Yield-Curve Control Policy under Inelastic Financial Markets

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Motivation: with equations

Example: IS equation with 3 maturities (short-term, 10 years, 30 years)

$$\underbrace{\hat{c}_t}_{\uparrow} = \mathbb{E}_t \left[\hat{c}_{t+1} - \left(\underbrace{\hat{oldsymbol{eta}_{t+1}^S}}_{\downarrow} - \hat{\pi}_{t+1} \right) \right]$$

where

$$\hat{r}_{t+1}^{S} = \underbrace{i_t}_{\text{Policy rate}} + w_t^{10} \cdot \left(\hat{r}_{t+1}^{10} - i_t\right) + w_t^{30} \cdot \left(\hat{r}_{t+1}^{30} - i_t\right)$$

Up to a first-order, portfolio demand (w_t^{10}, w_t^{30}) depends on relative returns:

$$\underbrace{w_t^{10}}_{\uparrow} = w^{10} \left(\underbrace{i_t}_{\downarrow}, \underbrace{\hat{r}_{t+1}^{10}}_{\uparrow}, \underbrace{\hat{r}_{t+1}^{30}}_{\downarrow} \right)$$

- Portfolio demand's elasticity with respect to corresponding returns is finite: market segmentation
- With $i_t \downarrow$, we have $(w_t^{10} \uparrow, w_t^{30} \uparrow)$, leading to $(\hat{r}_t^{10} \downarrow, \hat{r}_t^{30} \downarrow)$ (i.e., portfolio rebalancing), thereby $\hat{r}_{t+1}^{S} \downarrow$, but not one-to-one: cross-elasticity
- Then real effects: $\hat{c}_t \uparrow$

This paper

A quantitative macroeconomic framework that incorporates

- The general equilibrium term-structure of interest rates
- Multiple asset classes (government bonds and private bond)
- Endogenous portfolio rebalancing among different kinds of assets
- Market segmentation across different maturities bonds (how?: methodological contribution + estimation)

that makes LSAPs work in theory (e.g., a downward-sloping demand curve for each maturity bond)

- Government and central bank's explicit balance sheets
- A micro-founded welfare criterion

which are necessary for quantitative policy experiments (e.g., conventional vs. unconventional monetary policies)

What we do + findings

Takeaway (Conventional vs. Unconventional)

Unconventional monetary policy (e.g., yield-curve-control (YCC)) is powerful in terms of stabilization in both normal and ZLB

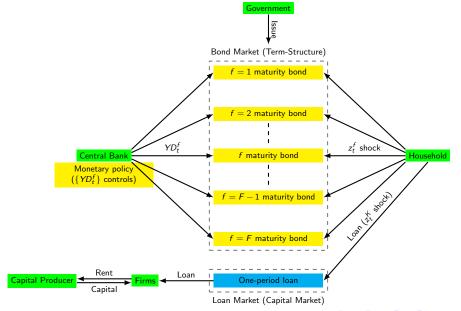
As a drawback, the economy experiences longer ZLB regimes

Mechanism: long term yields $\downarrow \implies$ portfolio shares of short term $\uparrow \implies$ short yields $\downarrow \implies$ ZLB duration $\uparrow \implies$ more reliance on LSAPs

'ZLB + LSAPs addicted economy'

→ Literature

The model: environment



The model: household

The representative household's problem (given B_0):

$$\max_{\substack{\{C_{t+j},N_{t+j}\}\\ \text{Loans}\\ \text{Subject to}\\ C_t + \frac{L_t}{P_t} + \frac{\sum_{f=1}^F B_t^{H,f}}{P_t} = \frac{\sum_{f=0}^{F-1} R_t^f B_{t-1}^{H,f+1}}{P_t} + \frac{R_t^K L_{t-1}}{P_t} + \frac{\int_0^1 \frac{W_t(\nu)N_t(\nu)}{P_t} \, \mathrm{d}\nu + \frac{\Lambda_t}{P_t}}{P_t}$$
Nominal bond purchase (f-maturity)

where

• ν: intermediate firm index such that:

$$N_t = \left(\int_0^1 N_t(\nu)^{\frac{\eta+1}{\eta}} d\nu\right)^{\frac{\eta}{\eta+1}}$$

• Q_t^f is the nominal price of f-maturity bond with:

$$(\mathsf{Return}) \ R_t^f = \frac{Q_t^f}{Q_{t-1}^{f+1}}, \ \ (\mathsf{Yield}) \ \ \mathsf{YD}_t^f = \left(\frac{1}{Q_t^f}\right)^{\frac{1}{f}}$$

The model: household and savings

Total savings:
$$S_t = B_t^H + L_t = \sum_{f=1}^F B_t^{H,f} + L_t$$

Usual bond allocation problem (Ricardian):

$$\max \sum_{f=1}^F \mathbb{E}_t \left[Q_{t,t+1} R_{t+1}^{f-1} B_t^{H,f} \right] \quad \text{s.t.} \quad \sum_{f=1}^F B_t^{H,f} = B_t^H, \quad B_t^{H,f} \geq 0$$

which gives (in equilibrium):

$$\mathbb{E}_{t}\left[Q_{t,t+1}R_{t+1}^{f-1}\right] = \mathbb{E}_{t}\left[Q_{t,t+1}R_{t+1}^{0}\right], \quad \forall f \implies \boxed{\mathbb{E}_{t}[\widehat{R}_{t+1}^{f-1}] = \widehat{R}_{t+1}^{0}}$$

$$\stackrel{\text{(Non Ricardian)}}{\longleftarrow} \stackrel{\text{(Expectations hypothesis)}}{\longleftarrow}$$

Our approach (Non-Ricardian):

- Split the household into a family $m \in [0, 1]$, each of which decides whether to invest in bonds or loan, subject to expectation shock \sim Fréchet
- A bond family m is split into members $n \in [0, 1]$, each of whom decides maturity f to invest in, subject to expectation shock \sim Fréchet

Bond portfolio (e.g., Eaton and Kortum (2002))

$$\lambda_t^{HB,f} \equiv \left(rac{z_t^f \ \mathbb{E}_t \left[Q_{t,t+1} R_{t+1}^{f-1}
ight]}{\Phi_t^B}
ight)^{\kappa_B} \stackrel{ ext{Portfol}}{ ext{Portfol}}$$
 $f ext{-maturity share}$
 $\Phi_t^B \equiv \left[\sum_{i=1}^F \left(z_t^j \mathbb{E}_t[Q_{t,t+1} R_{t+1}^{j-1}]
ight)^{\kappa_B}
ight]^{rac{1}{\kappa_B}}$

- Deviate from expectation hypothesis ⇒ ∃downward-sloping demand curve after loglinearization with finite demand elasticity and cross-elasticities
- Shape parameter κ_B : (inverse of) a degree of bonds market segmentation
- ullet $z_t^f=1,\,\kappa_B o\infty$, then again expectations hypothesis (i.e., Ricardian)

Effective bond market rates

$$R_{t+1}^{HB} = \sum_{f=0}^{F-1} \lambda_t^{HB,f+1} R_{t+1}^f$$

where

Loan share (e.g., Eaton and Kortum (2002)) $\lambda_t^K = \left(\frac{z_t^K \mathbb{E}_t \left[Q_{t,t+1} R_{t+1}^K\right]}{\Phi_t^S}\right)^{\kappa_S}$ Use the Loan share where

$$\Phi_t^S = \left[\left(\mathbb{E}_t[Q_{t,t+1} R_{t+1}^{HB}] \right)^{\kappa_S} + \left(z_t^K \mathbb{E}_t[Q_{t,t+1} R_{t+1}^K] \right)^{\kappa_S} \right]^{\frac{1}{\kappa_S}}$$

• Shape parameter κ_{S} : (inverse of) a degree of market segmentation between govern-

• \(\frac{1}{2}\)downward-sloping demand curve after log-linearization (for bonds and private loan)

ment bonds vs loan

Effective savings rate: governs intertemporal substitution

with finite demand elasticity and cross-elasticities

$$R_{t}^{S} = \left(1 - \lambda_{t-1}^{K}\right) R_{t}^{HB} + \lambda_{t-1}^{K} R_{t}^{K}$$

$$= \left(1 - \lambda_{t-1}^{K}\right) \sum_{t=0}^{F-1} \lambda_{t-1}^{HB,f+1} R_{t}^{f} + \lambda_{t-1}^{K} R_{t}^{K}$$

Enters Euler equation

Equilibrium + market clearing

Bond market equilibrium:

$$B_t^{H,f} + B_t^{G,f} + B_t^{CB,f} = 0, \quad \forall f = 1, \dots, F$$

Monetary policy

Central bank: monetary policy through balance sheet adjustments

- ullet Conventional: Taylor rules on YD_t^1 (only adjusting $B_t^{CB,1}$)
- Yield-curve-control (YCC): Taylor rules on $\left\{YD_t^f\right\}$ (adjusting $\left\{B_t^{CB,f}\right\}$)
- Subject to zero lower bound (ZLB)
- >> Conventional >>> Unconventional >>> Capital Producer, Firms, and Government

Steady-state U.S. calibrated yield curve (up to 30 years)

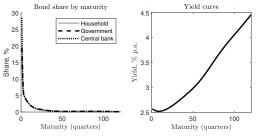


Figure: Steady-state bond portfolios of households, government, and central bank and the resultant yield curve (December 2002 - June 2007)

Estimation: $\kappa_B = 10$ from the aggregate bond portfolio data Estimation

Calibration: given $\kappa_B = 10$ and $\kappa_S = 6$ (from Kekre and Lenel (2023))

- $\{z^f\}_{f=1}^F$ (i.e., maturity preference for a maturity-f) \Longrightarrow yield curve slopes
- z^{K} (i.e., preference for private loan) \Longrightarrow the yield curve level
- Result: $z^1 = 1 >> z^f$ for $f \ge 2$ (e.g., safety liquidity premium)

Short-run analysis (Impulse-responses)

A shock to the preference for the short-term bond (impulse response to z_t^1)

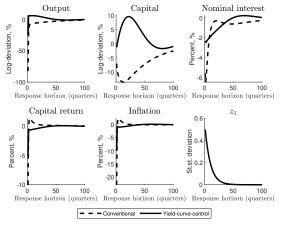


Figure: Impulse response to z_t^1 shock

With conventional policy

ullet Short yields, and output, \Longrightarrow other yields, capital return, and wage, and inflation,

With yield-curve-control (YCC): stabilizing (filling gaps in bond demand)

ZLB impulse response to z_t^1

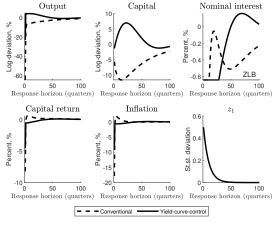


Figure: ZLB impulse response to z_t^1 shock

With yield-curve-control (YCC): stabilizing (filling gaps in bond demand)

But duration of ZLB episodes[†]

Long-term rates \rightarrow ZLB duration \uparrow \rightarrow ZLB IEF (z_t^K)

ZLB impulse response to an exogenous tax hike Normal IRF (tax)

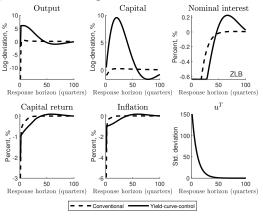


Figure: ZLB impulse response to ϵ_t^T shock

With conventional policy: non-Ricardian

• Tax $\uparrow \Longrightarrow$ bond supply $\downarrow \Longrightarrow$ ZLB \Rightarrow recessions (Caballero and Farhi, 2017)

With yield-curve-control (YCC): stabilizing

But duration of ZLB episodes↑

Policy comparison (Conventional, Yield-Curve-Control, and Mixed)

We also consider:

 Mixed policy: central bank starts controlling long-term rates only when FFR hits ZLB, thus YCC only at the ZLB

	Conventional	Yield-Curve-Control	Mixed Policy
Mean ZLB duration	4.5533 quarters	6.2103 quarters	5.5974 quarters
Median ZLB duration	3 quarters	3 quarters	2 quarters
ZLB frequency	15.9596%	13.4242%	17.4141%
Welfare	-1.393%	-1.2424%	-1.3662%

Table: Policy comparisons (ex-ante)

ZLB duration: Conventional < Mixed < YCC

ZLB frequency: **YCC** < Conventional < **Mixed**

Welfare: Conventional < Mixed < YCC

Thank you very much! (Appendix)

Key previous works (only a few among many) OD Back

- The term-structure and macroeconomy: Ang and Piazzesi (2003), Rudebush and Wu (2008), Bekaert et al. (2010)
- Central bank's endogenous balance sheet size as an another form of monetary policy: Gertler and Karadi (2011), Cúrdia and Woodford (2011), Christensen and Krogstrup (2018, 2019), Karadi and Nakov (2021), Sims and Wu (2021)
- ZLB and the supply of safe bonds: Swanson and Williams (2014), Caballero and Farhi (2017), Caballero et al. (2021)
- Welfare criterion with a trend inflation: Coibion et al. (2012)
- Preferred-habitat term-structure (and limited risk-bearing): Greenwood et al. (2020), Vayanos and Vila (2021), Gourinchas et al. (2021), Kekre et al. (2023)
- Preferred-habitat term-structure and the real economy in New Keynesian macroeconomics: Ray (2019), Droste, Gorodnichenko, and Ray (2021)
- Cross-elasticity and portfolio rebalancing: Alpanda and Kabaca (2020), Jansen et al. (2025)

Our paper: general equilibrium term-structure (without relying on factor models) + balance sheet quantities of government and central bank + yield-curve-control + novel way to generate and estimate market segmentation

Bond family m: a member n has the following expectation shock:

$$\mathbb{E}_{m,n,t}\left[Q_{t,t+1}R_{t+1}^{f-1}\right] = z_{n,t}^f \cdot \mathbb{E}_t\left[Q_{t,t+1}R_{t+1}^{f-1}\right], \quad \forall f = 1, \dots, F$$

with $z_{n,t}^f$ follows a Fréchet distribution with location parameter 0, scale parameter z_t^f , and shape parameter κ_B

Aggregation (Eaton and Kortum (2002))

$$\begin{array}{ll} \lambda_t^{HB,f} & \equiv \mathbb{P}\left(\mathbb{E}_{m,n,t}\left[Q_{t,t+1}R_{t+1}^{f-1}\right] = \max_{j}\left\{\mathbb{E}_{m,n,t}\left[Q_{t,t+1}R_{t+1}^{j-1}\right]\right\}\right) \\ & \qquad \qquad = \left(\frac{z_t^f\mathbb{E}_t\left[Q_{t,t+1}R_{t+1}^{f-1}\right]}{\Phi_t^B}\right)^{\kappa_B} \end{array}$$

- Deviate from expectation hypothesis ⇒ ∃downward-sloping demand curve after loglinearization with finite demand elasticity and cross-elasticities
- Shape parameter κ_B : (inverse of) a degree of bonds market segmentation

Effective bond market rates

$$R_{t+1}^{HB} = \sum_{f=0}^{F-1} \lambda_t^{HB,f+1} R_{t+1}^f$$

Loan vs. bond decision: a family *m* solves the following problem

$$\max \mathbb{E}_t \left[Q_{t,t+1} R_{t+1}^{HB} B_{m,t}^H \right] + z_{m,t}^K \cdot \mathbb{E}_t \left[Q_{t,t+1} R_{t+1}^K L_{m,t} \right] \quad \text{s.t.}$$

$$B_{m,t}^H + L_{m,t} = S_t, \quad B_{m,t}^H > 0, \quad \text{and} \quad L_{m,t} > 0$$

with $z_{m,t}^K$ follows a Fréchet distribution with location parameter 0, scale parameter z_t^K , and shape parameter κ_S

Aggregation (Eaton and Kortum (2002))



- downward-sloping demand curve after log-linearization (for bonds and private loan) with finite demand elasticity and cross-elasticities
- \bullet Shape parameter κ_5 : (inverse of) a degree of market segmentation between government bonds vs loan

Effective savings rate: governs intertemporal substitution

$$\begin{split} R_t^S &= \left(1 - \lambda_{t-1}^K\right) R_t^{HB} + \lambda_{t-1}^K R_t^K \\ &= \left(1 - \lambda_{t-1}^K\right) \sum_{f=0}^{F-1} \lambda_{t-1}^{HB,f+1} R_t^f + \lambda_{t-1}^K R_t^K \\ &= \left(1 - \lambda_{t-1}^K\right) \sum_{f=0}^{F-1} \lambda_{t-1}^{HB,f+1} R_t^f + \lambda_{t-1}^K R_t^K \end{split}$$

Conventional monetary policy

Under the conventional monetary policy, central banks set Taylor rules on YD_t^1 (i.e., the shortest yield) while not manipulating longer term bonds holdings

ullet Long-term yields fluctuate endogenously (in response to shocks + changes in short-term rate)

$$\begin{aligned} R_{t+1}^0 &\equiv YD_t^1 = \max\left\{YD_t^{1*}, \ \frac{1}{1}\right\} \\ YD_t^{1*} &= \overline{YD}^1 \left(\frac{YD_{t-1}^{1*}}{\overline{YD}^1}\right)^{\rho_1} \left(\frac{YD_{t-2}^{1*}}{\overline{YD}^1}\right)^{\rho_2} \left(\underbrace{\left(\frac{\Pi_t}{\overline{\Pi}}\right)^{\gamma_\pi^1} \left(\frac{Y_t}{\overline{Y}}\right)^{\gamma_y^1}}_{\text{Targeting}} \cdot \exp\left(\tilde{\varepsilon}_t^{YD^1}\right) \right)^{1-(\rho_1+\rho_2)} \end{aligned}$$
 MP shock $(f=1)$

$$\frac{B_t^{CB,f}}{A_t \bar{N}_t P_t} = \overline{\frac{B^{CB,f}}{A \bar{N} P}} \qquad \forall f = 2, \dots, F$$

Normalized holding of f > 1 fixed



Unconventional monetary policy: yield-curve-control (YCC)

In the unconventional monetary policy case, central bank targets all yields along the yield curve, assuming the Taylor-type rule for each maturity yield

• Back out the needed purchases of each maturity $\forall f$, which are endogenous

$$\begin{split} &R_{t+1}^{0} \equiv YD_{t}^{1} = \max\left\{YD_{t}^{1*}, \ \frac{1}{Y}\right\} \\ &YD_{t}^{1*} = \overline{YD}^{1} \left(\frac{YD_{t-1}^{1*}}{\overline{YD}^{1}}\right)^{\rho_{1}} \left(\frac{YD_{t-2}^{1*}}{\overline{YD}^{1}}\right)^{\rho_{2}} \left(\underbrace{\left(\frac{\Pi_{t}}{\overline{\Pi}}\right)^{\gamma_{\pi}^{1}} \left(\frac{Y_{t}}{\overline{Y}}\right)^{\gamma_{y}^{1}}}_{\text{Targeting}} \cdot \exp\left(\tilde{\varepsilon}_{t}^{YD^{1}}\right)\right)^{1-(\rho_{1}+\rho_{2})} \\ &YD_{t}^{f*} = \overline{YD}^{f} \left(\frac{YD_{t-1}^{f*}}{\overline{YD}^{f}}\right)^{\rho_{1}} \left(\frac{YD_{t-2}^{f*}}{\overline{YD}^{f}}\right)^{\rho_{2}} \left(\underbrace{\left(\frac{\Pi_{t}}{\overline{\Pi}}\right)^{\gamma_{\pi}^{f}} \left(\frac{Y_{t}}{\overline{Y}}\right)^{\gamma_{y}^{f}}}_{\text{Targeting}} \cdot \exp\left(\tilde{\varepsilon}_{t}^{YD^{f}}\right)\right)^{1-(\rho_{1}+\rho_{2})} \end{split}$$

Capital producer, firms, and government Goback

Capital producer: competitive producer of capital (lend capital to intermediate firms at price P_t^K)

Firms: standard with Cobb-Douglas production (pricing à la Calvo (1983))

• One financial friction: firms need secure private loans from the household to operate: for simplicity, borrow γ portion of the revenue it generates

$$\underbrace{L_t(\nu)}_{\text{Loan of firm }\nu} \ge \frac{\gamma}{\gamma} (1 + \zeta^F) P_t(\nu) Y_t(\nu), \forall \nu$$

Government: with the following budget constraint

$$\frac{B_{t}^{G}}{P_{t}} = \frac{R_{t}^{G}B_{t-1}^{G}}{P_{t}} - \begin{bmatrix} \zeta_{t}^{G} + \zeta_{t}^{F} - \zeta_{t}^{T} \\ \uparrow & \text{Production subsidy} \end{bmatrix} Y_{t}, \quad R_{t}^{G} = \sum_{f=0}^{F-1} \lambda_{t-1}^{G,f+1} R_{t}^{f}$$

$$\downarrow & \downarrow & \downarrow \\ \frac{G_{t}}{Y_{t}} \text{ (Exogenous)} \qquad \qquad \downarrow \text{(Exogenous)}$$

• Government: a natural issuer of the entire bond market

Estimation of κ_B \rightarrow Go back

From portfolio equations:

$$\lambda_t^{HB,f} = \left(\frac{z_t^f \mathbb{E}_t \left[Q_{t,t+1} R_{t+1}^{f-1}\right]}{\Phi_t^B}\right)^{\kappa_B}$$

leading to:

$$\begin{array}{l} \textit{f--maturity share} \\ \log \left(\lambda_t^{H,f} \right) - \log \left(\lambda_t^{H,I} \right) = \alpha^{fl} + \kappa_B \cdot E_t \left[r_{t+1}^{f-1} - r_{t+1}^{I-1} \right] + \varepsilon_t^{fl} \end{array}$$

Jordà local projection:

$$\log\left(\lambda_{t+h}^{H,f}\right) - \log\left(\lambda_{t+h}^{H,I}\right) = \alpha_h^{fl} + \kappa_{B,h} \cdot \left[yd_t^f - yd_t^I\right] + \mathbf{x_t}'\beta_h^{fl} + \varepsilon_{t+h}^{fl}, \ h \geq 0 \ ,$$

- Long maturity: $f=5\sim 10$ years and short: $I=15\sim 90$ days (bunching) for portfolio shares and use f=7 years and I=1 month for yields
- Instrument $yd_t^f yd_t^l$ with $yd_{t-1}^f yd_{t-1}^l$ (\perp demand shocks, e.g., z_t^f , z_t^l)
- Control variables (e.g., lagged log $\left(\lambda_{t-1}^{H,f}\right) \log\left(\lambda_{t-1}^{H,I}\right)$ for seriel correlation)

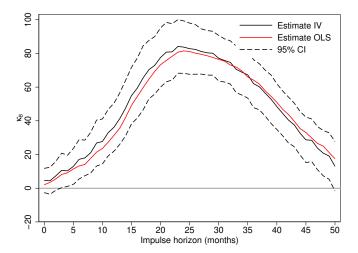


Figure: Impulse-Response to a shock in the yield spread, $yd_t^f-yd_t^l$. The figure presents the coefficient estimates for the bond portfolio elasticity, κ_B . The solid black line illustrates the estimate from the instrumental variables (IV) regression, with dashed lines indicating the 95% robust confidence intervals. The red line exhibits alternative OLS estimates. The sample period is from 2003m3 to 2019m3.

Government's bond supply effects



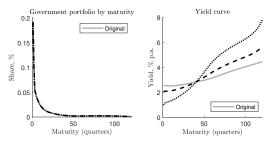


Figure: Government's bond issuance portfolio and yield curve

- Government's supply of f-maturity bond $\uparrow \Longrightarrow$ its yield \uparrow (i.e., price effect)
- Similar to Krishnamurthy and Vissing-Jorgensen (2012) and Greenwood and Vayanos (2014) in the long run

Central bank's bond demand effects



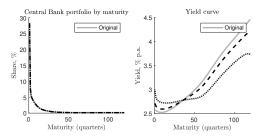


Figure: Central bank's bond demand portfolio and yield curve

Segmented markets ⇒ QE matters in the long run

A deficit ratio: comparative statics



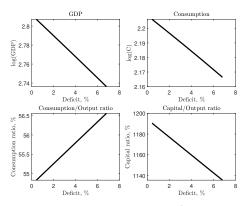


Figure: Variations in a deficit ratio $\zeta_t^{\mathcal{G}} + \zeta^{\mathcal{F}} - \zeta_t^{\mathcal{T}}$

A higher deficit ratio \Longrightarrow depressed economy (for $R^G \downarrow$)

A deficit ratio: comparative statics



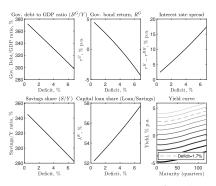


Figure: Variations in a deficit ratio $\zeta_t^{\mathcal{G}} + \zeta^{\mathcal{F}} - \zeta_t^{\mathcal{T}}$

A higher deficit ratio \Longrightarrow depressed economy (for $R^G \downarrow$)

An entire yield curve↓

ZLB impulse response to z_t^K

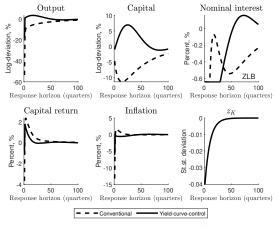


Figure: ZLB impulse response to z_t^K shock

With yield-curve-control (YCC): stabilizing (filling gaps in bond demand)

• But duration of ZLB episodes

Long-term rates ↓ ⇒ ZLB duration ↑ Boback

Impulse-response to an exogenous tax hike shock

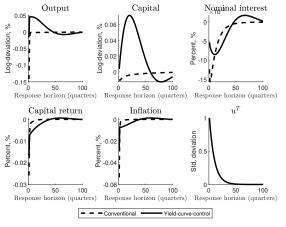


Figure: Impulse response to ϵ_t^T shock

 $Tax\uparrow \Longrightarrow bond supply\downarrow \Longrightarrow yields\downarrow$, loan rates \downarrow , and wages \downarrow (i.e., real effects)

• The yield-curve-control (YCC): stabilizing

