

## CSE 414 - Database Assignment 2

Seyda Nur DEMIR  
12.10.24 002

In this assignment you have to use the techniques mentioned in our lecture and slides. Any other technique will not be graded. You have to write down the answers to a paper and upload the photo of the paper to moodle.

1- Given  $R (A_1, A_2, A_3, A_4, A_5, A_6, A_7, A_8)$  and

$$F = \{ A_1 A_3 \rightarrow A_7, A_4 \rightarrow A_5 A_7, A_2 A_3 \rightarrow A_4, A_3 A_7 \rightarrow A_2 A_4, A_1 A_3 A_4 \rightarrow A_7, A_3 A_5 \rightarrow A_1 A_7 \}$$

After finding extraneous attributes and eliminating them and redundant functional dependencies, find the canonical cover of  $F$ . You have to define all the steps to get the canonical cover. Just writing the canonical cover without the steps will not be graded.

- Split the functional dependencies such that contain the single attribute

$$\begin{aligned} & \bullet A_1, A_3 \rightarrow A_7 \quad \bullet A_4 \rightarrow A_5 \quad \bullet A_4 \rightarrow A_7 \quad \bullet A_2 \rightarrow A_3 \quad \bullet A_3, A_7 \rightarrow A_2 \quad \bullet A_3 A_7 \rightarrow A_4 \\ & \bullet A_1, A_3, A_4 \rightarrow A_2 \quad \bullet A_3, A_5 \rightarrow A_1 \quad \bullet A_3, A_5 \rightarrow A_7 \end{aligned}$$

No redundant functional dependencies.

Find the redundant attributes on left hand side

$$\begin{aligned} & \bullet (A_1, A_3)^+ \rightarrow A_1, A_3, A_7, A_2 \\ & A_1, A_3, A_4 \rightarrow A_2 \text{ can be reduced as } A_1 A_3 \rightarrow A_2 \end{aligned}$$

And then canonical form is

$$\begin{aligned} & A_1 A_3 \rightarrow A_7, A_4 \rightarrow A_5, A_4 \rightarrow A_7, A_2 A_3 \rightarrow A_4, A_3 A_7 \rightarrow A_2, A_3 A_7 \rightarrow A_4 \\ & A_1 A_3 \rightarrow A_2, A_3 A_5 \rightarrow A_1, A_3 A_5 \rightarrow A_7 \end{aligned}$$

2- Given  $R(A_1, A_2, A_3, A_4, A_5, A_6)$  and

$A_1 A_2 \rightarrow A_3$   $A_1 A_4 \rightarrow A_5$   $A_2 \rightarrow A_4$   $A_1 A_6 \rightarrow A_2$

Find the  $\{A_1, A_2\}^+$  and  $\{A_1, A_6\}^+$

Why do we need closure? Explain using examples if necessary.

$$\bullet \{A_1, A_2\}^+ = \{A_1 A_2 A_3 A_4 A_5\} \text{ ( } A_1 A_2 \text{ } \\ \text{( } A_1 A_2 \rightarrow A_3, A_2 \rightarrow A_4, A_1 A_4 \rightarrow A_5 \text{ )}$$

$$\{A_1, A_6\}^+ = \{A_1 A_6 A_2 A_3 A_4 A_5\} \\ \text{( } A_1 A_6 \rightarrow A_2, A_2 \rightarrow A_4, A_1 A_4 \rightarrow A_5, A_1 A_2 \rightarrow A_3 \text{ )}$$

- The main purpose of the closure is the to find the all possible attributes are derived from a given set the functional dependency of a given set can find using closure. It has also importance to determine the key of the dataset is the candidate key or not and using closure find all attributes that functionally dependency on the other attributes.

$R(A, B, C, D)$   $\{A \rightarrow B, B \rightarrow C, C \rightarrow D\}$

$$\{A\}^+ = \{A B C D\}$$

A derived all functionality that direct or indirect depend on A.

3- Given  $R(A1, A2, A3, A4)$

$$F = \{A1 \rightarrow A2, A2 \rightarrow A3\}$$

$A1$  and  $A2$  are superkeys.

Is  $R$  in BCNF? Give the proof.

Suppose that we decomposed  $R$  into  $R1(A1A2)$ ,  $R2(A1A3)$ ,  $R3(A1A4)$ .

Are each of the relations in BCNF? Give the proof.

Is the decomposition dependency preserving? Give the proof.

- Let  $R$  be relational schema.  $X \rightarrow Y$  be only non-trivial functional dependency over  $R$  is BCNF if  $X$  is candidate key or superkey.  
If  $A1$  and  $A2$  are superkey the relation  $R$  will be in BCNF.  
The relation is in BCNF when the functional dependency is of the form Superkey  $\rightarrow$  attribute set.

All functional dependencies satisfying condition

$$A1 \rightarrow A2, A2 \rightarrow A3$$

In the both above case,  $A1$  and  $A2$  are superkeys of  $R$ .

So the relation of  $R$  is BCNF.

- A relation is in BCNF if  $X$  is a superkey for every functional dependency  $X \rightarrow Y$ .  $A1$  and  $A2$  are superkey means they can derive all the attributes if  $A1A2A3A4$ .

$R1$  has  $A1A2$  and both are superkeys,  $R1$  is BCNF.

$R2$  has  $A1A3$  and  $A1$  is superkey it can derive  $A3$ ,  $R2$  is BCNF.

$R3$  has no FD, but  $A1$  is superkey it can derive  $A4$ ,  $R3$  is BCNF.

- Decomposing the table into three tables  $R1$ ,  $R2$ ,  $R3$ .

Since there is no FD, FD's of decomposed relations

FD1:  $A1 \rightarrow A2$ , FD2:  $A2 \rightarrow A3$  and there is no FD derived from  $R3$ .

Finding the closures of the FD.

$$\text{closure}(A1) = \{A1, A2\}, \text{closure}(A2) = \{A2, A3\}$$

Finding union of closures:

$$\{A1A2\} \cup \{A2A3\} = \{A1A2A3\} = F$$

It is dependency preserving decomposition.