# Do Cost-of-Living Shocks Pass Through to Wages?<sup>1</sup>

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June 5, 2024

<sup>&</sup>lt;sup>1</sup>The views expressed in this paper are those of the authors and do not necessarily reflect the position of the Federal Reserve Bank of New York or the Federal Reserve System.

# Do Cost of Living Shocks Pass Through to Wages?

During COVID, both inflation and nominal wage growth surged.

- Question: are wages responding to inflation, or reflect tight labor markets?
- Concern about 1970's style wage-price spiral:

shock to specific sector ightarrow increased wage demands ightarrow generalized inflation

Sticky wage macro models: union wage setting (Erceg et al., 2000; Lorenzoni and Werning, 2023b) or ad-hoc real wage rigidity (Gagliardone and Gertler, 2023)

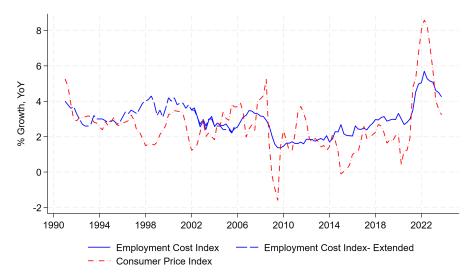
 Micro evidence: wage posting is dominant form of wage determination in the US. (Lachowska et al., 2022; Di Addario et al., 2023)

#### Big Question

If firms set wages, how do wages respond to shocks to cost-of-living?

- "Cost-of-living shock": raises price of consumption bundle, no direct effect on physical marginal product of labor.
- Example: labor intensive services (haircuts), endowment good (food).

# Inflation and wage growth: weak correlation at high frequencies, both surge post-COVID



# Wage Posting, OTJ Search: Weak Cost of Living → Wages

Firms set (post) wages (Lachowska et al., 2022; Di Addario et al., 2023), post vacancies.

- Optimal wage setting trades off wage costs and turnover costs.
- Cost of living affects wages only to the extent that recruiting or retaining workers is harder.

Workers search on the job, experience workplace preference shocks.

- Cost-of-living shocks affect relative value of working vs. nonemployment
  - Lower real wages → income & substitution effects.
  - Income stream from owning endowment goods: wealth effects.
- But: unemployment is rarely a credible threat.
  - ▶ Weak effect of benefit level on wages: (Jäger et al., 2020).
- Firms primarily concerned with job-to-job quits:

#### Related Literature

Wage Posting and/or On-the-Job Search in DSGE Models: Moscarini and Postel-Vinay (2016, 2023); de la Barrera i Bardalet (2023)

 We develop a tractable model and focus on the implications for cost of living shocks

**Supply shocks, inflation, and wage growth**: Lorenzoni and Werning (2023a,b); Gagliardone and Gertler (2023); Pilossoph and Ryngaert (2023)

• General equilibrium, focus on wage posting consistent with microevidence.

Micro evidence

#### Our purpose: tractability

Idiosyncratic preference shocks  $\rightarrow$  single wage in equilibrium.

# Roadmap

Model

2 Cost of Living Shocks

#### Final Consumption Goods

Perfectly-competitive final good producers bundle services  $Y_t$  and endowment good  $X_t$  into final consumption:

$$C_t = \left(\alpha_Y^{\frac{1}{\eta}} Y_t^{\frac{\eta - 1}{\eta}} + \alpha_X^{\frac{1}{\eta}} X_t^{\frac{\eta - 1}{\eta}}\right)^{\frac{\eta}{\eta - 1}},$$

with price index:

$$P_t = \left(\alpha_Y P_{y,t}^{1-\eta} + \alpha_X P_{x,t}^{1-\eta}\right)^{\frac{1}{1-\eta}}$$

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#### Endowment Good $X_t$ and Services Production $Y_t$

 $X_t$  appears each period:

- Each (identical) household receives the same amount
- Competitively & flexibly priced.

 $Y_t$  built from intermediates  $Y_t^j$  by a perfectly-competitive retail firm:

$$Y_{t} = \left( \int \left( Y_{t}^{j} \right)^{\frac{\epsilon - 1}{\epsilon}} dj \right)^{\frac{\epsilon}{\epsilon - 1}},$$

$$P_{y,t} = \left( \int \left( P_{y,t}^{j} \right)^{1 - \epsilon} dj \right)^{\frac{1}{1 - \epsilon}}.$$

#### Households

Maximize the present discounted sum of members' utility,

$$\sum_{t=0}^{\infty} \left(\frac{1}{1+\rho}\right)^t \left[ U_t \ln(C_t^u) + \int_0^{1-U_t} \ln\left(C_t(i,j(i))\right) di \right].$$

by choosing  $C^u_t$  (unemployment benefits) and linear tax/subsidy on employed workers, who consume all labor income:

$$C_t(i,j(i)) = \tau_t \frac{W_{j(i)t}}{P_t}$$

subject to the budget constraint

$$U_t C_t^u = \frac{D_t}{P_t} - \frac{B_t}{P_t} + \frac{(1+i_{t-1})B_{t-1}}{P_t} + (1-\tau_t) \int_0^{1-U_t} \frac{W_{j(i)t}}{P_t} di.$$

#### Consumption Sharing + Euler Equation

We assume an ad hoc consumption sharing rule

$$\frac{\bar{C}_t^e}{C_t^u} = \xi,$$

where  $\xi \geqslant 1$  and  $\bar{C}^e_t \equiv \frac{1}{1-U_t} \int_0^{1-U_t} C_t(i,j(i)) di$  is the average consumption of employed (Chodorow-Reich and Karabarbounis, 2016).

In a symmetric equilibrium with  $W_{jt} = W_t$ , household optimality requires

$$(C_t)^{-1} = \frac{1}{1+\rho}(1+r_{t,t+1})(C_{t+1})^{-1}.$$

# Workers' Discrete-Choice Problem 1/2

#### Timing:

- **1** At start of period t, firms post wages  $W_{jt}$  and vacancies  $V_{jt}$
- Fraction s of workers are exogenously separated.
- Total searchers includes some employed workers and all the unemployed:

$$S_t \equiv \lambda_{EE}(1 - U_{t-1}) + U_{t-1}$$

- Matches happen; workers choose to accept offers and/or quit: with
  - $V_t \equiv \int_0^1 V_{jt} dj, \ \theta_t \equiv \frac{V_t}{S_t}.$

The probability that:

Searching worker meets a firm's vacancy:

$$f(\theta_t) = \frac{M(V_t, S_t)}{S_t}$$

Searching firms meet a worker:

$$g(\theta_t) = \frac{M(V_t, S)}{V_t}$$

- Employed worker can consider quitting to unemployment:  $\lambda_{\it EU} \in (0,1)$
- $N_t$  is determined; production happens.

# Workers' Discrete-Choice Problem 2/2

Each worker i is **myopic**, making choices to maximize

$$\mathcal{V}_t(i,j) = \underbrace{\ln(C_t(i,j(i)))}_{= \begin{cases} \ln\left(\frac{\tau_t}{P_t}W_{j(i)t}\right), \text{ if employed} \end{cases} } + \underbrace{\iota_{ijt}}_{\text{Matching taste}}$$

$$= \begin{cases} \ln\left(\frac{\tau_t}{P_t}\frac{\bar{W}_t}{\xi}\right), \text{ if unemployed} \end{cases}$$

Where  $\iota_{ijt}$  is Type-1 extreme value with scale parameter  $\gamma^{-1}$  over workplaces drawn each period

#### Individual Recruiting and Separation Probabilities

The probability a vacancy attracts a matched searcher r() is

$$\underbrace{r_{kj}(W_{kt},W_{jt})}_{\text{Probability } j \text{ poaches} \atop \text{matched worker from } k} = \underbrace{W_{jt}^{\gamma}}_{W_{kt}^{\gamma}+W_{jt}^{\gamma}}, \qquad \underbrace{r_{uj}\left(\frac{\bar{W}_{t}}{\xi},W_{jt}\right)}_{\text{Probability } j \text{ recruits} \atop \text{matched unemployed worker}} = \underbrace{W_{jt}^{\gamma}}_{\left(\frac{\bar{W}_{t}}{\xi}\right)^{\gamma}+W_{jt}^{\gamma}},$$

where recall  $C_t(i,j) = \frac{\tau_t}{P_t} W_{jt}$  and  $C_t^u = \frac{\tau_t}{P_t} \frac{\vec{W}_t}{\xi}$ .

Similarly, separation probabilities s() for a worker matching with an outside job or considering unemployment:

$$\underbrace{s_{jk}\left(W_{jt},W_{kt}\right)}_{\text{Probability } j \text{ loses}} = \frac{W_{kt}^{\gamma}}{W_{kt}^{\gamma}+W_{jt}^{\gamma}}, \qquad \underbrace{s_{ju}\left(W_{jt},\frac{\bar{W}_{t}}{\xi}\right)}_{\text{Probability } j \text{ loses}} = \frac{\left(\frac{\bar{W}_{t}}{\xi}\right)^{\gamma}}{\left(\frac{\bar{W}_{t}}{\xi}\right)^{\gamma}+W_{jt}^{\gamma}},$$

These determine firm j's recruiting and separation rates,  $R(W_{jt})$  and  $S(W_{jt})$ .

#### Firm's Recruiting and Separation Rates

Define the probability a matched worker is employed or unemployed:

$$\phi_{E,t} \equiv \frac{\lambda_{EE}(1 - U_{t-1})}{S_t}$$
$$\phi_{U,t} \equiv \frac{U_{t-1}}{S_t} = 1 - \phi_{E,t}$$

In a symmetric equilibrium where  $W_{jt} = W_t \ \forall j, \ R(\cdot)_t$  and  $S(\cdot)_t$  becomes

$$R_{t} = g(\theta_{t}) \left( \phi_{E,t} \frac{1}{2} + \phi_{U,t} \left( \frac{\xi^{\gamma}}{1 + \xi^{\gamma}} \right) \right)$$

$$S_{t} = s + (1 - s) \left( \lambda_{EE} f(\theta_{t}) \frac{1}{2} + \lambda_{EU} \left( \frac{1}{1 + \xi^{\gamma}} \right) \right)$$

#### Intermediate Services Firms

Firm j maximizes profits facing to Rotemberg (1982) style adjustment costs:

$$\begin{aligned} \max_{\substack{\{P_{y,t}^{j}\}, \{Y_{t}^{j}\}, \\ \{N_{jt}\}, \{W_{jt}\}, \{V_{t}^{j}\}}} \sum_{t=0}^{\infty} \left(\frac{1}{1+\rho}\right)^{t} \left(P_{y,t}^{j} Y_{t}^{j} - W_{jt} N_{jt} - c \left(\frac{V_{jt}}{N_{j,t-1}}\right)^{\chi} V_{jt} W_{t} \right. \\ \left. - \frac{\psi}{2} \left(\frac{P_{y,t}^{j}}{P_{y,t-1}^{j}} - 1\right)^{2} Y_{t}^{j} P_{y,t}^{j} - \frac{\psi^{w}}{2} \left(\frac{W_{jt}}{W_{j,t-1}} - 1\right)^{2} W_{jt} N_{jt} \right) \end{aligned}$$

subject to the law of motion on employment:

$$N_{jt} = (1 - S(W_{jt}))N_{j,t-1} + R(W_{jt})V_{jt}.$$

Service firms produce using only labor

$$Y_t^j = N_{jt}$$

with demand from a retail firm

$$\frac{Y_t^j}{Y_t} = \left(\frac{P_{y,t}^j}{P_{y,t}}\right)^{-\epsilon}.$$

#### Closing the Model & Equilibrium

We close the model with a simple Taylor rule, with a potentially persistent policy shock  $\varepsilon_{i,t}$ :

$$\ln(1+i_t) = \phi_{\Pi} \ln(\Pi_{Y,t}) + \log(1+\varepsilon_{i,t})$$

A symmetric equilibrium consists of sequences of all endogenous prices and quantities such that:

- **1** Firms choose identical sequences such that  $W_{jt} = W_t$ ,  $N_{jt} = N_t$ ,  $V_{jt} = V_t$ ,  $P_{yt}^j = P_{y,t}$ , for all t,
- Workers and households maximize utility,
- Firms maximize profits,
- Product markets clear,

We linearize these necessary conditions around a non-stochastic steady state, and solve for the unique solution in e.g. Dynare.

#### Symmetric Equilibrium: Key Equations

Aggregate demand obeys standard Euler equation:

$$(C_t)^{-1} = \frac{1}{1+\rho} (1+r_{t,t+1}) (C_{t+1})^{-1}$$

Wage Inflation follows the wage Phillips curve

$$\begin{split} \psi^{w}\left(\Pi_{t}^{w}-1\right)\Pi_{t}^{w}+1 = &c(1+\chi)\left(\frac{V_{t}}{N_{t-1}}\right)^{\chi}\left\lfloor\frac{V_{t}}{N_{t}}\underbrace{\varepsilon_{R,W_{t}}}_{>0} + \left(-\underbrace{\varepsilon_{S,W_{t}}}_{<0}\right)\frac{N_{t-1}}{N_{t}}\frac{S_{t}}{R_{t}}\right\rfloor \\ &+\frac{1}{1+\rho}\psi^{w}\left(\Pi_{t+1}^{w}-1\right)\left(\Pi_{t+1}^{w}\right)^{2}\frac{N_{t+1}}{N_{t}}. \end{split}$$

 $\varepsilon_{R,W} - \varepsilon_{S,W}$ : measure of degree of labor market competition in dynamic monopsony models. Micro evidence Log-linear version

#### Value Meaning Reason

Match EE rates

Match voluntary EU rate. Qiu (2022)

BLS

**JOLTS** 

Bassier et al. (2022)

17

.044

.036

4.2

Parameters in the Monthly Benchmark New Keynesian Model

LO		- 1-1	, , , , , , , , , , , , , , , , , , , ,
ξ	2	Consumption ratio: $C_t^e/C_t^u$	See text
S	.01	Exogenous separation rate	Match JOLTS separations
$\gamma$	6	$Variance^{-1}$ of pref. shock	Match $\varepsilon_{R,W} - \varepsilon_{S,W}$

U	variance of pier. Shock	Widten CR,
10	EOS of intermediates $Y_{jt}$	
100	Price adjustment cost	
100	Wage adjustment cost	
1	FOS of $Y_{*}$ vs. $X_{*}$	

Unemployment rate

Monthly separation rate

Recruiting-Separation Elasticity

OTJ search probability Opportunity to quit

Parameter

 $\lambda_{\it EE}$ 

 $\lambda_{FII}$ 

 $\epsilon$ 

U

S

 $\varepsilon_{R,W} - \varepsilon_{S,W}$ 

.14

.30

$\psi$	100	Price adjustment cost
$\psi^{w}$	100	Wage adjustment cost
$\eta$	1	EOS of $Y_t$ vs. $X_t$
$\alpha_{X}$	.2	$X_t$ 's share in $C_t$

Ψ	100	wage adjustilient cost	
$\eta$	1	EOS of $Y_t$ vs. $X_t$	
$\alpha_X$	.2	$X_t$ 's share in $C_t$	
$\chi$	1	Convexity of vacancy costs	Bloesch and Larsen (2023)
С	30	Hiring cost shifter	Targeting $U$
	004	D' D .	M +  -     -

ho	.004 Discount Rate	Monthly model	
	Selected Model Mor	nents and Data in Steady State	
Moment	Meaning	Model Data Source	

.044

.036

4.4

#### Pass-Through in Our Baseline Model

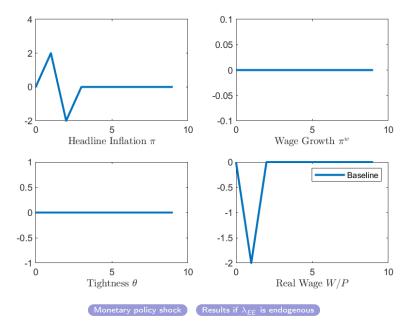
$$\ln W_t - \ln W_{t-1} = \beta_Q \check{Q}_t + \beta_U \check{U}_{t-1} + \frac{1}{1+\rho} \check{\Pi}_{t+1}^w \tag{1}$$

#### Thought Experiment (Cost of Living Shock)

-10% shock to  $X_t$  raises the price level, but monetary policy stabilizes employment, i.e.,  $\check{N}_t = 0$ 

- Pass through in our model is zero because there is no effect of the price level on the relative value of non-employment
  - Stabilizing the labor market stabilizes the right hand side of (1).
- This is different from a model where unions set wages, or neo-classical labor supply: depending on the strength of income, substitution, and wealth effects, wages can go up or down in response to this shock
  - For standard macro calibrations, a higher price level makes workers want to work less, so wages must rise to stabilize  $N_t$

#### Pass Through in Our Baseline Model is Zero



#### If Unemployment Gets More Attractive When Prices Rise

#### Alter the model

**Assumption**: household insures unemployed members against inflation, but not employed members

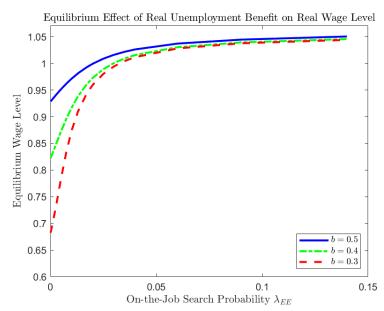
$$C_t(i,j(i)) = \frac{W_{j(i)t}}{P_t}(1+\tau_t)$$
$$C_t^U = b(1+\tau_t).$$

In a symmetric equilibrium, the separation and recruiting rates become

$$\begin{split} R_t &= g(\theta_t) \left( \phi_{E,t} \frac{1}{2} + \phi_{U,t} \frac{\left( \frac{W_t}{P_t} \right)^{\gamma}}{\left( \frac{W_t}{P_t} \right)^{\gamma} + b^{\gamma}} \right) \\ S_t &= s + (1 - s) \left( \lambda_{EE} f(\theta_t) \frac{1}{2} + \lambda_{EU} \frac{b^{\gamma}}{\left( \frac{W_t}{P_t} \right)^{\gamma} + b^{\gamma}} \right), \end{split}$$

When  $P_t \uparrow$ , unemployment becomes more attractive for a given  $W_t$ : firms must raise wages to retain workers. Model details

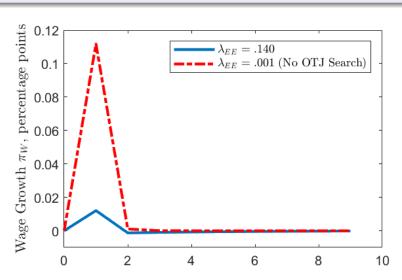
# OTJ Search Kills Effect of Unemployment Benefit on Wages



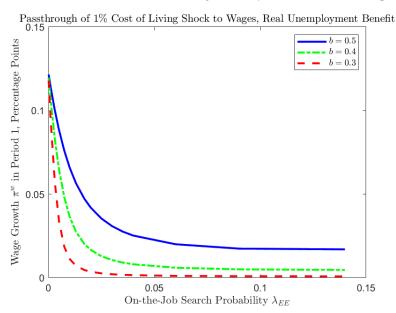
# On-the-Job Search Dramatically Dampens Pass-through

#### Thought Experiment (Cost of Living Shock)

1 Period, 10% drop in quantity of endowment good  $X_t$ 



# On-the-Job Search Dramatically Dampens Pass-through II



#### Conclusion

We develop a tractable New Keynesian model with wage-posting firms and on-thejob search consistent with a range of micro evidence.

- Wage posting → wage setting trades off wage costs vs. turnover costs.
- Wage growth is mostly driven by quits, not unemployment.
- On-the-job search dramatically dampens pass-through of cost of living shocks to wages.
- Bernanke & Blanchard (2024): "catch-up" effect, the tendency of workers to press for compensation for earlier unexpected price increases, appears limited in practice, with the estimated coefficient on the catch-up variable in the wage equation close to zero in most countries.
- Some macro evidence Empirics

**Implication**: COVID-era surge in wage growth will revert as labor market tightness reverts

# Thank you very much! (Appendix)

#### Micro Evidence

#### Model consistent with a range of micro evidence:

- Well-identified evidence on the sensitivity of recruiting and quitting to changes in wages (recruiting & separations elasticities) estimated in monopsony literature: e.g., Manning (2011); Azar et al. (2021); Datta (2023).
- Wage growth predicted by job-to-job transitions: e.g., Faberman & Justiniano (2015); Moscarini & Postel-Vinay (2016); Karahan et al. (2017).
- 3 Wages unresponsive to flow benefit of unemployment (Jäger et al., 2020)
- Wage posting more common than bargaining: current firm wage effects > past wage effects: e.g., Addario et al. (2021)

Back to related literature Back to equilibrium conditions

#### Simpler, Log-Linear Wage Phillips Curves: Goback

Leveraging the full structure of the model this simplifies to:

$$\check{\Pi}_{t}^{w} = \phi_{V} \check{V}_{t} + \phi_{U} \check{U}_{t-1} + \frac{1}{1+\rho} \check{\Pi}_{t+1}^{w}$$
(2)

With  $\phi_V > 0$  and  $\phi_U < 0$ ; our baseline calibration implies  $\phi_V$  is much larger than  $\phi_{II}$  in magnitude Comparative statics with  $\lambda_{EE}$ 

Let  $Q_t \equiv S_t - s$ , and rewrite (2) as

$$\check{\Pi}_t^w = \beta_Q \check{Q}_t + \beta_U \check{U}_{t-1} + \frac{1}{1+\rho} \check{\Pi}_{t+1}^w \tag{3}$$

With  $\beta_{O} > 0$  and  $\beta_{U}$  positive or negative, depending on the calibration

#### Wage Growth v.s. Labor Market Data, 1990Q4-2023 Goback



$$\ln W_t - \ln W_{t-1} = \hat{\beta}_0 + \hat{\beta}_Q \ln Q_t + \hat{\beta}_U \ln U_{t-1} + \varepsilon_t.$$

VARIABLES	(1) ECI	(2) ECI	(3) ECI	(4) ECI	(5) ECI
In $U_t$	-0.0055***	0.0003	0.0017		
In $Q_t$	(0.0009)	(0.0011) 0.0116***	(0.0012) 0.0119***	0.0116***	0.0116***
III Qt		(0.0020)	(0.0020)	(0.0024)	(0.0016)
In $U_t - In\ U_t^{f *}$		,	,	0.0003	,
				(0.0013)	
In $U_{t-1}$					0.0003
					(8000.0)
Observations	135	135	119	135	135

Standard errors in parentheses \*\*\* p<0.01, \*\* p<0.05, \* p<0.1

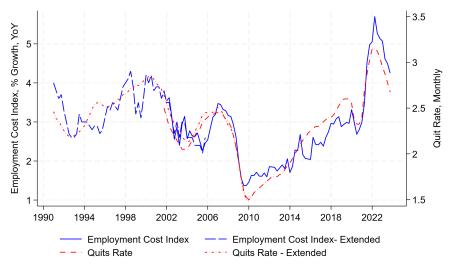
#### Comparing Model to Data Go back

$$\check{\Pi}_t^w = \beta_Q \check{Q}_t + \beta_U \check{U}_{t-1} + \frac{1}{1+\rho} \check{\Pi}_{t+1}^w$$

Source	$eta_{m{Q}}$	$eta_{m{U}}$
Baseline Model: $\chi=1$	0.0246	0.0009
Baseline Model: $\chi = 0$	0.0213	-0.0011
OLS using ECI 1990-Present	0.0116***	0.0003
	(0.0016)	(8000.0)

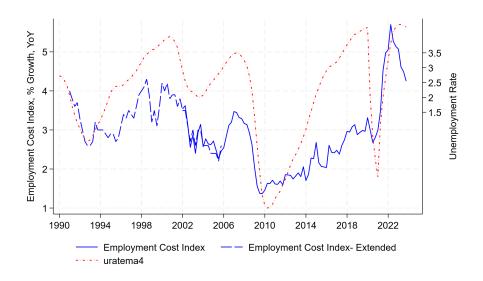
Standard errors in parentheses (Newey-West; 4 lags) \*\*\* p<0.01, \*\* p<0.05, \* p<0.1

# Quits Rate Captures Labor Market "Tightness" Go back

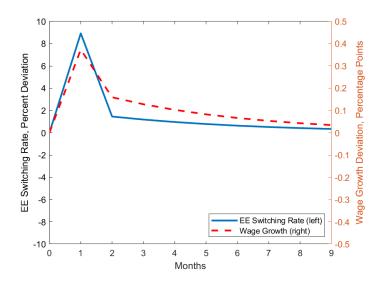


Extends results by, e.g., Faberman and Justiniano (2015) and Moscarini and Postel-Vinay (2017), through COVID shock and recovery.

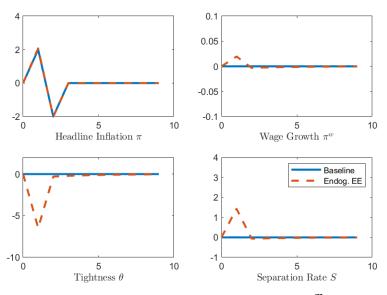
# Unemployment: Less So Go back



#### Expansionary 1% Decrease in the Policy Rate Go back



# Endogenous labor search intensity Go back



Baseline model, but now assuming:  $\lambda_{\textit{EE},t} = \lambda_{\textit{EE},0} \left( \frac{W_t}{P_t} \right)^{-m}$ 

#### Households Go back

Maximize the present discounted sum of members' utility,

$$\sum_{t=0}^{\infty} \left( \frac{1}{1+\rho} \right)^t \left[ U_t \ln(C_t^u) + \int_0^{1-U_t} \ln\left(C_t(i,j(i))\right) di \right]. \tag{4}$$

Assumption: household insures unemployed members against inflation, but not employed members

$$C_t(i,j(i)) = \frac{W_{j(i)t}}{P_t}(1+\tau_t)$$
$$C_t^U = b(1+\tau_t).$$

Households choose bonds  $\{B_t\}$ , "top-up"  $\{\tau_t\}$  to maximize (4) subject to the budget constraint:

$$U_t b(1+\tau_t) + (1-U_t) \frac{W_t}{P_t} (1+\tau_t) + \frac{B_t}{P_t} = \frac{D_t}{P_t} + \frac{(1+i_{t-1})B_{t-1}}{P_t} + \int_0^{1-U_t} \frac{W_{j(t)t}}{P_t} di.$$

In a symmetric equilibrium with  $W_{jt} = W_t$ , household optimality requires

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# Workers' Discrete-Choice Problem 1/2 Go back

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The probability that:

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Searching firms meet a worker:

$$g(\theta_t) = \frac{M(V_t, S)}{V_t}$$

- Employed worker can consider quitting to unemployment:  $\lambda_{EU} \in (0,1)$
- $N_t$  is determined; production happens.

### Workers' Discrete-Choice Problem 2/2 Go back



Each worker i is **myopic**, making choices to maximize

$$\begin{split} \mathcal{V}_t(i,j) = & \underbrace{\ln \left( C_t(i,j(i)) \right)}_{= \begin{cases} \ln \left( \frac{W_t}{P_t} (1+\tau_t) \right) \text{, if employed} \end{cases}} & + \underbrace{\iota_{ijt}}_{\text{Matching taste}} \\ = & \begin{cases} \ln \left( b(1+\tau_t) \right) \text{, if unemployed} \end{cases} \end{split}$$

Where  $\iota_{iit}$  is Type-1 extreme value with scale parameter  $\gamma^{-1}$  over workplaces drawn each period

#### Individual Recruiting and Separation Probabilities Goback



The probability a vacancy attracts a matched searcher r() is

$$\underbrace{r_{kj}(W_{kt},W_{jt})}_{\text{Probability } j \text{ poaches matched worker from } k} = \underbrace{W_{jt}^{\gamma}}_{W_{kt}^{\gamma}+W_{jt}^{\gamma}}, \qquad \underbrace{r_{uj}\left(b,\frac{W_{jt}}{P_t}\right)}_{\text{Probability } j \text{ recruits matched unemployed worker}} = \underbrace{\frac{\left(\frac{W_{jt}}{P_t}\right)^{\gamma}}{b^{\gamma}+\left(\frac{W_{jt}}{P_t}\right)^{\gamma}}},$$

where recall 
$$C_t(i,j) = rac{W_{jt}}{P_t}(1+ au_t)$$
 and  $C_t^u = b(1+ au_t)$ 

Similarly, separation probabilities for a worker matching with an outside job or considering unemployment:

$$\underbrace{s_{jk}\left(W_{jt},W_{kt}\right)}_{\text{Probability $j$ loses}} = \underbrace{W_{kt}^{\gamma}}_{W_{kt}^{\gamma}}, \\ \underbrace{w_{jt}^{\gamma}+W_{jt}^{\gamma}}_{\text{Probability $j$ loses}} = \underbrace{b^{\gamma}}_{b^{\gamma}+\left(\frac{W_{jt}}{P_{t}}\right)^{\gamma}}, \\ \underbrace{s_{ju}\left(\frac{W_{jt}}{P_{t}},b\right)}_{\text{Probability $j$ loses}} = \underbrace{b^{\gamma}}_{b^{\gamma}+\left(\frac{W_{jt}}{P_{t}}\right)^{\gamma}}, \\ \underbrace{w_{jt}^{\gamma}+W_{jt}^{\gamma}}_{\text{Probability $j$ loses}} = \underbrace{b^{\gamma}}_{b^{\gamma}+\left(\frac{W_{jt}}{P_{t}}\right)^{\gamma}}, \\ \underbrace{w_{jt}^{\gamma}+W_{jt}^{\gamma}}_{\text{Probability $j$ loses}} = \underbrace{b^{\gamma}}_{b^{\gamma}+\left(\frac{W_{jt}}{P_{t}}\right)^{\gamma}}, \\ \underbrace{w_{jt}^{\gamma}+W_{jt}^{\gamma}}_{\text{Probability $j$ loses}} = \underbrace{b^{\gamma}}_{b^{\gamma}+\left(\frac{W_{jt}}{P_{t}}\right)^{\gamma}}, \\ \underbrace{b^{\gamma}+\left(\frac{W_{jt}}{P_{t}}\right)^{\gamma}}_{\text{Probability $j$ loses}} = \underbrace{b^{\gamma}+\left(\frac{W_{jt}}{P_{t}}\right)^{\gamma}}_{\text{Probability $j$ loses}}_{\text{Probability $j$ loses}} = \underbrace{b^{\gamma}+\left(\frac{W_{jt}}{P_{t}}\right)^{\gamma}}_{\text{Probability $j$ loses}}_{\text{Probability $j$ loses}} = \underbrace{b^{\gamma}+\left(\frac{W_{jt}}{P_{t}}\right)^{\gamma}}_{\text{Probability $j$ loses}}_{\text{Probability $j$$$

### Firm's Recruiting and Separation Rates Goback

Define the probability a matched worker is employed or unemployed:

$$\phi_{E,t} \equiv \frac{\lambda_{EE}(1 - U_{t-1})}{\lambda_{EE}(1 - U_{t-1}) + U_{t-1}}$$
$$\phi_{U,t} = 1 - \phi_{E,t}.$$

# Firm's Recruiting and Separation Rates Goback

Define the probability a matched worker is employed or unemployed:

$$\begin{split} \phi_{E,t} &\equiv \frac{\lambda_{EE}(1-U_{t-1})}{\lambda_{EE}(1-U_{t-1})+U_{t-1}} \\ \phi_{U,t} &= 1-\phi_{E,t}. \end{split}$$

Recruiting rate is

$$R(W_{jt}) = g(\theta_t) \left[ \phi_{E,t} \int_k r_{kj}(W_{kt}, W_{jt}) \omega(W_{kt}) dW_{kt} + \phi_{U,t} r_{uj} \left( b, \frac{W_{jt}}{P_t} \right) \right],$$

with  $\omega(W_k)$  some density of wages that search workers currently earn, with an analogous definition for the separation rate  $S(W_i)$ .

$$S(\textit{W}_{jt}) = s + (1-s) \left[ \lambda_{\textit{EE}} f(\theta_t) \int_{\textit{k}} \textit{s}_{j\textit{k}}(\textit{W}_{jt}, \textit{W}_{\textit{kt}}) \textit{z}(\textit{W}_{\textit{kt}}) \textit{dW}_{\textit{kt}} + \lambda_{\textit{EU}} \textit{s}_{j\textit{u}} \left( \frac{\textit{W}_{jt}}{\textit{P}_t}, \textit{b} \right) \right]$$

with  $z(W_{kt})$  endogenous density of outside posted wages

## Firm's Recruiting and Separation Rates Goback



Define the probability a matched worker is employed or unemployed:

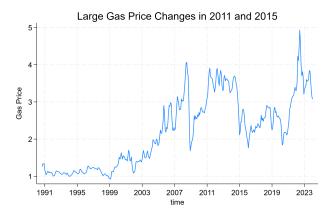
$$\begin{split} \phi_{E,t} &\equiv \frac{\lambda_{EE}(1-U_{t-1})}{\lambda_{EE}(1-U_{t-1})+U_{t-1}} \\ \phi_{U,t} &= 1-\phi_{E,t}. \end{split}$$

In a symmetric equilibrium where  $W_{jt} = W_t \ \forall j, \ R(\cdot)_t$  and  $S(\cdot)_t$  becomes

$$\begin{split} R_t &= g(\theta_t) \left( \phi_{E,t} \frac{1}{2} + \phi_{U,t} \frac{\left( \frac{W_t}{P_t} \right)^{\gamma}}{\left( \frac{W_t}{P_t} \right)^{\gamma} + b^{\gamma}} \right) \\ S_t &= s + (1 - s) \left( \lambda_{EE} f(\theta_t) \frac{1}{2} + \lambda_{EU} \frac{b^{\gamma}}{\left( \frac{W_t}{P_t} \right)^{\gamma} + b^{\gamma}} \right). \end{split}$$

### New Calibration with *b* Go back

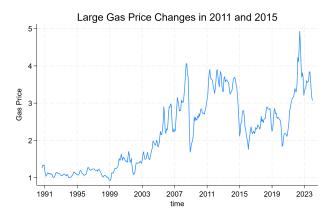
Parameter	Value	Meaning	Reaso	Reason		
$\lambda_{\it EE}$	.14	OTJ search probability	Matcl	Match EE rates		
$\lambda_{\it EU}$	.30	Opportunity to quit	Matcl	Match voluntary EU rate, Qiu (2022)		
Ь	0.45	Unemployment Benefit	Targe	t <i>U</i>		
5	.01	Exogenous separation rate	Matcl	Match JOLTS separations		
$\gamma$	6	T1EV scale parameter	Matcl	Match $\varepsilon_{R,W} - \varepsilon_{S,W}$		
$\epsilon$	10	EOS of intermediates $Y_{jt}$				
$\psi$	100	Price adjustment cost				
$\psi^{\sf w}$	100	Wage adjustment cost				
$\eta$	1	EOS of $Y_t$ vs. $X_t$				
$\alpha_X$	.2	$X_t$ 's share in $C_t$				
$\chi$	1	Convexity of vacancy costs	Bloes	Bloesch and Larsen (2023)		
C	30	Hiring cost shifter	Targe	Targeting $U$ , $S$		
ho	.004	Discount Rate	Monthly model			
Selected Model Moments and Data in Steady State						
Moment	Mear	Meaning		Data	Source	
U	Unemployment rate		.044	.044	BLS	
S	Mont	Monthly separation rate		.036	JOLTS	
$\varepsilon_{R,W} - \varepsilon_{S,W}$	Recruiting-Separation Elasticity		4.0	4.2	Bassier et al. (2022)	



Share of annual wages spent on gasoline in state j

$$share_{j} = \frac{vmt_{2010,j}}{\underbrace{20}_{20 \text{ miles per gallon}}} \times \$2 \times \frac{1}{statehourlywage_{2010} \times 2000}$$





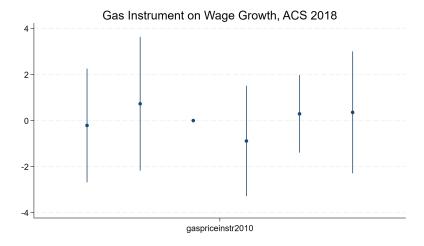
Shift: % change in national gas prices,  $\%\Delta P_t^g$ . The shift share instrument is

$$gasinst_{jt} = share_j \times \% \Delta P_t^g$$
.

Estimate:

$$\log W_{j,t+s} - \log W_{j,t-1} = \alpha_s + \beta_s \times gasinst_{jt} + e_{jt}$$
 (5)

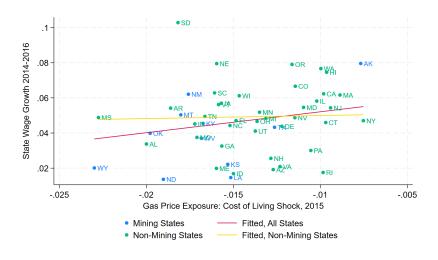




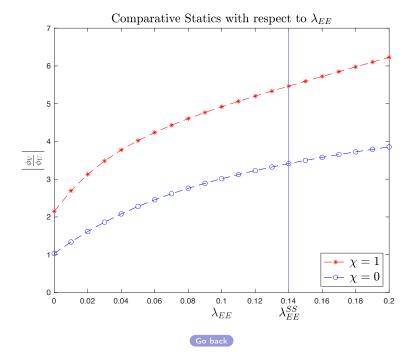












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