

## 21:640:238 **Foundations of Modern Math**

Summer 2016

## Quiz #1

Monday, June 6 2016

NAME:			

Please write clearly and properly.

Problem	Grade	
1		
2		
3		
Total		

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**Problem 1.** Describe the following sets extensionally (by listing their elements within braces). *No explanations are required.* 

(1)  $\{0, 2, 4, 6\} \cup \emptyset$ 

(2) 
$$\{0, \pi, -\frac{1}{7}, \heartsuit\} - \mathbb{Q}$$

(3) 
$$\{1, -2, \sqrt{2}\} \cap \mathbb{Q}^+$$

(4) 
$$\{x \in \mathbb{Z} : 2x^2 + 3x - 2 = 0\}$$

(5) 
$$\{x^3, x \in \{n \in \mathbb{N} : n < 4\}\}$$

(6) 
$$\mathcal{P}(\{0, \{4\}, \alpha\})$$

$$(7) \{0, 1\}^3$$

(8) 
$$\{0,\emptyset\} \times \{\{0\}\}$$

**Problem 2.** Find all partitions of the set  $\{0, 1, 2\}$ .

**Problem 3.** True or False? *No explanations are required.* 

(1) 
$$(A \cup B) \cap C = (A \cap C) \cup (B \cap C)$$
 for any sets A, B and C.

(2) 
$$(1,-1,3) \in \mathbb{Z}^3$$
.

(3) 
$$\mathbb{N} \subseteq \mathbb{R}^+$$
.

(4) Let 
$$A_n = \left[\frac{1}{n}, \frac{1}{n+1}\right]$$
. Then  $\bigcap_{n \in \mathbb{N}} A_n = \emptyset$ .

(5) Let 
$$V_x = \left[\frac{1}{x}, x\right]$$
 for  $x \in \mathbb{R}^+$ . Then  $\bigcup_{x \in [1, +\infty)} V_x = \mathbb{R}$ .