for TOPK at time  $\min(\lceil(score_k - score(p_i))/2\rceil + now, exp_1)$ . An event  $e_i$  is associated to every point  $p_i \notin TOPK$  and contains the following data:

- the event processing time, denoted as  $e_i.ept$ , indicating the time that  $p_i$  should be examined as a top-k candidate,  $e_i.ept = \min(\lceil (score_k score(p_i))/2 \rceil + now, exp_1)$ ,
- the *event generation time*, denoted as  $e_i.egt$ , storing the time instance that the event was generated, and

• the score of  $p_i$  at time  $e_i.egt$ , denoted as  $e_i.score$ .

Each event  $e_i$  is thus represented as a triplet  $\langle ept, egt, score \rangle$ . All scheduled events are organized by a priority queue, using the ept field for prioritization. The head of the queue contains the event that will be processed next, having the minimum ept value. This event will be processed if the current time equals the event processing time. For instance, if  $e_i$  is on the head, this event will be processed when  $e_i.ept = now$ . When the event  $e_i$  is processed the following actions are taken: i) the exact score of  $p_i$  is computed, ii) a new event is scheduled for  $p_i$  by computing a new value for ept.

Assume for the time being that there is no indexing scheme available. Evidently, the aforementioned approach will be more efficient than BFA, if  $SI_1(p_i)$  is long enough so that the cost of BFA during this period will be higher than that of an exact score computation. Each exact score computation costs *n* domination checks among points in the worst case. In BFA, each point  $p_i$ requires two domination checks per update; one for the incoming point and one for the expiring one. Therefore, the number of domination checks performed by BFA for the duration of the safe interval is  $2(e_i.ept - e_i.egt)$ . Consequently, BFA performs more domination checks when  $2(e_i.ept - e_i.egt) \ge n \Rightarrow (e_i.ept - e_i.egt) \ge n/2$ . This means that larger safe intervals are favorable since they lead to fewer exact score computations and therefore, less computational cost. However, safe intervals with duration more than n/2 are difficult to be produced, especially for large n and small k. For this reason, in the sequel we study two methods used by EVA to reduce the number of exact score computations. The first one focuses on bounding the score of existing points, whereas the second estimates the score of a newly arrived point.

#### 4.1 Upper-Bounding Scores of Existing Points

The event processing time  $e_i.ept$  of an event  $e_i$  is computed taking into account the worst case scenario, where  $score_k$  is reduced by one in each update, meaning that the k-th point of TOPK dominates all the outgoing points and none of the incoming points that arrived between the time  $e_i.ept$  and  $e_i.ept$ .

When an event is processed, we can reschedule the event, avoiding computing the score of the associated

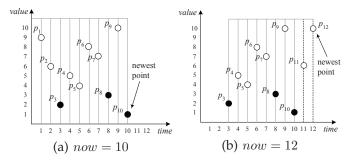


Fig. 3. Event time computation example.

point, if we keep up-to-date the scores of the top-k dominating points. Notice that the cost to update k scores is affordable since  $k \ll n$ . To compute the new event processing time, the score of the point is required which is not known. However, it is safe to use an upper bound: the score  $p_i$  is less than or equal to  $e_i.score + e_i.ept - e_i.egt$ . We use this bound in place of  $score(p_i)$  in Equation 1 to compute the new safe interval and thus, to schedule a new event for  $p_i$ .

Figure 3 shows a sliding window of length n=10 with 1-dimensional points, where the horizontal axis shows time instances. For convenience, we assume that point  $p_i$  arrived at the *i*-th time instance. Figure 3(a) shows the set of active points when now=10. For k=3, the top-3 dominating points are  $p_{10}$ ,  $p_3$  and  $p_8$  (black dots) and their corresponding scores are 9, 8 and 7 respectively. The minimum expiration time of the top-3 dominating points is  $exp_1 = 3 + 10 = 13$  ( $p_3$  will expire first) and the 3-rd best score is  $score_3 = 7$  (due to  $p_8$ ). We illustrate the computation of the event  $e_7$  of  $p_7$ . Currently we have that  $score(p_7)=3$  since  $p_7$  dominates  $p_1$ ,  $p_6$  and  $p_9$ . By substituting the values in Equation 1 we have that  $e_7.ept = \min(\lceil (7-3)/2 \rceil + 10, 13) = 12, e_7.egt = 10$  and  $e_7.score = 3$ . This means that  $p_7$  will be examined again as a possible candidate for TOPK when now=12, i.e., in the next two updates. Assume now that two updates occur and thus, now=12 as shown in Figure 3(b). The two oldest points ( $p_1$  and  $p_2$ ) have been expired and the set of active points is  $\{p_3,...,p_{12}\}$ . Since  $e_7.ept = now$ , point  $p_7$  should be examined. We recompute the event processing time of point  $p_7$ . The upper bound score estimation is  $score(p_7) \leq e_7.score + e_7.ept - e_7.egt =$ 3+12-10=5. We use this upper bound to recompute the event time, thus avoiding the exact score computation for  $score(p_7)$ . The value of  $score_3$  is still 7 and therefore,  $e_7.ept = \min(\lceil (7-5)/2 \rceil + 12, 13) = 13, e_7.egt = 12$  and  $e_7.score = 5$ , meaning that point  $p_7$  will be examined again in the subsequent update where now=13.

#### 4.2 Upper-Bounding Scores of Incoming Points

The computation of the event processing time  $e_i.ept$ requires the score of  $p_i$  or at least an upper bound. However, in the streaming scenario, new points continuously arrive and there is no information about their scores. To avoid computing scores from scratch, we try to find an upper bound of them. Let  $p_x$  be an incoming point. The key idea is to determine a point  $p_r$  with the following properties: (i) it dominates the incoming point  $p_x$ , and (ii) it is not part of *TOPK*. We denote this point as a *reference* point. If such a point exists, then we can compute an upper bound for  $score(p_x)$ , and use it in Equation 1 to calculate the event time of  $p_x$ . If now is the current time instance then  $score(p_r) \leq e_r.score + now - e_r.egt$ . Since,  $p_r$  dominates  $p_x$  then  $score(p_x) \leq score(p_r) - 1 \Rightarrow$  $score(p_x) \leq e_r.score + now - e_r.egt - 1$ . If there is no point satisfying these properties, then an exact score computation for  $p_x$  is performed.

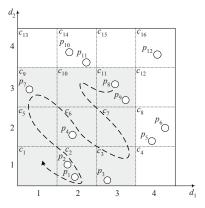


Fig. 4. Cell visiting order.

To locate a point that dominates the new point  $p_x$ , we search the grid cells that partially or fully dominate the cell  $c_i$  containing  $p_x$ . These cells lie at the lowerleft region with respect to the upper-right corner of  $c_i$ . A quick way to determine a point that dominates  $p_x$  and has the lowest score, is to use a cell visiting order as the one shown in Figure 4. Assume that a new point has been inserted in cell  $c_{11}$ . To determine the cells to be visited next, we use the locations of the cells in each dimension. The sum of cell coordinates (scc), specifies the search order. Cells with large scc values are examined first. After visiting  $c_{11}$  ( $scc(c_{11})=6$ ), the next cells in order are  $c_7$  and  $c_{10}$  ( $scc(c_7)=scc(c_{10})=5$ ). Ties are broken arbitrarily. Next, we visit  $c_3$ ,  $c_6$  and  $c_9$  $(scc(c_3)=scc(c_6)=scc(c_9)=4)$ . The search continues until either a convenient point  $p_r$  is found, or cell  $c_1$  is reached.

#### 4.3 Outline of EVA

The pseudocode of EVA (EVent-based Algorithm) is depicted in Figure 5. For each update, a sequence of operations is applied. First, the bookkeeping structure is updated (Line 1), meaning that the expiring point is deleted and the new one is inserted. Then, the scores of the top-k dominating points are updated (Line 1).

The incoming point  $p_x$  is processed to determine if it should be part of TOPK (Lines 2-8). The procedure FindReferencePoint() is called, which tries to locate a point  $p_r$  such that: (a) it dominates  $p_x$  and (b) it is not part of TOPK. If such a point does not exist or the upper bound of the score is larger than or equal to  $score_k$ , then the score of the  $p_x$  is computed from scratch. If  $score(p_x)$  is greater than  $score_k$ ,  $p_x$  is inserted in TOPK. Otherwise, an event for  $p_x$  is generated using the procedure ScheduleEvent() (Lines 19-26). This procedure takes three parameters: the id j of the point, its score(exact or an upper bound) and the current time instance now. First, it computes the event processing time and then, if this time is greater or equal to now, it inserts the event into the priority queue. Notice that, the event processing time is less than now, if the parameter score is larger than  $score_k$ . Thus, in Line 8, an event is always

```
Algorithm EVA (p_x, now)
    p_x: the incoming point
    now: the current time instance
1.
    update index; update scores of points in TOPK;
2.
    e_r.score = 0; e_r.egt = now;
    p_r \leftarrow \mathsf{FindReferencePoint}(p_x); e_r \leftarrow \mathsf{event} \ \mathsf{of} \ p_r;
    score(p_x) \leftarrow e_r.score + now - e_r.egt - 1;
5.
    if (score(p_x) \ge score_k) then
        compute score(p_x) from scratch;
7.
        if (score(p_x) \ge score_k) then insert p_x in TOPK;
    if (p_x \notin TOPK) then ScheduleEvent(x,score(p_x),now);
    e_i \leftarrow EventQueue.\mathsf{RemoveTop}(); // \text{ get the first event}
10. while (e_i.ept = now);
11.
        if (number of top-k points \geq k) then
12.
             score \leftarrow e_i.score + e_i.ept - e_i.egt;
13.
             ScheduleEvent(i,score,now);
14.
        if (e_i is not rescheduled) then
15.
             compute score(p_i) from scratch;
16.
             if (score(p_i) \ge score_k) then insert p_i in TOPK;
             else ScheduleEvent(i,score(p_i),now);
17.
18.
        e_i \leftarrow EventQueue. RemoveTop() // get the next event
19. function ScheduleEvent(j, score, now)
        exp_1 \leftarrow \text{minimum expiration time of points in } TOPK;
20.
21.
        ept \leftarrow \min(\lceil (score_k - score)/2 \rceil + now), exp_1);
22.
        if (ept \ge now) then
23.
             e_i.ept \leftarrow ept; e_i.egt \leftarrow now;
24.
             e_i.score \leftarrow score;
25.
             EventQueue.Insert(e_i);
```

Fig. 5. Outline of EVA.

generated, since either the upper bound (Line 5) or the exact score (Line 7) is less than  $score_k$ .

Finally, all events with event processing time equal to now are processed (Lines 9-18). For an event  $e_i$ , we try to recompute its  $e_i.ept$  value by using the upper bound of  $score(p_i)$  (Lines 12-13). If the event is re-inserted into the event priority queue, we consider the next event, otherwise if the upper bound estimation is poor, it is possible the computed event time to be less than now. In such a case, we proceed with the exact score computation of  $score(p_i)$  and either  $p_i$  is inserted in the top-k, or the event time is recomputed based on the exact score of  $p_i$  (Lines 14-17). Line 11 controls the expiration of a top-k dominating point. If a top-k point expires in now,  $score_k$  is not updated and therefore, we should not try to compute event times. In this case, we set  $score_k$  to -1, to force the insertion of another point in *TOPK*. The score of the point of the first examined event is computed and the point is inserted in TOPK. Next, we try to recompute the event time of the remaining events.

## 5 THE ADVANCED ALGORITHM

EVA has two important limitations. The first is that all points that are not part of TOPK, should be examined at the expiration time of a top-k dominating point. Moreover, the event time computation gives a large number of events and only a small percentage of them

will cause a change in TOPK. The second is that it is possible that many points have a score close to  $score_k$ , resulting in consecutive exact score computations. In the sequel, we discuss two significant optimizations towards alleviating these drawbacks, leading to the design of algorithm ADA ( $\underline{AD}$ vanced  $\underline{A}$ lgorithm).

#### 5.1 Advanced Event Time Computation

Let  $\Phi(p_i)$  denote the set of points that dominate  $p_i$  and expire later than  $p_i$ , i.e.,  $\Phi(p_i) = \{p_j \in \mathcal{P}, p_j \prec p_i \land p_j.exp > p_i.exp\}$ . Moreover, we denote by  $\Phi^+(p_i)$  the subset of  $\Phi(p_i)$  contained in TOPK, and by  $\Phi^-(p_i)$  the subset of  $\Phi(p_i)$  not contained in TOPK. Consequently,  $\Phi(p_i) = \Phi^+(p_i) \cup \Phi^-(p_i)$  and  $\Phi^+(p_i) \cap \Phi^-(p_i) = \emptyset$ . The key observation for a more efficient event time computation lies on the fact that if  $|\Phi^-(p_i)| > 0$ , then  $p_i$  has a chance to be part of TOPK only if these points will be included in TOPK in the future. Assume that  $p_i$  is dominated by  $p_i$  points which are not part of  $p_i$  and all of them expire later than  $p_i$  (i.e.,  $|\Phi^-(p_i)| = r$ ). Then, the following holds:

**Lemma 2**. Given the r-th minimum expiration time of the top-k dominating points, denoted as  $exp_r$  ( $0 \le r < k$ ) and the current time instance now, a point  $p_i$  with score  $score(p_i)$  cannot be part of TOPK in less than  $SI_2(p_i)$  time instances, where:

$$SI_2(p_i) = \min\{\lceil (score_{k-r} - score(p_i))/2 \rceil, exp_{r+1} - now \}$$
(2)

**Proof.** It suffices to prove that  $p_i$  can be part of TOPK if at least r+1 top-k points expire or  $score(p_i) \geq score_{k-r}$  (the (k-r)-th best score). Since there are r points that dominate  $p_i$  and expire later than  $p_i$ , these points have always higher score than  $p_i$  during its lifetime and therefore,  $p_i$  can be part of TOPK only after these points have been inserted in TOPK. If less than r+1 top-k points expire, all the available positions in TOPK will be covered by the points contained in  $\Phi^-(p_i)$ . Similarly,  $score(p_i)$  should be larger than  $score_{k-r}$ , otherwise the r points, which have higher score than  $score(p_i)$ , will be inserted in TOPK and therefore, the k-th score will be increased and will be larger than  $score(p_i)$ .

It is not hard to show that the safe interval computed by Lemma 1 is less than or equal to that computed by Lemma 2, i.e.,  $SI_1(p_i) \leq SI_2(p_i)$ . Equation 2 corresponds to Equation 1, if r=0. Otherwise, Equation 2 computes always larger safe intervals. Therefore, by using  $SI_2(p_i)$  fewer events are generated and consequently, the computational cost decreases. For instance, in Figure 3 assume that now=10, whereas  $TOPK=\{p_{10},p_3,p_8\}$  with scores 9, 8 and 7 respectively. According to Lemma 1, the event time of  $p_4$  is  $e_4.ept=\min(\lceil (7-5)/2\rceil+10,13)=11$ . Since  $p_5$  dominates  $p_4$  and expires later than  $p_4$ , it holds that  $|\Phi^-(p_4)|=1$ , which means that we can use the (k-1)-th score  $(score_{k-1})$  and the second minimum expiration

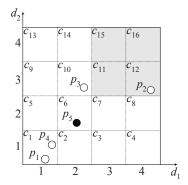


Fig. 6. Advanced event time computation.

time of the top-k dominating points  $(exp_2)$ . Thus, according to Lemma 2,  $e_4.ept = \min(\lceil (8-5)/2 \rceil + 10, 18) = 12$ .

A naïve approach to maintain  $|\Phi^-(p_i)|$  is to use a counter for each  $p_i$  and to update these counters for each arrival. More specifically, if the new point dominates  $p_i$  then we increase the counter of  $p_i$  by one. Since in the worst case all counters may require an update, it is expected that this approach will be inefficient. Thus, we use a different method which maintains a counter for each point,  $p_i.counter$ , and a counter for each cell,  $c_j.counter$ . The difference  $c_j.counter - p_i.counter$  is used as a lower bound for  $|\Phi^-(p_i)|$ . For instance, assume the 2-dimensional grid of Figure 6 and let n = 4 and k = 1, thus the answer of the query is  $p_1$ . A new point  $p_5$ (black dot) arrives and  $p_1$  expires. We increase by one all counters of cells fully dominated by the cell containing  $p_5$ , i.e., the shaded cells of Figure 6. The cost of this process is marginal. Moreover, we set the counter of the new point equal to the counter of the cell containing the new point, thus we have  $p_5.counter = c_6.counter$ . For this update, the cell counters are updated and the counter of the new point is initialized.

To use the difference  $c_i.counter - p_i.counter$  as a lower bound for  $|\Phi^-(p_i)|$  for a point  $p_i$ , we should update the point counters when there is a change in TOPK. In the case where a point  $p_j$  is inserted into TOPK, we increase by one the counters of all points dominated by  $p_i$  and expire before  $p_j$ , whereas in the case of a top-kexpiration, the counters of these points are decreased by one. In the example,  $p_4$  is inserted into TOPK because  $p_1$  expires. The counters of  $p_2$  and  $p_3$  are increased, since  $p_4$  dominates both of them and expires later than them. Before the update, we have  $p_3.counter = 1$ ,  $c_{10}.counter =$ 2 and therefore,  $c_{10}.counter - p_3.counter=1$ . After the update,  $p_3.counter$  increases by one (due to the insertion of  $p_4$  in TOPK) and thus,  $c_{10}.counter - p_3.counter = 0$ . In fact,  $|\Phi^-(p_3)| = 1$  since  $p_5$  dominates  $p_3$ , expires later, and  $p_5 \notin TOPK$ . The use of a lower bound for  $|\Phi^-(p_i)|$ results in a smaller safe interval according to Equation 2, but it will not introduce false positives in the result.

A better lower bound can be determined for  $|\Phi^-(p_i)|$  by considering points that partially dominate the cell containing  $p_i$ . In the case where an exact score computa-

tion is necessary for  $p_j$ , we decrease by one the counters of all points for which the following hold: (i) they belong to a cell that is partially dominated by the cell containing  $p_j$ , (ii)  $p_j$  dominates these points and (iii)  $p_j$  expires later than these points. In our example, assume that we cannot estimate the score of the new point  $p_5$  and therefore, an exact score computation is carried out. We decrease  $p_3.counter$  by one, since  $p_3$  belongs to cell  $c_{10}$  which is partially dominated by  $c_6$ ,  $p_5$  dominates  $p_3$  and  $p_5$  expires later than  $p_3$ . Therefore,  $|\Phi^-(p_3)|=1$ . Notice that this process does not impose additional overhead, because it is applied during exact score computations.

#### 5.2 Using Candidate Points

As mentioned before, one drawback of EVA is that if some points exist that their score is close to  $score_k$ , many exact score computations will be performed. The same holds even if the advanced event computation is applied. To overcome this problem, we propose to continuously evaluate the score of some special points called *candidate points*, whose event processing time is in the near future. The challenge is to maintain candidate points aiming at reducing the number of exact score computations.

To illustrate the idea of candidate points, assume a top-3 dominating query is applied in 1000 points and  $score_3$  is 200. Assume further that there is a point  $p_i$  with score 194 that expires after the points of TOPK. The event  $e_i$  will be processed in 3 time units. However, it is highly probable that in a so small time interval the scores of TOPK and  $p_i$  will not change. Therefore, an exact score computation will happen and  $e_i$  will be arranged to be processed again in 3 time units. When there are no drastic changes in TOPK, this process can continue for a large part of the lifespan of  $p_i$  and probably  $p_i$  will never be part of TOPK.

When an event  $e_i$  for point  $p_i$  is computed, if  $e_i.ept \leq now + \Delta t$  we insert  $p_i$  directly into the set of candidate points and we ignore the event; otherwise, we proceed in the normal way. The time threshold  $\Delta t$  is used to decide whether the event processing time is in the "near" future or not. To avoid a large number of candidate points, the parameter maxcand is used to define the maximum allowed number of maintained candidates. In our experiments,  $\Delta t$  is initialized to n/1000, and its value is adjusted automatically as follows: it decreases by one if the number of candidate points is greater than or equal to maxcand and increases by one if exact score computations are taking place. The value of maxcand is set to 1% of the sliding window size.

#### 5.3 Evicting Obsolete Events

In top-k dominating queries, we cannot prune points in contrast to skyline and top-k queries, since the domination power of the points depends on the other points. Therefore, the indexing structure used contains all points of the sliding window. On the other hand, events can be pruned, if the event processing time of a point is greater

than its expiration time. More specifically, let  $p_i$  be a point with an associated event  $e_i$ . If  $p_i.exp < e_i.ept$ , then  $p_i$  will expire before the event is processed. Such an event is characterized as *obsolete*. We can reduce the storage requirements if obsolete events are evicted. However, with less events fewer reference points are available, and thus we may affect running time. This is a trade-off between memory consumption and efficiency, and it is further studied in the performance evaluation.

#### 6 Performance Analysis

In this section, we perform an analysis towards upperbounding the expected number of exact score computations required for a sequence of m updates. Recall, that in our model, each arrival of a new point is immediately followed by an expiration of the oldest one. Following related research in the area [23], we assume that: (i) points are distributed uniformly in the unit ddimensional hypercube, and (ii) there is no correlation between the dimensions.

The cost of an exact score computation depends on the number of points that must be examined. Let g denote the number of cells in each dimension. Therefore, the total number of cells equals  $g^d$ . The following lemma gives the expected number of the partially dominated cells for any grid cell.

**Lemma 3**. The expected number of points that must be examined during an exact score computation is given by:

$$\frac{n}{2^d} \cdot \left( \left( \frac{g+1}{g} \right)^d - \left( \frac{g-1}{g} \right)^d \right) \tag{3}$$

**Proof**. By treating each dimension separately, the expected number of partially plus the number of fully dominated cells is given by:

$$\overline{FDPD} = \frac{1}{g^d} \cdot \prod_{j=1}^d \sum_{i=1}^g i = \left(\frac{g+1}{2}\right)^d$$

Again, by treating each dimension separately, the expected number of fully dominated cells is given by:

$$\overline{FD} = \frac{1}{g^d} \cdot \prod_{j=1}^d \sum_{i=1}^{g-1} i = \left(\frac{g-1}{2}\right)^d$$

By subtracting  $\overline{FD}$  from  $\overline{FDPD}$  we get that the expected number of partially dominated cells is:

$$\overline{PD} = \left(\frac{g+1}{2}\right)^d - \left(\frac{g-1}{2}\right)^d$$

Due to the uniformity assumption, there are on average  $\frac{n}{q^d}$  points in each cell, and thus, the result follows.

In the sequel, we provide an upper bound on the expected number of exact score computations required for m update operations. According to EVA, there are three cases where an exact score computation can happen during an update: i) an incoming point must enter

TOPK or the skyline of the rest of the points (with probability  $P_a$ ), ii) the expiring point belongs to TOPK (with probability  $P_e$ ) and iii) an examined event associated to a point p cannot be rescheduled (with probability  $P_p$ ). In our analysis we use the result of [9], which states that the expected number of skyline points  $\overline{sky}(u)$  for a set of u points in d dimensions by assuming independence among the dimensions is  $O(\ln^{(d-1)}u/(d-1)!)$ .

The probability that an incoming point  $p_x$  will cause an exact score computation is at most the probability that: i)  $p_x$  will land on a cell occupied by one of the k points of TOPK, ii) on a cell containing at least one skyline point of the rest n-k points, or iii) on an empty cell lying in the lower-left region of the skyline border. By the uniformity and independence assumption it follows that the expected number of empty cells is  $c/e^{n/c}$ , where  $c=g^d$  is the total number of cells. The result follows by considering that we have a balls-and-bins game and using the linearity of expectation as shown in [21]. By using the pessimistic assumption that each TOPK point and each of the  $\overline{sky}(n-k)$  points lie in a different cell, it follows that  $p_x$  will cause an exact score computation with probability<sup>2</sup> at most:

$$P_a \le \frac{k + \overline{sky}(n-k) + c/e^{n/c}}{c} \tag{4}$$

When a point expires, with probability  $P_e$  it will be one of the k points of TOPK. According to the uniformity and independence assumption it holds that:

$$P_e = k/n (5)$$

Moreover, the processing of an event associated to point p will cause an exact score computation, if and only if  $score_k$  is reduced in every update occurred during the safe interval  $SI_1(p)$ . Otherwise, the event will be rescheduled. The value of  $score_k$  is reduced during an update if the k-th best point dominates the expired point and does not dominate the new point. This probability equals the volume dominated by the k-th point multiplied by the remaining volume for each update during  $SI_1(p)$ . Therefore, we have:

$$P_p = \frac{score_k}{n} \cdot \frac{n - score_k}{n} \cdot \frac{score_k - 1}{n} \cdot \frac{n - score_k + 1}{n}$$
$$\cdots \frac{score_k - SI_1(p) + 1}{n} \cdot \frac{n - score_k + SI_1(p) - 1}{n} \Rightarrow$$

$$P_p = \prod_{i=0}^{SI_1(p)-1} \frac{(score_k - j) \cdot (n - score_k + j)}{n^2}$$

To simplify the analysis, we use only the first term of the product. Therefore, the probability  $P_p$ , that the processing of an event will cause an exact score computation satisfies the following inequality:

2. Evidently, this holds in the case that the parameter c assumes a convenient value to ensure that  $P_a$  is less than or equal to 1.

$$P_p \le \frac{score_k}{n} \cdot \frac{n - score_k}{n} \tag{6}$$

When an update occurs, an expiration with probability  $P_e$  will cause at most  $\overline{sky}(n-k)$  exact score computations. Otherwise, with probability  $P_a$  one exact score computation will take place. In case where neither a top-k expires or a top-k arrives or the new point belongs to the skyline of the n-k points, an update can cause at most  $\overline{sky}(n-k)$  exact score computations with probability  $P_p$ . Therefore, we can derive the expected number of exact score computations in the i-th update, denoted as  $E[\mathcal{X}_i]$ , by using Equations 4, 5 and 6. Let  $\mathcal{X}=\mathcal{X}_1+\mathcal{X}_2+...+\mathcal{X}_m$  be the random variable counting the total number of exact score computations performed in m updates. By the linearity of expectation we have that  $E[\mathcal{X}] = \sum_{0 \leq i \leq m} E[\mathcal{X}_i]$ . By substitutions and algebraic manipulations we get that  $E[\mathcal{X}]$  is:

$$O(m(P_a \cdot (1 - P_e) + P_e \cdot S + (1 - P_a) \cdot (1 - P_e) \cdot P_p \cdot S))$$

where,  $S=\overline{sky}(n-k)$ . The above bound is quite pessimistic, since several worst-case assumptions have been performed. For example, we have assumed that when a new point enters the skyline of the n-k points, then  $\overline{sky}(n-k)$  exact score computations will be performed, which is an overestimation. In addition, we assumed that all empty cells estimated by the balls-and-bins game are located in the lower-left corner, which again is an upper bound. We avoided the use of simplistic arguments aiming at an analysis with theoretic basis. In practice, as we have validated through experimentation, the number of exact score computations performed is far less. However, this is the first step to provide a closed-form formula to estimate the cost of the algorithms.

## 7 APPROXIMATE SOLUTIONS

So far our study has centered on *exact* algorithms, providing 100% correct and up-to-date answers to a top-k dominating query. However, in many modern applications (e.g., decision support, information retrieval), exact answers are, typically, not needed to draw useful conclusions; instead, *approximate* results are often sufficient [3], [31]. The effectiveness of an approximate solution is measured by considering the *accuracy* of the result, which corresponds to the fraction of the correct top-k dominating points returned by the algorithm over the actual number of top-k dominating points. In the sequel, we study two approximate solutions: i) a randomized approach based on probabilistic bounds and ii) a more aggressive approach without probabilistic guarantees.

#### 7.1 Approximation with Probabilistic Guarantees

The exact algorithms calculate the event time of a point  $p_i$  based either on the exact score or the maximum score. To evaluate the query accurately, the maximum possible score is computed by using the worst case scenario, in

which the score of the k-th dominating point is reduced in each update, whereas the score of  $p_i$  increases. This way, a safe upper bound is generated. However, the exact score of  $p_i$  rarely (if not ever) approaches the maximum value. By using an approximation, a more realistic value (closer to the exact score) may be computed, speeding up query execution and, on the other hand, possibly sacrificing the accuracy of the result.

From elementary probability theory, it holds that the sum of squared errors around an arbitrary value is minimized if this value is the true mean. The key idea is to maintain a random sample [34], [2], [38] of points in a cell and compute their mean score. This value is used as an approximation for the score of any other point of this particular cell. The sample size should be large enough so as to guarantee that the estimated score will not be very far from the true mean. To determine a convenient sample size we use the Hoeffding inequalities [11]. Assume s independent random variables  $\mathcal{Z}_1, ..., \mathcal{Z}_s$  such that  $\alpha \leq \mathcal{Z}_i \leq \beta$ , i=1,...,s. Let  $\mathcal{Z}=(1/s)\sum_{i=1}^s \mathcal{Z}_i$  and  $\mu=E[\mathcal{Z}]$  (the expectation of  $\mathcal{Z}$ ). For any  $\xi>0$ , the onesided and two-sided forms of the Hoeffding inequality have as follows:

$$Prob\{\mathcal{Z} - \mu \le \xi\} \ge 1 - e^{-2s\xi^2/(\beta - \alpha)^2} \tag{7}$$

$$Prob\{|\mathcal{Z} - \mu| \le \xi\} \ge 1 - 2e^{-2s\xi^2/(\beta - \alpha)^2}$$
 (8)

If  $\mathcal{Z} \geq \mu$ , then the mean value is overestimated, meaning that no false negatives appear. On the other hand, if  $\mathcal{Z} < \mu$  then some points may be missed, because  $\mathcal{Z}$  cannot be used as an upper bound. Therefore, we try to bound the error selecting an appropriate value for s to increase the probability that  $\mu - \mathcal{Z} \leq \xi$ . From Equations 7 and 8 it is not hard to deduce that:

$$Prob\{\mu - \mathcal{Z} \le \xi\} \ge 1 - e^{-2s\xi^2/(\beta - \alpha)^2} \tag{9}$$

By setting  $\delta = Prob\{\mu - Z \leq \xi\}$  and solving for s, we get an expression that gives the minimum number of samples required to have a maximum error  $\xi$  with probability at least  $\delta$ :

$$s = (\beta - \alpha)^2 \cdot \frac{\ln\left(\frac{1}{1 - \delta}\right)}{2\xi^2} \tag{10}$$

In our case, the bound is used to compute the number of samples that must be maintained for each cell  $c_j$ , in order to monitor the average score in  $c_j$ . The score of an arbitrarily selected point lies between 0 and n-1. However, if samples are taken from a specific cell  $c_j$  then  $minscore(c_j) \leq score(p_i) \leq maxscore(c_j)$ . We refer back to Figure 6 to illustrate the idea. For any point  $p_i$  hosted in cell  $c_1$  it holds that  $3 \leq score(p_i) \leq 5$ . The value of maxscore is determined by counting the number of points contained in the partially and fully dominated cells, whereas the value of minscore equals the number of points contained in the fully dominated cells. Therefore, the number of samples is determined by substituting in Equation 10 the appropriate values for

 $\xi$ ,  $\delta$ , and setting  $\alpha = minscore(c_j)$ ,  $\beta = maxscore(c_j)$ . The key observation is that if  $\xi$  may be expressed as a percentage of the score range, rather than an absolute value. Formally, by setting  $\xi = \varepsilon(\beta - \alpha)$  we have that:

$$s = \frac{\ln\left(\frac{1}{1-\delta}\right)}{2\varepsilon^2} \tag{11}$$

We argue, that it is neither practical nor meaningful to maintain a sample for every cell because: (i) the advanced event computation may be sufficient to exclude some points and therefore, a better estimation is not necessary for these points and (ii) a cell may be dominated by another cell for which we already maintain samples. In addition, a large number of sample points may lead to increased costs because the exact scores of the sample points must be monitored during updates. Thus, we maintain samples only for a small number of cells, determined using the maximum possible score of a point in a cell. We use again the parameter  $\Delta t$ , which determines if the event is in the near future or not. The following heuristic is applied: if  $maxscore(c_i) > score_k - \Delta t$  and  $c_i$  is not dominated by another cell with a sample, then we keep a sample for  $c_i$ .

The above technique is combined with ADA, which is the best exact algorithm as will be demonstrated in Section 9. In addition to the estimation performed by ADA for the score of a point  $p_i$ , a second estimation is performed using the sample points, provided that a sample exists for the cell containing  $p_i$ . Between the two estimated values the minimum is chosen. The new algorithm is termed AHBA (Approximate Hoeffding Bound Algorithm) and it has the nice property that the error introduced in the score estimation is controllable.

#### 7.2 "Quick-and-Dirty" Approximation

Algorithms ADA and AHBA try to reduce the number of events and the number of exact score computations assuming, pessimistically, that all points have a possibility to become part of the result. However, by assuming that the data distribution does not change rapidly, it is possible to ignore some points by excluding them from the event generation mechanism.

If the score of a point is low, we expect that it will remain low during its lifetime (by assuming that data distribution does not change significantly). Let  $minscore(c_j)$  denote the smallest possible score of all points contained in cell  $c_j$ . All points belonging to  $c_j$  are excluded from event processing if  $score_1 - score_k < score_k - minscore(c_j)$ . This algorithm, denoted as AMSA (Approximate Minimum Score Algorithm), uses an aggressive heuristic-based technique to speed-up processing, but it does not provide any guarantees regarding accuracy. Evidently, when the data distribution changes rapidly then this heuristic is not appropriate and EVA, ADA or AHBA should be used instead.

## 8 ALTERNATIVE SLIDING WINDOW SCHEMES

In the beginning of our exploration, we considered that a count-based sliding window is used and in particular, each update involves one arrival of a new point and one expiration of the oldest point. In this section, we discuss briefly how other sliding window models are supported by our algorithms. More specifically, we discuss how Lemma 1 and Lemma 2 adapt to these cases. All the other issues (e.g., event time computation) are addressed in a straight-forward manner.

- I) Time-based window with one arrival and one expiration in each update: Since we have one insertion in each time instance, we also have one expiration in each time instance. Thus, Lemmas 1 and 2 remain unchanged.
- II) Time-based window with multiple arrivals and expirations: In general, the number of arrivals/expirations varies for each time instance. We compute the minimum number of updates that can occur without  $p_i$  being part of TOPK. Lemmas 1 and 2 are the same, but their first part measure the number of updates instead of time instances. Therefore, Lemma 1 states that point  $p_i$  cannot be part of TOPK in less than  $\lceil ((score_k score(p_i))/2) \rceil$  updates or  $exp_1 now$  time instances. Lemma 2 is handled similarly.

**III) Count-based window with multiple arrivals and expirations:** Both Lemmas 1 and 2 give the minimum number of updates required instead of the minimum time instances. Therefore, we need to express  $exp_1 - now$  as the number of updates required for the first expiration of a point of TOPK. Assume that  $exp_1$  corresponds to the expiration time of  $p_i$ , i.e.,  $p_i.exp = exp_1$ . We can use the index i to denote the update (e.g., i is an id of the i-th update). Let  $p_j$  be the last inserted point. Then,  $exp_1 = p_i.exp = i + n$ , where n is the size of the window and now = j. Again, Lemma 2 is handled similarly.

The previous observations show that the changes required in the proposed algorithms to support other sliding window models are marginal.

## 9 Performance Evaluation Study

All algorithms have been implemented in C++ and the experiments have been conducted on a Pentium@3.0GHz Win XP machine, with 1GB of RAM. The synthetic data sets are the IND (independent) and the ANT (anticorrelated), generated by using the process described in [4]. Additionally, two real-life data sets have been used: FC (Forest Cover) (http://kdd.ics.uci.edu) containing 581,012 records with attributes such as elevation, slope, horizontal distance to hydrology, etc. and ZIL (Zillow) (http://www.zillow.com) containing 1,252,208 real estate records with 5 correlated attributes.

The computational cost is expressed by the running time per 1000 updates (arrivals/expirations). The update operations of the start-up phase (first n arrivals) is not counted in the measurements. The default values for the parameters, if not otherwise specified, are: n=2,000,000, d=4 and k=256. The maximum number of candidate points is set to 1% of the window size and the parameter  $\Delta t$  is set to n/1000. The error  $\varepsilon$  of the Hoeffding bound is set to 10% of the range of a cell, whereas. a 90% confidence is used, i.e.,  $\delta=0.9$ .

First, we study the performance of the algorithms with respect to the number of active points (window size). Figure 7 depicts the CPU time for IND and ANT data sets, by varying the window size from 1 million to 5 millions. The y-axis is illustrated in logarithmic scale. It is evident, that BFA is not appropriate for the streaming scenario and therefore it is omitted from subsequent experiments. ADA outperforms EVA, because ADA generates fewer events and performs fewer exact score computations, resulting in better performance. As expected, the difference between the two methods is more significant in the ANT data set, since the difference in score values of the points do not vary significantly. ADA overcomes this problem by computing larger event times due to the advanced event computation and mainly due to the use of candidate points.

Next, we study the performance with respect to dimensionality. The corresponding results are given in Figure 8. For IND and ANT data sets the window size is set to 2 millions, for FC is set to 500,000 and for ZIL is set to 1 million. Again, we observe that ADA is significantly more efficient than EVA due to the reason we mentioned previously. As the dimensionality increases, the scores of the points become lower since the probability that a point dominates another is significantly reduced. Therefore, EVA produces more events than ADA, and more exact score computations are involved. As expected, AHBA and AMSA are always more efficient than EVA and ADA. In particular, AMSA shows the best performance since it does not use samples to guarantee the accuracy of the result. An interesting result is depicted in Figure 8(d). In ZIL data set, the approximate algorithms perform better as dimensionality increases. This is because ZIL is correlated and therefore, in spaces with high dimensionality the points are distributed in more

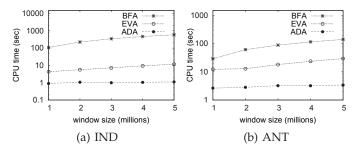


Fig. 7. Running time vs. window size (number of points).

cells and thus, the cost of maintaining sample scores and the points in TOPK is reduced. For AHBA and AMSA this cost dominates the overall cost in a correlated data set and therefore the running time is reduced. Recall, that the number of cells per dimension is fixed, thus in spaces with higher dimensionality, the number of cells increases.

Next, we study the running time vs k. The results are depicted in Figure 9. As expected, the approximate algorithms are always more efficient than the exact ones. Moreover, AMSA and ADA are always better than AHBA and EVA respectively. In addition, the performance of AHBA is similar to that of ADA for very small values of k (i.e., k < 10). Recall that AHBA reduces the number of exact score computations. The number of events processed by ADA and AHBA is similar. Therefore, if the number of exact score computations is small, the cost for sample maintenance in this case cannot equalize the cost of exact score computations. In this case we observe that for very small values of k (< 15) the performance of ADA and AHBA is similar. The gap becomes even more significant for larger values of k.

The next experiment studies the behavior of AHBA for different values of the error  $\varepsilon$  and the probability  $\delta$  of the Hoeffding bound as defined in Equation 11. Figure 10 depicts the running time of AHBA and ADA. The parameter  $\varepsilon$  assumes values from a 1% to 5%, whereas  $\delta$ is set to 0.99, 0.95 and 0.90. As expected, the running time is improved when  $\varepsilon$  increases and  $\delta$  decreases, whereas accuracy is not compromised significantly as it is illustrated in Table 2, which shows the accuracy achieved for the ANT and FC data sets, for the same values of  $\varepsilon$  and  $\delta$  used in Figures 10(b) and 10(c) respectively. Accuracy is measured as follows: assume that TOPK' is the result of the approximate algorithm. For each update, the accuracy is computed as  $|TOPK \cap TOPK'|/k$ . Mean accuracy is presented as the average accuracy of all updates, excluding those of the start-up phase.

Next, we compare the accuracy of AHBA and AMSA. The results are given in Table 3 for  $\varepsilon=10\%$  and  $\delta=0.9$ . As expected, AHBA achieves the best accuracy in all cases in comparison to AMSA. In addition, AHBA may detect a change in TOPK after some updates, in contrast to AMSA which will loose the change completely if the specific point was pruned. Furthermore, AHBA has the nice property that it will miss the points with the lowest scores first. Both AHBA and AMSA have the

TABLE 2 Mean accuracy (%) for different values of  $\varepsilon$  and  $\delta$ .

		ANT		FC			
ε	δ=0.99	δ=0.95	δ=0.90	δ=0.99	δ=0.95	δ=0.90	
1%	100	100	100	99.9	99.8	99.8	
2%	100	100	100	99.8	99.8	99.5	
3%	100	100	99.9	99.5	99.5	98.9	
4%	99.9	99.9	99.9	99.1	98.0	97.8	
5%	99.9	99.9	99.9	98.3	97.5	97.4	

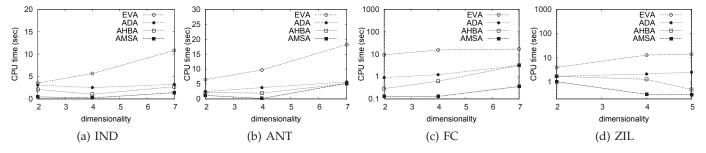


Fig. 8. Running time vs. dimensionality (d).

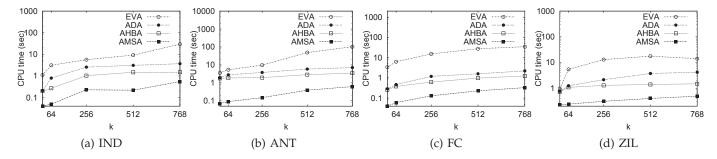


Fig. 9. Running time vs. number of answers (k).

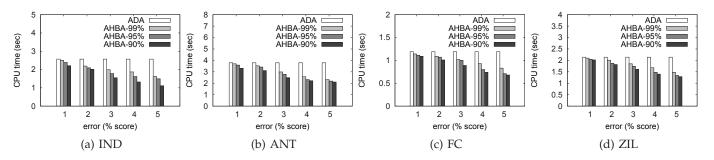


Fig. 10. Running time vs. error ( $\varepsilon$ ) and probability ( $\delta$ ) of the Hoeffding bound.

TABLE 3 Mean accuracy (%) vs. k ( $\varepsilon=10\%,\,\delta=0.9$ ).

	IN	D	Al	T	F	С	ZI	L
k	AHBA	AMSA	AHBA	AMSA	AHBA	AMSA	AHBA	AMSA
16	100	100	100	100	81.7	79.6	100.0	99.9
64	100	100	100	99.6	86.9	84.3	99.8	99.6
256	99.9	99.8	99.9	99.2	92.8	91.4	99.6	99.3
512	99.8	99.5	99.8	98.4	94.2	93.8	99.1	98.6

worst performance for FC data set. In FC, the top-k points are changed frequently, thus the approximate algorithms achieve poor accuracy since they cannot detect all changes. This phenomenon is minimized as k increases, because the query result is not varied drastically. In general, AMSA offers better response time than AHBA, as shown previously, but shows worse accuracy.

Next, we measure the number of events that each method processes, the number of exact score computations, and the total number of comparisons (between numbers). Table 4 illustrates the results per 1000 updates for the ANT data set. It is evident, that ADA reduces

TABLE 4
Cost analysis per 1000 updates (ANT data set).

		#events	#exact score	#comparisons
k	algorithm	processed	computations	(millions)
16	EVA	1147.3	15.2	26.4
	ADA	1052.7	3.8	12.5
	AHBA	1005.4	0.0	10.6
	AMSA	1000.0	0.0	0.07
64	EVA	201,219.0	22.0	33.7
	ADA	22,247.3	8.7	18.4
	AHBA	22,146.3	0.0	10.8
	AMSA	1000.0	0.0	0.3
	EVA	201,508.9	50.1	65.3
256	ADA	22,361.1	14.7	25.7
230	AHBA	22,170.5	0.1	11.6
	AMSA	1000.0	0.0	1.1
512	EVA	802,160.8	296.0	332.2
	ADA	123,942.3	22.6	36.0
	AHBA	123,819.1	0.3	14.0
	AMSA	999.6	0.0	2.8

significantly the number of the examined events and the exact score computations, especially for large values of k. This happens due to the use of the advanced event computation. Additionally, the number of exact score

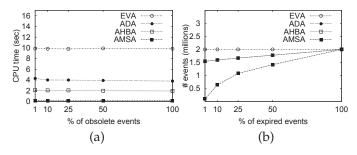


Fig. 11. Running time (a) and number of events (b) vs. percentage of maintained obsolete events (ANT).

computations is reduced mainly due to the use of candidate points, as described in Section 5.2. AHBA and ADA process almost the same number of events. The main advantage of AHBA is that it further reduces the number of exact score computations by using sampling. AMSA manages to reduce further both the number of processed events and the number of exact score computations, offering the best running time, but without guarantees.

Next, we examine the storage requirements of the algorithms. EVA uses only the events, whereas ADA, AHBA and AMSA use events, counters for the advanced event computation and candidates points. Moreover, AHBA maintains samples. The worst memory consumption is 30.54 MB for AHBA, 30.52 for ADA and AMSA and 22.91 for EVA, for the default set, taking account all data sets. Recall from Section 5.3, that obsolete events have an event processing time larger than the expiration time of the associated point and thus, they may be discarded to reduce memory consumption. However, by discarding obsolete events, the number of points that may be used as reference points is reduced. In all experiments, the algorithms maintain all obsolete events and therefore ADA and AMSA have similar memory consumption. AHBA has a small overhead in memory due to the maintenance of sample points.

It is evident, that the major storage cost is due to events. Although the memory requirements are low, we study the effect of obsolete event pruning. In this experiment, a fraction of them is being used while the remaining are pruned. The motivation behind this choice is to check if the elimination of obsolete events has an impact on the running time of the algorithms. The results for the ANT data set are depicted in Figure 11. The results for IND, FC and ZIL are similar and thus omitted. Figure 11(a) shows the running time with respect to the ratio of obsolete events that each method maintains. For example, ADA has 460,248 obsolete events when 1% of them are kept, whereas AMSA has 1,919,567 obsolete events. Since the running time is almost unaffected, it does not pay off to keep a high percentage of obsolete events, because this will impact storage. On the other hand, storage savings are significant, especially for AMSA, as it is depicted in Figure 11(b). Algorithms ADA and AHBA process almost the same number of events, since they

both use the advanced event computation technique. AMSA achieves even better storage savings due to the aggressive point elimination technique applied, whereas EVA cannot reduce the number of processed events, because it does not produce obsolete events.

#### 10 CONCLUSIONS

Top-k dominating queries have been proposed recently as an alternative to skyline and top-k queries. This query has a number of attractive properties such as: an intuitive ranking function is used, the result is unaffected by dimension scaling and the number of results is bounded by k. This paper is the first study of top-k dominating query processing algorithms in a streaming environment.

The two proposed methods, EVA and ADA consistently outperform the baseline algorithm, whereas ADA shows the best overall performance, being orders of magnitude faster than the brute-force approach. An analysis is performed for the proposed techniques to derive an upper bound for the expected number of exact score computations that may occur. In addition, we have studied two approximate algorithms, AHBA and AMSA, which sacrifice accuracy for faster computation. AHBA is based on sampling and offers probabilistic guarantees regarding the approximation error. On the other hand, AMSA is based on event pruning leading to faster processing with less accuracy compared to AHBA.

The three algorithms, ADA, AHBA and AMSA, can work in combination. If we have to be strict regarding accuracy then ADA must be used. In case a heavy system load is detected and accuracy may be compromised (but within limits) then AHBA may be activated. Finally, if an even more fast solution is required AMSA may be used. Since all algorithms are based on the event-based framework, they can operate in a synergetic manner, offering significant flexibility.

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