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**Algorithm 1** insert(key  $K$ , pointer  $P$ )

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1: if tree is empty then
2:   create an empty leaf node  $L$ , which is also the root
3: else
4:   Find the leaf node  $L$  that should contain key value  $K$ 
5: end if
6: if  $L$  has less than  $n - 1$  key values then
7:   insert_in_leaf( $L, K, P$ )
8: else
9:   Create node  $L'$ 
10:  Copy  $L.P_1, \dots, L.K_{n-1}$  to a block of memory  $T$  that can hold  $n$  (key and pointer) pairs
11:  insert_in_leaf( $T, K, P$ )
12:  Set  $L'.P_n = L.P_n$ 
13:  Set  $L.P_n = L'$ 
14:  Erase  $L.P_1$  through  $L.K_{n-1}$  from  $L$ 
15:  Copy  $T.P_1$  through  $T.K_{\lceil n/2 \rceil}$  from  $T$  into  $L$  starting at  $L.P_1$ 
16:  Copy  $T.P_{\lceil n/2 \rceil + 1}$  through  $T.K_n$  from  $T$  into  $L'$  starting at  $L'.P_1$ 
17:  Let  $K'$  be the smallest key in  $L'$ 
18:  insert_in_parent( $L, K', L'$ )
19: end if
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**Algorithm 2** insert\_in\_leaf(node  $L$ , key  $K$ , pointer  $P$ )

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1: if  $K < L.K_1$  then
2:   insert  $P, K$  into  $L$  just before  $L.P_1$ 
3: else
4:   Let  $K_i$  be the highest value in  $L$  that is less than or equal to  $K$ 
5:   Insert  $P, K$  into  $L$  just after  $L.K_i$ 
6: end if
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**Algorithm 3** insert\_in\_parent(node  $N$ , key  $K'$ , pointer  $N'$ )

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1: if  $N$  is the root of the tree then
2:   Create a new node  $R$  containing  $N, K', N'$ 
3:   Make  $R$  the root of the tree return
4: end if
5: Let  $P = \text{parent}(N)$ 
6: if  $P$  has less than  $n$  pointers then
7:   insert( $K', N'$ ) in  $P$  just after  $N$ 
8: else
9:   Copy  $P$  to a block of memory  $T$  that hold  $P$  and  $(K' \& N')$ 
10:  Insert( $K', N'$ ) into  $T$  just after  $N$ 
11:  Erase all entries from  $P$ 
12:  Create node  $P'$ 
13:  Copy  $T.P_1, \dots, T.P_{\lceil (n+1)/2 \rceil}$  into  $P$ 
14:  Let  $K'' = T.K_{\lceil (n+1)/2 \rceil}$ 
15:  Copy  $T.P_{\lceil (n+1)/2 \rceil + 1}, \dots, T.P_{n+1}$  into  $P'$ 
16:  insert_in_parent( $P, K'', P'$ )
17: end if
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