

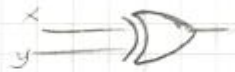
$\bar{E} \text{ XOR} = \text{XOR}$

Gate

Equivalentence = EXNOR = EXV

x	y	f = x ⊕ y
0	0	0
1	0	1
2	1	1
3	1	0

$$f = x \cdot \bar{y} + \bar{x} \cdot y = x \oplus y$$

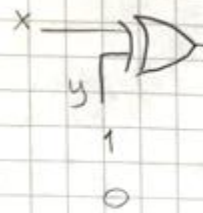


x	y	f = x ⊙ y
0	0	1
1	0	0
2	1	0
3	1	1



$$f = x \odot y = x \cdot y + \bar{x} \cdot \bar{y}$$

Controlled Logic level conversion



$$f = x \oplus y = x \cdot \bar{y} + \bar{x} \cdot y$$

\bar{x} Conversion Mode $\leftarrow 0$

x Transfer Mode $\leftarrow 1$



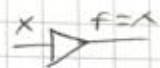
$$f = x \cdot y + x \cdot \bar{y}$$

$$f = \bar{x}$$

$$f = x$$

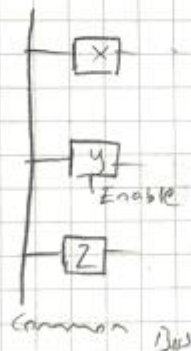
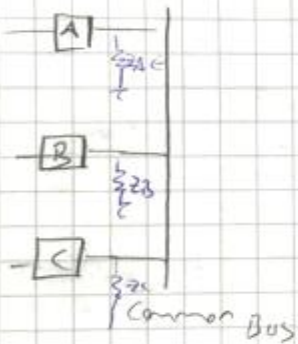
Buffer

x	y
0	0
1	1



signalle in serieller digitalcode
ideal hale geführt.

Tristate Gates



$$\frac{1}{Z_{in}} = \frac{1}{Z_X} + \frac{1}{Z_Y} + \frac{1}{Z_Z}$$



Tristate Buffer



E	F
0	X
1	H/Z

Yükser
empedans

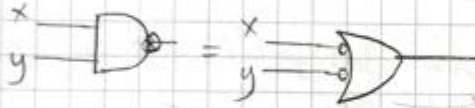
E	F
0	H/Z
1	X

CONJUNATE GATE SYMBOL (ALTERNATE GATE SYMBOL)

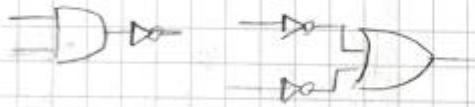
De Morgan

$$(\overline{x \cdot y}) = (\bar{x} + \bar{y})$$

$$(x \cdot y)(L) = (\bar{x} + \bar{y})(H)$$



→ Bu bir
alternat
gate
symbol'dur



Standard Gate
Symbol

↓
Alternate
Gate Symbol

De Morgan

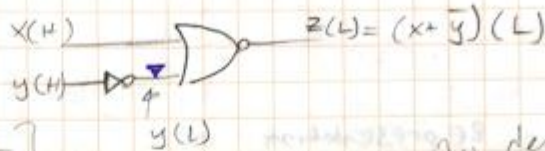
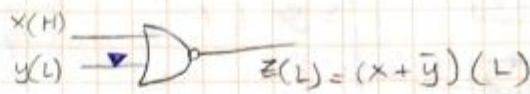
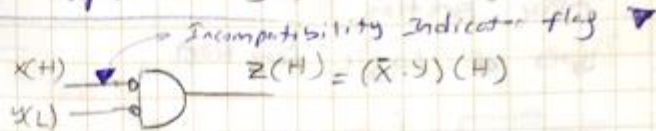
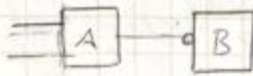
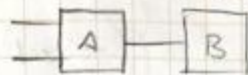
$$\overline{x + y} = \bar{x} \cdot \bar{y}$$



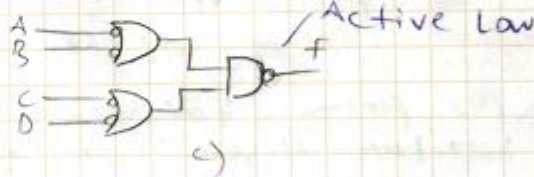
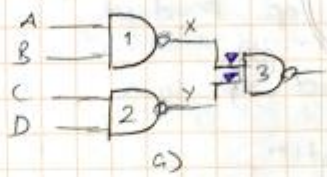
Standard

Alternate

Logic Level Incompatibility (Last series uyum sağlanmadı)



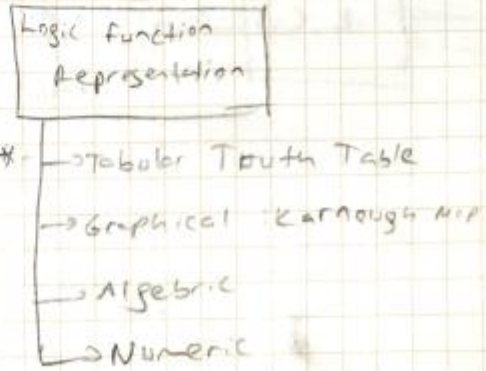
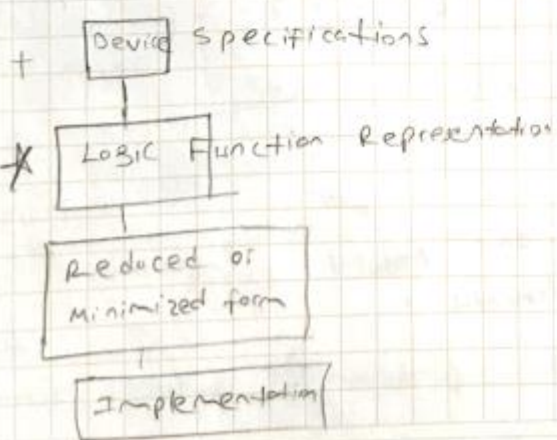
dec	A	B	C	D	f
0	0	0	0	0	0
1	0	0	0	1	0
2	0	0	1	0	0
3	0	0	1	1	1
4	0	1	0	0	0
5	0	1	0	1	0
6	0	1	1	0	0
7	0	1	1	1	1
8	1	0	0	0	0
9	1	0	0	1	0
10	1	0	1	0	0
11	1	0	1	1	1
12	1	1	0	0	1
13	1	1	0	1	1
14	1	1	1	0	1
15	1	1	1	1	1



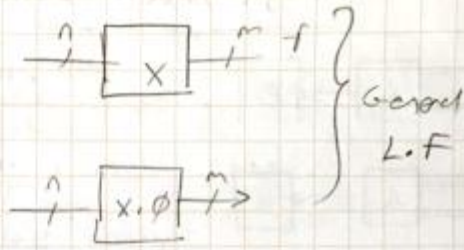
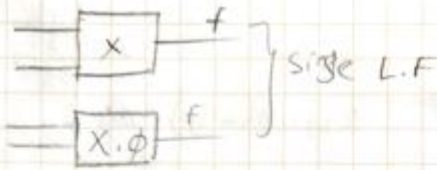
Bu derledim }
 Gelir (dışardan)
 farket olma
 sonun dışından
 derledim olma

Alternative semboller kullanarak logic uygun şekilde gösterilebilir.

LOGIC FUNCTION



Logic function Types of Logic functions



Algebraic Representation

- SOP Sum of Product
- POS Product of Sum

SOP Representation

Product Term
Minterm

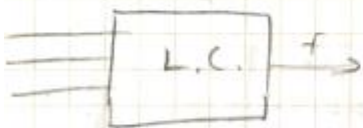
Algebraic Representation

SOP \rightarrow SOP form fonksiyonun Logic 1 değerini aldy, nolukla ilistin bir gosterir.

POS \rightarrow POS form fonksiyonun Logic 0 değerini aldy, nolukla ilistin bir gosterir.

SOP presentation:

- A, B, C Literal



- $AB, AC, BC, \bar{A}B, A\bar{C}, \bar{B}\bar{C}$ } Product Term
- $ABC, \bar{A}BC, A\bar{B}C, \dots, \bar{A}\bar{B}\bar{C}$ }

Minterm \rightarrow Girdilerin birleştirmesi sonucu minterm değeri

Canonical Product term
Fundamental "

Minterm = canonical product term = fundamental product term

minterm code

Uncomplemented variable x logic 1

Complemented variable \bar{x} logic 0

$$m_i = \bar{A}BC = m_3$$

$$(011) \rightarrow 3$$

↓
Canonical SOP form → Eğer bütün terimlerinin tümü minterm ise buna denir.

örnek

$$f(A,B,C) = \bar{A}\bar{B}\bar{C} + A\bar{B}\bar{C} + \bar{A}BC + ABC$$

Canonical SOP form $(010) + (110) + (011) + (111)$

↓	↓	↓	↓
2	6	3	7
m_2	m_6	m_3	m_7

$$\text{Numerical Representation} = m_2 + m_3 + m_6 + m_7$$

$$= \sum m(2, 3, 6, 7)$$

Logic functions gösteren birer sistemdir

Minterm	BC	A	B	C	
m_0	0	0	0	0	0
m_1	1	0	0	1	0
m_2	2	0	1	0	1
m_3	3	0	1	1	1
m_4	4	1	0	0	0
m_5	5	1	0	1	0
m_6	6	1	1	0	1
m_7	7	1	1	1	1

$$f = \sum m(2, 3, 6, 7)$$

$$f = \bar{A}\bar{B}\bar{C} + \bar{A}B\bar{C} + A\bar{B}\bar{C} + ABC$$

Bu üç gosterim de aynı şeyi ifade ederler ve aynı doğruluk değeri verir.

for generating the Canonical SOP form

$$f(A,B,C) = A + \bar{B}C + \bar{A}BC \quad \text{Canonical form}$$

$$1) x + \bar{x} = 1$$

$$f(A,B,C) = A(B + \bar{B})(C + \bar{C}) + (A + \bar{A})\bar{B}C + \bar{A}BC$$

2) Distributive

$$f(A, B, C) = ABC + AB\bar{C} + A\bar{B}C + A\bar{B}\bar{C} + A\bar{B}C + A\bar{B}C + A\bar{B}C$$

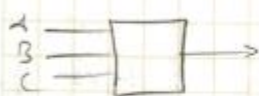
3) $X + X = X$

$$f = ABC + AB\bar{C} + A\bar{B}C + A\bar{B}\bar{C} + \bar{A}B\bar{C} + \bar{A}BC$$

$$f = \sum m(7, 6, 5, 4, 1, 3)$$

$$f = \sum m(1, 3, 4, 5, 6, 7)$$

POS (Product of Sum) Representation



• $A, B, C, \bar{A}, \dots, \bar{C}$ Literal

• $A+B, A+C, B+C, \bar{A}+\bar{B}, \dots, \bar{B}+\bar{C}$

• $ABC, A+\bar{B}+\bar{C}, \dots, \bar{A}+\bar{B}+\bar{C}$ } Sum Term / Maxterm

Sum Term

Maxterm $M_i \Rightarrow$ Maxterm code

Complemented Variable \bar{x} logic 1 } $\bar{A} + \bar{B} + C + \bar{D} = M_{13}$

Uncomplemented Variable x logic 0 } $1 \ 1 \ 0 \ 1$
13

$$\bar{m}_i = M_i$$

$$m_5 = A\bar{B}C$$

$$\bar{M}_i = m_i$$

$$\bar{m}_5 = \bar{A}\bar{B}C = \bar{A} + \bar{B} + \bar{C} \rightarrow M_5$$

Canonical POS form \rightarrow Boolean term (or) Maxterm also

$$f(A, B, C) = (A+B+\bar{C}) (\bar{A}+\bar{B}+\bar{C}) (\bar{A}+B+C) (A+B+C)$$

$$0 \ 0 \ 1 \quad 1 \ 0 \ 1 \quad 1 \ 0 \ 0 \quad 0 \ 0 \ 0$$

M_1

M_5

M_4

M_0

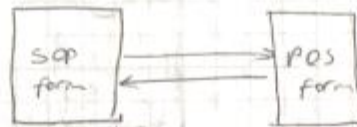
$$= \prod M(0, 1, 4, 5)$$

↓
decimal
number

OSOW

Dec	x	y	z	f
0	0	0	0	0
1	0	0	1	0
2	0	1	0	1
3	0	1	1	1
4	1	0	0	0
5	1	0	1	0
6	1	1	0	1
7	1	1	1	1

Conversion Between POS and SOP forms



1) from SOP to POS form

$$f(x, y, z) = x\bar{z} + \bar{x}y + \bar{y}z$$

De Morgan theorem:

$$f(x, y, z) = x\bar{z} + \bar{x}y + \bar{y}z \Rightarrow f^d(x, y, z) = (\bar{x} + \bar{z}) \cdot (\bar{x} + \bar{y}) \cdot (y + \bar{z})$$

$$f^d(x, y, z) = \bar{x}\bar{y}\bar{z} + x y z$$

$$f^d(x, y, z) \cdot f(x, y, z) = (\bar{x} + \bar{y} + \bar{z}) \cdot (x + y + z)$$

2) from POS to SOP form

$$f(x, y, z) = (x + y)(\bar{x} + \bar{z})(x + \bar{y} + \bar{z})$$

$$= x\bar{z} + \bar{x}y + yz$$