### Causality and observational studies

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### Agenda

- What is causality
- Randomized experiments
- Calculating effects
- Observational studies

### Causal Inference

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**Causal inference** is the attempt to derive causal connection based on the conditions of the occurrence of an effect

#### Causal effects

Think of the causal effect as the difference between what happened and what could have happened with/without a treatment (or change in X)

 $X \rightarrow Y$ 

T -> Y

How do we know whether those variables are causally related?

 $X \rightarrow Y$ 

 $T \rightarrow Y$ 

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Do they occur together?

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If X goes up, Y goes up

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If X happens, Y happens

If T, then change in Y

If two things happen together a lot, we say they are correlated

# Correlation and causation

Does correlation imply causation?

#### Correlation not causation

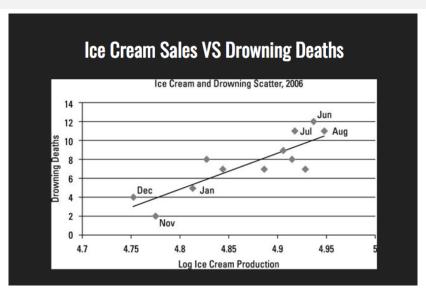


Figure 1: Ice cream sales and drowning incidents

#### Correlation not causation

### Number of people who drowned by falling into a pool

#### Films Nicolas Cage appeared in

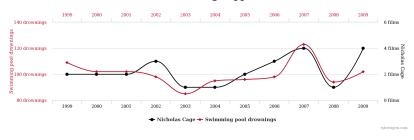


Figure 2: Cage films and pool incidents

#### Factual and counterfactual?

Factual: What happened

Counterfactual: What would have happened

**Fundamental problem of causal inference**: We can never observe counterfactuals, must be inferred

Fundamental problem of causal inference in a movie: Sliding Doors

(1998) https://www.youtube.com/watch?v=BvUbv4iwbDs

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- A judge with a daughter gave a pro-choice ruling
- Would she/he have done that if she/he had a son instead?

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- Experimental setting:
  - Randomly assign canvassers to have a conversation about transgender right or a conversation about recycling
  - -Trans rights conversations focused on "perspective taking"
- Outcome of interest: support for trans rights policies

# A tale of two respondents

	Conversation script (T)	Support for Nondiscrimination law (Y)
Respondent 1	Recycling	No
Respondent 2	Trans rights	Yes

# A tale of two respondents

	Conversation script (T)	Support for Nondiscrimination law (Y	
Respondent 1 Respondent 2	Recycling Trans rights	No Yes	

 Key interest: Did the second respondent support the law because of the perspective-taking conversation?

# Translating into math

Useful to have **compact** notation for referring to **treatment** variable

$$T_i = \begin{cases} 1, & \text{if respondent } i \text{ had trans rights conversation} \\ 0, & \text{if respondent } i \text{ had recycling conversation} \end{cases}$$

Similar notation for the outcome variable:

$$Y_i = \begin{cases} 1, & \text{if respondent } i \text{ supports trans nondiscrimination laws} \\ 0, & \text{if respondent } i \text{ doesn't support nondiscrimination laws} \end{cases}$$

i is a placeholder to refer to a generic unit/respondent:  $Y_{12}$  is the outcome for the 12th unit

# A tale of two respondents (redux)

	Conversation script (T)	Support for Nondiscrimination law (Y)
Respondent 1 Respondent 2	Recycling Trans rights	No Yes

becomes...

i	$T_i$	$Y_i$
Respondent 1	0	0
Respondent 2	1	1

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#### Two potential outcomes:

- $Y_i(1)$ : would respondent i support ND laws if they had trans rights script?
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Causal effect:  $Y_i(1) - Y_i(0)$ 

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• 
$$Y_i(1) - Y_i(0) = 0 \rightsquigarrow$$

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#### Potential outcomes

i	$T_i$	Yi	$Y_i(1)$	$Y_i(0)$
Respondent 1	0	0	???	0
Respondent 2	1	1	1	???

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- Observe  $Y_i(1) Y_i(0) = 1$  or  $Y_i(1) Y_i(0) = 0$
- To infer causal effect, we need to infer the missing counterfactuals!

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 ~ find a state similar to NJ that didn't increase minimum wage

## Imperfect matches

The problem: we cannot match on everything (imperfect matches)

- Say we match *i* (treated) and *j* (control)
- $Y_i(1) \neq Y_i(1)$  due to **selection bias**
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- How can we correct for that? Randomization!

# 2. Randomized experiments

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Randomization ensures **balance** between treatment and control groups

- Treatment and control group are identical on average
- Similar on both observable and unobservable characteristics

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How many in our sample support nondiscrimination laws?

$$Y_1 + Y_2 + Y_3 + ... + Y_n$$

Notation is a bit chunky so we often use the **Sigma notation**:

$$\sum_{i=1}^{n} Y_i = Y_1 + Y_2 + Y_3 + \dots + Y_n$$

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 $\sum_{i=1}^{n} Y_i$  simply means sum each value from  $Y_1$  to  $Y_n$ 

## **Averages**

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Suppose we surveyed 6 people and 3 supported gay marriage:

$$\overline{Y} = \frac{(1+1+1+0+0+0)}{6} = 0.5$$

We want to estimate the average causal effects over all units:

Sample Average Treatment Effect (SATE) 
$$=\frac{1}{n}\sum_{i=1}^n[Y_i(1)-Y_i(0)]$$
  $=\frac{1}{n}\sum_{i=1}^nY_i(1)-\frac{1}{n}\sum_{i=1}^nY_i(0)$ 

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When will the difference-in-means is a good estimate of the SATE?

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Average in the control group will be similar to average if all untreated:

$$\overline{Y}_{control} \approx \frac{1}{n} \sum_{i=1}^{n} Y_i(0)$$

• Implies difference-in-means should be close to SATE:

## Why randomization works

- Under an RCT, treatment and control groups are random samples
- Average in the treatment group will be similar to average if all treated:

$$\overline{Y}_{treated} \approx \frac{1}{n} \sum_{i=1}^{n} Y_i(1)$$

Average in the control group will be similar to average if all untreated:

$$\overline{Y}_{control} \approx \frac{1}{n} \sum_{i=1}^{n} Y_i(0)$$

Implies difference-in-means should be close to SATE:

$$\overline{Y}_{treated} - \overline{Y}_{control} \approx \frac{1}{n} \sum_{i=1}^{n} Y_i(1) - \frac{1}{n} \sum_{i=1}^{n} Y_i(0) = \frac{1}{n} \sum_{i=1}^{n} [Y_i(1) - Y_i(0)] = \mathsf{SATE}$$

## Some potential problems with $\operatorname{RCTs}$

Placebo effects:

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 Respondents will be affected by any intervention, even if they shouldn't have any effectively

#### Hawthorne effects:

## Some potential problems with RCTs

#### Placebo effects:

 Respondents will be affected by any intervention, even if they shouldn't have any effectively

#### Hawthorne effects:

 Respondents act differently just knowing that they are under study

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We can check in the actual data for some pretreatment variable X

- $\overline{X}_{treated}$ : average value of variable for treated group
- $\overline{X}_{control}$ : average value of variable for control group
- Under randomization,  $\overline{X}_{treated} \overline{X}_{control} \approx 0$

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#### Outcome:

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#### Treatment:

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**Treatment**: officers who are randomly assigned to take a year long statistic course

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#### Control group:

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**Treatment**: officers who are randomly assigned to take a year long statistic course

**Control group**: officers who are randomly assigned and not taking a year-long stat course

## An example of balance checking (cont)

Balance checking means the differences in pretretment variables should not exist among officers between the two groups on average

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## An example of balance checking (cont)

Balance checking means the differences in pretretment variables should not exist among officers between the two groups on average

What would be examples of pretreatment variables?

These could be gender, age, race, tenure, income, marital status, education, or any other characteristics

• Instead of 1 treatment, we might have multiple **treatment** arms:

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  - $\overline{Y}_{treated,B} \overline{Y}_{treated,C}$ , etc
- If treatment arms are randomly assigned, these differences will be good estimators for each causal contrast

## Randomized Experiments from Blacklist

• Blacklist Season 6 Episode 20 (19:39)

# 3. Calculating effects

#### Transphobia study data

Now we RetuRn to R to illustrate how to calculate the effects!

## reinstall TPDdata if necessary
library(TPDdata)

Variable	Description
age female voted_gen_14 voted_gen_12 treat_ind racename democrat nondiscrim_pre nondiscrim_post	Age of the Respondent (R) in years  1=R marked "Female" on voter reg., 0 otherwise  1 if R voted in the 2014 general election  1 if R voted in the 2012 general election  1 if R assigned to trans rights script, 0 for recycling name of racial identity indicated on voter file  1 if R is a registered Democrat  1 if R supports nondiscrim. law at baseline  1 if R supports nondiscrim. law after 3 months

#### Peak at the data

```
## # A tibble: 565 x 9
        age female voted gen 14 voted gen~1 treat~2 racen~3 democ~4 nondi~5 nondi~6
      <dbl> <dbl>
                                       <dh1>
##
                          <dh1>
                                               <dhl> <chr>>
                                                               <dh1>
                                                                        <dh1>
                                                                                <dh1>
         29
                                                   O Africa~
##
         59
                                                   1 Africa~
         35
                                                   1 Africa~
##
         63
                                                   1 Africa~
         65
                                                   1 Africa~
         51
                                                   0 Caucas~
##
         26
                                                   0 Africa~
         62
                                                   1 Africa~
         37
                                                   0 Caucas~
         51
## 10
                                                   0 Caucas~
     ... with 555 more rows, and abbreviated variable names 1: voted gen_12,
       2: treat_ind, 3: racename, 4: democrat, 5: nondiscrim_pre,
## #
       6: nondiscrim_post
```

trans

## Calculate the average outcomes in each group

```
treat_mean <- trans |>
  filter(treat_ind == 1) |>
  summarize(nondiscrim_mean = mean(nondiscrim_post))
treat_mean

## # A tibble: 1 x 1
## nondiscrim_mean
## <dbl>
## 1 0.687
```

## Calculate the average outcomes in each group

```
treat mean <- trans |>
 filter(treat_ind == 1) |>
 summarize(nondiscrim_mean = mean(nondiscrim_post))
treat mean
## # A tibble: 1 x 1
##
    nondiscrim mean
               <dbl>
##
## 1
               0.687
control mean <- trans |>
 filter(treat_ind == 0) |>
  summarize(nondiscrim_mean = mean(nondiscrim_post))
control_mean
## # A tibble: 1 x 1
    nondiscrim_mean
##
##
               <dbl>
## 1
               0.648
```

# Calculating the difference-in means

```
treat_mean - control_mean
```

```
## nondiscrim_mean
## 1 0.03896674
```

We will see more ways to do this throughout the semester

# Checking balance on numeric covariates

We can use group\_by to see how the mean of covariates varies by group:

### Checking balance on categorical covariates

Or we can group by treatment and a categorical control:

```
trans |>
 group_by(treat_ind, racename) |>
 summarize(n = n())
## `summarise()` has grouped output by 'treat_ind'. You can override using the
## `.groups` argument.
## # A tibble: 9 x 3
## # Groups: treat ind [2]
##
    treat ind racename
                                n
##
        <dbl> <chr>
                           <int>
## 1
           O African American
                               58
## 2
           0 Asian
## 3
         O Caucasian
                               77
           0 Hispanic
## 4
                              150
## 5
           1 African American
                               68
## 6
           1 Asian
                               4
## 7
           1 Caucasian
                               75
## 8
           1 Hispanic
                              130
           1 Native American
## 9
```

Hard to read!

pivot\_wider() takes data from a single column and moves it into multiple columns based on a grouping variable:

```
trans |>
  group_by(treat_ind, racename) |>
  summarize(n = n()) |>
  pivot_wider(
    names_from = treat_ind,
    values_from = n
)
```

pivot\_wider() takes data from a single column and moves it into multiple columns based on a grouping variable:

```
trans |>
  group_by(treat_ind, racename) |>
  summarize(n = n()) |>
  pivot_wider(
    names_from = treat_ind,
    values_from = n
)
```

names\_from tells us what variable will map onto the columns
values\_from tells us what values should be mapped into those
columns

```
trans |>
 group_by(treat_ind, racename) |>
 summarize(n = n()) >
 pivot_wider(
   names from = treat ind,
   values_from = n
## `summarise()` has grouped output by 'treat_ind'. You can override using the
## `.groups` argument.
## # A tibble: 5 x 3
##
                        `0` `1`
    racename
## <chr>
                     <int> <int>
## 1 African American
                        58
                              68
## 2 Asian
                            4
## 3 Caucasian
                        77 75
## 4 Hispanic
                       150
                             130
## 5 Native American
                        NΑ
                               1
```

### Calculating diff-in-means by group

```
trans |>
 mutate(
   treat ind = if else(treat ind == 1, "Treated", "Control"),
   party = if_else(democrat == 1, "Democrat", "Non-Democrat")
 ) |>
 group_by(treat_ind, party) |>
 summarize(nondiscrim_mean = mean(nondiscrim_post)) |>
 pivot wider(
   names from = treat_ind,
   values from = nondiscrim mean
 ) |>
 mutate(
   diff in means = Treated - Control
```

## 1 Democrat 0.704 0.754 0.0498 ## 2 Non-Democrat 0.605 0.628 0.0234

• Can newspaper endorsements change voters' minds?

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Why not compare vote choice of readers of different papers?

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- Liberals  $\approx$  New York Times, conservatives  $\approx$  Wall Street Journal

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Our case: British newspapers switching their endorsements

 Some news papers endorsing Tories in 1992 switched to Labour in 1997

• Can newspaper endorsements change voters' minds?

Why not compare vote choice of readers of different papers?

- Problem: readers choose papers based on their previous beliefs
- Liberals  $\approx$  New York Times, conservatives  $\approx$  Wall Street Journal

Our case: British newspapers switching their endorsements

- Some news papers endorsing Tories in 1992 switched to Labour in 1997
- Treated group:: readers of Tory -> Labour papers
- Control group:: readers of papers who didn't switch

# Codebook for newspapers data

Variable	Description
to_labour	Read a newspaper that switched endorsement to Labour between 1992 and 1997 (1=yes, $0=no$ )
vote_lab_92	Did respondent vote for Labour in 1992 election (1=yes, 0=no)?
vote_lab_97	Did respondent vote for Labour in 1997 election $(1=yes, 0=no)$ ?
age	Age of respondent
male	Does the respondent identify as Male $(1=yes, 0=no)$
parent_labour	Does the respondent' identify as 's parents vote for Labour (1=yes, 0=no)
work_class	Does the responedent identify as working class (1=yes, 0=no)?

#### library(tidyverse) library(TPDdata) newspapers

```
## # A tibble: 1,593 x 7
     to_labour vote_lab_92 vote_lab_97
                                             age male parent_labour work_class
##
##
         <db1>
                     <dbl>
                                 <dbl> <hvn_lbll> <dbl>
                                                              <db1>
                                                                          <dbl>
## 1
             0
                                              33
                                                     0
                                              51
                                                     0
## 3
                                              46
                                                     0
                                              45
## 5
                                              29
                                              47
                                              34
                                              31
                                              24
## 10
                                              48
                                                     0
## # ... with 1,583 more rows
```

Example of an observational study:

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**External validity**: can the conclusions/estimated effects be generalized beyond this study?

- RCTs weaker here because often very expensive to conduct on representative
- Observational studies often have larger/more representative samples that improve external validity

 $\begin{tabular}{ll} \textbf{Confounder}: pre-treatment variable affecting both treatment \& the outcome \\ \end{tabular}$ 

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- Leftists (X) more likely to read newspapers switching to Labour (T)
- Leftists (X) also more likely to vote for Labour (Y)

**Confounder**: pre-treatment variable affecting both treatment & the outcome

- Leftists (X) more likely to read newspapers switching to Labour (T)
- Leftists (X) also more likely to vote for Labour (Y)

Counfounding bias in the estimated SATE due to these differences

**Confounder**: pre-treatment variable affecting both treatment & the outcome

- Leftists (X) more likely to read newspapers switching to Labour (T)
- Leftists (X) also more likely to vote for Labour (Y)

Counfounding bias in the estimated SATE due to these differences

- $\overline{Y}_{control}$  not a good proxy for  $Y_i(0)$  in treated group
- one type: **selection bias** from self-selection into treatment

How can we find a good comparison group?

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Depends on the data we have available

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Three general types of observational study **research designs**:

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1 Cross-sectional design: compare outcomes treated and control unites at one point in time

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- 2 Before-and-after design: compare outcomes before and after a unit has been treated, but need over-time data on treated group

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Three general types of observational study **research designs**:

- 1 Cross-sectional design: compare outcomes treated and control unites at one point in time
- 2 Before-and-after design: compare outcomes before and after a unit has been treated, but need over-time data on treated group
- 3 Difference-in-differences design: use before/after information for the treated and control group; need over-time on treated & control group

# Cross-sectional design

Compare treatment and control groups after treatment happens

 Readers of switching papers vs. readers of non-switching papers in 1997

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Compare treatment and control groups after treatment happens

 Readers of switching papers vs. readers of non-switching papers in 1997

Treatment & control groups assumed identical on average as in RCT

Sometimes called unconfoundedness or as-if randomized

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Compare treatment and control groups after treatment happens

 Readers of switching papers vs. readers of non-switching papers in 1997

Treatment & control groups assumed identical on average as in RCT

Sometimes called unconfoundedness or as-if randomized

Cross-section comparison estimate:

$$\overline{Y}_{treated}^{after} - \overline{Y}_{control}^{after}$$

Could there be counfounders?

## Cross-sectional design in R

```
switched <- newspapers |>
 filter(to labour ==1) |>
  summarize(mean(vote_lab 97))
no_change <- newspapers |>
 filter(to_labour == 0) |>
  summarize(mean(vote lab 97))
switched - no change
##
    mean(vote_lab_97)
            0.1404826
## 1
```

**Statistical control**: adjust for confounders using statistical procedures

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- Compare treated and control groups within levels of a confounder
- Remaining effect can't be due to the confounder

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One type of statistical control: subclassfication

- Compare treated and control groups within levels of a confounder
- Remaining effect can't be due to the confounder

Treat to inference: we can only control for observed variables  $\approx$  threat of **unmeasured confounding** 

### Statistical control in R

```
newspapers |>
  group_by(parent_labour, to_labour) |>
  summarize(avg_vote = mean(vote_lab_97)) |>
  pivot_wider(
    names_from = to_labour,
    values_from = avg_vote
) |>
  mutate(diff_by_parent = `1` - `0`)
```

## `summarise()` has grouped output by 'parent\_labour'. You

Compare readers of party-switching newspapers before & after switch

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Advantage: all person-specific features held fixed

• comparing within a person over time

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Before-and-after estimate:

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Threat to inference: time-varying counfounders

Compare readers of party-switching newspapers before & after switch

Advantage: all person-specific features held fixed

comparing within a person over time

Before-and-after estimate:

$$\overline{Y}_{treated}^{after} - \overline{Y}_{treated}^{before}$$

Threat to inference: **time-varying counfounders** 

 time trend: Labour just did better overall in 1997 compared to 1992

## Before and after in R

```
newspapers |>
 mutate(
   vote_change = vote_lab_97 - vote_lab_92
  ) |>
  summarize(avg_change = mean(vote_change))
## # A tibble: 1 x 1
## avg_change
       <dbl>
##
## 1 0.119
```

Key idea: use the before-and-after difference of **control group** to infer what would have happened to **treatment group** without treatment

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DiD estimate:

$$\underbrace{(\overline{Y}_{treated}^{after} - \overline{Y}_{treated}^{before})}_{trend in treated group} - \underbrace{(\overline{Y}_{control}^{after} - \overline{Y}_{control}^{before})}_{trend in control group}$$

Key idea: use the before-and-after difference of **control group** to infer what would have happened to **treatment group** without treatment

DiD estimate:

$$\underbrace{\left(\overline{Y}_{\textit{treated}}^{\textit{after}} - \overline{Y}_{\textit{treated}}^{\textit{before}}\right)}_{\textit{trend in treated group}} - \underbrace{\left(\overline{Y}_{\textit{control}}^{\textit{after}} - \overline{Y}_{\textit{control}}^{\textit{before}}\right)}_{\textit{trend in control group}}$$

Change in treated group above and beyond the change in control group

Key idea: use the before-and-after difference of **control group** to infer what would have happened to **treatment group** without treatment

DiD estimate:

$$\underbrace{\left(\overline{Y}_{treated}^{after} - \overline{Y}_{treated}^{before}\right)}_{trend in treated group} - \underbrace{\left(\overline{Y}_{control}^{after} - \overline{Y}_{control}^{before}\right)}_{trend in control group}$$

Change in treated group above and beyond the change in control group

### Parallel time trend assumption

- Changes in vote of readers of non-switching papers roughly the same as changes that readers of switching papers would have been if they read non-switching papers
- Threat to inference: non-parallel trends

### Difference-in-differences in R

```
newspapers |>
 mutate(
   vote_change = vote_lab_97 - vote_lab_92,
   to_labour = if_else(to_labour ==1, "switched", "unswitched")
 ) |>
 group_by(to_labour) |>
 summarize(avg_change = mean(vote_change)) |>
 pivot_wider(
   names_from = to_labour,
   values from = avg change
 ) |>
 mutate(DID = switched - unswitched)
## # A tibble: 1 x 3
## switched unswitched DID
## <dbl> <dbl> <dbl>
## 1 0.190 0.110 0.0796
```

### 1. Cross-sectional comparison

• Compare treated units with control unites after treatment

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- Assumption: treated and control units are comparable

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Compare the same units before and after treatment

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### 2. Before-and-after comparison

- Compare the same units before and after treatment
- Assumption: no time-varying confounding

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- Compare treated units with control unites after treatment
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- Compare the same units before and after treatment
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#### 3. Differences-in-differences

• Assumption: parallel trends assumptions

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- Assumption: parallel trends assumptions
- Under this assumption, it accounts for unit-specific and time-varying confounding

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All rely on assumptions that can't be verified to handle confounding

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All rely on assumptions that can't be verified to handle confounding

RCTs handle confounding by design (gold standard)