

Let C = number of cloud symbols
 R = number of ripple symbols
 u = number of unresolved symbols
 $P_{c,r,u}(c,r,u)$ = probability of being in state (c,r,u)
 m = input block length

Assume we have collected $m+\phi$ coded symbols. If we look at the probability-generating function of $P_{c,r,u}$ we see that

$$D_u(x,y) = \sum_{c=0}^{\phi+m} \sum_{r=1}^{\phi+m} P_{c,r,u} x^c y^{r-1} = \sum_{c=0}^{\phi+m} \sum_{r=0}^{\phi+m} P_{c,r,u} x^c y^{r-1} - \sum_{c=0}^{\phi+m} P_{c,r,u}(c,0,u) x^c y^{-1}$$

$$\Rightarrow D_u(1,1) = \sum_{c=0}^{\phi+m} \sum_{r=0}^{\phi+m} P_{c,r,u} - \sum_{c=0}^{\phi+m} P_{c,r,u}(c,0,u)$$

$$= 1 - \Pr\{\text{Decoding failure when } u \text{ symbols are unresolved}\}$$

$$\Rightarrow P_F(\phi) \triangleq \sum_{u=1}^{m+\phi} \Pr\{\text{Decoding failure when } u \text{ symbols are unresolved}\}$$

$$= \sum_{u=1}^{m+\phi} (1 - D_u(1,1))$$

Find by numerically evaluating expression in Theorem 1 in Karp2004.

Peeling decoder failure probability when
 $m+\phi$ symbols have been collected

