

Imperfect Competition and Rents in Labor and Product Markets: The Case of the Construction Industry

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Empirical context: We link the universe of U.S. **firm** and **worker** tax returns with records we collected from **procurement auctions**.

This Paper (1/2)

Framework for jointly analyzing **labor** and **product** market power.

- **Distinguish** supply and demand factors in both markets.
- **Closed-form** identification of all model parameters.
- **Measures** of rents and incidence of procurement.
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Identify returns to labor and product demand elasticities:

- **Challenge:** Unobserved firm-specific productivity shocks.
- **Approach:** Invert the bidding strategy in the **auction**.
- **Preview:** technology \approx CRS, 16% price markup.

This Paper (2/2)

Model estimates:

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Model counterfactuals:

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- **Intuition:** Cut **employment** to exploit **labor** \Rightarrow less **output** means higher **prices** \Rightarrow mitigates incentive to cut.
- **Quantitative finding:** Reducing labor supply elasticity in half,
 - if the firm were a **price-taker**: 22% less employment
 - with **product market power**: 12% less employment

Related Literature

Wage inequality, imperfect competition, compensating differentials

- Rosen 1986; Murphy and Topel 1990; Gibbons and Katz 1992; Abowd Lemieux 1993; Abowd et al 1999; Hamermesh 1999; Pierce 2001; Bhaskar et al 2002; Manning 2003, 2011; Mas and Pallais 2017; Wiswall and Zafar 2017; Card et al 2013, 2016, 2018; Maestas et al 2018; Caldwell Oehlsen 2018; Berger et al 2019; Jarosch et al 2019; Chan et al 2020; Bassier et al 2020; Hershbein et al 2020; Azar Berry Marinescu 2020; many more

Inferring monopsony from pass-through of firm-specific shocks

- van Reenen 1996; Kline et al 2019; Howell Brown 2020; Lamadon Mogstad Setzler 2022

Empirical designs for auctions

- Ferraz et al 2015; Lee 2017; Cho 2018; Hvide Meling 2019; Gugler et al 2020

1. Framework with Labor and Product Market Power
2. Data Sources
3. Recovering Key Model Parameters
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Model

We develop a model with imperfect competition in both **labor** and **product** markets.

The model serves several purposes:

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Key equations provided by the model in **blue**, they will be:

- Labor supply curve
- Product demand curve
- Optimal intermediate inputs
- Optimal auction bid
- Rents expression

Preferences If employed by firm j at wage W_{jt} , worker i utility is

$$\mathcal{U}_{it}(j, W_{jt}) = \log W_{jt} + g_{jt} + \eta_{ijt} \quad (1)$$

- g_{jt} is common, gives rise to *vertical* differentiation
- η_{ijt} is idiosyncratic to worker i , gives *horizontal* differentiation

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Firm-specific labor supply curve:

$$W_{jt} = L_{jt}^{\theta} U_{jt} \quad \implies \quad w_{jt} = \theta \ell_{jt} + u_{jt} \quad (2)$$

where $1/\theta$ is the LS elasticity and U_{jt} is the firm-specific amenity

- Strategically small: no firm can shift aggregate labor supply

Technology

Production Function Firms produce using labor L , capital K , and intermediate inputs M in the Akerberg et al (2015) technology,

$$Q_{jt} = \min\{\Omega_{jt} L_{jt}^{\beta_L} K_{jt}^{\beta_K}, \beta_M M_{jt}\} \exp(e_{jt}) \quad (3)$$

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Composite Production If capital market is perfect, simplifies to

$$Q_{jt} = \min\{\Phi_{jt} L_{jt}^{\rho}, \beta_M M_{jt}\} \exp(e_{jt}) \quad (4)$$

where ρ is composite labor returns and Φ_{jt} is composite TFP.

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Optimal intermediate inputs Defining $X_{jt} \equiv p_M M_{jt}$, the Leontief FOC and competitive market for intermediate inputs gives,

$$X_{jt} = \frac{p_M}{\beta_M} L_{jt}^{\rho} \Phi_{jt} \quad \implies \quad x_{jt} = \kappa_X + \rho \ell_{jt} + \phi_{jt} \quad (5)$$

Firm's Problem

Output Let G denote govt market and H denote private market.
Denote output in G by Q_{jt}^G and in H by Q_{jt}^H

- First-stage: Firms bid to produce \bar{Q}^G , $D_{jt} = 1$ if winner
- Second-stage: Choose total output $Q_{jt} = \bar{Q}^G D_{jt} + Q_{jt}^H$

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Private Market Firms face downward-sloping demand,

$$P_{jt}^H = p_H \left(Q_{jt}^H \right)^{-\epsilon} \implies R_{jt}^H = p_H \left(Q_{jt}^H \right)^{1-\epsilon} \implies r_{jt}^H = \kappa_R + (1-\epsilon)q_{jt}^H \quad (6)$$

where $1/\epsilon$ is the price elasticity of demand

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Firm's Problem Given $Q_j \geq \bar{Q}^G d$ and auction outcome $D_j = d$,

$$\max_{L_{djt}, K_{djt}, M_{djt}} \pi_{djt}^H = R_{djt}^H - W_{djt}L_{djt} - p_M M_{djt} - p_K K_{djt} \quad (7)$$

subject to the labor supply curve, the product demand curve, and the production function.

Government Market for Procurements

Opportunity Cost Given private market profits π_{djt}^H if $D_{jt} = d$,

$$\sigma_u(\phi_{jt}) = \pi_{0jt}^H - \pi_{1jt}^H > 0, \quad (8)$$

Auction problem Firm j chooses optimal bid Z_{jt} that solves,

$$\max_{Z_{jt}} \underbrace{(Z_{jt} - \sigma_u(\phi_{jt}))}_{\text{payoff}} \times \underbrace{\Pr(D_{jt} = 1|Z_{jt})}_{\text{probability of winning}} \quad (9)$$

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Optimal bid Unique symmetric equilibrium is defined by,

$$s_u(\phi_{jt}) = \sigma_u(\phi_{jt}) \delta_u(\phi_{jt}), \quad \delta_u(\phi_{jt}) \equiv 1 + \frac{\int_{\bar{\sigma}}^{\sigma} [1 - F_u(\tilde{\sigma})]^{l-1} d\tilde{\sigma}}{\sigma_u(\phi_{jt}) [1 - F_u(\sigma_u(\phi_{jt}))]^{l-1}}$$

where l is number of bidders and δ is markup on opportunity cost

Defining Worker Rents

Notation Suppose firm j increases wage from W_{jt} to \widetilde{W}_{jt} , and denote worker i 's preferred firm excluding j as j_t^*

Worker Rents The equivalent variation V_{ijt} for the wage change is

$$\underbrace{\max \left\{ \begin{array}{l} \log \widetilde{W}_{jt} + g_{jt} + \eta_{ijt}, \\ \log W_{j_t^* t} + g_{j_t^* t} + \eta_{ij_t^* t} \end{array} \right\}}_{\text{utility with wage increase at firm } j} = \underbrace{\max \left\{ \begin{array}{l} \log (W_{jt} + V_{ijt}) + g_{jt} + \eta_{ijt}, \\ \log (W_{j_t^* t} + V_{ijt}) + g_{j_t^* t} + \eta_{ij_t^* t} \end{array} \right\}}_{\text{equivalent utility at the initial choice of firm}}$$

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Sum of Worker Rents Using our functional form to simplify,

$$V_{jt} \equiv \sum_i V_{ijt} = \frac{\widetilde{B}_{jt} - B_{jt}}{1 + 1/\theta} \quad (10)$$

where $\widetilde{B}_{jt} - B_{jt}$ is the change in wage bill and $1/\theta$ is LS elasticity

Rents and Incidence

Incidence of Procurements

$$\underbrace{V_{1jt}}_{\text{Total rents}} = \underbrace{V_{0jt}}_{\text{Baseline rents}} + \underbrace{V_{\Delta jt}}_{\text{Incidence}} = \underbrace{\frac{B_{0jt}}{1 + 1/\theta}}_{\text{Baseline rents}} + \underbrace{\frac{B_{1jt} - B_{0jt}}{1 + 1/\theta}}_{\text{Incidence}} \quad (11)$$

Incidence for Incumbents and New Hires

$$\underbrace{V_{\Delta jt}}_{\text{Incidence}} = \underbrace{L_{0jt} (W_{1jt} - W_{0jt})}_{\text{Incidence for incumbents}} + \underbrace{W_{1jt} (L_{1jt} - L_{0jt}) - \frac{B_{1jt} - B_{0jt}}{1 + \theta}}_{\text{Incidence for new hires}}.$$

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Firm Rents

$$\underbrace{\pi_{1jt}}_{\text{Total firm rents}} = \underbrace{\pi_{0jt}}_{\text{Baseline firm rents}} + \underbrace{\pi_{\Delta jt}}_{\text{Incidence on firms}} \quad (12)$$

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Data Sources (1/2)

US tax data 2001-15 universe of business and worker tax returns

Firms: Business tax returns include balance sheet and other information for C-corps, S-corps, and partnerships

- **firm:** tax entity (EIN)
- **sales:** gross receipts from business operations (not dividends)
- **profits:** EBITD (earnings before interest, taxes, deductions)
- **intermediate inputs:** COGS (cost of goods sold)
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Workers: W-2 records on employment and total earnings

- **labor:** link workers to their highest-paying employer with earnings above FTE threshold, restrict to age 25-60
- **contractors:** also observe indep. contractors (Form 1099)

Data Sources (2/2)

Auction data Firm-auction records on bids and winners of department of transportation (DOT) procurement contracts

- state DOTs use auctions to procure construction and landscaping work on roads and bridges
- First-price sealed-bid auctions (output price = lowest bid), where we observe bid of each firm, not only the winner
- FOIA or webscraped from BidX.com & state-specific websites
- Cover more than **100,000** auctions by 28 state DOTs, including large states like California, Texas, and Florida
- No evidence of collusion [▶ test results](#)

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Final data Link tax returns to auction records by fuzzy matching on firm name and address

- Final data: **8,000** unique firms, **360,000** unique workers
- 6 states provide EIN, used for training algorithm & robustness

Descriptive Statistics for the Linked Sample

	Sample Size	Share of the Construction Sector	
Number of Firms	7,876	0.9%	
Workers per Firm	46	11.7%	
	Value Per Firm (\$ millions)	Mean of the Log	Share of the Construction Sector (%)
Sales	19.927	15.061	12.1%
EBITD	9.159	14.075	9.6%
Intermediate Costs	14.661	14.719	12.4%
Wage bill	2.737	13.549	13.4%

- Final sample: 8,000 unique firms, 360,000 unique workers
- Average firm has 46 employees and \$9M in profits

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Recovering Key Model Parameters

Using the key equations provided by the model that were in **blue** above, we now identify and estimate:

- **Labor supply** elasticity (4 slides)
- **Firm technology** & **product demand** elasticities (2 slides)

Labor Supply Elasticity (1/4)

Goal: Identify the labor supply elasticity, $1/\theta$.

Model: Log inverse labor supply curve is,

$$w_{jt} = \theta \ell_{jt} + u_{jt} = \theta \ell_{jt} + \psi_j + \xi_t + \nu_{jt} \quad (13)$$

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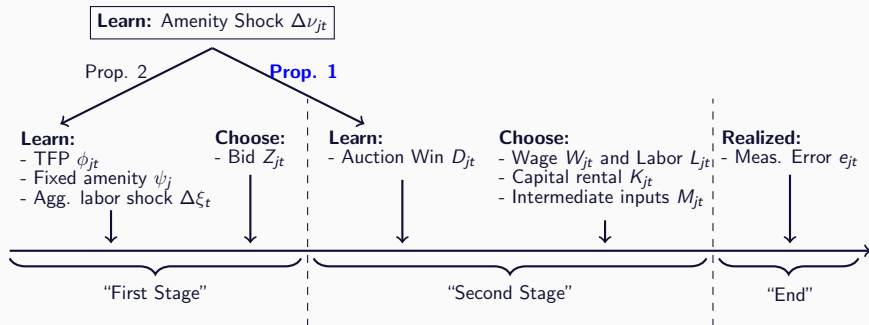
Easy to deal with:

- Time-invariant firm-specific amenities ψ_j (take differences)
- Aggregate labor supply shocks $\Delta \xi_t$ (add year fixed effects)

$$\Delta w_{jt} = \theta \Delta \ell_{jt} + \Delta \xi_t + \Delta \nu_{jt} \quad (14)$$

Challenge: Regression of change in log wage on change in log employment biased for θ due to firm-specific amenity shock $\Delta \nu_{jt}$

Sequence of Events within Time Period t



Labor Supply Elasticity (2/4)

Assumption 1. $\Delta\nu_{jt}$ not in information set at “First Stage” of t when bid is placed in auction $\implies D_{jt} \perp \Delta\nu_{jt}$.

- Time delay assumptions are standard for identification in empirical IO (Akerberg et al 2015; Gandhi et al 2020).
- Delay is between *estimating* labor cost (bidding at beginning of period t) and actually hiring labor (middle of period t)

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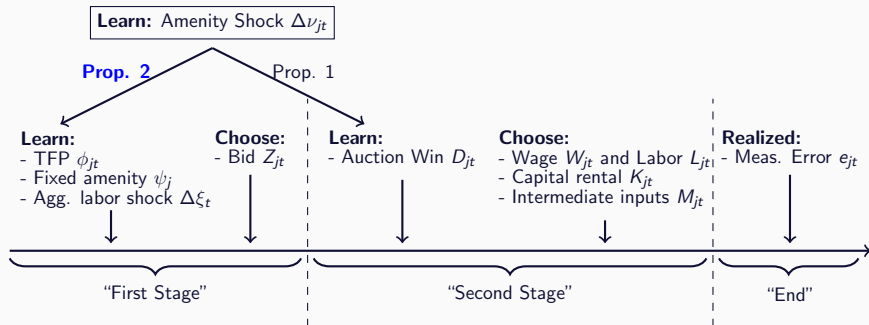
Proposition 1. θ is recovered by the IV estimator,

$$\theta_{IV} \equiv \frac{\text{Cov}[\Delta w_{jt}, D_{jt}]}{\text{Cov}[\Delta \ell_{jt}, D_{jt}]} \quad (15)$$

Important to emphasize what is **not** restricted by Assumption 1:

- no additional restrictions on joint dist of $(Z_{jt}, D_{jt}, \phi_{jt}, \psi_j, \xi_t)$.
- allows $\text{Var}(\Delta\nu_{jt}) > 0$, clear step forward in this literature.
- allows $\Delta\ell_{jt}, \Delta w_{jt}$ to depend on $\Delta\nu_{jt}$, no time delay here.

Sequence of Events within Time Period t



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Intuition:

- First-price auctions \implies winning fully determined by bids Z_{jt} .
- Restrict sample to $\tau_{jt} \leq \bar{\tau}$. As $\bar{\tau} \rightarrow 0^+$, Z_{jt} of winners=losers.
- Therefore, $\mathbb{E}[\Delta \nu_{jt}]$ of winners and losers converges as $\bar{\tau} \rightarrow 0^+$

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Proposition 2: θ is recovered by the RDD estimator,

$$\theta_{\bar{\tau}} \equiv \frac{\mathbb{E}[\Delta w_{jt} | \tau_{jt} = 0] - \mathbb{E}[\Delta w_{jt} | 0 < \tau_{jt} \leq \bar{\tau}]}{\mathbb{E}[\Delta \ell_{jt} | \tau_{jt} = 0] - \mathbb{E}[\Delta \ell_{jt} | 0 < \tau_{jt} \leq \bar{\tau}]} \quad (16)$$

where $\bar{\tau}$ is a proximity parameter and the conditioning on ι is implicit. Then, $\lim_{\bar{\tau} \rightarrow 0^+} \theta_{\bar{\tau}} = \theta$.

Labor Supply Elasticity (4/4)

Results using multiplicity of approaches:

- Estimator of Proposition 1: $1/\theta = 4.1$, markdown = 0.80
- Estimator of Proposition 2: $1/\theta = 3.5$, markdown = 0.78
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Labor Supply Elasticity (4/4)

Results using multiplicity of approaches:

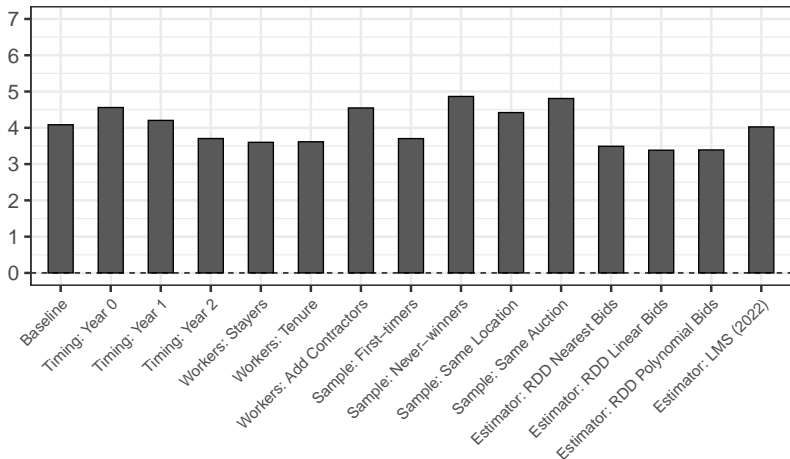
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Sensitivity checks:

- Passes falsification test using IV on the pre-period outcomes
- No evidence of bias from slow adjustments over time
- No evidence of bias from worker composition changes
- No evidence of bias from local aggregate shocks
- Not sensitive to alternative choices of auction loser sample
- Not sensitive to right-to-work or prevailing wage law coverage
- Not sensitive to alternative parameterizations of Proposition 2
- Various checks using this sample and external BLS and Census wage surveys indicate wage effects not due to hours responses
- ... [▶ more](#)

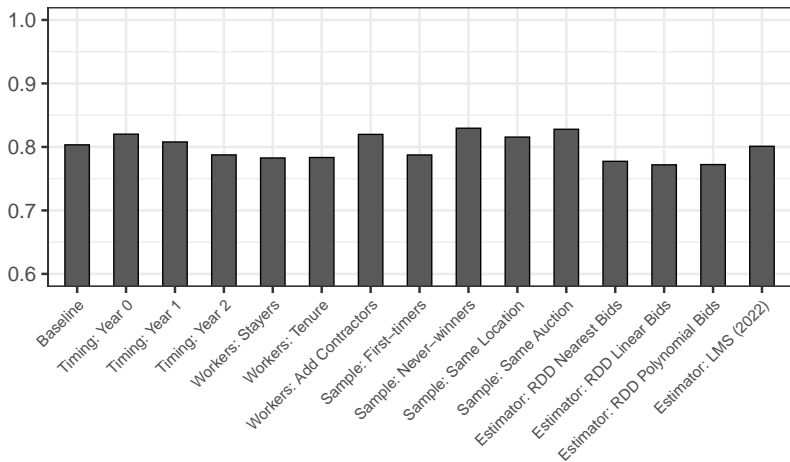
Robustness: Labor Supply Elasticity Specifications

Labor supply elasticity $1/\theta$:



Robustness: Wage Markdown Specifications

Wage markdown $\frac{1}{1+\theta}$:



Technology and Product Demand Elasticities (1/2)

Goal: Identify the composite returns to labor, ρ .

Model: Optimal intermediate inputs imply,

$$x_{jt} = \kappa_X + \rho \ell_{jt} + \phi_{jt} \quad (17)$$

Challenge: log TFP ϕ is a determinant of both log labor ℓ and log intermediate input expenditures x .

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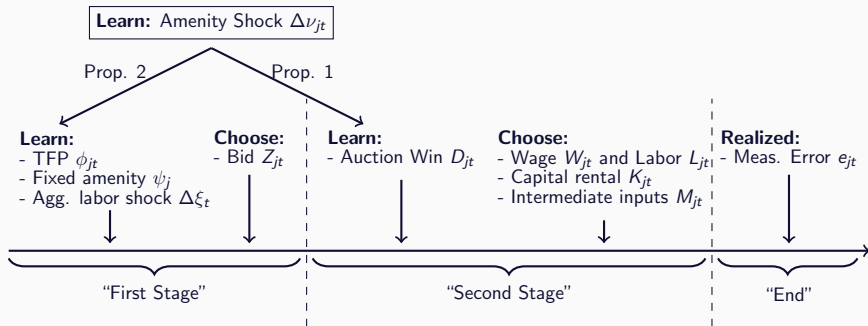
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Proposition 3: Controlling for (Z_{jt}, u_{jt}) controls for ϕ_{jt} :

$$\frac{\text{Cov}[x_{jt}, \ell_{jt} | \hat{u}_{jt}, Z_{jt}]}{\text{Var}[\ell_{jt} | \hat{u}_{jt}, Z_{jt}]} = \frac{\text{Cov}[x_{jt}, \ell_{jt} | \hat{u}_{jt}, \phi_{jt}]}{\text{Var}[\ell_{jt} | \hat{u}_{jt}, \phi_{jt}]} = \rho \quad (18)$$

Sequence of Events within Time Period t



Technology and Product Demand Elasticities (2/2)

Goal: Identify the product demand elasticity, $1/\epsilon$.

We extend the de Loecker Eeckhout Unger (2020) measure of inverse markups to incorporate labor market power ($\theta > 0$):

$$\overbrace{(1 - \epsilon)}^{\text{markup}^{-1}} = \frac{\overbrace{(1 + \theta)}^{\text{markdown}^{-1}}}{\beta_L} \frac{B_{jt}}{R_{jt}} + \frac{X_{jt}}{R_{jt}} = \overbrace{(1 + \theta)}^{\text{markdown}^{-1}} \frac{s_L}{\beta_L} + s_M \quad (19)$$

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Product demand elasticity: We estimate $1/\epsilon = 7.3$, which gives a **price markup**, $(1/\epsilon)/(1/\epsilon - 1)$, that is 16% above marginal cost.

Composite returns to labor: We estimate $\rho = 1.09$, just above **constant returns to scale**, in line with the literature (e.g. Combes Duranton & Gobillon 2021 find CRS in housing construction).

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- Robust to using main identifying moments instead of GMM.
- Robust to Cobb-Douglas instead of Leontief prod function.
- Robust to relaxing the auction symmetry assumption.
- Robust to controlling for aggregate price shocks.

1. Framework with Labor and Product Market Power
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3. Recovering Key Model Parameters
4. Results from Estimated Model
5. Interactions between Labor and Product Market Power

Results from Estimated Model (1/5): Double Markdown

$$W_{jt} = \overbrace{\frac{1}{1+\theta}}^{\text{markdown}} \times \text{MRPL}_{jt}$$

A natural measure of monopsony power is the **markdown**

- We estimate a **markdown** of 0.80, so workers are paid 20% below the marginal revenue product of labor (MRPL)

Results from Estimated Model (1/5): Double Markdown

$$W_{jt} = \overbrace{\frac{1}{1+\theta}}^{\text{markdown}} \times \text{MRPL}_{jt} = \underbrace{\frac{1}{1+\theta}}_{\text{double markdown}} \times \overbrace{\left(\frac{1/\epsilon}{1/\epsilon - 1}\right)^{-1}}^{\text{inverse markup}} \times \underbrace{P_{jt} \times \text{MPL}_{jt}}_{\text{VMPL}}$$

A natural measure of monopsony power is the **markdown**

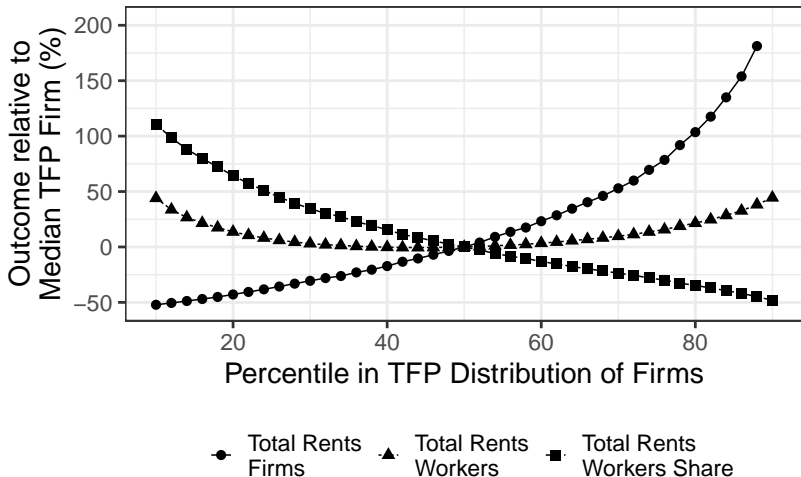
- We estimate a **markdown** of 0.80, so workers are paid 20% below the marginal revenue product of labor (MRPL)
- But MRPL depends on **product market power**
- Special case w/o intermediate inputs: MRPL equals **inverse markup** times the value of the marginal product of labor (MPL) at fixed prices, so **higher markup** \Rightarrow **lower wage**
- We estimate a **composite markdown** of 0.69, so workers are paid 31% below VMPL, versus 20% if ignoring the markup

Results from Estimated Model (2/5): Baseline Rents

		Actual	Counterf.	Difference	
		$d = 1$	$d = 0$	Level	Relative
Labor market					
L_{jt}	Employment (#)	24.7	12.8	11.9	92.7%
W_{jt}	Wage (\$1K)	59.1	50.4	8.8	17.4%
B_{jt}	Wage bill (\$1K)	1,459.6	645.2	814.4	126.2%
Rents					
V_{jt}	Worker rents (\$1K/L)	11.6	5.1	6.5	126.2%
π_{jt}	Firm profits (\$1K/L)	43.1	33.4	9.6	28.7%

In the actual economy ($d = 1$), per-capita worker rents $\frac{W}{1+1/\theta}$ are about \$12,000 per year, less than 1/4 of all rents.

Results from Estimated Model (3/5): Rents and TFP



Workers' share of rents is smaller at more productive firms.

Results from Estimated Model (4/5): Marginal Rents

		Actual	Counterf.	Difference	
		$d = 1$	$d = 0$	Level	Relative
Labor market					
L_{jt}	Employment (#)	24.7	12.8	11.9	92.7%
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We simulate winning versus losing an auction among winners.

Hiring to fulfill the government contract leads to bidding up wages, running up worker rents, with only a small increase in firm rents.

Results from Estimated Model (5/5): Output/Crowd-out

		Actual	Counterf.	Difference	
		$d = 1$	$d = 0$	Level	Relative
Input Expenditures					
B_{jt}	Wage bill (\$1K)	1,459.6	645.2	814.4	126.2%
X_{jt}	Intermediate inputs (\$1K)	4,715.1	2,308.6	2,406.5	104.2%
$p_K K_{jt}$	Capital rentals (\$1K)	1,724.7	762.4	962.3	126.2%
Total production					
Q_{jt}	Output (#)	38.3	18.7	19.5	104.2%
R_{jt}	Revenue (\$1K)	8,962.1	4,541.6	4,420.5	97.3%
Private production					
Q_{jt}^H	Output (#)	13.7	18.7	-5.1	-27.0%
R_{jt}^H	Revenue (\$1K)	3,460.7	4,541.6	-1,080.9	-23.8%

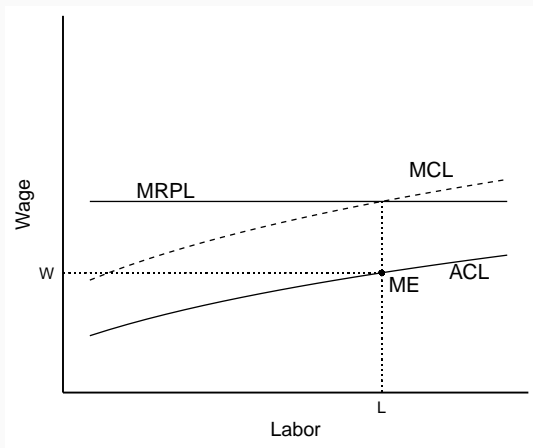
The government contract nearly doubles the firm's revenues.

However, it crowds out about 1/4 of private sector output.

Note that output declines more than revenues due to markups.

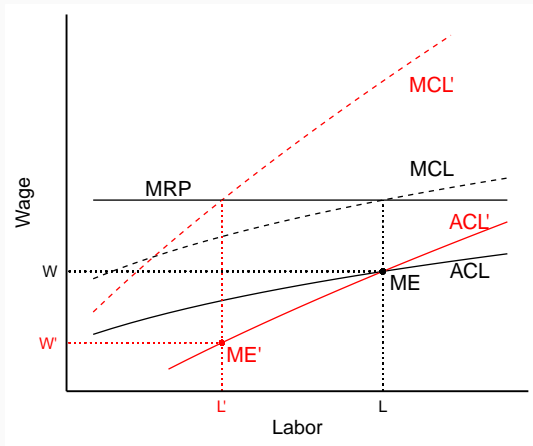
1. Framework with Labor and Product Market Power
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Theory: Impacts of Labor Market Power (1/3)



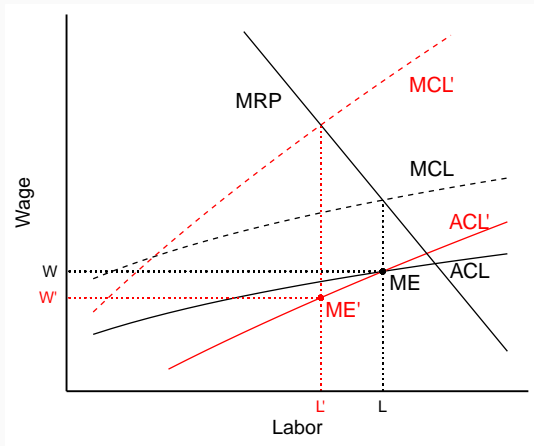
- No price-setting power \implies flat MRPL curve
- Labor market power: upward-sloping MCL
 - Firm chooses L such that $MRPL = MCL$, $W < MRPL$

Theory: Impacts of Labor Market Power (2/3)



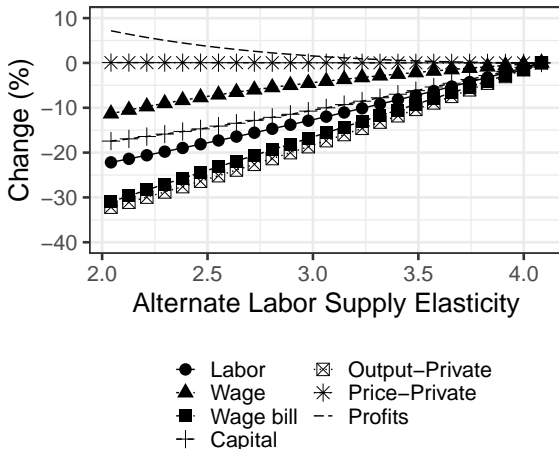
- No price-setting power \Rightarrow flat MRPL curve
- More labor market power \Rightarrow steeper MCL (red)
 \Rightarrow less employment, greater wage markdown

Theory: Impacts of Labor Market Power (3/3)



- Firm has **price-setting power** \Rightarrow downward-sloping MRPL
- Cut employment \Rightarrow cut output \Rightarrow higher output price \Rightarrow incentive not to cut employment as much

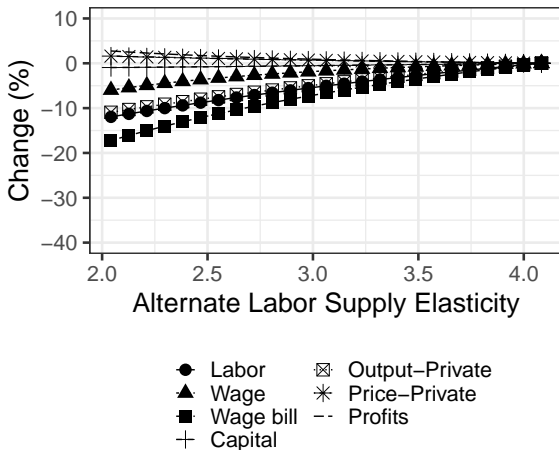
Model Simulation: Impacts of Labor Market Power (1/2)



Consider reducing LS elasticity $1/\theta$ in half

- Simulate from estimated model, counterfactually set $\epsilon = 0$
- Employment \downarrow 22%, wages \downarrow 11%, profits \uparrow 7%

Model Simulation: Impacts of Labor Market Power (2/2)



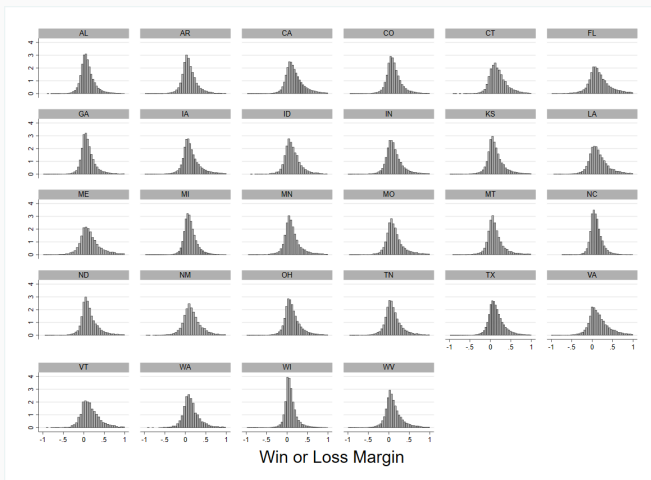
- Simulate from estimated model, use estimated $1/\epsilon = 7.3$
- Employment \downarrow 12%, wages \downarrow 6%, profits \uparrow 3% \implies impacts of labor market power mitigated by product market power

Conclusions

- Developed a framework for jointly analyzing **labor** and **product** market power
- Leveraged features of **procurement auctions** to recover **labor supply**, **technology**, and **product demand**
- We estimate that the markdown on the marginal revenue product of labor is 20%. Furthermore, there is a **double wage markdown** of 31% due to **product** market power
- Firms capture more than 3/4 of rents, high productivity firms share less, but workers capture a high share of marginal rents
- Simulations from estimated model show that impacts of **labor** market power depend on degree of **product** market power

Appendix

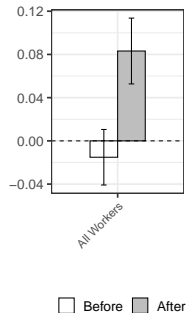
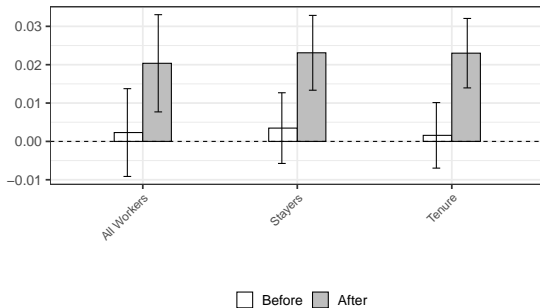
Visual test of collusion from Chassang et al (2022)



None of our 28 states has a “missing mass” of close losing bids. Chassang Kawai Nakabayashi Ortner (2022 ECMA) show that such patterns should be found broadly under collusive behavior.

Falsification using Pre-period

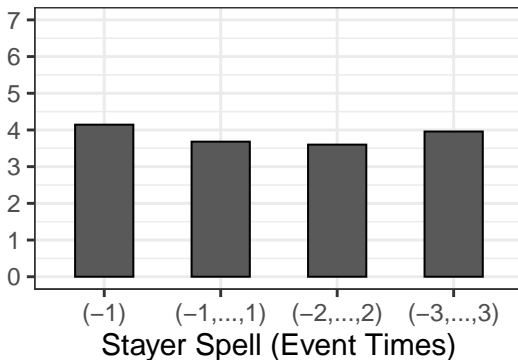
Effects on wages (left) and employment (right):



◀ Back

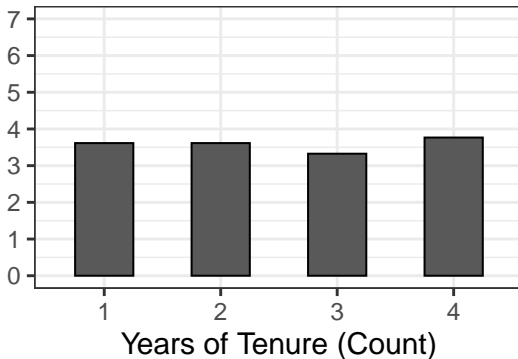
Stayers and Tenure Samples (1/2)

Labor supply elasticity by stayer spell:



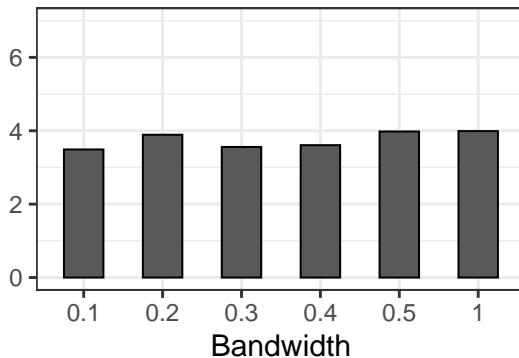
Stayers and Tenure Samples (2/2)

Labor supply elasticity by tenure length:



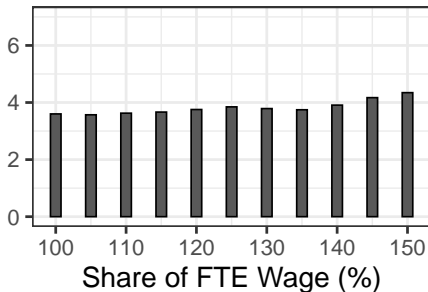
Bandwidths in the Prop 2 estimator (1/1)

Labor supply elasticity for alternative bandwidths ($\bar{\tau}$):



Hours and full-time status (1/2)

Labor supply elasticity by FTE threshold (as % of min. wage):

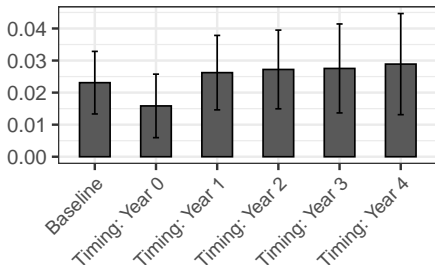


Other notes:

- US construction industry during 2001-2015 was 4.6% part-time labor vs 13.9% in entire private sector (BLS)
- LMS estimator in Norway: revenue shock pass-through of 0.092 (annual earnings) and 0.091 (hourly wages)

Hours and full-time status (2/2)

Wage effects persist over time (inconsistent with over-time pay):

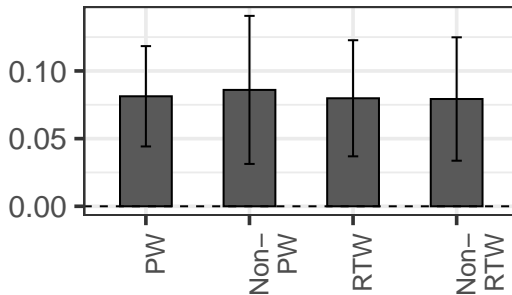


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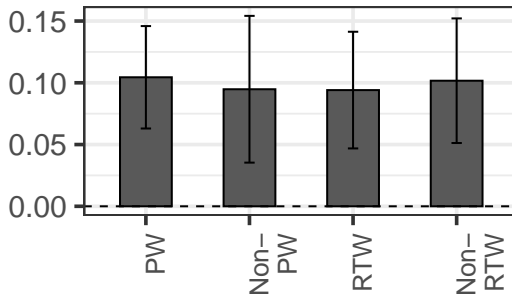
Right-to-Work and Prevailing Wage States (1/2)

Effects on employment:



Right-to-Work and Prevailing Wage States (2/2)

Effects on wage bill:



Measurement Error Orthogonality

The goal is to estimate $1 - \epsilon$ using the relationship:

$$r_{jt} = \kappa_R + (1-\epsilon) x_{jt} + (1-\epsilon) e_{jt}$$

where e_{jt} is the error in the relationship between log revenues r_{jt} and log intermediates x_{jt} . The key identifying restriction is,

$$\text{Cov}(x_{jt}, e_{jt}) = 0$$

This orthogonality condition is satisfied under the assumption by Akerberg et al. (2015) that the firm has no information about e_{jt} at the time inputs are chosen:

*“The $[e_{jt}]$ represent shocks to production or productivity that are **not observable (or predictable)** by firms before making their input decisions at t ... $[e_{jt}]$ can also represent (potentially serially correlated) measurement error in the output variable.” Akerberg et al. (2015, ECMA)*

Indeed, x_{jt} should be uncorrelated with e_{jt} if e_{jt} is completely unpredictable at the time x_{jt} is chosen.