• | num "*" OptSign num

1. Grammatiken – Grundbegriffe

```
a)
VT(G) = { "DATA", ", ", ", ", "*", id, num, str, "+", "-", "(", ")", "=", expr } | = 13
| VN(G) = { DataDecl, DataDeclRest, DataNameList, DataValueList, DataName, DataNameList,
DataDoList, DataValue, DataDoListRest } | = 9
b)
shortest:
   • DATA id / num /
   • DATA id / str /
   • DATA id / id /
c)
Direkt rekursiv:
   • DataDeclRest: links
   • DataNameList: rechts
   • DataValueList: links
   • DataDoList: zentral
   • DataDoListRest: links
Indirekt rekursiv:
   • DataDoList => DataDoListRest: zentral
   • DataDoListRest => DataDoList: zentral
d)
DataStat -> "Data" DataDecl DataDeclRest.
DataDeclRest -> ε | DataDeclRest DataDecl | DataDeclRest ", " DataDecl .
DataDecl -> DataNameList "/" DataValueList "/".
DataNameList -> DataName | DataName ", " DataNameList .
DataName -> id | DataDoList .
DataValueList -> DataValue | DataValueList ", " DataValue .
DataValue -> OptSign num | str | id
   • | num "*" id
```

- | num "*" str
- | id "*" id
- | id "*" OptSign num
- | id "*" str
- •

OptSign -> ϵ | "+" | "+".

DataDoList -> "(" DataDoList DataDoListRest ")"

- | "(" id "(" IdList ")" DataDoListRest ")"
- . IdList -> id | IdList ", " id .

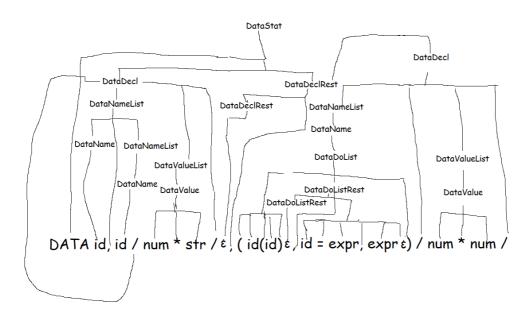
DataDoListRest -> ε

- | DataDoListRest ", " DataDoList
- | DataDoListRest ", " id "(" ExprList ")"
- | DataDoListRest ", " id "=" expr ", " expr
- | DataDoListRest ", " id "=" expr ", " expr, expr
- •

ExprList -> expr | ExprList "," expr .

EBNF ist lesbarer, da man mit weniger Alternativen durch Verwendung von "[" und "]" benötigt kann und keine Rekursion mit NTs für das mehrfache Vorkommen von [Terminal-]Symbolen verwenden muss.

e)



Für diesen Satz gib es nur einen Syntaxbaum, da es bei jeder Regel nur eine Alternative gibt, die zu diesem gegeben Satz führt.

2. Konstruktion einer Grammatik

Regelsystem

S -> OptSign LeadingDigit MiddleDigits UnevenNaturalDigit | OptSign UnevenNaturalDigit . // man könnte auch OptSign weglassen und dafür 4 weitere Alternativen in "S" hinzufügen

OptSign -> ϵ | + | - .

MiddleDigits -> ϵ | 0 MiddleDigits | LeadingDigit MiddleDigits .

UnevenNaturalDigit -> 1 | 3 | 5 | 7 | 9.

LeadingDigit -> UnevenNaturalDigit | 2 | 4 | 6 | 8.

EBNF

 $S = [\ + \ | \ - \] \ [\ (1|2|3|4|5|6|7|8|9) \ \{ \ (0|1|2|3|4|5|6|7|8|9) \ \} \] \ (1|3|5|7|9) \ .$

3. Oo-Implementierung von Grammatiken

No changes made to existing code. I used C++20.

a)

main.cpp

(next page)

```
Grammar* newEpsilonFreeGrammarOf(Grammar* g) {
     // step 1
     VNt deletable = g->deletableNTs();
     // step 2
     // use symbolpool to get instances by name
     // (symbols from initial creation are still stored in SymbolPoolData)
     SymbolPool sp{};
     GrammarBuilder gb{ g->root }; // reuse old root for now
     // for each rule
     // c++20 structured binding
    for (const auto& [ NTSymbol *const & nt, const SequenceSet & sequenceSet] : g->rules)
         // iterate over old sequence set
        for (const Sequence* seq : sequenceSet)
             // begone epsilon
             if (seq->isEpsilon()) continue;
             // add copy
             gb.addRule(nt, new Sequence(*seq));
             // evaluate which indices of current sequence are deletable NTs
             std::vector<int> deletableNTindices{};
             for (int i = 0; i < seq->size(); i++) {
                 Symbol* currSy = seq->at(_Pos:i);
                 if (currSy->isNT() &&
                     deletable.contains(dynamic_cast<NTSymbol*>(currSy))) {
                     deletableNTindices.push_back(_Val: i);
             }
             // add the current sequence with every possible combination
             // of not including NTs in deletableNTindices
             // 2^n(-1) iterations
             for (int i = 0; i < 1 << deletableNTindices.size(); ++i) {
                 Sequence* copy = new Sequence(*seq);
                 for (int j = deletableNTindices.size() - 1; j >= 0; --j) {
                     // generate all possible combinations
                     // of indices in deletableNTindices
                     int symbolsRemoved = 0;
                     if (((1 << j) \& i) > 0) {
                         copy->removeSymbolAt(deletableNTindicesidx:[j - symbolsRemoved]);
                         symbolsRemoved += 1;
                     }
                 // don't add empty alternatives
                 // also duplicates are ignored
                 if (!copy->isEpsilon()) gb.addRule(nt, seq:copy);
                 else delete copy;
        }
     }
     // step 3
     if (deletable.contains(sy:g->root)) {
         // add S' (or rather name of original root node + ')
        NTSymbol* newRoot = sp.ntSymbol(g->root->name + "'");
        gb.addRule(nt:newRoot, seqs:{ new Sequence({q->root}), new Sequence() /* eps */ });
        gb.setNewRoot(newRoot);
     return gb.buildGrammar();
```

Testcode:

```
gb2 = new GrammarBuilder(string("G1.txt"));
    g2 = gb2->buildGrammar();
    Grammar* epsilonFree = newEpsilonFreeGrammarOf(g2);

    cout << "grammar from text file:" << endl << *g2 << endl;
    cout << "newEpsilonFreeGrammarOf(g2):" << endl << *epsilonFree << endl;
    delete epsilonFree;</pre>
```

Result:

```
START Main
symbol pool: 0 terminals and 0 nonterminals
  terminals
  nonterminals =
TESTCASE 4
grammar from text file:
G(S):
S -> A B C
A -> eps | B B
B -> C C | a
VNt = { A, B, C, S }, deletable: { A, B, C, S }
VT = { a, b }
newEpsilonFreeGrammarOf(g2):
G(S'):
S' -> eps | S
S -> A | A B | A B C | A C | B | B C | C
A -> B | B B
B -> C | C C | a
 -> A | A A | b
VNt = { A, B, C, S, S' }, deletable: { S' }
VT = { a, b }
symbol pool: 2 terminals and 5 nonterminals
  terminals
             = { a, b }
  nonterminals = { C, S, A, B, S' }
elapsed time: 0.021
END Main
```

b) and also c)

main.cpp

```
void languageOfRecursive(
    Language* language,
    NTSymbol* const originalNTSymbol,
    const RulesMap& rules,
    Sequence* currSentence,
    int maxLen
1) {
    int i = 0;
    while (i < currSentence->size() && (*currSentence)[i]->isT()) {
        i++;
    // only tSymbols left?
    if (i == currSentence->size()) {
         if (currSentence->size() <= maxLen)
             language->addSentence(currSentence);
            delete currSentence;
        return;
    NTSymbol* ntSy = dynamic_cast<NTSymbol*>((*currSentence)[i]);
    // do same stuff recursive for all alternatives substituted
    for (Sequence * alternative : rules[ntSy])
         // this alternative makes the sentence too long - skip
         if (currSentence->length() + alternative->length() - 1 > maxLen) continue;
         // ignore this alternative if it does not contribute to the language directly
         if (alternative->length() == 1 && (*alternative)[0]->isNT()
            && *originalNTSymbol == *(*alternative)[0]) continue;
         Sequence* derivedSentence = new Sequence(*currSentence);
         derivedSentence->removeSymbolAt(idx:i);
         derivedSentence->append(seq:alternative);
         languageOfRecursive(language, originalNTSymbol: ntSy, rules, currSentence: derivedSentence, maxLen);
    delete currSentence;
}
¡Language* languageOf(const Grammar* g, int maxLen) {
    Language* language = new Language(maxLen);
    Sequence* s = new Sequence(g->root);
    languageOfRecursive(language, originalNTSymbol: g->root, g->rules, currSentence: s, maxLen);
    return language;
}
```

Language.h

(next page)

```
∃// Language.h:
                                                            SWE, 2022
  // --
  // Lengwidsch
∃#ifndef Language_h
  #define Language_h
±#include <vector>
  #include <set>
 #include <iostream>
 #include "ObjectCounter.h"
 #include "SequenceStuff.h"
ḋclass Language :
      private ObjectCounter<Language> {
      friend std::ostream& operator <<(std::ostream& os, const Language& language);
      private:
          SequenceSet sentences{};
          int maxLength;
      public:
         Language(int maxLength);
          Sequence& at(int i) const;
          void addSentence(Sequence* s);
          bool hasSentence(Sequence* s) const;
 };
  #endif
□// end of Language.h
 //========
```

Language.cpp

(next page)

```
SWE, 2022
  // -
  // Lengwidsch
  //======
≡#include <exception>
  #include "Language.h"
  #include "SymbolStuff.h"
  #include "SequenceStuff.h"
std::ostream& operator <<(std::ostream& os, const Language& language) {</pre>
      os << "L(G(S)): maxLength=" << language.maxLength << " {\n";
      for (const Sequence* sentence : language.sentences) {
          os << *sentence << "\n";
      os << "}";
      return os;
  }
Sequence& Language::at(int idx) const {
      if (idx >= sentences.size() || idx < 0)
          throw std::invalid_argument("invalid index");
      auto SequenceSet::...onst_iterator it = sentences.cbegin();
      std::advance(& _Where: it, _Off: idx);
      return **it;
  }
_Language::Language(int maxLength)
      : maxLength{maxLength} {
}

    □void Language::addSentence(Sequence* s) {
      if (hasSentence(s)) {
          delete s;
          return;
      sentences.insert(_Val:s);
bool Language::hasSentence(Sequence* s) const {
      for (const Symbol* sy : *s) {
          if (sy->isNT())
               throw std::runtime_error("NT found in sentence");
      }
      for (const Sequence* curr : sentences) {
          // Sequence already has equality comparison (op ==) implemented
          if (*curr == *s) {
              return true;
          }
      return false;

□ // end of Language.h
```

Testcode:

```
=#elif TESTCASE == 5
         gb2 = new GrammarBuilder(string("G23.txt"));
         g2 = gb2->buildGrammar();
         Grammar* epsilonFree = newEpsilonFreeGrammarOf(g2);
         Language* languageG2 = languageOf(g:epsilonFree, maxLen:6);
         Sequence& s1 = languageG2->at(i:1);
         Sequence madeUpSequence{
             sp->symbolFor(name: "a"),
              sp->symbolFor(name: "a"),
              sp->symbolFor(name: "b"),
              sp->symbolFor(name: "b")
         };
         Sequence madeUpSequenceNotContained{
              sp->symbolFor(name: "a"),
              sp->symbolFor(name: "b"),
              sp->symbolFor(name: "b"),
              sp->symbolFor(name: "b")
         };
         cout << "grammar from text file:" << endl << *g2 << endl;
         cout << "newEpsilonFreeGrammarOf(g2):" << endl << *epsilonFree << endl;</pre>
         cout << "language(g2):" << endl << *languageG2 << endl;</pre>
         cout << "s1: " << s1 << endl;
         cout << "languageG2.hasSentence(s1): " << boolalpha</pre>
              << languageG2->hasSentence(&s1) << endl;
         cout << "madeUpSequence: " << madeUpSequence << endl;</pre>
         cout << "languageG2.hasSentence(madeUpSequence): " << boolalpha</pre>
              << languageG2->hasSentence(&madeUpSequence) << endl;
         cout << "madeUpSequence: " << madeUpSequenceNotContained << endl;</pre>
         cout << "languageG2.hasSentence(madeUpSequenceNotContained): " << boolalpha</pre>
              << languageG2->hasSentence(&madeUpSequenceNotContained) << endl;</pre>
         delete epsilonFree;
         delete languageG2;
=#else // none of the TESTCASEs above
```

Result:

```
Microsoft Visual Studio Debug Console

START Main

symbol pool: 0 terminals and 0 nonterminals

terminals = { }

nonterminals = { }

TESTCASE 5

grammar from text file:

G(S):

S -> a B | b A

B -> a B B | b | b S

A -> a | a S | b A A

---

VNt = { A, B, S }, deletable: { }

VT = { a, b }
```

```
newEpsilonFreeGrammarOf(g2):
   G(S):
   S -> a B | b A
  B -> a B B | b | b S
eam A->a|aS|bAA
   VNt = { A, B, S }, deletable: { }
uenVT = \{a, b\}
:h;
   language(g2):
   L(G(S)): maxLength=6 {
 ma a a b b a b
   a b
(inaabbba
encaababb
encaabb
   aabbab
   aabbba
   aaabbb
   abaabb
   abba
   abbaab
ldeababba
___abbaba
   ababab
   abab
   baabba
   b a
   abbbaa
   baaabb
   baab
   baabab
   baba
   babaab
   bbaa
   bbaaba
   bbabaa
   babbaa
   bababa
   bbaaab
   bbaaba
tefabbaaab
\Sysbbbaaa
\Sys<sup>*</sup>}
\Syss1: a b
\SyslanguageG2.hasSentence(s1): true
\SysmadeUpSequence: a a b b
\Sys languageG2.hasSentence(madeUpSequence): true
\SysmadeUpSequence: a b b b
de 0languageG2.hasSentence(madeUpSequenceNotContained): false
\Sys
\Sys
\Sys symbol pool: 2 terminals and 3 nonterminals
    terminals
                = { a, b }
e 0
    nonterminals = { S, A, B }
e 0
ted
   elapsed time: 0.024
   END Main
```

Man kann erkennen, dass die länge der generieten Sätze immer gerade ist und jeder Satz gleich viele a wie b hat.

Ja kann man. Jedes NT B terminiert in genau ein b und jedes NT A terminiert in genau ein a. Wenn die Ableitung mit S -> a B anfängt, dann befindet sich schon ein a im Satz und das B wird schlussendlich zu einem b. Bei der dritten Alternative von B kommen ein a sowie zwei B hinzu. Die Ableitung S -> a B -> a a B B halt 2 a und 2 B und wir wissen bereits, dass jedes B in genau ein B terminiert oder es geschieht wieder die gleiche Ableitung von B -> a B B, wodurch effektiv nur 1 a und 1 B hinzukommen. Wenn schlussendlich alle B in b abgeleitet werden, gibt es gleich viele a wie b. Das gleiche gilt auch für die Ableitung B -> b S, da wie bei der ersten Alternative ein weiteres B mit b ersetzt wird und ein weiterer Satz S dazukommt, der später auch wieder in gleich viele a und B abgeleitet werden kann und jedes B wieder in ein b abgeleitet wird oder in ein b und ein S. Das gleiche gilt auch in die andere Richtung S -> a B, da die Regeln im NTSymbol B nur b und A mit a und B getauscht haben.