A Unified Theory of the Term-Structure and Monetary Stabilization

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Canadian Economics Association Meetings (CEA 2022)

May 31, 2022

Motivation

Bernanke (2014): "QE works in practice but not in theory"

Blanchard (2016): "Solution is to introduce two interest rates, the policy rate set by the central bank in the <u>LM equation</u> and the rate at which people and firms can borrow, which enters the <u>IS equation</u>, and then to discuss how the financial system determines the spread between the two."

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- A need for a macro-finance framework addressing Bernanke (2014)
 - Perennial ZLB environment (e.g. Rachel and Smith (2017)) and indispensable LSAPs (QE1, QE2, Covid-19 responses)
 - Need for a deviation from the 'expectation hypothesis'

⇒ quantity matters!

- Addressing Blanchard (2016)
 - Term-structure + private bond market needed

This paper

A quantitative (very grand) macroeconomic framework that incorporates

- The general equilibrium term-structure of interest rates
- Multiple asset classes (government bonds vs. private bond)
- Endogenous portfolio shares among different kinds of assets

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 - Market segmentation across different maturities (how?: methodological contribution)

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 Market segmentation across different maturities (how?: methodological contribution)

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- 6 Government and central bank's explicit balance sheets
- A micro-founded welfare criterion

which are necessary for quantitative policy experiments (ex. conventional vs. unconventional monetary policies)

What we do + findings

- 1. **Provide** an efficient way to generate the market segmentation across bonds of different maturities based on Eaton and Kortum (2002)
 - Each atomic investor subject to some expectation shock ~ Fréchet: these shocks have a structural meaning (liquidity premium)
 - Downward-sloping demand curve for each asset (bond of each maturity)
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 ⇒ quantity matters!

2. Compare conventional (standard) monetary policy where

- Central bank adjusts its balance sheet holding of the shortest-term bond to control the shortest-term yield
- The shortest-term yield follows the Taylor rule (targeting business cycle)

with the unconventional (general) monetary policy where

- Central bank adjusts its entire bond portfolio along the yield curve to control
 yields (yields of which maturities to be controlled: chosen by central bank)
- Controlled yields follow the Taylor rule (targeting business cycle)

What we do + findings

Big Findings (Conventional vs. Unconventional)

- Quantity matters! (confirm results in Krishnamurthy and Vissing-Jorgensen (2012) and Greenwood and Vayanos (2014) in theory)
- Unconventional monetary policy is very powerful in terms of stabilization in both normal and ZLB periods
- 3 As a drawback, the economy gets addicted to its power under ZLB regimes

Why?: long term yields $\downarrow \implies$ downward pressure on short term yields $\downarrow \implies$ ZLB frequency and duration $\uparrow \implies$ more reliance on LSAPs

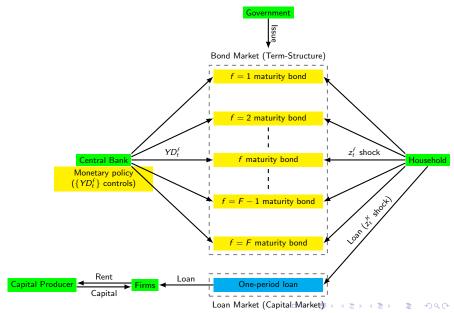
: from the household's endogenous portfolio choices

'ZLB+LSAPs addicted economy'

▶ Literature

The Model

The model: environment



The model: household

The representative household's problem (given B_0):

$$\max_{\substack{\{C_{t+j},N_{t+j}\}\\ \text{Loans}}} \mathbb{E}_t \sum_{j=0}^{\infty} \beta^j \left[\log\left(C_{t+j}\right) - \left(\frac{\eta}{\eta+1}\right) \left(\frac{N_{t+j}}{\bar{N}_{t+j}}\right)^{1+\frac{1}{\eta}} \right]$$
 subject to
$$C_t + \frac{L_t}{P_t} + \frac{\sum_{f=1}^F B_t^{H,f}}{P_t} = \frac{\sum_{f=0}^{F-1} R_t^f B_{t-1}^{H,f+1}}{P_t} + \frac{R_t^K L_{t-1}}{P_t} + \int_0^1 \frac{W_t(\nu) N_t(\nu)}{P_t} \, \mathrm{d}\nu + \frac{\Lambda_t}{P_t}$$
 Nominal bond purchase
$$(f\text{-maturity})$$

where

• ν : intermediate firm index such that:

$$N_t = \left(\int_0^1 N_t(
u)^{rac{\eta+1}{\eta}} \ \mathrm{d}
u
ight)^{rac{\eta}{\eta+1}}$$

• Q_t^f is the nominal price of f-maturity bond with:

(Return)
$$R_t^f = \frac{Q_t^f}{Q_{t-1}^{f+1}}$$
, (Yield) $YD_t^f = \left(\frac{1}{Q_t^f}\right)^{\frac{1}{f}}$

The model: household and savings

Total savings:
$$S_t = B_t^H + L_t = \sum_{f=1}^{r} B_t^{H,f} + L_t$$

Usual bond allocation problem (Ricardian):

$$\max \sum_{f=1}^F \mathbb{E}_t \left[Q_{t,t+1} R_{t+1}^{f-1} B_t^{H,f} \right] \quad \text{s.t.} \quad \sum_{f=1}^F B_t^{H,f} = B_t^H, \quad B_t^{H,f} \geq 0$$

which gives (in equilibrium):

$$\mathbb{E}_t \left[Q_{t,t+1} R_{t+1}^{f-1} \right] = \mathbb{E}_t \left[Q_{t,t+1} R_{t+1}^0 \right], \quad \forall f \implies \boxed{\mathbb{E}_t \left[\widehat{R}_{t+1}^{f-1} \right] = \widehat{R}_{t+1}^0}$$

'Expectation hypothesis'

⇒ quantity does not matter!

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Our approach:

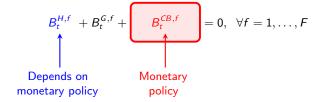
'Expectation hypothesis'

 \implies quantity does not matter!

- Split the household into a family $m \in [0, 1]$, each of which decides whether to invest in bonds or loan, subject to expectation shock \sim Fréchet
- If a family m is a bond family, it is split into members $n \in [0, 1]$, who decides maturity f to invest in, subject to expectation shock \sim Fréchet $\stackrel{\triangleright}{}$ Bond

Equilibrium + market clearing

Bond market equilibrium:



Central bank: balance sheet adjustment ←⇒ monetary policy

Market clearing:

$$C_t = (1 - \zeta_t^G) Y_t + (1 - \delta) K_t - K_{t+1}.$$

Monetary Policy (Conventional vs. Unconventional)

Standard (conventional) monetary policy

In the standard monetary policy case, central bank sets Taylor-type rules on YD_t^1 (the shortest yield) while not manipulating longer term bonds holdings

 Long-term yields fluctuate endogenously (in response to shocks + changes in short-term rate)

$$R_{t+1}^{0} \equiv YD_{t}^{1} = \max\left\{YD_{t}^{1*}, \frac{1}{1}\right\}$$

$$ZLB$$

$$YD_{t}^{1*} = \overline{YD}^{1}\underbrace{\left(\frac{\Pi_{t}}{\overline{\overline{\Gamma}}}\right)^{\gamma_{\pi}^{1}}\left(\frac{Y_{t}}{\overline{Y}}\right)^{\gamma_{y}^{1}}}_{\text{Targeting}} \cdot \exp\left(\frac{\widetilde{\varepsilon}_{t}^{YD^{1}}}{}\right)$$

$$MP \text{ shock } (f = 1)$$

$$\frac{B_t^{CB,f}}{A_t \bar{N}_t P_t} = \frac{\overline{B^{CB,f}}}{A \bar{N} P} \qquad \forall f = 2, \dots, F$$

Normalized holding of f > 1 fixed

General (unconventional) monetary policy

In the general monetary policy case, central bank targets all yields along the yield curve, assuming the Taylor-type rule for each maturity yield

• Back out the needed purchases of each maturity $\forall f$ (endogenous)

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$$YD_{t}^{GP,f} = \overline{YD}^{GP,f}\left(\frac{\Pi_{t}}{\overline{\Pi}}\right)^{\gamma_{\pi}^{f}}\left(\frac{Y_{t}}{\overline{Y}}\right)^{\gamma_{y}^{f}} \cdot \exp\left(\tilde{\varepsilon}_{t}^{YD^{f}}\right), \quad f \geq 2$$

$$\bullet \text{ Yield-curve-control (YCC) policy}$$

rield-curve-control (1 CC) policy

Steady-state (long-run) analysis

Steady-state U.S. calibrated yield-curve (up to 30 years)

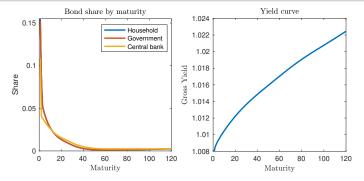


Figure: Steady-state bond portfolios of household, government, and central bank and the resultant yield curve

Calibration

- Given κ_B, κ_S (degrees of market segmentations), calibrate $\frac{\{z^f\}_{f=1}^F}{f}$ (preference for a maturity-f bond) and \underline{z}^K (preference for loan) \implies match the U.S. average yield curve (before 2007)
- Result: $\underline{z^1} = \underline{1}$ is much higher than $\underline{z^f}$ for $f \ge 2$ (safety liquidity premium)

Government's bond supply effects

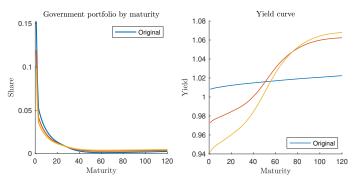


Figure: Government's bond issuance portfolio and yield curve

- Government's supply of f-maturity bond $\uparrow \Rightarrow$ its yield \uparrow (price effect)
- Similar to Krishnamurthy and Vissing-Jorgensen (2012) and Greenwood and Vayanos (2014)

Central bank's bond demand effects

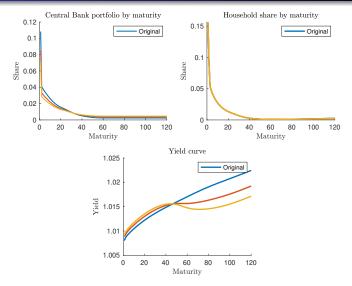


Figure: Central bank's bond demand portfolio and yield curve

Short-run analysis (Impulse-responses)

Summary

Again...

Big Findings (Conventional vs. Unconventional)

- Unconventional monetary policy is very powerful in terms of stabilization in both normal and ZLB periods
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Why?: long term yields $\downarrow \Longrightarrow$ downward pressure on short term yields $\downarrow \Longrightarrow$ ZLB frequency and duration $\uparrow \Longrightarrow$ more reliance on LSAPs

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Welfare (similar to Coibion et al. (2012)) Trend inflation term $\mathbb{E} U_t - \bar{U}^F = \Omega_0 + \Omega_n \mathrm{Var}(\hat{n}_t) + \Omega_\pi \mathrm{Var}(\bar{\pi}_t) + \text{t.i.p} + \text{h.o.t}$

A shock to the preference for the short-term bond (impulse response to z_t^1)

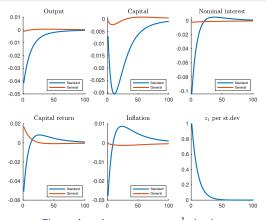


Figure: Impulse response to z_t^1 shock

With standard (conventional) policy

Short yields↓ ⇒ yields, capital return, and wage↓ ⇒ output↓ (labor supply↓)
 and inflation↓

With general (unconventional) policy: stabilizing (filling gaps in bond demand)

ZLB impulse response to z_t^1

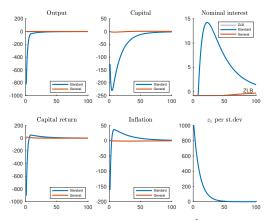


Figure: ZLB impulse response to z_t^1 shock

With general (unconventional) policy: stabilizing (filling gaps in bond demand)

But duration of ZLB episodes↑

$$ZLB \Longrightarrow long-term\ rates \downarrow \Longrightarrow ZLB\ possibility \uparrow \longrightarrow ZLB\ IRF\ (z_t^K)$$

ZLB impulse response to an exogenous tax hike Normal IRF (tax)

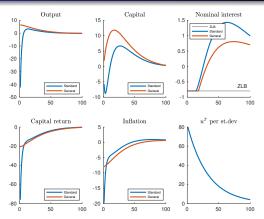


Figure: ZLB impulse response to $\boldsymbol{\epsilon}_t^T$ shock

With standard (conventional) policy

• Tax $\uparrow \Longrightarrow$ bond supply $\downarrow \Longrightarrow$ ZLB \Longrightarrow recessions (Caballero and Farhi (2017))

With general (unconventional) policy: stabilizing (even creating a boom)

But duration of ZLB episodes[†]



Policy comparison (Standard, General, and Mixed)

We also consider:

 Mixed policy: central bank starts controlling long-term rates only when FFR hits ZLB, thus General (unconventional) only at the ZLB

	Standard Policy	General Policy	Mixed Policy
Mean ZLB duration	1.6511 quarters	6.3355 quarters	7.9672 quarters
Median ZLB duration	1 quarters	1 quarters	1 quarters
ZLB frequency	8.2556%	21.8222%	21.6%
Welfare	-1.3503%	-0.90471%	-0.90302%

Table: Policy comparisons (ex-ante)

ZLB duration: General < Mixed (Mixed is less stabilizing)

ZLB frequency: General > Mixed (General: long-term rates↓ even before ZLB)

Welfare: Standard << General < Mixed

Thank you very much! (Appendix)

Key previous works (only a few among many) •• Go back

- The term-structure and macroeconomy: Ang and Piazzesi (2003), Rudebush and Wu (2008), Bekaert et al. (2010)
- Central bank's endogenous balance sheet size as an another form of monetary policy: Gertler and Karadi (2011), Cúrdia and Woodford (2011), Christensen and Krogstrup (2018, 2019), Karadi and Nakov (2021), Sims and Wu (2021)

Our paper: general equilibrium term-structure (without relying on factor models) + balance sheet quantities of government and central bank + yield-curve-control

- Zero lower bound (ZLB) and issuance of safe bonds: Swanson and Williams (2014), Caballero and Farhi (2017), Caballero et al. (2021)
- Welfare criterion with a trend inflation: Coibion et al. (2012)
- Preferred-habitat term-structure (and limited risk-bearing): Vayanos and Vila (2021), Greenwood et al. (2020), Gourinchas et al. (2021)
- Preferred-habitat term-structure in New-Keynesian macroeconomics: Ray (2019), Droste, Gorodnichenko, and Ray (2021)

Our paper: create a quantitative framework providing implications of prior works + new policy implications + novel way to generate market segmentation

Bond family m: a member n has the following expectation shock:

$$\mathbb{E}_{m,n,t}\left[Q_{t,t+1}R_{t+1}^{f-1}\right] = \mathbf{z}_{n,t}^{f} \cdot \mathbb{E}_{t}\left[Q_{t,t+1}R_{t+1}^{f-1}\right], \quad \forall f = 1, \dots, F$$

with $z_{n,t}^f$ follows a Fréchet distribution with location parameter 0, scale parameter z_t^f , and shape parameter κ_B

• Note: $z_t^f = 1$, $\kappa_B \to \infty$, then $\mathbb{E}_{m,n,t} \to \mathbb{E}_t$ (rational expectation)

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Aggregation (Eaton and Kortum (2002))

$$\lambda_t^{HB,f} \equiv \mathbb{P}\left(\mathbb{E}_{m,n,t}\left[Q_{t,t+1}R_{t+1}^{f-1}\right] = \max_{j}\left\{\mathbb{E}_{m,n,t}\left[Q_{t,t+1}R_{t+1}^{j-1}\right]\right\}\right)$$

$$= \left(\frac{z_t^f\mathbb{E}_t\left[Q_{t,t+1}R_{t+1}^{f-1}\right]}{\Phi_t^B}\right)^{\kappa_B}$$
maturity share

- f-maturity share
 - Deviate from expectation hypothesis ⇒ ∃downward-sloping demand curve after log-linearization (market segmentation effect)
 - Shape parameter κ_B : (inverse of) a degree of bonds market segmentation

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$$f\text{-maturity share}$$

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Effective bond market rates

$$R_{t+1}^{HB} = \sum_{t=0}^{F-1} \lambda_t^{HB,f+1} R_{t+1}^f$$
 P Go back

Loan vs. bond decision: a family *m* solves the following problem

$$\max \mathbb{E}_t \left[Q_{t,t+1} R_{t+1}^{HB} B_{m,t}^H \right] + z_{m,t}^K \cdot \mathbb{E}_t \left[Q_{t,t+1} R_{t+1}^K L_{m,t} \right] \quad \text{s.t.}$$

$$B_{m,t}^H + L_{m,t} = S_t, \quad B_{m,t}^H \ge 0, \quad \text{and} \quad L_{m,t} \ge 0$$

with $\mathbf{z}_{m,t}^K$ follows a Fréchet distribution with location parameter 0, scale parameter \mathbf{z}_t^K , and shape parameter κ_S

Loan vs. bond decision: a family *m* solves the following problem

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Aggregation (Eaton and Kortum (2002))

$$\lambda_{t}^{K} = \left(\frac{z_{t}^{K} \mathbb{E}_{t} \left[Q_{t,t+1} R_{t+1}^{K}\right]}{\Phi_{t}^{S}}\right)^{\kappa_{S}}$$

- ■downward-sloping demand curve after log-linearization (for loan and bonds)
- Shape parameter κ_S : (inverse of) a degree of market segmentation between government bonds vs loan

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Effective savings rate: governs intertemporal substitution

$$\begin{split} R_t^{\mathcal{S}} &= \left(1 - \lambda_{t-1}^K\right) R_t^{HB} + \lambda_{t-1}^K R_t^K \\ &= \left(1 - \lambda_{t-1}^K\right) \sum_{f=0}^{F-1} \lambda_{t-1}^{HB,f+1} R_t^f + \lambda_{t-1}^K R_t^K & \text{$^{\text{Go back}}$} \end{split}$$

Capital producer, firms, and government Goback

Capital producer: competitive producer of capital (lend capital to intermediate firms at price P_t^K)

Firms: standard with Cobb-Douglas production (pricing à la Calvo (1983))

 One financial friction: firms need secure <u>loans</u> from the household to borrow capital from the capital producer:

$$\underbrace{L_t(\nu)}_{\text{Loan of firm }\nu} \geq \underbrace{P_t^K K_t(\nu)}_{\text{Capital borrowing expense}}, \forall \nu$$

Government: with the following budget constraint

$$\frac{B_{t}^{G}}{P_{t}} = \frac{R_{t}^{G}B_{t-1}^{G}}{P_{t}} - \begin{bmatrix} \zeta_{t}^{G} + \zeta_{t}^{F} - \zeta_{t}^{T} \\ \uparrow & \text{Production subsidy} \end{bmatrix} Y_{t}, \quad R_{t}^{G} = \sum_{f=0}^{F-1} \lambda_{t-1}^{G,f+1} R_{t}^{f}$$

$$\frac{G_{t}}{Y_{t}} \text{ (Exogenous)} \qquad \frac{T_{t}}{Y_{t}} \text{ (Exogenous)} \qquad \text{(Exogenous)}$$

• Government: a natural issuer of the entire bond market

A deficit ratio: comparative statics

→ Go back

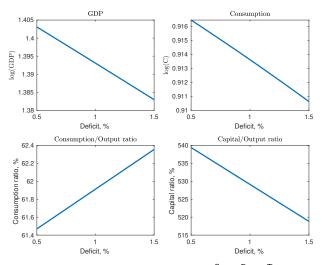


Figure: Variations in a deficit ratio $\zeta^{\textit{G}}_t + \zeta^{\textit{F}} - \zeta^{\textit{T}}_t$

A deficit ratio: comparative statics

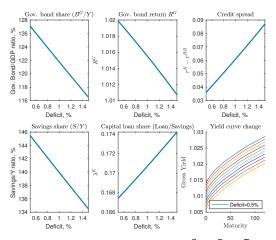


Figure: Variations in a deficit ratio $\zeta_t^G + \zeta^F - \zeta_t^T$

- A higher deficit ratio \Rightarrow depressed economy (for $R^G \downarrow$)
 - An entire yield curve

Impulse-response to an exogenous tax hike shock

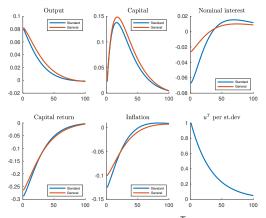


Figure: Impulse response to ϵ_t^T shock

 $Tax^{\uparrow} \Rightarrow bond supply \downarrow \Rightarrow downward pressures on yields, loan rates, and wages$

- Monetary response (policy rate↓) ⇒ output↑ (even creating a boom)
- Standard: policy rate↓ more (cannot control long-term yields)

ZLB impulse response to z_t^K

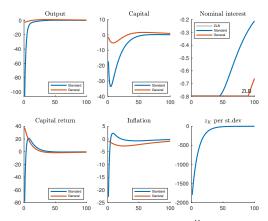


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